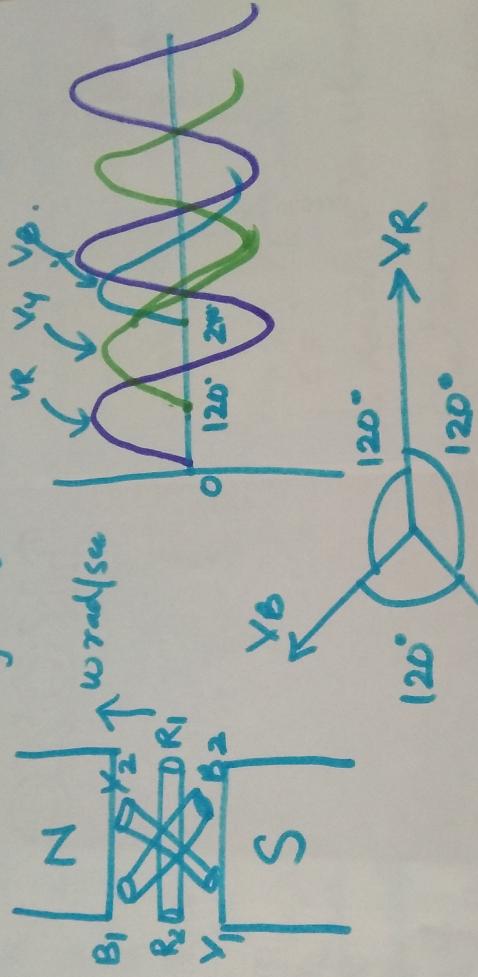


Three phase Circuits:

Single Phase Voltage can be generated by rotating a coil (winding) in a magnetic field (only one armature winding).
 For 3^Φ generation:- 3 separate windings displaced from each other by equal electrical angles.



Three winding R, Y, & B. - Identical and have same angular velocity, voltage induced of same magnitude & freq.
 $V_R = V_m \sin \omega t$
 $V_Y = V_m \sin(\omega t - 120^\circ)$
 $V_B = V_m \sin(\omega t - 240^\circ)$

$$\begin{aligned}
 \text{Resultant} &= V_R + V_Y + V_B = \\
 &= V_m \sin \omega t + V_m \sin(\omega t - 120^\circ) + V_m \sin(\omega t - 240^\circ) \\
 &= V_m [\sin \omega t + 2 \sin(\omega t - 180^\circ) \cos 60^\circ] \\
 &= V_m [\sin \omega t - 2 \sin(\omega t - 60^\circ)] \\
 &= 0
 \end{aligned}$$

2

Sum of the three Voltages at every instant is zero
Phase Sequence :- The order in which the voltages in three phases reaches their maximum value.

Phase Voltage :- the voltage induced in each winding

Phase Current :- The current flowing through each winding is called phase current.

Line Voltages :- The voltage available b/w any pair of terminal or lines.

Line current :- The current flowing through each line.

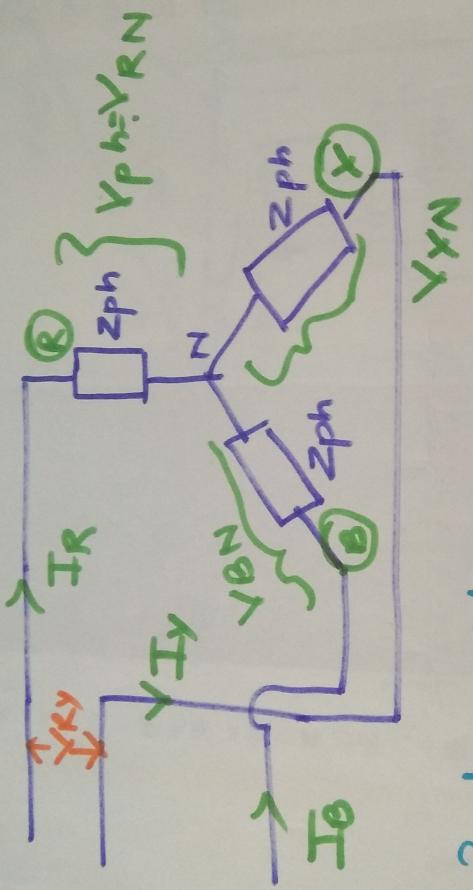
Balanced A/m :- A 3φ 81/m is said to be balanced if

- Voltages in the three phases are equal in magnitude but differ in phase from each other by 120° .
- Currents in the three phases are equal in magnitude & differ in phase from each other by 120° .
- The loads connected across the three phases are identical i.e all loads have same magnitude & p.f.

