

**Machine Learning Assignment Group 71**  
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**Assignment - 2 - Naive Bayes**

Procedure :

1. Preprocess Data - Drop the id column as it is not a feature.
2. Fill the missing value in the data, using the mode viz. max frequency element of the corresponding feature, and encode the discrete features using an inbuilt function from sklearn.
3. Train the Naive Bayes classifier across 5-folds and report the average accuracy across different folds.

4. Finding out the class probability using the formula :

$$P(C\_i) = (\text{No. of samples classified as } C\_i) / (\text{Total no. of samples})$$

5. Find out the probability matrix using the formula :

$$P(X\_j | C\_i) = (\text{No. of samples classified as } C\_i, \text{ having feature } j = X\_j) / (\text{No. of samples classified as } C\_i)$$

For continuous features, however, we use :

$$P(X\_j | C\_i) \sim N(m, \text{var}); m, \text{var} = \text{Mean and Variance of feature } j, \text{ across all samples classified as } C\_i$$

6. For test data, find out the probability of sample  $X = (X\_j1, X\_j2, X\_j3 \dots)$  by the formula :

$$P(C\_i | X) = \{ [P(X\_j1 | C\_i) * P(X\_j2 | C\_i) \dots] * P(C\_i) \} / (\sum_i [P(X\_j1 | C\_i) * P(X\_j2 | C\_i) \dots] * P(C\_i))$$

$$\text{Predicted class} = \max_i P(C\_i | X)$$

7. For performing Principal Component Analysis on the given data, keeping 95% of the variance, we calculated the no. of components with explained variance ratio less just above or equal to 95%.
8. Transform the given data to the found components using an inbuilt function, plot the cumulative sum of explained variance ratios and eigenvalues of the components.
9. Trained the classifier on the transformed data and reported the test accuracy. (Repeat steps 3-6)
10. Remove outliers from the sample, using the following rule: Samples having max feature values beyond  $\pm 3 \times \text{std}$  of a feature are outliers.
11. Using the sequential backward selection process to remove features, i.e., given the accuracy of given features set  $F$ , on the test data(= acc\_prev) calculate :
$$\text{acc\_i} = \text{Test accuracy of features } F-f\_i$$
Remove feature, where acc\_i - acc\_prev is maximum.
12. Run the process, starting from all features till the point where no improvement is possible i.e., acc\_i - acc\_prev is negative for all present features.
13. Trained the classifier on the transformed data and reported the test accuracy. (Repeat steps 3-6)

14. Observations :

| Split Number | Accuracy            |
|--------------|---------------------|
| 1            | 0.5019364833462432  |
| 2            | 0.4965143299767622  |
| 3            | 0.5243996901626646  |
| 4            | 0.5058094500387297  |
| 5            | 0.49147286821705427 |

