

SE2052: PROGRAMMING PARADIGMS

BNF AND EBNF

BY JEEWAKA PERERA

Updated on: 11/2/2025

WHY STUDY GRAMMAR IN PROGRAMMING?

- Defines valid syntax for programming languages.
- Used in compilers, interpreters, and parsers.
- Helps prevent syntax errors.

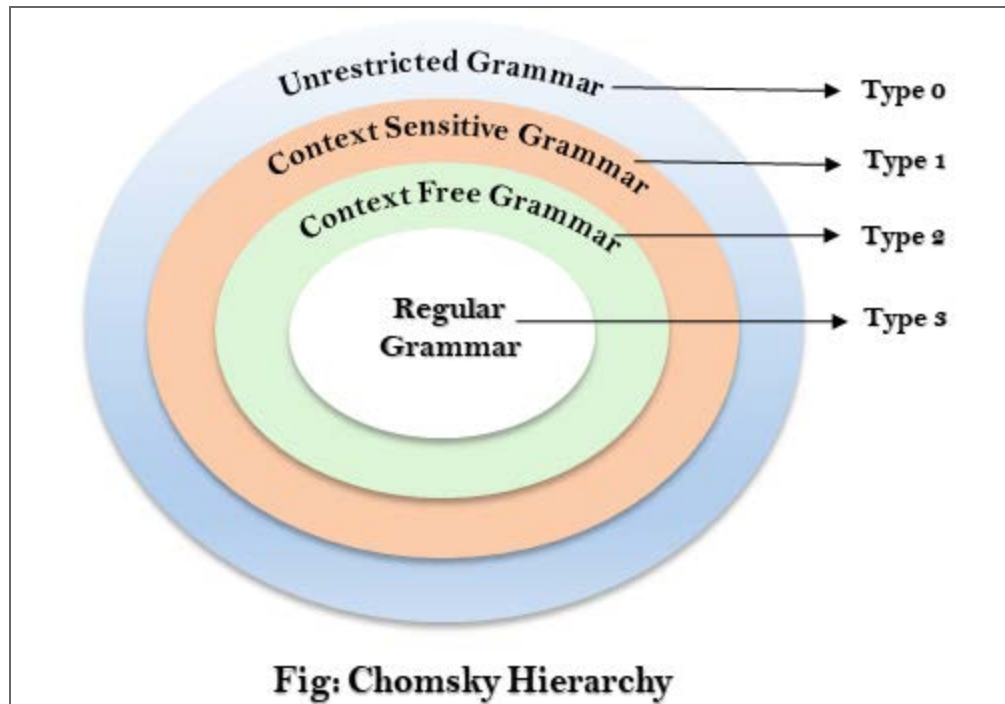
Think of grammar in programming like rules in natural languages.

WHAT IS SYNTAX IN PROGRAMMING?

- Syntax defines the structure of a programming language.
- Example: Grammar rules ensure valid statements.
- Think of it like grammar in natural languages.
- Syntax of a programming language is the form of its expressions, statements, and program units.
- Semantics is the meaning of those expressions, statements, and program units.

TYPES OF GRAMMARS (CHOMSKY HIERARCHY)

1. **Type 0:** Unrestricted Grammar
2. **Type 1:** Context-Sensitive Grammar
3. **Type 2:** Context-Free Grammar (CFG)
4. **Type 3:** Regular Grammar



EXAMPLES OF DIFFERENT GRAMMAR TYPES

Regular Grammar (Type 3):

$$S \rightarrow aS \mid bS \mid \epsilon$$

Used for Analysis (Tokens in Regex).

Context-Free Grammar (Type 2):

$$S \rightarrow S + S \mid S * S \mid (S) \mid \text{number}$$

Used for Syntax Analysis (Parsing).

DARK AGE BEFORE BNF

- Before BNF, programming language syntax was described informally.
- Each compiler was built manually without a structured grammar.

MOTIVATION FOR BNF

- Before BNF, ambiguities in syntax caused compiler issues.
- BNF introduced precise and structured grammar rules.
- Enabled the development of automated parsers for compilers.

INTRODUCTION OF BNF

John Backus introduced BNF in 1959.

- First used to define the ALGOL 60 programming language.
- Created a notation for programming languages.

BNF allowed programming languages to be clearly specified for the first time.

COMPONENTS OF BNF

- Terminals – The actual symbols (e.g., keywords, numbers, operators).
- Non-terminals – Abstract names for patterns (e.g., `` , ``).
- Production Rules – Define how non-terminals expand into terminals.

TERMINALS IN BNF

Terminals are the basic symbols in a language.

