Do we need demographic data to forecast populationresponses to climate change?

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Summary

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- 1. Rapid climate change has generated growing interest in forecasts of future population trajectories. Traditional population models, typically built using detailed demographic observations from one study site, can address climate change impacts at one location, but are difficult to scale up to the landscape and regional scales relevant to management decisions.

 An alternative is to build models using population-level data that are much easier to collect over broad spatial scales than individual-level data. However, such models ignore the fact that climate drives population growth through its influence on individual performance.
 - 2. Here, we test the consequences of aggregating individual responses when forecasting climate change impacts on four perennial grass species in a semi-arid grassland in Montana, USA. We parameterized two population models for each species, one based on individual-level data (survival, growth and recruitment) and one on population-level data (percent cover), and compared their accuracy, precision, and sensitivity to climate variables. For both models we used Bayesian ridge regression to identify the optimal predictive model in

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terms of climate covariate strengths.

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- 23 3. The individual-level model was more accurate and precise than the aggregated model when
 24 predicting out-of-sample observations. When comparing climate effects from both models,
 25 the population-level model missed important climate effects from at least one vital rate
 26 for each species. Increasing the sample size at the population-level would not necessarily
 27 reduce forecast uncertainty; the way to reduce uncertainty is to capture unique climate
 28 dependence of individual vital rates.
- 4. *Synthesis*. Our analysis indicates that there is no shortcut to forecasting climate change impacts on plant populations detailed demographic data are essential. Despite the superiority of the individual-level model, the forecasts it generated still were too uncertain to be useful for decision-makers. We need new methods to collect demographic data efficiently across environmental gradients in space and time.
- Key-words: forecasting, climate change, grassland, integral projection model, population model

35 Introduction

- Perhaps the greatest challenge for ecology in the 21st century is to forecast the impacts of envi-
- ronmental change (Clark et al. 2001, Petchey et al. 2015). Forecasts require sophisticated mod-
- eling approaches that fully account for uncertainty and variability in both ecological process and
- model parameters (Luo et al. 2011, but see Perretti et al. 2013 for an argument against modeling
- the ecological process). The increasing statistical sophistication of population models (Rees and
- 41 Ellner 2009) makes them promising tools for predicting the impacts of environmental change
- on species persistence and abundance. But reconciling the scales at which population models
- 43 are parameterized and the scales at which environmental changes play out remains a challenge
- (Clark et al. 2010, 2012, Freckleton et al. 2011, Queenborough et al. 2011). The problem is that
- most population models are built using data from a single study site because collecting those data,

- which involves tracking the fates of individuals plants, is so difficult. The resulting models cannot
- be applied to the landscape and regional scales relevant to decision-making without information
- 48 about how the fitted parameters respond to spatial variation in biotic and abiotic drivers (Sæther
- et al. 2007). The limited spatial extent of individual-level demographic datasets constrains our
- ability to use population models to address applied questions about the consequences of climate
- 51 change.
- The inability of most population models to address landscape-scale problems may explain
- why land managers and conservation planners have embraced species distribution models
- (SDMs) (see Guisan and Thuiller 2005 for a review). SDMs typically rely on easy-to-collect
- presence/absence data (but see Clark et al. 2014 for new methods) and remotely-sensed
- environmental covariates that allow researchers to model large spatial extents (e.g., Maiorano et
- 57 al. 2013). Thus, it is relatively straightforward to parameterize and project SDMs over landscapes
- and regions. However, the limitations of SDMs are well known (Pearson and Dawson 2003, Elith
- and Leathwick 2009, Araújo and Peterson 2012). Ideally, researchers would provide managers
- with landscape-scale population models, combining the extent of SDMs with information about
- dynamics and species abundances (Schurr et al. 2012, Merow et al. 2014).
- 62 Aggregate measures of population status, rather than individual performance, offer an intrigu-
- ing alternative for modeling populations (Clark and Bjørnstad 2004, Freckleton et al. 2011).
- Population-level data cannot provide inference about demographic mechanisms, but might be
- sufficient for modeling future population states, especially since such data are feasible to collect
- 66 across broad spatial extents (e.g., Queenborough et al. 2011). The choice between individual
- and population-level data involves a difficult trade-off: while individual-level data leads to more
- 68 mechanistic models, population-level data leads to models that can be applied over greater spa-
- tial and temporal extents. An open question is how much forecasting skill is lost when we build
- models based on population rather than individual-level data.
- To date, most empirical population modelers have relied on individual-level data, with few at-

