



# Array Implementaion: Polynomials & Sparse Matrix

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Alok Kumar Jagadev



# Polynomials

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A single variable polynomial  $p(x) = 4x^6 + 10x^4 - 5x + 3$

Remark: order of this polynomial is 6 (highest exponent)

- Representing Polynomials

- In general, the polynomial are represented as:

$$A(x) = a_{m-1}x^{e_{m-1}} + \dots + a_0x^{e_0}$$

- where the  $a_i$  are nonzero coefficients and the  $e_i$  are nonnegative integer exponents such that

$$e_{m-1} > e_{m-2} > \dots > e_1 > e_0 \geq 0 .$$



# Polynomial

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How to implement this?

There are different ways of implementing the polynomial ADT:

- Array (not recommended)
- Double Array (inefficient)
- Array of Structure (inefficient)
- Linked List (preferred and recommended)

# Polynomial

Array Implementation:

$$p_1(x) = 8x^3 + 3x^2 + 2x + 6$$

$$p_2(x) = 23x^4 + 18x - 3$$

$p_1(x)$

0	1	2	3
6	2	3	8

$p_2(x)$

0	1	2	3	4
-3	18	0	0	23

0

2

0

2

4

Index  
represents  
exponents



# Polynomial

---

This is why arrays are not good to represent polynomials:

$$p_3(x) = 16x^{21} - 3x^5 + 2x + 6$$

0	1	2	3	4	5	...	20	21
6	2	0	0	0	-3	...	0	16



WASTE OF SPACE!



# Polynomial

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- Advantages of using an Array
  - good for non-sparse polynomials.
  - easy to store and retrieve.
- Disadvantages of using an Array:
  - Allocate array size ahead of time.
  - huge array size required for sparse polynomials. Waste of space and runtime.



# Polynomial Addition

---

```
#include<stdio.h>
#include<math.h>

float a[50], b[50], c[50], d[50];
int main() {
    int i;
    int deg1, deg2;
    int k=0, l=0, m=0;
    printf("Enter the highest degree of polynomial1: ");
    scanf("%d", &deg1);
    for(i=0; i<=deg1; i++) {
        printf("\nEnter the coeff of x^%d :", i);
        scanf("%f", &a[i]);
    }
```



# Polynomial Addition

---

```
printf("\nEnter the highest degree of polynomial2: ");
scanf("%d", &deg2);
for(i=0; i<=deg2; i++) {
    printf("\nEnter the coeff of x^%d : ", i);
    scanf("%f", &b[i]);
}
printf("\nPolynomial 1 = %.1f", a[0]);
for(i=1; i<=deg1; i++)
    printf("+ %.1fx^%d", a[i], i);
printf("\nPolynomial 2 = %.1f", b[0]);
for(i=1; i<=deg2; i++)
    printf("+ %.1fx^%d", b[i], i);
```





# Polynomial Addition

---

```
if(deg1>deg2) {  
    for(i=0; i<=deg2; i++) {  
        c[m] = a[i] + b[i];  
        m++;  
    }  
    for(i=deg2+1; i<=deg1; i++) {  
        c[m] = a[i];  
        m++;  
    }  
}
```

```
else {  
    for(i=0; i<=deg1; i++) {  
        c[m] = a[i] + b[i];  
        m++;  
    }  
    for(i=deg1+1; i<=deg2; i++) {  
        c[m] = b[i];  
        m++;  
    }  
}
```



# Polynomial Addition

---

```
printf("\npolynomial after addition = %.1f",  
c[0]);  
for(i=1; i<m; i++)  
    printf("+ %.1fx^%d", c[i], i);  
return 0;  
}
```

