Do we need demographic data to forecast plant population dynamics?

Andrew T. Tredennick[1]*, **Mevin B. Hooten[2,3,4], and Peter B. Adler[1]**

[1]*Department of Wildland Resources and the Ecology Center, 5230 Old Main Hill, Utah State University,*

Logan, Utah 84322, USA; [2]*U.S. Geological Survey, Colorado Cooperative Fish and Wildlife Research Unit,*

Fort Collins, CO 80523, USA; [3]*Department of Fish, Wildlife, and Conservation Biology, Colorado State*

University, Fort Collins, CO 80523 USA; [4]*Department of Statistics, Colorado State University, Fort Collins,*

CO 80523 USA

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Corresponding author:

Andrew Tredennick (atredenn@gmail.com)

Department of Wildland Resources and the Ecology Center

5230 Old Main Hill

Utah State University

Logan, Utah 84322, USA

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Summary

1 Rapid environmental change has generated growing interest in forecasts of future popu-
lation trajectories. Traditional population models built with detailed demographic obser-

*Corresponding author: E-mail: atredenn@gmail.com

vations from one study site can address the impacts of environmental change at particular locations, but are difficult to scale up to the landscape and regional scales relevant to management decisions. An alternative is to build models using population-level data which are much easier to collect than individual-level data over broad spatial scales. However, it is unknown whether models built using population-level data adequately capture the effects of density-dependence and environmental forcing that are necessary to generate skillful forecasts.

2 Here, we test the consequences of aggregating individual responses when forecasting the population states (percent cover) and trajectories of four perennial grass species in a semi-arid grassland in Montana, USA. We parameterized two population models for each species, one based on individual-level data (survival, growth and recruitment) and one on population-level data (percent cover), and compared their forecasting accuracy and forecast horizons with and without the inclusion of climate covariates. For both models we used Bayesian ridge regression to weight the influence of climate covariates for optimal prediction.

3 In the absence of climate effects, we found no significant difference between the forecast accuracy of models based on individual-level data and models based on population-level data. Climate effects were weak, but increased forecast accuracy for two species. Increases in accuracy with climate covariates were similar between model types.

4 In our case study, percent cover models generated forecasts as accurate as those from a demographic model. For the goal of forecasting, models based on aggregated individual-level data may offer a practical alternative to data-intensive demographic models. Long time series of percent cover data already exist for many plant species. Modelers should exploit these data to predict the impacts of environmental change.

Key-words: forecasting, climate change, grassland, integral projection model, population model, statistical regularization, ridge regression

Introduction

Perhaps the greatest challenge for ecology in the 21st century is to forecast the impacts of environmental change (Clark et al. 2001, Petchey et al. 2015). Forecasts require sophisticated modeling approaches that fully account for uncertainty and variability in both ecological process and model parameters (Luo et al. 2011, but see Perretti et al. 2013). The increasing statistical sophistication of population models (Rees and Ellner 2009) makes them promising tools for predicting the impacts of environmental change on species persistence and abundance. But reconciling the scales at which population models are parameterized with the scales at which environmental changes play out remains a challenge (Clark et al. 2010, 2012, Freckleton et al. 2011, Queenborough et al. 2011). Most population models are built using demographic data from a single study site because tracking the fates of individuals is so difficult. The resulting models cannot be applied to the landscape and regional scales relevant to decision-making without information about how the estimated parameters respond to spatial variation in biotic and abiotic drivers (Sæther et al. 2007). The limited spatial extent of individual-level demographic datasets constrains our ability to use population models to address applied questions about the consequences of climate change.

Aggregate measures of population status, rather than individual performance, offer an intriguing alternative for modeling populations (Clark and Bjørnstad 2004, Freckleton et al. 2011). Population-level data cannot provide inference about demographic mechanisms, but might be sufficient for modeling future population states, especially because population-level data, such as plant percent cover, are feasible to collect across broad spatial extents (e.g., Queenborough et al. 2011). The choice between individual and population-level data involves a difficult trade-off: while individual-level data are necessary for mechanistic models, population-level data enable models that can be applied over greater spatial and temporal extents. An open question is how much forecasting skill is lost when we build models based on population rather than individual-level data.

To date, most empirical population modelers have relied on individual-level data, with few attempts to capitalize on population-level measures. An important exception was an effort by Taylor and Hastings (2004) to model the population growth rate of an invasive species to identify the best strategies for invasion control. They used a "density-structured" model where the state variable is a discrete density state rather than a continuous density measure. Such models do not require individual-level demographic data and can adequately describe population dynamics. Building on Taylor and Hastings (2004), Freckleton et al. (2011) showed that density-structured models compare well to continuous models in theory, and Queenborough et al. (2011) provide empirical evidence that density-structured models are capable of reproducing population dynamics at landscape spatial scales, even if some precision is lost when compared to fully continuous models. Density-structured models based on animal counts have also begun to find a home in dynamic species distribution models (Mieszkowska et al. 2013, Hefley and Hooten 2016). However, previous tests of density-structured population models have yet to assess their ability to forecast out-of-sample observations, and they have not included environmental covariates, which are necessary to forecast population responses to climate change.

Addressing climate change questions with models fit to population-level data is potentially problematic. Population growth (or decline) is the outcome of demographic processes such as survival, growth, and recruitment that occur at the level of individual plants. Climate can affect each demographic process in unique, potentially opposing, ways (Dalgleish et al. 2011). These unique climate responses may be difficult to resolve in statistical models based on population-level data where demographic processes are not identifiable. Futhermore, models based on aggregated data may reflect short-term effects of one vital rate more than others whose importance may only emerge over the long-term. For example, a one-year change in a plant species' cover or biomass might reflect individual growth or shrinkage, whereas the long-term trajectory of the population might be more influenced by recruitment. The same is true for density dependence: intraspecific density depedence may act most strongly on vital rates, like recruitment, that are difficult to identify from population-level data. If density dependence and/or important climate effects are missed

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because of the aggregation inherent in population-level data, then population models built with such data will make uninformative or unreliable forecasts.

We compared the forecasting skill (accuracy and precision) of statistical and population models based on aggregated, population-level data with the skill of models based on individual-level data. We used a demographic dataset that tracks the fates of individual plants from four species over 14 years to build two kinds of single-species population models, traditional models using individual growth, survival, and recruitment data and alternative models based on population-level (basal cover) data. We simulated the models to answer two questions motivated by the fact that the effects of intraspecific competition (density dependence) and interannual weather variability act at the level of the individual (Clark et al. 2011). First, can population models fit using aggregated individual-level data (percent cover) adequately capture density dependence to produce forecasts as skillful as those from models fit to demographic data? Second, can population models fit using aggregated data adequately capture the influence of climate on population growth and, in turn, produce forecasts as skillful as those from models fit to demographic data?