tempts to capitalize on population-level measures. An important exception was an effort by Taylor and Hastings (2004) to model the population growth rate of an invasive species to identify the best strategies for invasion control. They used a "density-structured" model where the state variable is a discrete density state rather than a continuous density measure. Such models do not require individual-level demographic data and can adequately describe population dynamics. Building on Taylor and Hastings (2004), Freckleton et al. (2011) showed that density-structured models compare well to continuous models in theory, and Queenborough et al. (2011) provide empirical evidence that density-structured models are capable of reproducing population dynamics at landscape spatial scales, even if some precision is lost when compared to fully continuous 80 models. The appeal of density-structured approaches is clear. However, none of these models 81 included environmental covariates. Addressing climate change questions with models fit to population-level data is potentially problematic. It is individuals, not populations, that respond to climate variables (Clark et al. 2012). Ignoring this fact amounts to an "ecological fallacy", where inference about the individual relies on statistical inference on the group (Piantadosi et al. 1988). Population growth (or decline) is the outcome of demographic processes such as survival, growth, and recruitment that occur at the level of individual plants. Climate can affect each demographic process in unique, potentially opossing, ways (Dalgleish et al. 2011). These unique climate responses may be difficult to resolve in statistical models based on population-level data where demographic processes are not identifiable. If important climate effects are missed because of the aggregation inherent in in population-level data, then population models built with such data will make uninformative or unreliable forecasts. Here, we compare the forecasting skill of statistical and population models based on aggregated, population-level data with models based on individual-level data. We used a unique demographic dataset that tracks the fates of individual plants from four species over 14 years to build two kinds of single-species population models, traditional models using individual growth, survival,

and recruitment data and alternative models based on basal cover. In both models, interannual

variation is explained, in part, by climate covariates. We first quantify forecasting skill using cross-validation. We then performed simulations to quantify the sensitivities of species' cover to small perturbations in average precipitation and temperature. Based on the cross-validation results, predictions of individual level models were clearly better, but, unfortunately, still too uncertain to inform management decisions.

Our demographic data come from the Fort Keogh Livestock and Range Research Laboratory in

eastern Montana's northern mixed prairie near Miles City, Montana, USA (46° 19' N, 105° 48'

Materials and Methods

105 Study site and data

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W). The dataset is freely available on Ecological Archives² (Anderson et al. 2011), and inter-108 ested readers should refer to the metadata for a complete description. The site is about 800 m 109 above sea level and mean annual precipitation (1878-2009) is 334 mm, with most annual precipi-110 tation falling from April through September. The community is grass-dominated and we focused 111 on the four most abundant grass species: Bouteloua gracilis (BOGR), Hesperostipa comata 112 (HECO), Pascopyrum smithii (PASM), and Poa secunda (POSE) (Fig. 1). 113 From 1932 to 1945 individual plants were identified and mapped annually in 44 1-m² quadrats using a pantograph. The quadrats were distributed in six pastures, each assigned a grazing treatment of light (1.24 ha/animal unit month), moderate (0.92 ha/aum), and heavy (0.76 ha/aum) stocking rates (two pastures per treatment). In this analysis we account for potential differences among the grazing treatments, but do not focus on grazing×climate interactions. The annual maps of the 118 quadrats were digitized and the fates of individual plants tracked and extracted using a computer 119 program (Lauenroth and Adler 2008, Chu et al. 2014). Daily climate data are available for the 120 duration of the data collection period (1932 - 1945) from the Miles City airport, Wiley Field, 9 121 km from the study site. 122

²http://esapubs.org/archive/ecol/E092/143/

We modeled each grass population based on two levels of data: individual and quadrat (Fig. 2).