## Output

Enter the highest degree of polynomial1: 3

Enter the coeff of  $x^0$  :2

Enter the coeff of  $x^1$  :3

Enter the coeff of  $x^2$  :5

Enter the coeff of  $x^3$  :1

Enter the highest degree of polynomial2: 2

Enter the coeff of  $x^0$  :7

Enter the coeff of  $x^1$  :8

Enter the coeff of  $x^2$  :5

polynomial 1 =  $2.0 + 3.0x^1 + 5.0x^2 + 1.0x^3$

polynomial 2 =  $7.0 + 8.0x^1 + 5.0x^2$

polynomial after addition =  $9.0 + 11.0x^1 + 10.0x^2 + 1.0x^3$



# Polynomial

---

Double Array Implementation:

Represent the following two polynomials:

$$p_1(x) = 23x^9 + 18x^7 - 41x^6 + 163x^4 - 5x + 3$$

$$p_2(x) = 4x^6 + 10x^4 + 12x + 8$$

# Polynomial

$$p_1(x) = 23x^9 + 18x^7 - 41x^6 + 163x^4 - 5x + 3$$

$$p_2(x) = 4x^6 + 10x^4 + 12x + 8$$

Diagram illustrating the representation of two polynomials,  $p_1(x)$  and  $p_2(x)$ , in a coefficient array.

The array is a 2x10 grid where the top row contains coefficients and the bottom row contains exponents.

23	18	-41	163	-5	3	4	10	12	8
9	7	6	4	1	0	6	4	1	0

Annotations:

- Coefficient:** Points to the top row of the array.
- Exponent:** Points to the bottom row of the array.
- Start  $p_1(x)$ :** Points to the first cell (index 0) of the array.
- End  $p_1(x)$ :** Points to the cell at index 5 (exponent 0).
- Start  $p_2(x)$ :** Points to the cell at index 6 (exponent 6).
- End  $p_2(x)$ :** Points to the last cell (index 9, exponent 0).

Exponents are labeled below the array: 0, 2, 8.



# Polynomial

---

Advantages of using two array:

- save space (compact)

Disadvantages of using two Array:

- difficult to maintain
- have to allocate array size ahead of time
- more code required for misc. operations.



# Polynomial using structure

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Structure Implementation:

```
struct poly {  
    float coeff;  
    int exp; };  
struct poly p[50];
```



# Polynomial Addition

---

```
#include<stdio.h>
#include<math.h>
struct poly {
    float coeff;
    int exp; };
struct poly a[50], b[50], c[50], d[50];
int main() {
    int nterm1, nterm2, nterm3;
    int i, k=0, l=0, m=0;
    printf("Enter the number of non-zero terms in Polynomial1: ");
    scanf("%d", &nterm1);
    for(i=0; i<nterm1; i++) {
        printf("\nEnter the coeff of %d th term: ", i);
        scanf("%f", &a[i].coeff);
        printf("\nEnter the exp of %d th term: ", i);
        scanf("%f", &a[i].exp);
    }
```



# Polynomial Addition

---

```
printf("\nEnter the number of non-zero terms in Polynomial2: ");
scanf("%d", &nterm2);
for(i=0; i<nterm2; i++) {
    printf("\nEnter the coeff of %d th term: ", i);
    scanf("%f", &b[i].coeff);
    printf("\nEnter the exp of %d th term: ", i);
    scanf("%f", &b[i].exp);
}
printf("\nPolynomial 1 = %.1f", a[0].coeff);
for(i=1; i<nterm1; i++)
    printf("+ %.1fx^%d", a[i].coeff, a[i].exp);
printf("\nPolynomial 2 = %.1f", b[0].coeff);
for(i=1; i<nterm2; i++)
    printf("+ %.1fx^%d", b[i].coeff, b[i].exp);
```





# Polynomial Addition

---

```
while(k<nterm1 && l<nterm2) {  
    if(a[k].exp < b[l].exp) {  
        c[m].coeff = a[k].coeff;  
        c[m].exp = a[k].exp;  
        k++; m++;    }  
    else if(a[k].exp > b[l].exp) {  
        c[m].coeff = b[l].coeff;  
        c[m].exp = b[l].exp;  
        l++; m++;    }  
    else {  
        c[m].coeff = a[k].coeff + b[l].coeff;  
        c[m].exp = a[k].exp;  
        k++; l++; m++; }  
}
```