Materials and Methods

Overview of analysis

Below we describe our focal plant populations, the population models we use to make predictions, and how we compare model forecasts, but offer a brief overview here. We used two types of data: individual-level data and percent cover data. Using the individual-level data we fit three vital rate regressions (survival, growth, and rectruitment) to build an Integral Projection Model (IPM) for simulating the plant populations. Using the percent cover data we fit a simple, Gompertz-style population growth model, which we refer to as a quadrat-based model (QBM). Both model types (IPM and QBM) we fit and simulate versions with and without climate covariates. We used Bayesian ridge regression to weight the importance of each climate covariate. We then performed cross-validation to assess each model's ability to predict out-of-sample data.

We compared the forecast accuracy (ρ, correlation between observations and predictions) and mean absolute error (MAE) between the IPM and the QBM to test our expectation that the IPM should outperform the QBM. Lastly, we use in-sample forecasts to quantify each model's forecast horizon (Petchey et al. 2015).

Study site and data

Our demographic data come from a northern mixed grass prairie at the Fort Keogh Livestock and Range Research Laboratory near Miles City, Montana, USA ($46°$ 19' N, $105°$ 48' W). The dataset is available on Ecological Archives[1] (Anderson et al. 2011), and interested readers should refer to the metadata for a complete description. The site is 800 m above sea level and mean annual precipitation (1878-2009) is 334 mm, with most annual precipitation falling from April through September. The community is grass-dominated, and we focused on the four most abundant grass species: *Bouteloua gracilis* (BOGR), *Hesperostipa comata* (HECO), *Pascopyrum smithii* (PASM), and *Poa secunda* (POSE) (Fig. 1 and Table 1). *B. gracilis* is a warm-season perennial grass, whereas *H. comata*, *P. smithii*, and *Poa secunda* are cool-season perennial grasses. The growing season begins in early spring (typically in April) and lasts through mid-summer (typically in June).

From 1932 to 1945, individual plants were identified and mapped annually in 44 1-m^2 quadrats using a pantograph. The quadrats were distributed among six pastures, each assigned a grazing treatment of light (1.24 ha/animal unit month), moderate (0.92 ha/aum), and heavy (0.76 ha/aum) stocking rates (two pastures per treatment). In this analysis, we accounted for potential differences among the grazing treatments, but do not focus on grazing×climate interactions. The annual maps of the quadrats were digitized and the fates of individual plants tracked and extracted using a computer program (Lauenroth and Adler 2008, Chu et al. 2014). The permanent quadrats have not been relocated, but their distribution in six different pastures means the data represent a broad spatial distribution for the study area. Daily climate data are available for the duration of

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[1]http://esapubs.org/archive/ecol/E092/143/

the data collection period (1932 - 1945) from the Miles City airport, Wiley Field, 9 km from the study site.

We modeled each grass population based on two levels of data: individual and quadrat. The individual data are the "raw" data. For the quadrat-level data we simply sum individual basal cover for each quadrat by species. This is equivalent to a near-perfect census of quadrat percent cover because measurement error at the individual-level is small (Chu and Adler 2015). Based on these two datasets of 13 year-to-year transitions, we can compare population models built using individual-level data and aggregated, quadrat-level data. At the individual level, we explicitly model three vital rates: growth, survival, and recruitment. At the quadrat level, we model population growth as change in percent cover of quadrats with non-zero cover in year *t* and in year *t-1*, ignoring within-quadrat extirpation and colonization events because they are very rare in our time series ($N = 16$ and $N = 13$, respectively, across all species). Sample sizes for each species and vital rate model are shown in Table 1.

All R code and data necessary to reproduce our analysis is archived on GitHub as release v1.0[2] (http://github.com/atredennick/MicroMesoForecast/releases). We have also deposited the v1.0 release on Dryad (*link here after acceptance*).

Statistical models of vital rates

At both levels of inference (individual and quadrat), the building blocks of our population models are vital rate regressions. For individual-level data, we fit regressions for survival, growth, and recruitment for each species. At the quadrat-level, we fit a single regression model for population growth. We describe the statistical models separately because they required different approaches. For both model types, we fit vital rate models with and without climate covariates. Models with climate effects contain five climate covariates that we chose *a priori* based on previous model selection efforts using these data (Chu et al. 2016) and expert advice (Lance Vermeire, *personal*

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[2]*Note to reviewers*: so that v1.0 will be associated with the published version of the manuscript, we have released v0.2 to be associated with this review version.

communication): "water year" precipitation at *t*-2 (lagppt); April through June precipitation at *t*-1 and *t* (ppt1 and ppt2, respectively) and April through June temperature at *t*-1 and *t* (TmeanSpr1 and TmeanSpr2, respectively), where *t*-1 to *t* is the transition of interest. We also include interactions among same-year climate covariates (e.g., ppt1 × TmeansSpr1), resulting in a total of seven climate covariates.

We fit all models using a hierarchical Bayesian approach. We focus on the main process and the model likelihood in what follows (full model descriptions are in the Supporting Information). For the likelihood models, $\mathbf{y}^X$ is always the relevant vector of observations for vital rate X ($X = S$, G, R, or P) for survival, growth, recruitment, or population growth). For example, $\mathbf{y}^S$ is a vector of 0s and 1s indicating whether a genet survives from *t* to *t+1*, or not, for all observation years and quadrats. All model parameters are species-specific, but we omit subscripts for species in model descriptions below to reduce visual clutter. For brevity, we only describe models with climate covariates included, but models without climate covariates are simply the models described below with the climate effects removed.

Vital rate models at the individual level   We used logistic regression to model the probability that genet *i* in quadrat *q* survives from time *t* to *t+1* ($s_{i,q,t}$):

$$y^S_{i,q,t} \sim \text{Bernoulli}(s_{i,q,t}), \tag{1}$$

$$\text{logit}(s_{i,q,t}) = \beta_{0,t} + \beta_{s,t}x_{i,q,t} + \beta_{Q,q} + \mathbf{z}'_t\boldsymbol{\beta}_c + \beta_{d,1}w_{i,t} + \beta_{d,2}(x_{i,q,t}w_{i,q,t}), \tag{2}$$

where $x_{i,q,t}$ is the log of genet *i* basal area at time *t*, $\beta_{0,t}$ is a year specific intercept, $\beta_{Q,q}$ is the random effect of the *q*th quadrat to account for spatial location, $\beta_{s,t}$ is the year-specific slope parameter for size, $\mathbf{z}$ is a vector of *p* climate covariates specific to year *t*, $\boldsymbol{\beta}_c$ is a vector of fixed climate effects of length *p*, $\beta_{d,1}$ is the effect of intraspecific crowding experienced by the focal genet at time *t* ($w_{i,q,t}$), and $\beta_{d,2}$ is a size by crowding ($x_{i,q,t}w_{i,q,t}$) interaction effect.