X X X

Interconnection of 3 φ :-
 1) Star or Wye
 2) Delta or Mesh

(3)



3 phase Voltages : V_{ph}
 V_{RN}, V_{YN}, V_{BN} are equal in magnitude

120° apart

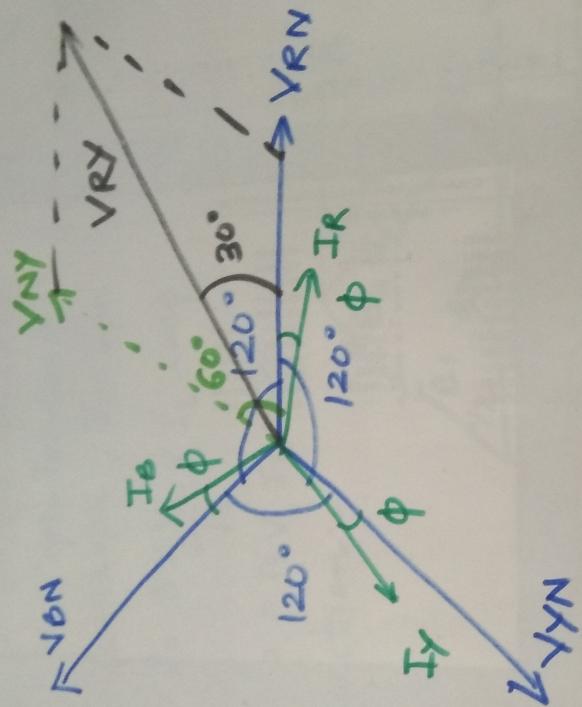
V_{YN} lags behind V_{RN} by 120° & V_{AN} lags behind V_{RN} by 240°.

$$V_{ph} = V_{RN} = V_{YN} = V_{BN}$$

V_L - Line Voltages = $V_{RY} = V_{YB} = V_R$

$$\begin{aligned} \bar{V}_{RY} &= V_R - V_Y = \bar{V}_{RN} + \bar{V}_{NY} \\ \bar{V}_{YB} &= \bar{V}_{YN} + \bar{V}_{BN} \\ V_{BR} &= \sqrt{V_{BN}^2 + V_{RN}^2} \end{aligned}$$

Phasor diagram:-



angle b/w V_{RN} & V_{YN} = 120°

V_{NY} is antiphase V_{YN}

angle b/w V_{RN} & V_{NY} = 60°

$$\text{At } V_RY = V_{RN} + V_{NY} + 2V_{RN} \times V_{NY} \cos(120^\circ)$$

$$= V_{RN}^2 + V_{NY}^2 + 2V_{RN} \times V_{NY} \cos 60^\circ$$

$$V_{RN} = V_{ph}, \quad V_{RY} = V_L$$

$$= V_{ph}^2 + V_{ph}^2 + 2V_{ph}^2 \times \frac{1}{2}$$

$$V_L = 3V_{ph}^2. \quad V_L$$

(5)