# Polynomial Addition

---

```
while(k<nterm1) {
    c[m].coeff = a[k].coeff;
    c[m].exp = a[k].exp;
    k++; m++;
}
while(l<nterm2) {
    c[m].coeff = b[l].coeff;
    c[m].exp = b[l].exp;
    l++; m++;
}
nterm3 = m-1;
printf("\npolynomial after addition = %.1f", c[0].coeff);
for(i=1; i<nterm3; i++)
    printf("+ %.1fx^%d", c[i].coeff, c[i].exp);
return 0;
}
```



# Polynomial Multiplication

---

```
#include<stdio.h>
#include<math.h>

float a[50], b[50], c[50], d[50];
int main() {
    int i;
    int deg1,deg2;
    int k=0,l=0,m=0;
    printf("Enter the highest degree of polynomial1: ");
    scanf("%d", &deg1);
    for(i=0; i<=deg1; i++) {
        printf("\nEnter the coeff of x^%d :", i);
        scanf("%f", &a[i]);
    }
}
```



# Polynomial Multiplication

---

```
printf("\nEnter the highest degree of polynomial2: ");
scanf("%d", &deg2);
for(i=0; i<=deg2; i++) {
    printf("\nEnter the coeff of x^%d : ", i);
    scanf("%f", &b[i]);
}
printf("\nPolynomial 1 = %.1f", a[0]);
for(i=1; i<=deg1; i++)
    printf("+ %.1fx^%d", a[i], i);
printf("\nPolynomial 2 = %.1f", b[0]);
for(i=1; i<=deg2; i++)
    printf("+ %.1fx^%d", b[i], i);
```



# Polynomial Multiplication

---

```
deg3 = deg1+deg2;
for (int i = 0; i<=deg3; i++)
    c[i] = 0;
for (int i=0; i<=deg1; i++) {
    for (int j=0; j<=deg2; j++)
        c[i+j] += a[i] * b[j];
}
printf("\nPolynomial after multiplication = %.1f", c[0]);
for(i=1; i<=deg3; i++)
    printf("+ %.1fx^%d", c[i], i);
return 0;
}
```



# Polynomial Multiplication

---

## Output

Enter the highest degree of polynomial1:2

Enter the coeff of  $x^0$  :2

Enter the coeff of  $x^1$  :3

Enter the coeff of  $x^2$  :4

Enter the highest degree of polynomial2:3

Enter the coeff of  $x^0$  :5

Enter the coeff of  $x^1$  :6

Enter the coeff of  $x^2$  :7

Enter the coeff of  $x^3$  :2

Polynomial 1 =  $2.0 + 3.0x^1 + 4.0x^2$

Polynomial 2 =  $5.0 + 6.0x^1 + 7.0x^2 + 2.0x^3$

Polynomial after multiplication =  $10.0 + 27.0x^1 + 52.0x^2 + 49.0x^3 + 34.0x^4 + 8.0x^5$



# Polynomial Multiplication

---

```
#include<stdio.h>
#include<math.h>
struct poly {
    float coeff;
    int exp; };
struct poly a[50], b[50], c[50], d[50];
int main() {
    int nterm1, nterm2, nterm3;
    int i, j, k, l=0, m=0;
    float prod;
    printf("Enter the number of non-zero terms in Polynomial1: ");
    scanf("%d", &nterm1);
    for(i=0; i<nterm1; i++) {
        printf("\nEnter the coeff of %d th term: ", i);
        scanf("%f", &a[i].coeff);
        printf("\nEnter the exp of %d th term: ", i);
        scanf("%f", &a[i].exp);    }
```