We follow the approach of Chu and Adler (2015) to estimate crowding, assuming that the crowding experienced by a focal genet depends on distance to each neighbor genet and the neighbor's

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size, u:

$$w_{i,q,t} = \sum_k e^{-\delta d_{ik,q,t}^2} u_{k,q,t}. \tag{3}$$

In equation 3, $w_{i,q,t}$ is the crowding that genet i in year t experiences from k conspecific neighbors ($u_{k,q,t}$) in quadrat q. The spatial scale over which conspecific neighbors exert influence on any genet is determined by δ. The function is applied for all k conspecific genets that neighbor the focal genet at time t, and $d_{ik,q,t}$ is the distance between genet i and conspecific genet k in quadrat q. We use regression-specific (survival and growth) δ values estimated by Chu and Adler (2015).

We modeled growth as a Gaussian process describing log genet size ($y_{i,q,t+1}^G$) at time $t + 1$ in quadrat q as a function of log size at time t and climate covariates:

$$y_{i,q,t+1}^G \sim \text{Normal}(\mu_{i,q,t+1}, \sigma_{x_{i,q,t+1}}^2), \tag{4}$$

$$\mu_{i,q,t+1} = \beta_{0,t} + \beta_{s,t} x_{i,q,t} + \beta_{Q,q} + \mathbf{z}_t' \boldsymbol{\beta}_c + \beta_{d,1} w_{i,q,t} + \beta_{d,2}(x_{i,q,t} w_{i,q,t}), \tag{5}$$

where $\mu_{i,q,t+1}$ is log of genet is predicted size at time t + 1, and all other parameters are as described for the survival regression. We capture non-constant error variance in growth by modeling the variance in the growth regression ($\sigma_{xi,q,t+1}^2$) as a nonlinear function of predicted genet size:

$$\sigma_{x_{i,q,t+1}}^2 = a \exp[b \times \mu_{i,q,t+1}], \tag{6}$$

where $\mu_{i,q,t+1}$ is log of predicted genet size predicted from the growth regression (Eq. 4), and a and b are constants.

Our data allows us to track new recruits, but we cannot assign a specific parent to new genets. Therefore, we model recruitment at the quadrat level. We assume the number of individuals, $y_{q,t+1}^R$, recruiting at time $t + 1$ in quadrat q follows a negative binomial distribution:

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$$y_{q,t+1}^{R} \sim \text{NegBin}(\lambda_{q,t+1}, \phi), \tag{7}$$

where λ is the mean intensity and ϕ is the size parameter. We define λ as a function of quadrat composition and climate in the previous year:

$$\lambda_{q,t+1} = \tilde{c}_{q,t} \exp\left(\beta_{0,t} + \beta_{Q,q} + \mathbf{z}_t' \boldsymbol{\beta}_c + \beta_d \sqrt{\tilde{c}_{q,t}} \right), \tag{8}$$

where $\tilde{c}_{q,t}$ is effective cover (cm^2) of the focal species in quadrat q at time t, and all other terms are as in the survival and growth regressions. Effective cover is a mixture of observed cover (c) in the focal quadrat (q) and the mean cover across the entire group ($\bar{c}$) of Q quadrats in which q is located:

$$\tilde{c}_{q,t} = p c_{q,t} + (1 - p) \bar{c}_{Q,t}, \tag{9}$$

where p is a mixing fraction between 0 and 1 that is estimated when fitting the model.

Population model at the quadrat level   The statistical approach used to model aggregated data depends on the type of data collected. We have percent cover data, which can easily be transformed to proportion data in our case because plant areas were scaled by plot area. An obvious choice for fitting a linear model to proportion data is beta regression because the support of the beta distribution is (0,1), which does not include true zeros or ones. However, when we used fitted model parameters from a beta regression in a quadrat-based population model, the simulated population tended toward 100% cover for all species. We therefore chose a modeling approach based on a truncated log-normal likelihood. The model for quadrat cover change from time t to $t + 1$ is

$$y_{q,t+1}^{P} \sim \text{LogNormal}(\mu_{q,t+1}, \sigma^2)_0^1, \tag{10}$$

$$\mu_{q,t+1} = \beta_{0,t} + \beta_{s,t} x_{q,t} + \beta_{Q,q} + \mathbf{z}_t' \boldsymbol{\beta}_c, \tag{11}$$

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where $\mu_{q,t+1}$ is the log of proportional cover in quadrat q at time $t + 1$, and all other parameters are as in the individual-level growth model (Eq. 4) except that x now represents log of proportional cover. The log normal likelihood includes a truncation (subscript 0, superscript 1) to ensure that predicted values do not exceed 100% cover.

Model fitting and statistical regularization

Model fitting   Our Bayesian approach to fitting the vital rate models required choosing appropriate priors for unknown parameters and deciding which, if any, of those priors should be hierarchical. For each species, we fit yearly size effects and yearly intercepts hierarchically, where year-specific coefficients were drawn from global distributions representing the mean size effect and intercept. Quadrat random effects were also fit hierarchically, with quadrat offsets being drawn from distributions with mean zero and a shared variance term (independent Gaussian priors). Climate effects were modeled as independent covariates whose prior distributions were optimized for prediction using statistical regularization (see **Statistical regularization: Bayesian ridge regression** below).

All of our analyses (model fitting and simulating) were conducted in R (R Core Team 2013). We used the 'No-U-Turn' Hamiltonian Monte Carlo sampler in Stan (Stan Development Team 2014a) to estimate the posterior distributions of model parameters using the package `rstan` (Stan Development Team 2014b). We obtained posterior distributions for all model parameters from three parallel MCMC chains run for 1,000 iterations after discarding an initial 1,000 iterations. Such short MCMC chains are possible because the Stan sampler reduces the number of iterations needed to achieve convergence. We assessed convergence visually and checked that scale reduction factors for all parameters were less than 1.1. There were six instances where the scale reduction factor for a particular parameter was greater than 1.1. In those cases, we checked the traceplots of the violating parameter and discovered that one chain, out of three, was poorly behaved. Therefore, we removed that chain from the analysis, leaving two well-mixed and converged chains for those six parameters. For the purposes of including parameter uncertainty

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265 in our population models, we retained the final 1,000 iterations from each of the three MCMC

266 chains to be used as randomly drawn values during population simulation. We report the poste-

267 rior mean, standard deviation, and 95% Bayesian Credible Intervals for every parameter of each

268 model for each species in the Supporting Information (Tables S5-S20).