The individual data is the "raw" data. For the quadrat-level we data we simply sum individual
basal cover for each quadrat by species. This is equivalent to a near-perfect census of quadrat
percent cover because previous analysis shows that measurement error at the individual-level is
small (Chu and Adler 2014). Based on these two datasets we can compare population models
built using individual-level data and aggregated, quadrat-level data.

All R code and data necessary to reproduce our analysis is archived on GitHub as release v1.0³

All R code and data necessary to reproduce our analysis is archived on GitHub as release v1.0³
(http://github.com/atredennick/MicroMesoForecast/releases). That stable release will remain
static as a record of this analysis, but subsequent versions may appear if we update this work. We
have also deposited the v1.0 release on Dryad (*link here after acceptance*).

Stastical models of vital rates

At both levels of inference (individual and quadrat), the building blocks of our population models are vital rate regressions. For individual-level data, we fit regressions for survival, growth, 135 and recruitment for each species. At the quadrat-level, we fit a single regression model for pop-136 ulation growth. We describe the statistical models separately since fitting the models required 137 different approaches. All models contain five climate covariates that we chose a priori: "water 138 year" precipitation at t-1 (lagppt); April through June precipitation at t-1 and t-2 (ppt1 and ppt2, 139 respectively) and April through June temperature at t-1 and t-2 (TmeanSpr1 and TmeanSpr2, 140 respectively), where t is the observation year. We also include interactions among same-year 141 climate covariates (e.g., ppt1 \times TmeansSpr1) and climate \times size interactions. Climate \times size 142 interactions are for climate main effects only; we do not include interactions between size and 143 pairs of interacting climate effects. 144

We fit all models using a hierarchical Bayesian approach. The models are fully descibed in Appendix A, so here we focus on the main process and the model likelihood. For the likelihood

³Note to reviewers: so that v1.0 will be associated with the published version of the manuscript, we have released v0.1 to be associated with this review version.

models, \mathbf{y}^X is always the relevant vector of observations for vital rate X (X = S, G, R, orP for survival, growth, recruitment, or population growth). For example, \mathbf{y}^S is a vector of 0's and 1's indicating whether a genet survives from t to t+1, or not.

Vital rate models at the individual level We used logistic regression to model survival probability (S) of genet i from species j in quadrat group Q from time t to t+1:

$$logit(S_{ijQ,t}) = \gamma_{i,t}^{S} + \phi_{iQ}^{S} + \beta_{i,t}^{S} x_{ij,t} + \omega_{i}^{S} w_{ij,t} + \nu_{i}^{S} w_{ij,t} x_{ij,t} + \theta_{ik}^{S} C_{k,t}$$
(1)

$$y_{ijQ,t}^S \sim \text{Bernoulli}(S_{ijQ,t})$$
 (2)

where $x_{ij,t}$ is the log of genet size, $\gamma_{j,t}^S$ is a year-specific intercept, $\beta_{j,t}^S$ is the year-specific slope parameter for size, ϕ^S_{jQ} is the random effect of quadrat group location, and θ^S_k is the fixed pa-153 rameter for the effect of the kth climate covariate at time t ($C_{k,t}$). Note that the vector of climate 154 covariates (C) includes climate variable interactions and climate x size interactions. We include 155 density-dependence by estimating the effect of crowding on the focal individual by other individ-156 uals of the same species. ω is the effect of crowding and $w_{t,Q}$ is the crowding experienced by the 157 focal individual at time t in quadrat group Q. We include a size×crowding interaction effect (ν^S). 158 We modeled growth as a Gaussian process describing genet size at time t+1 as a function of size 159 at t and climate covariates: 160

$$x_{ijQ,t+1} = \gamma_{j,t}^G + \phi_{jQ}^G + \beta_{j,t}^G x_{ij,t} + \omega_j^G w_{ij,t} + \nu_j^S w_{ij,t} x_{ij,t} + \theta_{jk}^G C_{k,t}$$
 (3)

$$y_{ijQ,t}^G \sim \text{Normal}(x_{ijQ,t+1}, \varepsilon_{ij,t})$$
 (4)

where x is log genet size and all other parameters are as described for the survival regression.