# Polynomial Multiplication

---

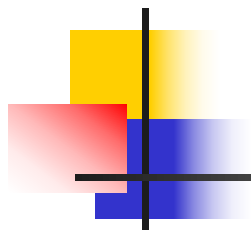
```
printf("\nEnter the number of non-zero terms in Polynomial2: ");
scanf("%d", &nterm2);
for(i=0; i<nterm2; i++) {
    printf("\nEnter the coeff of %d th term: ", i);
    scanf("%f", &b[i].coeff);
    printf("\nEnter the exp of %d th term: ", i);
    scanf("%f", &b[i].exp);
}
printf("\nPolynomial 1 = %.1f", a[0].coeff);
for(i=1; i<nterm1; i++)
    printf("+ %.1fx^%d", a[i].coeff, a[i].exp);
printf("\nPolynomial 2 = %.1f", b[0].coeff);
for(i=1; i<nterm2; i++)
    printf("+ %.1fx^%d", b[i].coeff, b[i].exp);
```





# Polynomial Multiplication

```
for (int i=0; i<nterm1; i++) {  
    for (int j=0; j<ntern2; j++) {  
        prod = a[i].coeff*b[j].coeff;  
        for (int k=0; k<m; k++) {  
            if(a[i].exp+b[j].exp == c[k].exp) {  
                c[k].coeff += prod;  
                break; }  
        }  
        c[m].exp=a[i].exp+b[j].exp;  
        c[m++].coeff = prod;  
    }  
}  
nterm3 = m-1;  
printf("\nPolynomial after multiplication = %.1f", c[0].coeff);  
for(i=1; i<nterm3; i++)  
    printf("+ %.1fx^%d", c[i].coeff, c[i].exp);  
return 0; }
```



# Sparse Matrix



# Sparse Matrix

---

- A matrix is a two-dimensional **data object** made of  $m$  rows and  $n$  columns having total  $m \times n$  values.
- If most of the elements of the matrix have 0 value, then it is called a sparse matrix.
- Why to use Sparse Matrix instead of simple matrix?
  - Storage: less memory used to store only those non-zero elements.
  - Computing time: Computing time can be reduced by logically designing a data structure traversing only non-zero elements.



# Sparse Matrix

	col 1	col 2	col 3
row 1	-27	3	4
row 2	6	82	-2
row 3	109	-64	11
row 4	12	8	9
row 5	48	27	47

5×3

(a) 15/15

Two matrices

	col0	col1	col2	col3	col4	col5
row0	15	0	0	22	0	-15
row1	0	11	3	0	0	0
row2	0	0	0	-6	0	0
row3	0	0	0	0	0	0
row4	91	0	0	0	0	0
row5	0	0	28	0	0	0

6×6

(b) 8/36

sparse matrix

data structure?



# Sparse Matrix: Array Representation

- Represented by a two-dimensional array.
- Sparse matrix wastes space
- Each element is characterized by **<row, col, value>**.

	row col value		
	<hr/>		
	# of rows (columns)		# of nonzero terms
	↓	↓	
a[0]	6	6	8
[1]	0	0	15
[2]	0	3	22
[3]	0	5	-15
[4]	1	1	11
[5]	1	2	3
[6]	2	3	-6
[7]	4	0	91
[8]	5	2	28

row, column in ascending order



# Sparse Matrix: Program

```
#include<stdio.h>
int main() {
    // Assume 4x5 sparse matrix
    int smat[4][5] =
        { {0 , 0 , 3 , 0 , 4 },
          {0 , 0 , 5 , 7 , 0 },
          {0 , 0 , 0 , 0 , 0 },
          {0 , 2 , 6 , 0 , 0 }
        };
    int i, j, k, size = 0;
    for (i = 0; i < 4; i++)
        for (j = 0; j < 5; j++)
            if (smat[i][j] != 0)
                size++;
    int sm[size+1][3];
```

```
    k = 0;
    sm[k][0] = 4; sm[k][1] = 5; sm[k][2] = size;
    k++;
    for (i = 0; i < 4; i++)
        for (j = 0; j < 5; j++)
            if (smat[i][j] != 0) {
                sm[k][0] = i; sm[k][1] = j;
                sm[k][2] = smat[i][j]; k++;
            }
    for (int i=0; i<=size; i++) {
        for (int j=0; j<3; j++)
            printf("%d ", sm[i][j]);
        printf("\n");
    }
    return 0; }
```