Statistical regularization: Bayesian ridge regression For models with climate covari-

270 ates, our objective is to model the response of our focal grass species to interannual variation in

271 climate, even if those responses are weak. Therefore, we avoid selecting among models with all

272 possible combinations of climate covariates, and instead use Bayesian ridge regression to regu-

273 late, or constrain, the posterior distributions of each climate covariate (Gerber et al. 2015, Hooten

274 and Hobbs 2015). Ridge regression is a specific application of statistical regularization that seeks

275 to optimize model generality by trading off bias and variance. As the name implies, statistical reg-

276 ularization involves the use of a regulator that constrains an optimization. The natural regulator in

277 a Bayesian application is the prior on the coefficient of interest. Each of our statistical models in-

278 cludes the effects of climate covariates via the term $\mathbf{z}'_t\boldsymbol{\beta}_c$ with prior $\boldsymbol{\beta}_c \sim \mathrm{Normal}(\boldsymbol{\mu}_{\beta_c}, \sigma^2_{\beta_c}\mathbf{I})$. Be-

279 cause we standardized all climate covariates to have mean zero and variance one, we set $\boldsymbol{\mu}_{\beta_c} = 0$

280 and let $\sigma^2_{\beta_c}$ serve as the regulator that shrinks covariates toward zero – the smaller the prior vari-

281 ance, the more the posteriors of $\boldsymbol{\beta}_c$ are shrunk toward zero, and the stronger the penalty (Hooten

282 and Hobbs 2015).

283 To find the optimal penalty (i.e., optimal value of the hyperparameter $\sigma^2_{\beta_c}$), we fit each statistical

284 model with a range of values for $\sigma^2_{\beta_c}$ and compared predictive scores from leave-one-year-out

285 cross-validation. We performed the grid search over 24 values of $\sigma^2_{\beta_c}$, ranging from $\sigma^2_{\beta_c} = 0.01$

286 to $\sigma^2_{\beta_c} = 2.25$. For each statistical model and each species, we fit $13 \times 24 = 312$ iterations of

287 the model fitting algorithm to search $\sigma^2_{\beta_c}$ for the optimal value (13 years to leave out for cross-

288 validation and 24 values of $\sigma^2_{\beta_c}$) – a total of 4,992 model fits. We calculated the log pointwise

289 predictive density (*lppd*) to score each model's ability to predict the left-out data (Gelman et al.

290 2014). Thus, for training data y_{train} and held-out data y_{hold} at a given value of σ^2_θ across all MCMC

samples $s = 1, 2, ..., S$ and all hold outs of data from year t to year T, and letting θ represent all unknowns, *lppd* is

$$\text{lppd}_{\text{CV}} = \sum_{t=1}^{T} \log_e \int [y_{t,\text{hold}}|\theta][\theta|y_{\text{train}}]d\theta, \tag{12}$$

and computed as

$$\sum_{t=1}^{T} \log_e \left(\frac{1}{S} \sum_{s=1}^{S} (y_{t,\text{hold}}|\theta_{ts}) \right). \tag{13}$$

We chose the optimal prior variance for each species-statistical model combination as the one that produced the highest *lppd* and then fit each species-statistical model combination using the full data set for each species and the optimal prior variance. We calculated the *lppd* from posterior samples using the algorithm from Vehtari et al. (2016).

Population models

Using samples from the posterior distribution of the vital rate statistical models, it is straightforward to simulate the population models. We used an Integral Projection Model (IPM) to simulate populations based on individual-level data (Ellner and Rees 2006) and a quadrat-based version of an individually-based model (Quadrat-Based Model, QBM) to simulate populations based on quadrat-level data. We describe each in turn.

Integral projection model   We use a stochastic IPM (Rees and Ellner 2009) to simulate our focal populations based on the vital rate regressions described above. In all simulations, we ignore the random year effects so that interannual variation is driven solely by climate. We fit the random year effects in the vital rate regressions to avoid over-attributing variation to climate covariates. Our IPM follows the specification of Chu and Adler (2015) where the population of species j is $n(u_j, t)$, giving the density of sized-u genets at time t. Genet size is on the natural log scale, so that $n(u_j, t)du$ is the number of genets whose area (on the arithmetic scale) is between e^{u_j} and $e^{u_j + du}$. The function for any size v at time $t + 1$ is

$$n(v_j, t+1) = \int_{L_j}^{U_j} k_j(v_j, u_j, \bar{w}_j(u_j))n(u_j, t)du_j, \tag{14}$$

where $k_j(v_j, u_j, \bar{w}_j)$ is the population kernel that describes all possible transitions from size u to v and $\bar{w}_j$ is a scalar representing the average intraspecific crowding experienced by a genet of size u_j and species j. The integral is evaluated over all possible sizes between predefined lower (L) and upper (U) size limits that extend beyond the range of observed genet sizes.

The IPM is spatially-implicit, thus, we cannot calculate neighborhood crowding for specific genets (w_{ij}). Instead, we use an approximation ($\bar{w}_j$) that captures the essential features of neighborhood interactions (Adler et al. 2010). This approximation relies on a 'no-overlap' rule for conspecific genets to approximate the overdispersion of large genets in space (Adler et al. 2010).

The population kernel is defined as the joint contributions of survival (S), growth (G), and recruitment (R):

$$k_j(v_j, u_j, \bar{w}_j) = S_j(u_j, \bar{w}_j(u_j))G_j(v_j, u_j, \bar{w}_j(u_j)) + R_j(v_j, u_j, \bar{w}_j), \tag{15}$$

which means we are calculating growth (G) for individuals that survive (S) from time t to $t+1$ and adding in newly recruited (R) individuals of an average sized one-year-old genet for the focal species. Note the S, G, and R are incorporated in the IPM using the fitted vital rate regressions. Our statistical model for recruitment (R, described above) returns the number of new recruits produced per quadrat. Following previous work (Adler et al. 2012, Chu and Adler 2015), we assume that fecundity increases linearly with size ($R_j(v_j, u_j, \bar{w}_j) = e^{u_j}R_j(v_j, \bar{w}_j)$) to incorporate the recruitment function in the spatially-implicit IPM.

We used random draws from the final 1,000 iterations from each of three MCMC chains for each vital rate regression to carry-through parameter uncertainty into our population models. At each time step, we drew the full parameter set (climate effects and density-dependence fixed effects) from a randomly selected MCMC iteration. Relatively unimportant climate covariates

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337 (those that broadly overlap 0) will have little effect on the mean of the simulation results, but can

338 contribute to their variation. To retain temporal variation associated with random year effects, we

339 used posterior estimates of the mean temporal effect and the standard deviation of that effect to

340 generate a random year effect for unobserved years. That is, for some future year T, the intercept

341 is $\beta_{0,T} \sim \text{Normal}(\beta_0, \sigma_{\beta_0})$ and the effect of size is $\beta_{s,T} \sim \text{Normal}(\beta_s, \sigma_{\beta_s})$.