We capture non-constant error variance in growth by modeling the variance around the growth

regression (ε) as a nonlinear function of predicted genet size:

$$\varepsilon_{ij,t} = ae^{bx_{ijQ,t+1}} \tag{5}$$

Our data allows us to track new recruits, but we cannot assign a specific parent to new genets.

Therefore, we model recruitment at the quadrat level: the number of new individuals of species jin quadrat q recruiting at time t+1 as a function of quadrat "effective cover" (A') in the previous
year (t). Effective cover is a mixture of observed cover (A) in the focal quadrat (q) and the mean
cover across the entire group (\bar{A}) of Q quadrats in which q is located:

$$A'_{jq,t} = p_j A_{jq,t} + (1 - p_j) \bar{A}_{jQ,t}$$
(6)

where p is a mixing fraction between 0 and 1 that is estimated within the model.

We assume the number of individuals, y^R , recruiting at time t+1 follows a negative binomial distribution:

$$y_{jq,t+1}^R \sim \text{NegBin}(\lambda_{jq,t+1}, \zeta)$$
 (7)

where λ is the mean intensity and ζ is the size parameter. We define λ as:

$$\lambda_{jq,t+1} = A'_{jq,t} e^{(\gamma_{j,t}^R + \phi_{jQ}^R + \theta_{jk}^R C_{k,t} + \omega^R \sqrt{A'_{q,t}})}$$
(8)

where A' is effective cover (cm²) of species j in quadrat q and all other terms are as in the survival and growth regressions.

Population model at the quadrat level The statistical approach used to model aggregated data depends on the type of data collected. We have percent cover data, which can easily be trans-176 formed to proportion data. We first considered fitting three vital rate models analogous to those 177 we fit at the individual level: one for probability of extirpation within a quadrat (analagous to 178 survival), one for cover change within a quadrat (analagous to growth), and one for probability 179 of colonization within a quadrat (analagous to recruitment). However, within-quadrat extirpation 180 and colonization events were rare in our time series (N = 9 and N = 10, respectively, across all 181 species). Given the broad spatial distribution of the quadrats we are studying, it is safe to assume 182 that these events are in fact rare enough to be ignored for our purposes. So we constrained our sta-183 tistical modeling of vital rates at the population level to change in percent cover within quadrats. 184 For the remaining discussion of statistical modeling, we refer to proportion data, which is simply 185 percent cover divided by 100. 186 An obvious choice for fitting a linear model to proportion data is beta regression because the 187 support of the beta distribution is [0,1], not including true zeros or ones. However, when we 188

support of the beta distribution is [0,1], not including true zeros or ones. However, when we used fitted model parameters from a beta regression in a quadrat-based population model, the simulated population tended toward 100% cover for all species. We therefore chose a more constrained modeling approach based on a truncated log-normal likelihood. The model for quadrat cover change from time t to t+1 is

$$x_{jq,t+1} = \gamma_{j,t}^{P} + \phi_{jQ}^{P} + \beta_{j,t}^{P} x_{jq,t} + \theta_{jk}^{P} C_{k,t}$$
(9)

$$y_{jq,t+1}^P \sim \text{LogNormal}(x_{jq,t+1}, \tau_j) \mathbf{T}[0, 1]$$
(10)

where $x_{jq,t}$ is the log of species' j proportional cover in quadrat q at time t and all other parameters are as in the individual-level growth model (Eq. 3). Again, note that the climate covariate vector (\mathbf{C}) includes the climate×cover interaction. The log normal likelihood includes a truncation (T[0,1]) to ensure that predicted values do not exceed 100% cover.