## **Output:**

```
4 5 6
0 2 3
0 4 4
1 2 5
1 3 7
3 1 2
3 2 6
```

# Sparse Matrix: Transpose

	<u>row col value</u>				<u>row col value</u>			
	# of rows (columns)				# of nonzero terms			
	↓	↓	↓					
a[0]	6	6	8		b[0]	6	6	8
[1]	0	0	15		[1]	0	0	15
[2]	0	3	22		[2]	0	4	91
[3]	0	5	-15		[3]	1	1	11
[4]	1	1	11	transpose	[4]	2	1	3
[5]	1	2	3	→	[5]	2	5	28
[6]	2	3	-6		[6]	3	0	22
[7]	4	0	91		[7]	3	2	-6
[8]	5	2	28		[8]	5	0	-15
	(a)				(b)			
row, column in ascending order								

Sparse matrix and its transpose stored as triples



# Sparse Matrix: Representation

---

Sparse\_matrix Create(max\_row, max\_col) :

```
#define TERMS 101 /* maximum number of terms +1 */  
typedef struct {  
    int col;  
    int row;  
    int value;  
} Sparse;  
Sparse a[TERMS]
```

# of rows (columns)  
# of nonzero terms





# Transpose a Matrix

---

- (1) for each **row**  $i$   
    element  $\langle i, j, \text{value} \rangle$  store  
    in element  $\langle j, i, \text{value} \rangle$  of the transpose

Difficulty: where to put  $\langle j, i, \text{value} \rangle$

$(0, 0, 15) \rightarrow (0, 0, 15)$

$(0, 3, 22) \rightarrow (3, 0, 22)$

$(0, 5, -15) \rightarrow (5, 0, -15)$

$(1, 1, 11) \rightarrow (1, 1, 11)$

Move elements down very often.

Approach:

- (2) For all elements in **column**  $j$ ,  
    place element  $\langle i, j, \text{value} \rangle$  in element  $\langle j, i, \text{value} \rangle$



# Sparse Matrix: Transpose

```
void transpose (Sparse a[], Sparse b[]) {
```

```
    int n, i, j, k;
```

```
    n = a[0].value;
```

```
    b[0].row = a[0].col;
```

```
    b[0].col = a[0].row;
```

```
    b[0].value = n;
```

```
    if (n > 0) {      /* non zero matrix */
```

```
        k = 1;
```

```
        for (i = 0; i < a[0].col; i++)
```

```
            /* transpose by columns in a */
```

```
                for( j = 1; j <= n; j++)
```

```
                    /* find elements from the  
                       current column */
```

```
                    if (a[j].col == i) {
```

```
                        /* element is in current  
                           column, add it to b */
```

a[0]	6	6	8
[1]	0	0	15
[2]	0	3	22
[3]	0	5	-15
[4]	1	1	11
[5]	1	2	3
[6]	2	3	-6
[7]	4	0	91
[8]	5	2	28

b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]	2	5	28
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15



# Sparse Matrix: Transpose

columns elements

```
b[k].row = a[j].col;  
b[k].col = a[j].row;  
b[k].value = a[j].value;  
k++
```

Transpose of a sparse matrix

Scan the array “columns” times.  
The array has “*elements*” elements.