342 **Quadrat-based model**   To simulate our quadrat-based model (QBM), we iterate the quadrat-

343 level statistical model (Eqs. 9-10). We use the same approach for drawing parameter values

344 as described for the IPM. After drawing the appropriate parameter set, we calculate the mean

345 response (log cover at $t+1$ is μ_{t+1}) according to Eq. 10. We make a random draw from a [0,1]

346 truncated lognormal distribution with mean equal to μ_{t+1} from Eq. 10 and the variance estimate

347 from the fitted model. We project the model forward by drawing a new parameter set (unique

348 to climate year and MCMC iteration) at each timestep. Random year effects are included as

349 described above for the IPM.

350 **Model validation**

351 To test each model's ability to forecast population states, we made out-of-sample predictions

352 using leave-one-year-out cross validation. For both levels of modeling and for models with and

353 without climate covariates, we fit the vital rate models using observations from all years except

354 one, and then used those fitted parameters in the population models to perform a one-step-ahead

355 forecast for the year whose observations were withheld from model fitting. We made predic-

356 tions for each observed quadrat in each focal year, initializing each simulation with cover in the

357 quadrat the previous year. Because we were making quadrat-specific predictions, we incorpo-

358 rated the group random effect on the intercept for both models. We repeated this procedure for

359 all 13 observation years, making 100 one-step-ahead forecasts for each quadrat-year combination

360 with parameter uncertainty included via random draw from the MCMC chain as described above.

361 As described above, year-specific parameters for left-out data were drawn from the posterior

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distribution of the mean intercept.

This cross-validation procedure allowed us to compare the accuracy and precision of the two modeling approaches (IPM versus QBM) with and without climate covariates. We first calculated the median predicted cover across the 100 simulations for each quadrat-year and then calculated forecast skill as the correlation (ρ) between forecasts and observations. We calculated forecast error as mean absolute error (MAE) between forecasts and observations. We compared ρ and MAE between model types and within model types between models with and without climate covariates using one-sided *t* tests with adjusted degrees of freedom following Wilcox (2009) and standard errors calculated using the HC4 estimator of Cribari-Neto (2004). Statistical tests for comparing correlations and error were conducted using algorithms from Ye et al. (2015).

Forecast horizons

An important feature of any forecasting model is the rate at which forecast skill declines as the time between an observation and a forecast increases. In particular, we are interested in the temporal distance at which forecast skill falls below a threshold: the so-called ecological forecast horizon (Petchey et al. 2015). To assess the forecast horizons of our models, we initiate the forecast model with the population state at some time *t* and make sequential forecasts of the population at times $t + 1, t + 2, \ldots, t + T$ where *T* is the maximum number of years between the initial year and the final year of our observations. For example, if we initialize the forecast model with percent cover in 1940, we are able to make five forecasts up to the year 1945. Forecast models are not re-initialized with observations between years. Thus, in our current example, the model forecast for percent cover in 1941 has a forecast horizon of one year, the forecast in 1942 has a forecast horizon of two years, and so on. We performed these simulations for all model types (IPM with/without climate; QBM with/without climate) using mean parameter values for all possible initial years. For a given forecast distance, we averaged the correlation between forecasts and observations. Note that these forecasts are all made using in-sample data because we used

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model fits from the full data set. Nonetheless, these simulations offer insight into the differences among model forecast horizons. We chose a forecast accuracy of $\rho = 0.5$ as our forecast proficiency threshold. So, the forecast horizon is the temporal distance at which forecast accuracy falls below $\rho = 0.5$.

Results

The IPM and QBM generated one-step-ahead forecasts of similar skill for out-of-sample observations, with an average correlation between predictions and observations (ρ) of 0.72 across all models and species (Fig. 2). Without climate covariates, the accuracy of forecasts from the IPM were not statistically greater than the accuracy of forecasts from the QBM (Fig. 2) and overall error was similar (mean absolute error; Fig. S1, Supporting Information). With climate covariates, the best out-of-sample predictive model (highest *lppd*) for each species and vital rate typically resulted from highly constrained priors on the climate effects (Fig. S2, Supporting Information). Thus, the posterior distributions of climate effects included in our models overlapped zero and generally shrunk toward zero, though for some species-vital rate combinations, important effects (80% credible interval does not include zero) did emerge (Fig. 3).

Despite the weak climate effects, including climate covariates did increase the accuracy of forecasts for two species: *B. gracilis* and *Poa secunda* (Fig. 2). However, only for *B. gracilis* were the skill increases statistically significant at $\alpha = 0.05$ for the IPM ($t_{(279)} = 1.70$, $P = 0.045$) and the QBM ($t_{(279)} = 1.80$, $P = 0.037$). Similarly, forecast error decreased significantly with the inclusion of climate covariates for the *B. gracilis* IPM ($t_{(280)} = -3.72$, $P = 0.029$) and QBM ($t_{(280)} = -3.34$, $P < 0.0001$), and for the *Poa secunda* IPM ($t_{(196)} = -1.90$, $P < 0.0001$) and QBM ($t_{(196)} = -2.47$, $P = 0.007$) (Fig. S2, Supporting Information). In no case did including climate covariates significantly decrease forecast skill (Table S21), despite small changes in the mean skill (Fig. 2).

IPM forecasts were significantly more accurate than the QBM in only one case (Fig. 2): forecast accuracy of *P. smithii* percent cover from an IPM with climate covariates was greater than the

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accuracy from the QBM with climate covariates ($t_{(215)} = 1.92$, $P = 0.028$). However, adding climate covariates decreased the skill of both models, and the difference between the IPM and QBM emerges only because skill decreased less for the IPM than the QBM. Results from all pairwise statistical tests are shown in Table S22 of the Supporting Information.

With climate covariates included \textcolor{blue{and using mean parameter values, the accuracy of both models' forecasts declined as the distance between the last observation and the forecast increased}, but they did so at similar rates (Fig. 4). The only exception is for *Poa secunda*, where QBM forecast accuracy remained steady as the temporal distance of the forecast increased, whereas IPM forecast accuracy declined (Fig. 4). The forecast horizons were short: forecast accuracy fell below $\rho = 0.5$ after one year for the IPM for most species, and after four years, at most, for the QBM (Fig. 4). Across the different temporal distances from the observation to the forecast, the IPM was never more accurate than the QBM (Table S23). Likewise, the QBM was rarely more accurate the IPM, the only exception being for *H. comata* at temporal distances of two ($t_{(115)} = 2.39$, $P = 0.002$) and three years ($t_{(98)} = 2.04$, $P = 0.022$) (Table S24). There were some cases where the QBM was more accurate than the IPM for *Poa secunda*, but neither model exceeded the forecast profieciency threshold by a large margin (Fig. 4, Table S24).