$$\text{Power}_x = I_{ph} \quad P = 3 \times \text{power in each phase}$$

$$P = 3 \times V_{ph} I_{ph} \cos \phi$$

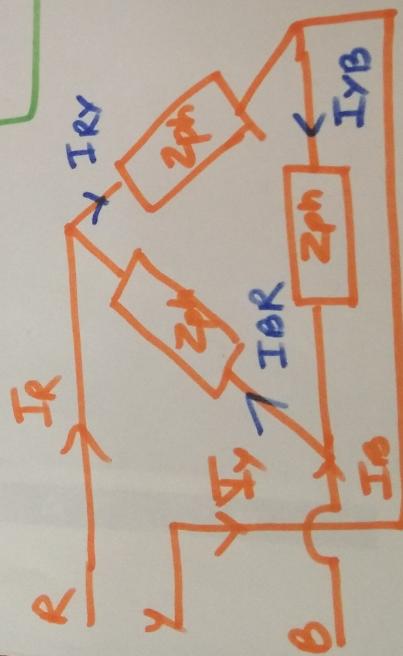
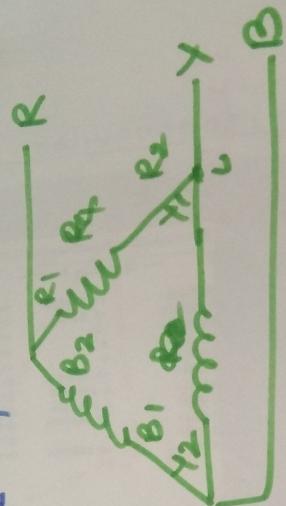
$$= 3 V_{ph} I_{ph} \cos \phi$$

$$V_L = \sqrt{3} V_{ph}, \quad I_L = I_{ph}$$

$$P = \frac{3 \times V_L \times I_L \cos \phi}{\sqrt{3}}$$

$$P = \sqrt{3} V_L I_L \cos \phi$$

Delta connection:-



$$I_{ph} = I_{RY} = \frac{I_Y B - I_B Y}{Z_{RY}}$$

$$I_{BR}$$

$$I_L = I_R = I_Y = I_B$$

$$\bar{I}_R + \bar{I}_{BR} = \bar{I}_{RY}$$

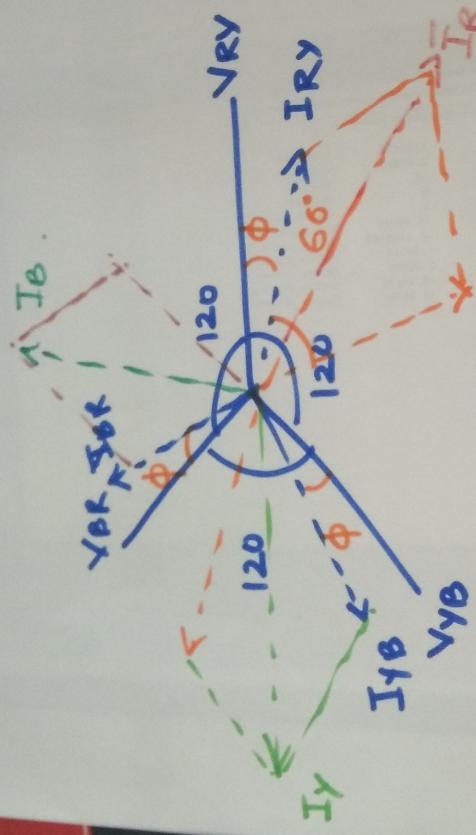
$$\bar{I}_R = \bar{I}_{RY} + (-\bar{I}_{BR})$$

$$\bar{I}_Y + \bar{I}_{RY} = \bar{I}_{YB} + (-\bar{I}_{RY})$$

$$\bar{I}_Y = \bar{I}_{YB} + (-\bar{I}_{RY})$$

Phaser diagram :-

(6)



$$I_R^2 = I_{RY}^2 + I_{BR}^2 + 2 I_{RY} I_{BR} \cos(120^\circ - \phi)$$

$$I_L^2 = I_{ph}^2 + I_{ph}^2 + 2 I_{ph} I_{ph} \cos 60^\circ$$

$$I_L = 3 I_{ph}$$

$$\boxed{I_L = \sqrt{3} I_{ph}}$$

$$P = 3 \times \text{power in each phase}$$

$$= 3 \times I_{ph} \times V_{ph} \cos \phi$$

$$= 3 V_L \times I_L \cos \phi$$

$$= 3 V_L \times \frac{I_L}{\sqrt{3}} \cos \phi$$