a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]	0	4	91
[3]	0	5	-15	[3]	1	1	11
[4]	1	1	11	[4]	2	1	3
[5]	1	2	3	[5]	2	5	28
[6]	2	3	-6	[6]	3	0	22
[7]	4	0	91	[7]	3	2	-6
[8]	5	2	28	[8]	5	0	-15

==>  $O(\text{columns} \times \text{elements})$



# Sparse Matrix: Transpose

---

**Discussion:** compared with 2-D array representation

- $O(\text{columns} \times \text{elements})$  vs.  $O(\text{columns} \times \text{rows})$
- $\text{elements} \rightarrow \text{columns} \times \text{rows}$  when **nonsparse**
  - $O(\text{columns} \times \text{columns} \times \text{rows})$

**Inefficient:** Scan the array “*columns*” times.

**Solution:**

- Determine the # of elements in each column of the original matrix.
- Determine what will be the the starting positions of each row in the transpose matrix.



# Sparse Matrix

---

a[0]	6	6	8
[1]	0	0	15
[2]	0	3	22
[3]	0	5	-15
[4]	1	1	11
[5]	1	2	3
[6]	2	3	-6
[7]	4	0	91
[8]	5	2	28

b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]	2	5	28
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15

	[0]	[1]	[2]	[3]	[4]	[5]
row_terms =	2	1	2	2	0	1
starting_pos =	1	3	4	6	8	8



# Sparse Matrix: Transpose

a[0]	6	6	8
[1]	0	0	15
[2]	0	3	22
[3]	0	5	-15
[4]	1	1	11
[5]	1	2	3
[6]	2	3	-6
[7]	4	0	91
[8]	5	2	28

columns

elements

columns

```
void fast_transpose(term a[ ], term b[ ]) {
    int row_terms[MAX_COL], starting_pos[MAX_COL];
    int i, j, num_cols = a[0].col, num_terms = a[0].value;
    b[0].row = num_cols; b[0].col = a[0].row;
    b[0].value = num_terms;
    if (num_terms > 0) { /*nonzero matrix*/
        for (i = 0; i < num_cols; i++)
            row_terms[i] = 0;
        for (i = 1; i <= num_terms; i++)
            row_terms[a[i].col]++
        starting_pos[0] = 1;
        for (i = 1; i < num_cols; i++)
            starting_pos[i] = starting_pos[i-1] + row_terms[i-1];
    }
}
```

	[0]	[1]	[2]	[3]	[4]	[5]
row_terms =	2	1	2	2	0	1
starting_pos =	1	3	4	6	8	8



# Sparse Matrix: Transpose

elements

```
for (i=1; i <= num_terms, i++) {  
    j = starting_pos[a[i].col]++;  
    b[j].row = a[i].col;  
    b[j].col = a[i].row;  
    b[j].value = a[i].value;  
}  
}
```

Fast transpose of a sparse matrix

a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]	0	4	91
[3]	0	5	-15	[3]	1	1	11
[4]	1	1	11	[4]	2	1	3
[5]	1	2	3	[5]	2	5	28
[6]	2	3	-6	[6]	3	0	22
[7]	4	0	91	[7]	3	2	-6
[8]	5	2	28	[8]	5	0	-15

	[0]	[1]	[2]	[3]	[4]	[5]
row_terms =	2	1	2	2	0	1
starting_pos =	1	3	4	6	8	8

Compared with 2-D array representation:  $O(\text{columns} + \text{elements})$  vs.  $O(\text{columns} \times \text{rows})$   
elements  $\rightarrow$  columns  $\times$  rows:  $O(\text{columns} + \text{elements}) \rightarrow O(\text{columns} \times \text{rows})$

Cost: Additional *row\_terms* and *starting\_pos* arrays are required.

Let the two arrays *row\_terms* and *starting\_pos* be shared.