Discussion

Our comparison of a traditional, demographic population model without environmental forcing (the IPM) to an equivalent model inspired by density-structured models (the QBM) showed that, generally, IPM forecasts of out-of-sample plant population states were no more accurate than forecasts from the QBM (Fig. 2; 'no-climate' bars). This result overturned our expectation that the IPM would out-perform the QBM, thanks to its mechanistic representation of the perennial life cycle, and confirms theoretical (Freckleton et al. 2011) and empirical work (Taylor and Hastings 2004, Queenborough et al. 2011) showing that density-structured models can be useful surrogates for demographic models when the goal is to estimate or forecast population states over

large spatial extents.

We also expected the inclusion of environmental forcing to reveal more differences between the models. Interannual variation in weather can affect vital rates in different ways (Dalgleish et al. 2011), so, estimates of climate effects on plant population growth may be biased or non-identifiable when the underlying statistical model is fit using population-level data that integrates over the potentially unique climate responses of individual vital rates. We found some evidence that the QBM failed to detect climate effects for three species (*B. gracilis*, *H. comata*, and *Poa secunda*), where important climate effects were identified in the individual vital rate models but not in the percent cover model (Fig. 3). However, for the two species where including climate covariates increased forecast accuracy (*B. gracilis* and *Poa secunda*), forecast skill (Fig. 2) and error (Fig. S2) were equivalent between the IPM and QBM.

The higher accuracy of the IPM and QBM with climate covariates for *B. gracilis* and *Poa secunda* highlights the advantage of contemporary modeling and variable selection approaches such as ridge regression and LASSO over techniques that would exclude "non-significant" effects from final models. Ridge regression allows researchers to retain covariates whose effects may be difficult to identify in noisy data or short time series. This is especially important when forecasting the impacts of climate variability, where it is important to include to effects of forcing variables (e.g., temperature and precipitation) even if such effects are difficult to identify. Indeed, we failed to detect strong climate effects in the QBM for *B. gracilis* and *Poa secunda*, but including climate covariates still improved forecasting skill (Fig. 2). If a species is truly unresponsive to a given climate variable, statistical regularization techniques will shrink the mean and variance of a covariate estimate toward zero (Hooten and Hobbs 2015). Of course, no matter what model selection approach is adopted, a critical step is identifying the appropriate candidate covariates, which we attempted to do based on our knowledge of this semi-arid plant community. However, the climate covariates we chose required aggregating daily weather data over discrete time periods. It is possible that we did not choose the optimal time periods over which to aggregate. New methods using functional linear models (or splines) may offer a data-driven approach for identi-

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fying the appropriate time periods over which to aggregate to produce a tractable set of candidate climate variables (Teller et al. 2016).

We also expected IPM forecast accuracy to decline at a lower rate than the QBM as the time between the last observation and the forecast increased. In principle, more mechanistic models should produce better predictions, especially under novel conditions (Evans 2012, Schindler and Hilborn 2015). In our case, the IPM explicitly models the influence of weather on recruitment and survival, effects that may be poorly represented in the QBM because recruitment and survival mainly affect small plants that contribute little to year-to-year changes in percent cover. Over time, of course, the addition and subtraction of small plants can have large effects on population growth, so explicitly modeling these effects could contribute to a longer forecast horizon. However, we found no evidence that the forecast horizon for the IPM was greater than the QBM (Fig. 4). On the contrary, the QBM tended to have a slightly longer forecast horizon than the IPM for most species (Fig. 4). The QBM has fewer processes, so may better capture near term dynamics when populations do not fluctuate widely, as in our case. When populations do not fluctuate widely, often the best forecast for population size at *t+1* is the size at time *t*. Thus, a simpler model such as the QBM may be well-suited for predicting populations that fluctuate mildly around an equilibrium.

Our comparison of a model based on individual-level data with one based on percent cover data is not an exhaustive test. Understanding the reasons why the percent cover-based model matched the skill of a demographic model for our focal species may help us anticipate situations in which a percent-cover approach would fail. First, for none of our species did a climate covariate have a strong negative effect on one vital rate and a strong positive effect on a different vital rate (Fig. 3). As noted by Freckleton et al. (2011), complex age or stage structure can compromise predictions from models that aggregate over life-histories, and the same should be true when aggregating across vital rates with contrasting responses to climate drivers. Second, our particular recruitment model is already so aggregated – it averages across seed production, germination and establishment – that it may fail to detect important demographic responses to climate, putting our

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individual-based model and percent cover model on more equal footing. More finely resolved recruitment data might help our individual-based model outperform the population-level model. As advocated by Freckleton et al. (2011), knowledge of a species' population ecology should guide the modeling approach. Third, our percent cover data are essentially error-free because we were able to aggregate indiviual plant areas to calculate percent cover. Percent cover data collected by typical sampling protocals (e.g., Daubenmire frames) will include error that would affect population forecasts due to misspecifing the initial conditions and/or biasing model parameters (Queenborough et al. 2011). Thus, it may be that our percent cover model performed just as well as the individual-based model because percent cover was perfectly measured. One way to account for such error is to develop a sampling model that relates the observations (estimated percent cover in a plot) to the true state (percent cover derived from individual plant measurements in the same plot) (Hobbs and Hooten 2015).

Although our main goal was to compare individual-based and population-level modeling approaches relative to one another, it is worth reflecting on the absolute forecasting skill of our models. In particular, the forecast horizon of both models, defined as the time horizon at which the correlation between predictions and observations falls below $\rho = 0.5$, is less than five years for all species. Such short forecast horizons are not encouraging. Unfortunately, we have little to offer on how to improve population forecasts that has not already been proposed (Mouquet et al. 2015, Petchey et al. 2015). Longer time-series should improve our ability to detect exogenous drivers such as climate (Teller et al. 2016), and modeling larger spatial extents may reduce parameter uncertainty (Petchey et al. 2015). We may also have to shift our perspective from making explicit point forecasts to making moving average forecasts (Petchey et al. 2015). For example, Integral Projection Models are typically capable of estimating equilibrium abundances (e.g., Adler et al. 2012), which may be more appropriate for dynamic systems.