Model fitting and stastical regularization

Model fitting Our Bayesian approach to fitting the vital rate models required choosing ap-198 propriate priors for unknown parameters and deciding which, if any, of those priors should be 199 hierarchical. We decided to fit models where all terms were fit by species. Within a species, we 200 fit yearly size effects and yearly intercepts hierarchically where year-specific coefficients were 201 drawn from global distributions representing the mean size effect and intercept. Quadrat random 202 effects were also fit hierarchically, with quadrat offsets being drawn from distributions with mean 203 zero and a shared variance term (independent Gaussian priors, Appendix A). Climate effects were 204 not modeled hierarchically, and each was given a diffuse prior distribution. We used standard 205 diffuse priors for all unknown parameters (Appendix A). 206 All of our analyses (model fitting and simulating) were conducted in R (R Core Team 2013). We 207 used the 'No-U-Turn' MCMC sampler in Stan (Stan Development Team 2014a) to estimate the 208 posterior distributions of model parameters using the package 'rstan' (Stan Development Team 209 2014b). We obtained posterior distributions for all model parameters from three parallel MCMC 210 chains run for 1,000 iterations after discarding an initial 1,000 iterations. Such short MCMC 211 chains may surprise readers more familiar with other MCMC samplers (i.e. JAGS or WinBUGS), 212 but the Stan sampler is exceptionally efficient, which reduces the number of iterations needed to 213 achieve convergence. We assessed convergence visually and made sure scale reduction factors 214 for all parameters were less than 1.01. For the purposes of including parameter uncertainty in our 215 population models, we saved the final 1,000 iterations from each of the three MCMC chains to 216 be used as randomly drawn values during population simulation. This step alleviates the need 217 to reduce model parameters by model selection since sampling from the full parameter space 218 in the MCMC ensures that if a parameter broadly overlaps zero, on average the effect in the 219 population models will also be near zero. We report the posterior mean, standard deviation, and 220 95% Bayesian Credible Intervals for every parameter of each model for each species in Appendix 221 В. 222

Statistical regularization: Bayesian ridge regression Our objective is to model the response of our focal grass species to interannual variation in climate, even if those responses are 224 weak. Therefore, we avoid selecting among models with all possible combinations of climate 225 covariates, and instead use Bayesian ridge regression to regulate, or constrain, the posterior dis-226 tributions of each climate covariate (Hooten and Hobbs 2015). Ridge regression is a specific 227 application of statistical regularization that seeks to optimize model generality by trading off bias 228 and variance. As the name implies, statistical regularization involves the use of a regulator that 229 constrains an optimization. The natural regulator in a Bayesian application is the prior on the 230 coefficient of interest. Each of our statistical models includes the effects of climate covariates 231 via the term $\mathbf{c}'\boldsymbol{\theta}$ with prior $\boldsymbol{\theta} \sim \text{Normal}(\boldsymbol{\mu}_{\boldsymbol{\theta}}, \sigma_{\boldsymbol{\theta}}^2)$. Since we standardized all climate covariates, 232 including interaction terms, to have mean zero and variance one we can set $\mu_{\theta}=0$, letting σ_{θ}^2 233 serve as the regulator that can shrink covariates toward zero – the smaller the prior variance, the 234 more θ is shrunk toward zero, and the stronger the penalty (Hooten and Hobbs 2015). 235 To find the optimal penalty (i.e., optimal value of the hyperparameter σ_{θ}^2), we fit each statistical 236 model with a range of values for σ_{θ}^2 and compared predictive scores from leave-one-year-out 237 cross-validation. We performed the grid search over 24 evenly-spaced values of σ_{θ}^2 , ranging from 238 $\sigma_{\theta}^2 = 0.01$ to $\sigma_{\theta}^2 = 2.25$. For each statistical model and each species we fit $13 \times 24 = 312$ models (13 years to leave out for cross-validation and 24 values of σ_{θ}^2) – a total of 4992 models. We calculated the log pointwise predictive density (lppd) to score each model's ability to predict the left-out data. Thus, for training data y_{train} and held-out data y_{hold} at a given value of σ_{θ}^2 across all MCMC samples s = 1, 2, ..., S and all hold outs of data from year t to year T, lppd is

$$lppd_{CV} = \sum_{t=1}^{T} log_e \int [y_{t,hold}|\theta] [\theta|y_{train}] d\theta,$$
(11)

244 and computed as

$$\sum_{t=1}^{T} \log_e \left(\frac{1}{S} \sum_{s=1}^{S} (y_{t,hold} | \theta_{ts}) \right). \tag{12}$$

We chose the optimal prior variance for each species-statistical model combination as the one that produced the highest lppd and then fit each species-statistical model combination using the full data set for each species and the optimal prior variance. In some cases lppd was highest at the highest (most vague) value of prior variance, in which case we explored a slightly expanded range of prior variances (e.g., $\sigma_{\theta}^2 > 2.25$).