- They appear exactly as written in the language.
- Examples of terminals:

```
+ - * / ( ) 0-9 if while int
```

Think of terminals as fixed words or symbols in a language.

NON-TERMINALS IN BNF

- Non-terminals represent patterns or structures.
- They are enclosed in angle brackets (`< >`).
- Examples:

```
<expression>    <term>    <statement>    <loop>
```

Think of non-terminals as placeholders for complex patterns.

PRODUCTION RULES

- Production rules define how non-terminals expand.
- Uses the `::=` operator.
- Example rule:

```
<expression> ::= <term> | <expression> "+" <term>
```

This means an `expression` is either a `term` or an `expression` followed by `+` and another `term`.

FULL EXAMPLE OF BNF

```
<expression> ::= <term> | <expression> "+" <term> | <expression> "-" <term> | <expression> "*" <term> | <expression> "/" <term>
<term> ::= <factor> | <term> "*" <factor> | <term> "/" <factor>
<factor> ::= <number> | "(" <expression> ")"
<number> ::= <digit> | <number> <digit>
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

✅ This defines a basic arithmetic expression.

ACTIVITY: IDENTIFY COMPONENTS

Given the rule:

```
<statement> ::= "if" "(" <condition> ")" "{" <body> "}"
```

Identify:

- Terminals
- Non-terminals
- Production rule structure

QUICK QUIZ

Which of the following is not a valid BNF rule?

1. `<expr> ::= <expr> "+" <term>`
2. `term ::= number | "(" expr ")"`
3. `<expr> = <expr> "+" <term>`
4. `<factor> ::= "0" | "1" | ... | "9"`

Discuss and explain your answer!



BNF vs EBNF

IF statement structure:

`<statement> ::= "if" "(" <condition> ")" "{" <body> "}"`

`"if"` → The literal keyword `"if"` (a terminal symbol).

`"("` and `)"` → Parentheses that enclose the condition.

`<condition>` → A non-terminal that represents the condition to evaluate.

`"{"` and `"}"` → Curly braces that enclose the body of the statement.

`<body>` → A non-terminal representing the statements inside the `if` block.

Expanding it to if-else statement:

**<statement> ::= "if" "(" <condition> ")" "{" <body> "}" <optional_else>
<optional_else> ::= "else" "{" <body> "}" | ϵ**

Note : Epsilon represents an empty production (i.e., nothing), which simulates the optional behavior

Standard BNF does not support optional elements directly; everything must be explicitly defined using separate rules.

EBNF

Extended Backus-Naur Form (EBNF) is an improved version of **Backus-Naur Form (BNF)** used to describe the syntax of programming languages in a more **concise and readable** way. It introduces additional symbols to make grammar definitions easier to write and understand.

EBNF extends BNF by:

- ✓ **Making rules more compact**
- ✓ **Adding optional elements** (without requiring extra rules)
- ✓ **Allowing repetition without recursion**
- ✓ **More concise syntax. Hence, improved readability**

Key Features of EBNF

1) Allow optional parts directly. Square brackets [...] indicate optional parts. The else block is optional below.

```
<if-statement> ::= "if" "(" <condition> ")" "{" <body> "}" [ "else" "{" <body> "}" ]
```

2) Repetition using curly braces. Following mean a number consists of at least one digit, followed by zero or more digits

```
<number> ::= <digit> { <digit> }
```

3) Parentheses are used to group elements.

```
<term> ::= <factor> ("*" | "/" <factor>)*
```

A <term> is a <factor> followed by zero or more occurrences of "*" or "/" with another <factor>.

BNF

$\langle \text{expression} \rangle ::= \langle \text{term} \rangle \mid \langle \text{expression} \rangle + \langle \text{term} \rangle \mid \langle \text{expression} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{factor} \rangle \mid \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{term} \rangle / \langle \text{factor} \rangle$

$\langle \text{factor} \rangle ::= \langle \text{number} \rangle \mid (\langle \text{expression} \rangle)$

$\langle \text{number} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{number} \rangle \langle \text{digit} \rangle$

$\langle \text{digit} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$

EBNF

$\langle \text{expression} \rangle ::= \langle \text{term} \rangle (("+" \mid "-") \langle \text{term} \rangle)^*$

$\langle \text{term} \rangle ::= \langle \text{factor} \rangle (("*" \mid "/") \langle \text{factor} \rangle)^*$

$\langle \text{factor} \rangle ::= \langle \text{number} \rangle \mid "(" \langle \text{expression} \rangle ")"$

$\langle \text{number} \rangle ::= \langle \text{digit} \rangle \{ \langle \text{digit} \rangle \}$

$\langle \text{digit} \rangle ::= "0" \mid "1" \mid "2" \mid "3" \mid "4" \mid "5" \mid "6" \mid "7" \mid "8" \mid "9"$

If – else if - else