In conclusion, we found that models based on individual-level demographic data generally failed to generate more skillful population forecasts than models based on population-level data. This finding runs counter to our expectations, but is consistent with recent theoretical (Freckleton et

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al. 2011) and empirical work (Queenborough et al. 2011). Moreover, for the two species where including climate covariates improved forecast skill, both models generated equally skillful one-step-ahead forecasts. Thus, we conclude that models based on population-level data, rather than individual-level data, may be adequate for forecasting the states and dynamics of plant populations. Unfortunately, our analysis, where climate effects were relatively unimportant in vital rate regressions, did not allow us to sufficiently test our prediction that individual-level data is neccessary to generate skillful forecasts if different vital rates respond to climate in unique, potentially opposing, ways. Nonetheless, our results are encouraging for the use of easy-to-collect population-level data for forecasting the state of plant populations.

Acknowledgments

Data Accessibility

The data used in this paper have been archived on Ecological Archives: http://esapubs.org/ archive/ecol/E092/143/. All data and R code necessary to reproduce our work has been deposited on Figshare (link) and is also available on GitHub (http://github.com/atredennick/ MicroMesoForecast).

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Tables

Table 1: Description of data. The observations span 13 year-to-year transitions.

| Species	Vital Rate Model	Num. Obs.	Num. Quadrats
B. gracilis	Growth	5670	29
	Survival	10102	33
	Recruitment	304	33
	Percent cover	281	29
H. comata	Growth	1990	16
	Survival	3257	18
	Recruitment	304	18
	Percent cover	171	17
P. smithii	Growth	8052	19
	Survival	11344	19
	Recruitment	304	19
	Percent cover	217	19
Poa secunda	Growth	3018	18
	Survival	4650	18
	Recruitment	304	18
	Percent cover	197	18