Population models

With the posterior distribution of the vital rate statistical models in hand, it is straightforward to simulate the population models. We used an Integral Projection Model (IPM) to model populations based on individual-level data (Ellner and Rees 2006) and a quadrat-based version of an individually-based model (Quadrat-Based Model, QBM) to model populations based on quadrat-level data. We describe each in turn.

Integral projection model We use a stochastic IPM (Rees and Ellner 2009) that includes
the climate covariates from the vital rate statistical models. In all simulations we ignore the random year effects so that interannual variation is driven solely by climate. We fit the random year
effects in the vital rate regressions to avoid over-attributing variation to climate covariates. Our
IPM follows the specification of Chu and Adler (2015) where the population of species j is a
density function $n(u_j, t)$ giving the density of sized-u genets at time t. Genet size is on the natural log scale, so that $n(u_j, t)du$ is the number of genets whose area (on the arithmetic scale) is
between e^{u_j} and e^{u_j+du} . The density function for any size v at time t+1 is

$$n(v_j, t+1) = \int_{L_j}^{U_j} k_j(v_j, u_j, \bar{w}_j(u_j)) n(u_j, t)$$
(13)

where $k_j(v_j, u_j, \bar{w}_j)$ is the population kernel that describes all possible transitions from size u to v and \bar{w}_j is a scalar representing the average intraspecific crowding experienced by a genet of size u_j and species j. The integral is evaluated over all possible sizes between predefined lower

(L) and upper (U) size limits that extend beyond the range of observed genet sizes.

Since the IPM is spatially-implicit, we cannot calculate neighborhood crowding for specific genets (w_{ij}) . Instead, we use an approximation (\bar{w}_j) that captures the essential features of neighborhood interactions (Adler et al. 2010). This approximation relies on a 'no-overlap' rule for conspecific genets to approximate the overdispersion of large genets in space (Adler et al. 2010). The population kernel is defined as the joint contributions of survival (S), growth (G), and recruitment (R):

which means we are calculating growth (G) for individuals that survive (S) from time t to t+1

$$k_i(v_i, u_i, \bar{w}_i) = S_i(u_i, \bar{w}_i(u_i))G_i(v_i, u_i, \bar{w}_i(u_i)) + R_i(v_i, u_i, \bar{w}_i), \tag{14}$$

and adding in newly recruited (R) individuals of an average sized one-year-old genet for the 275 focal species. Our stastical model for recruitment (R, described above) returns the number of 276 new recruit produced per quadrat. Following previous work (Adler et al. 2012, Chu and Adler 277 2015), we assume that fecundity increases linearly with size $(R_i(v_i, u_i, \bar{w}_i) = e^{u_i}R_i(v_i, \bar{w}_i))$ to 278 incorporate the recruitment function in the spatially-implicit IPM. We used random draws from the final 1,000 iterations from each of three MCMC chains to intro-280 duce stochasticity into our population models. At each time step, we randomly selected climate 281 covariates from one of the 14 observed years. Then, we drew the full parameter set (climate ef-282 fects and density-dependence fixed effects) from a randomly selected MCMC iteration. Using 283 this approach, rather than simply using coefficient point estimates, captures the effect of parame-284 ter uncertainty. Relatively unimportant climate covariates (those that broadly overlap 0) will have 285 little effect on the mean of the simulation results, but can contribute to their variation. Since our 286 focus was on the contribution of climate covariates to population states, we set the random year 287 effects and the random group effects to zero. 288

Quad-based model To simulate our quad-based model (QBM), we simply iterate the quadrat-level statistical model (Eqs. 9-10). We use the same approach for drawing parameter values as described for the IPM. After drawing the appropriate parameter set, we calculate the mean response (population cover at $t+1 = x_{t+1}$) according to Eq. 9. We then make a random draw from a [0,1] truncated lognormal distribution with mean equal to x_{t+1} from Eq. 9 and the variance estimate from the fitted model. We can then project the model forward by drawing a new parameter set (unique to climate year and MCMC iteration) at each timestep. As with the IPM, random year effects are ignored for all simulations.