# Sparse Matrix Addition

---

```
void read_sp_mat(int sp[][3]) {
    int r, c, i, j, n;
    printf("\nEnter r and c : ");
    scanf("%d %d", &r, &c);
    printf("\nEnter # of nonzero elements : ");
    scanf("%d", &n);
    printf("\nEnter the elements \n");
    j=1;
    for(i=1; i <= n; i++) {
        printf("\nEnter row no : ");
        scanf("%d", &sp[j][0]);
        printf("\nEnter col no : ");
        scanf("%d", &sp[j][1]);
        printf("\nEnter the value : ");
        scanf("%d", &sp[j][2]);
        j++;
    }
}
```

```
sp[0][0] = r;
sp[0][1] = c;
sp[0][2] = n;
```

Matrix 1: (4×4)

Row Col Value

4	4	5
1	2	10
1	4	12
3	3	5
4	1	15
4	2	12

Matrix 2: (4×4)

Row Col Value

4	4	5
1	3	8
2	4	23
3	3	9
4	1	20
4	2	25





# Sparse Matrix Addition

---

```
int add_sp_mat(int sp1[][3], sp2[][3], sp3[][3]) {
    int r, c, i, j, k1, k2, k3, tot1 ,tot2;
    if( sp1[0][0] != sp2[0][0] || sp1[0][1] != sp2[0][1] ) {
        printf("Invalid matrix size ");
        exit(0);
    }
    tot1 = sp1[0][2]; tot2 = sp2[0][2];
    k1 = k2 = k3 = 1;
    while ( k1 <= tot1 && k2 <= tot2) {
        if ( sp1[k1][0] < sp2[k2][0] ) {
            sp3[k3][0] = sp1[k1][0];
            sp3[k3][1] = sp1[k1][1];
            sp3[k3][2] = sp1[k1][2];
            k3++; k1++;
        }
        else
            if ( sp1[k1][0] > sp2[k2][0] ) {
                sp3[k3][0] = sp2[k2][0];
                sp3[k3][1] = sp2[k2][1];
                sp3[k3][2] = sp2[k2][2];
                k3++; k2++;
            }
        else
            if(sp1[k1][1] < sp2[k2][1]) {
                sp3[k3][0]=sp1[k1][0];
                sp3[k3][1]=sp1[k1][1];
                sp3[k3][2]=sp1[k1][2];
                k1++; k3++;
            }
    }
```



# Sparse Matrix Addition

---

```
else
if(sp1[k1][1] > sp2[k2][1]) {
    sp3[k3][0]=sp2[k2][0];
    sp3[k3][1]=sp2[k2][1];
    sp3[k3][2]=sp2[k2][2];
    k2++;
    k3++;
}
else //if ( sp1[k1][0] == sp2[k2][0] )
{
    sp3[k3][0] = sp2[k2][0];
    sp3[k3][1] = sp2[k2][1];
    sp3[k3][2] = sp1[k1][2] + sp2[k2][2];
    k3++;k2++;k1++;
}
}
```

```
while ( k1 <=tot1 ) {
    sp3[k3][0] = sp1[k1][0];
    sp3[k3][1] = sp1[k1][1];
    sp3[k3][2] = sp1[k1][2];
    k3++;k1++;
}
while ( k2 <= tot2 ) {
    sp3[k3][0] = sp2[k2][0];
    sp3[k3][1] = sp2[k2][1];
    sp3[k3][2] = sp2[k2][2];
    k3++;k2++;
}
sp3[0][0] = sp1[0][0];
sp3[0][1] = sp1[0][1];
sp3[0][2] = k3-1;
}
```



# Sparse Matrix Addition: Example

---

Matrix 1: (4×4)

Row Col Value

4	4	5
1	2	10
1	4	12
3	3	5
4	1	15
4	2	12

Matrix 2: (4×4)

Row Col Value

4	4	5
1	3	8
2	4	23
3	3	9
4	1	20
4	2	25

Result of Addition: (4×4)

Row Col Value

4	4	7
1	2	10
1	3	8
1	4	12
2	4	23
3	3	14
4	1	35
4	2	37