Figures
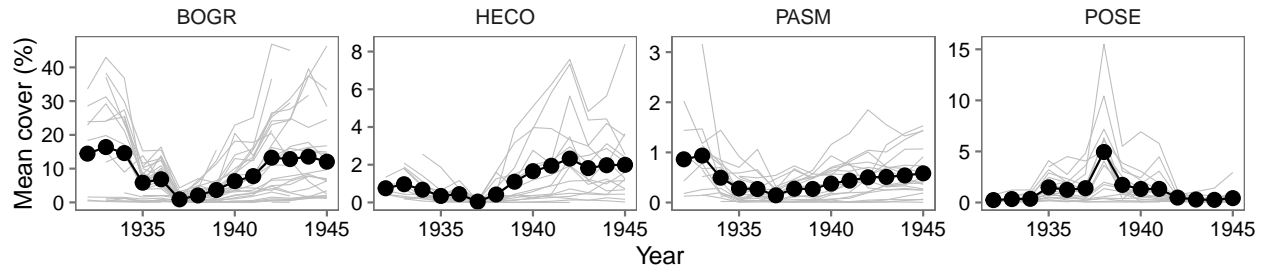
Figure 1: Time series of average percent cover over all quadrats for our four focal species: *Bouteloua gracilis* (BOGR), *Hesperostipa comata* (HECO), *Pascopyrum smithii* (PASM), and *Poa secunda* (POSE). Light grey lines show trajectories of individual quadrats. Note the different y-axis scales across panels. See Table 1 for sample size information.
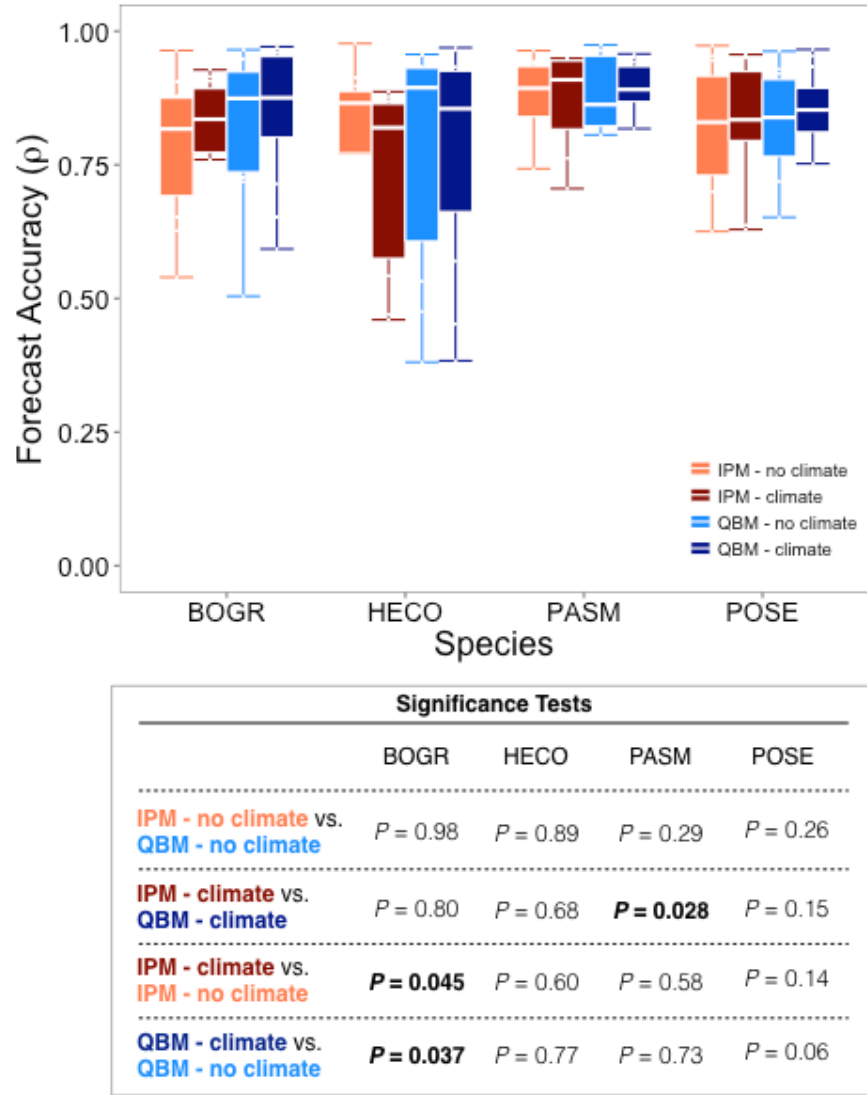
Figure 2: Comparisons of one-step-ahead, out-of-sample forecast accuracy between the IPM and QBM models with and without the inclusion of climate covariates. Boxplots show the distribution of ρ averaged over quadrats for each cross-validation year (i.e., 13 values of ρ for each species-model combination). For each comparison, P-values are from one-sided t tests designed to assess whether the first model in the comparison statement had higher accuracy than the second model in the comparison statement (see details in Table S22). Statistical tests relied on correlation values for each quadrat-year-species combination, after averaging over model reps for each combination. In no case did adding climate covariates decrease forecast accuracy (Table S21). Species codes are as in Fig. 1.
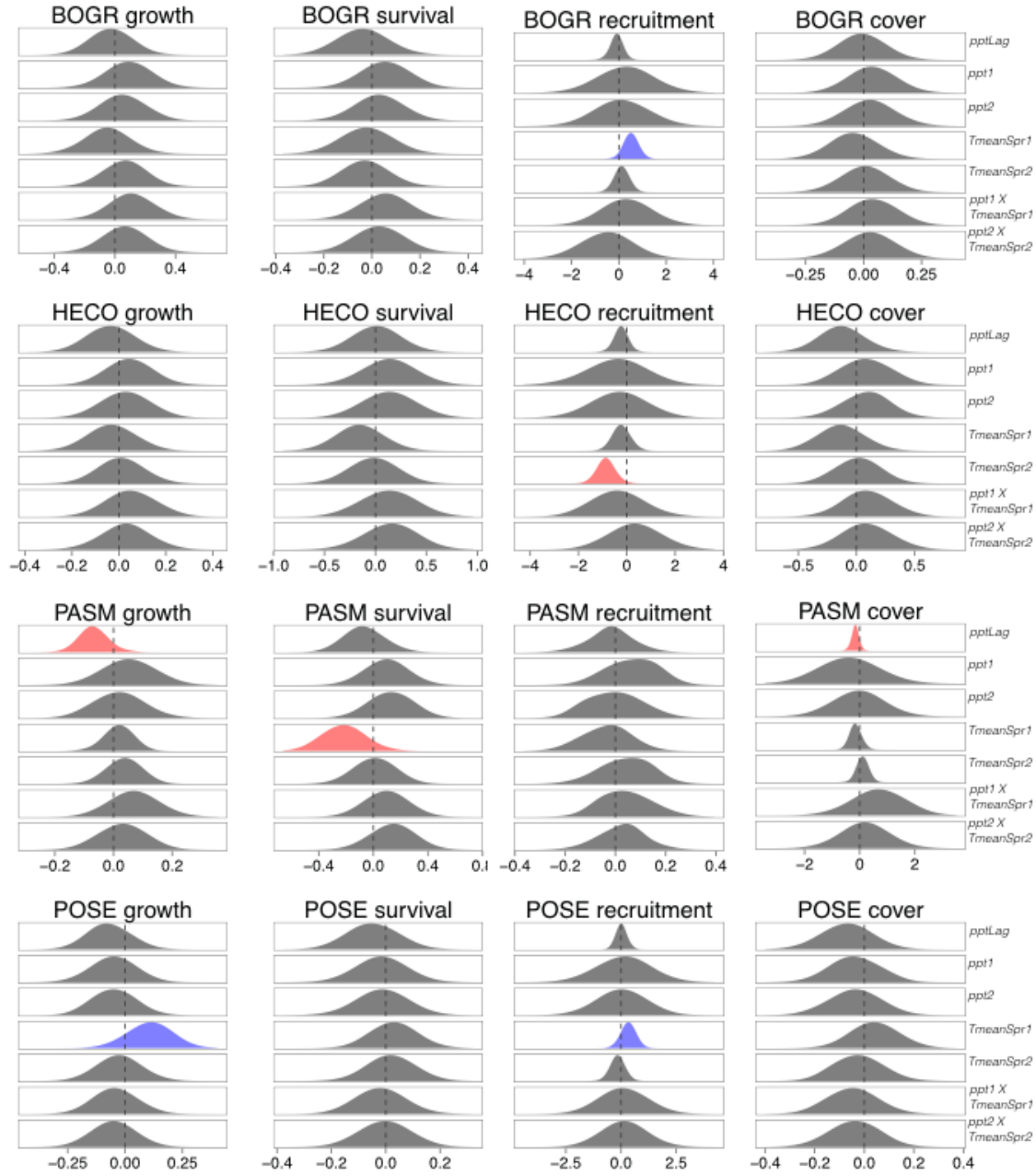
Figure 3: Posterior distributions of climate effects (β_C) for each species and vital rate statistical model. Because our priors were constrained via ridge-regression, we highlight climate effects whose 80% credible intervals do not overlap zero (red for negative coefficients, blue for positive coefficients). Kernel bandwidths of posterior densities were adjusted by a factor of 4 for visual clarity. Species codes are as in Fig. 1. Climate covariate codes: *pptLag* = "water year" precipitation at *t*-2; *ppt1* = April through June precipitation at *t*-1; *ppt2* = April through June precipitation at *t*; *TmeanSpr1* = April through June temperature at *t*-1; *TmeanSpr2* = April through June temperature at *t*.
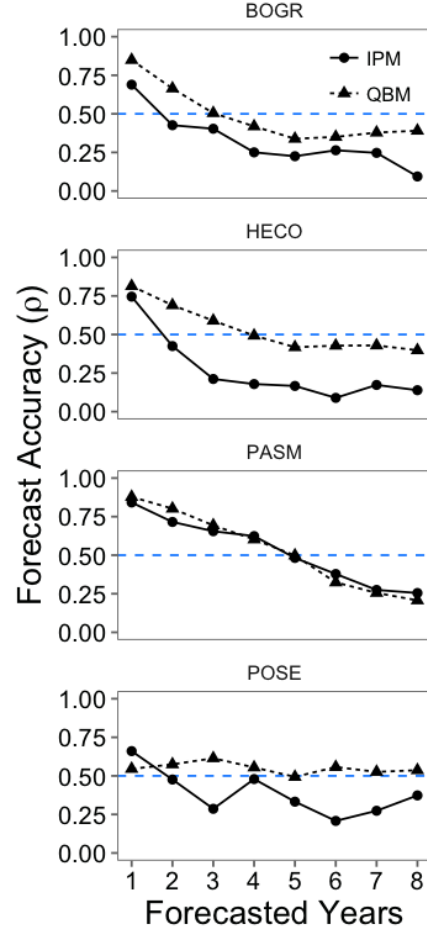
Figure 4: The forecast horizons for both models with climate covariates included and using mean parameter values. Points show the average accuracy (ρ, correlation between observations and predictions) across all forecasts at a given distance between the last observation and the forecast, where forecasts are made for in-sample data. We only examine the forecast accuracy of models with climate covariates included because in no case did including climate covariates significantly decrease accuracy (see Fig. 2). The dashed blue line indicates a forecast proficiency threshold of $\rho = 0.5$. Species codes are as in Fig. 1 and statistical comparisons between the IPM and QBM at each forecast distance are in Tables S23 and S24.

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