```
<statement> ::= "if" "(" <condition> ")" "{" <body> "}"  
               { "else if" "(" <condition> ")" "{" <body> "}" }  
               [ "else" "{" <body> "}" ]
```



Which is invalid BNF rule?

- 1) $\langle \text{digit} \rangle ::= "0" \mid "1" \mid "2" \mid "3" \mid "4" \mid "5" \mid "6" \mid "7" \mid "8" \mid "9"$
- 2) $\langle \text{number} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{number} \rangle \langle \text{digit} \rangle$
- 3) $\langle \text{expression} \rangle ::= \langle \text{term} \rangle \{ ("+" \mid "-") \langle \text{term} \rangle \}$
- 4) $\langle \text{statement} \rangle ::= \text{"while" "("} \langle \text{condition} \rangle \text{"}" "{"} \langle \text{body} \rangle \text{"}"}$



GUIDED ACTIVITY

We need to define a BNF grammar for an **Aircraft Autopilot Alert System**.

- Monitors **altitude, pitch, and error margin**.
- Auto-corrects minor errors.
- Sends alerts for serious issues.

Question: What are the key components we need to model?

STEP 1: IDENTIFY INPUTS

Inputs are measurable factors:

- **Altitude:** "low", "normal", "high".
- **Pitch:** "up", "level", "down".
- **Error Margin:** "low", "moderate", "high".

Now, let's write the BNF for this!



WRITING BNF FOR INPUTS

```
<altitude> ::= "low" | "normal" | "high"  
<pitch> ::= "up" | "level" | "down"  
<error> ::= "low" | "moderate" | "high"
```

✅ These are our terminals because they are fixed values.

STEP 2: IDENTIFY SYSTEM MESSAGES

The system needs to generate messages:

- **Auto-correct:** Adjust flight path if error is low.
- **Alert:** Warn if error is high.

How do we express this in BNF?



WRITING BNF FOR SYSTEM MESSAGES

```
<decision> ::= <autocorrect> | <alert>  
<autocorrect> ::= "Auto-correcting flight path..."  
<alert> ::= "ALERT! Manual intervention required."
```



The system selects a decision based on the error level.

STEP 3: COMBINE STATUS & DECISION

We now define the full message structure:

- The status includes altitude, pitch, and error.
- The decision follows based on error margin.

Let's write this in BNF.



FULL BNF (BASIC VERSION)

```
<message> ::= <status> <decision>
```

```
<status> ::= "Altitude:" <altitude> "Pitch:" <pitch> "
```

```
<altitude> ::= "low" | "normal" | "high"
```

```
<pitch> ::= "up" | "level" | "down"
```

```
<error> ::= "low" | "moderate" | "high"
```

```
<decision> ::= <autocorrect> | <alert>
```

```
<autocorrect> ::= "Auto-correcting flight path..."
```

```
<alert> ::= "ALERT! Manual intervention required."
```

EXAMPLE OUTPUTS

Altitude: high Pitch: down Error: low
Auto-correcting flight path...





Altitude: normal Pitch: level Error: high
ALERT! Manual intervention required.



STUDENT ACTIVITY

We need to define a **BNF grammar** for an aircraft autopilot alert system.

The system monitors:

-  **Altitude**
-  **Pitch**
-  **Error margin**
-  **Weather conditions**

Based on these, the system decides whether to **auto-correct** or trigger an **alert**.

🔧 STEP 1: IDENTIFY INPUTS

These are the monitored factors:

- **Altitude:**

low | normal | high

- **Pitch:**

up | level | down

- **Error Margin:**

low | moderate | high




- **Weather:**

clear | storm | turbulence

Task: How do we write this in BNF?

STEP 2: DEFINE SYSTEM BEHAVIOR

The system should:

-  Auto-correct if error is
low
- .
-  Trigger an alert if error is
high
- .
-  Allow pilot override.

How do we represent these decisions in BNF?

STEP 3: DEFINE ALERT CONDITIONS

The system triggers different alerts based on conditions:

-  **Low Fuel Warning:**

Altitude = low & Error = high

-  **Stall Warning:**

Pitch = up & Error = (moderate | high)

-  **Severe Turbulence Alert:**

Weather = turbulence & Error = high

-  **Critical Weather Alert:**

Weather = storm

-  **Manual Override:** If pilot takes control.

Task: Write BNF rules to capture these alerts.