97 Model validation

To test each model's ability to forecast population state, we made out-of-sample predictions using leave-one-year-out cross validation. For both levels of modeling, we fit the vital rate models 299 using observations from all years except one, and then used those fitted parameters in the popula-300 tion models to perform a one-step-ahead forecast for the year whose observations were withheld 30 from model fitting. Within each observation year, several quadrats were sampled. We made predictions for each observed quadrat in the focal year, initializing each simulation with cover in the quadrat the previous year. Since we were making quadrat-specific predictions, we incorporated the group random effect on the intercept for both models. We repeated this procedure for all 13 observation years, making 100 one-step-ahead forecasts for each quadrat-year combination 306 with parameter uncertainty included via random draw from the MCMC chain as described above. 307 Random year effects were set to zero since year effects cannot be assigned to unobserved years. 308 This cross-validation procedure allowed us to compare accuracy and precision of the two mod-300 eling approaches (IPM versus QBM). We first calculated the median predicted cover across the 310 100 simulations for each quadrat-year and then calculated the absolute error as the absolute value 311 of the difference between the observed cover for a given quadrat-year and the median predic-312 tion. To arrive at mean absolute error (MAE), we then averaged the absolute error within each

species across the quadrat-year specific errors. We use MAE as our measure of accuracy. To measure precision we calculated the distance between the upper and lower 90th quantiles of the 100 predictions and averaged this value over quadrat-years for each species.

Testing sensitivity to climate covariates

With our fitted and validated models in hand, we ran simulations for each model type (IPM 318 and QBM) under four climate perturbation scenarios: (1) observed climate, (2) precipitation in-319 creased by 1%, (3) temperature increased by 1%, and (4) precipitation and temperature increased 320 by 1%. We ran the simulations for 2,500 time steps, enough to estimate equilibrium cover after 321 discarding an initial 500 time steps as burn-in. Each simulation was run under two parameter 322 scenarios: (1) using mean parameter estimates and (2) using randomly drawn parameters from 323 the MCMC chain. We use (1) to detect the overall sensitivity of equilibrium cover to climate, and 324 we use (2) to show the impact of model and parameter uncertainty on forecast precision. 325 As an effort to identify potential discrepencies between IPM and QBM forecasts, we also ran 326 simulations designed to quantify the sensitivities of individual and combined vital rates to cli-327 mate for the IPM. Specifically, we ran simulations for the above climate scenarios, but applied 328 the perturbed climate covariates to survival, growth, or recruitment vital rates individually and 329 in pairwise combinations. This allowed us to isolate the vital rate(s) most sensitive to climate. 330 For this analysis, we used mean parameter estimates to reduce the sources of uncertainty in the 331 sensitivity estimates. 332 We expected the IPM to produce more accurate and precise forecasts due to either (1) the smaller 333 sample size of the quadrat level data sets compared to the individual level data sets, leading to 334 larger parameter uncertainty for the QBM, or (2) the QBM climate effects being weakly associated with one or more vital rate climate effects at the individual level. To assess the impact 336 of sample size on QBM parameter uncertainty we refit the QBM statistical model (Eqs. 9-10) 337 after removing sets of 2, 5, 10, and 15 quadrats. We fit 10 models at each level of quadrat removal (2, 5, 10, 15 quadrats), removing a different randomly selected set of quadrats for each
fit. We calculated the standard deviation of climate main effects (pptLag, ppt1, ppt2, TmeanSpr1,
and TmeanSpr2) for each model and averaged those over replicates within each set of quadrat
removals. This allowed us to regress parameter uncertainty against sample size.

To deterime if the QBM climate effects are correlated with climate effects for each vital rate
model in the IPM, we simply regressed the QBM climate coefficients against each vital rate
model's climate coefficients and calculated Pearson's ρ. Strong correlations indicate the QBM
is capable of detecting climate effects associated with individual vital rates. A weak correlation
indicates the QBM "misses" the climate effect on a particular vital rate.