**Fig (a): Accuracy across different splits**

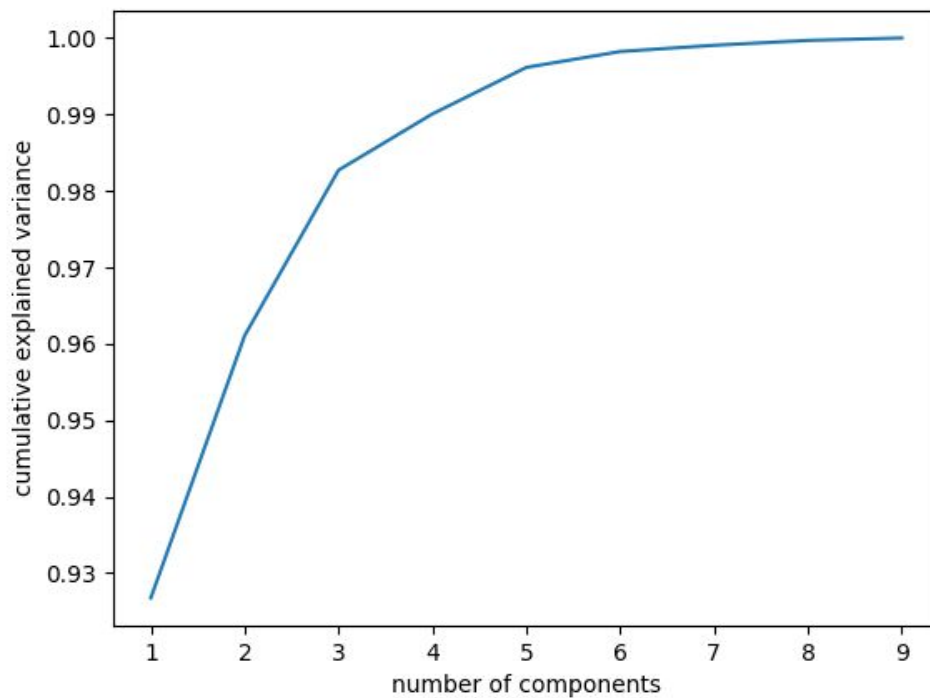
**Results : On kfold :-**

Average train accuracy = 0.5041800419121046

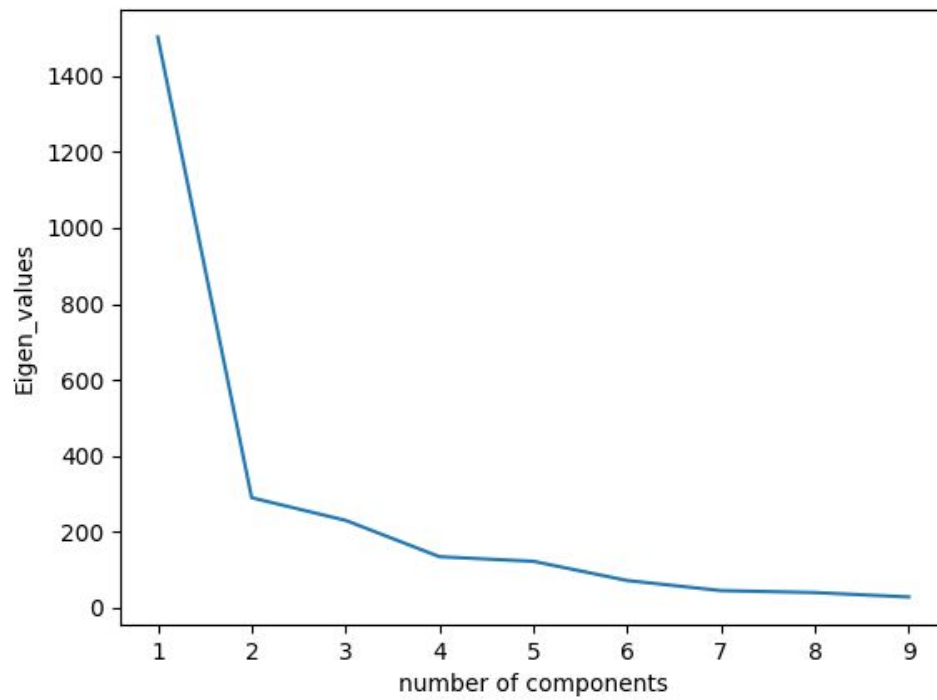
**On Test set :-**

Test accuracy = 0.5012391573729864

**Part (b) Principal Component Analysis:-**



**Fig (c) Explained variance plot during PCA.**



**Fig (c) Eigenvalue plot during PCA**

Observations after PCA

| Split Number | Accuracy            |
|--------------|---------------------|
| 1            | 0.3996901626646011  |
| 2            | 0.3756777691711851  |
| 3            | 0.418280402788536   |
| 4            | 0.37412858249419056 |
| 5            | 0.3875968992248062  |

**Fig (a): Accuracy across different splits**

**Results : On kfold :-**

Average train accuracy = 0.39107476326866386

**On Test set :-**

Test accuracy = 0.3990086741016109

### Part ( c )

#### (i) Removal of feature outliers :-

-> Samples before removal: 8068

-> Samples after removal: 7927

#### (ii) Sequential backward selection

**Initial features:** Gender, Ever\_Married, Age, Graduated, Profession, Work\_Experience, Spending\_Score, Family\_Size, Var\_1

**Remaining features:** Ever\_Married, Age, Graduated, Profession, Spending\_Score, Family\_Size, Var\_1

#### Observations :

| Split Number | Accuracy            |
|--------------|---------------------|
| 1            | 0.46887312844759654 |
| 2            | 0.5157728706624606  |
| 3            | 0.48974763406940064 |
| 4            | 0.5299684542586751  |
| 5            | 0.47712933753943215 |

**Fig (a): Accuracy across different splits**

#### Results : On kfold :-

Average train accuracy = 0.496298284995513

#### On Test set :-

Test accuracy = 0.5044136191677175