Results

349 Comparison of forecast models

Sensitivity of models to climate

The response of a population to climate change is a result of the aggregate effects of climate on individual vital rates. Since the IPM approach relies on vital rate regressions, we were able to quantify the sensitivity of each vital rate in isolation and in pairwise combinations. Across all 353 species, climate covariates can have opposing effects on different vital rates (Fig. 3). Growth was the most sensitive vital rate for all species, showing a negative response to increased precipitation, 355 and stronger positive response to increased temperature, and a mostly positive response when 356 both climate factors are increased (Fig. 3). B. gracilis survival rates were sensitive to tempera-357 ture, resulting in an increase in plant cover under increased temperature (Fig. 3a). In isolation, 358 recruitment and survival were insensitive to climate factors for *H. comata* (Fig. 3b). Survival and 359 recruitment of *P. smithii* were both sensitive, negatively, to temperature and precipitation (Fig. 360 3c). P. secunda equilibrium cover was sensitive to the climate effects on survival and recruitment, 361 showing a negative effect on both vital rates for increased precipition, but a strong positive effect 362

on survival with increased temperature (Fig. 3d). Equilibrium cover responded negatively when increased precipitation and temperature affect recruitment (Fig. 3d). At least two of three vital rates were sensitive to climate for each species (Fig. 3).

Sources of uncertainty in the QBM

Sample size had a relatively weak effect on QBM climate parameter uncertainty after the number 367 of quadrats used in fitting exceeded about 10 (Fig. 5). Inverse-gaussian fits show that increasing 368 sample size beyond the number of quadrats we used would result in diminishing returns in terms 369 of parameter certainty (Fig. 5). 370 Climate effects estimated from the QBM are most correlated with climate effects from the growth 371 regression at the individual level (Fig. 6). In no case does the QBM statistical model have strong correlations across all three vital rates (Fig. 6). QBM climate effects were most weakly correlated with those from individual-level recruitment models for B. gracilis, H. comata, and P. secunda (Fig. 6a,b,d). For *P. smithii*, QBM climate effects showed no correlation with the survival model 375 effects (Fig. 6c). 376

77 Model forecasts

Forecasts based on 1% climate changes were extremely uncertain when we considered model 378 error and parameter uncertainty (Fig. 6; simulations with mean parameters are in Appendix D 379 for comparison). As expected based on model validation (Table 1), QBM projections were more 380 uncertain than IPM projections for all species except *P. smithiii* (Fig. 6). IPM forecasts for *P.* 381 smithiii were very uncertain due to a very high instrinsic rate of recruitment combined with un-382 certainty in climate coefficients which lead to high recruitment boom years and subsequent busts 383 when young plants suffer high mortality (Appendx C). When we included model error and parameter uncertainty, forecast changes in proportional cover always spanned a wide range of negative 385 to positive values. In other words, neither model could predict whether a climate perturbation 386

would increase or decrease equilibrium population size.

Discussion

Population models built using individual-level data allow inference on demographic processes, 389 but they can only forecast future population states across the (typically limited) spatial extent of 390 the observations. Population-level data are much easier to collect across broad spatial extents, 391 so models built using such data offer an appealing alternative to traditional population models 392 (Queenborough et al. 2011). However, density-structured models rely on the aggregation of 393 individual-level data. This creates a potential problem if such models are to be used in a climate 394 change context because it is individuals, not populations, which respond to climate (Clark et al. 395 2012). Are models based on population-level metrics as sensitive to climate as models based on 396 individual-level metrics? Do these two types of models produce consistent forecasts? Do we need 397 detailed demographic data to forecast the impacts of climate change? 398

399 The importance of demographic data

Our comparison of a traditional, demographic population model (the IPM) with a model inspired 400 by density-structured models (the QBM) showed that the IPM outperformed the QBM: the IPM 401 was more accurate and precise than the QBM in out-of-sample cross validation (Table 1). The 402 superiority of the IPM could reflect either differences in sample size or the effect of averaging 403 over unique effects of climate on each individual-level vital rate. Although increasing sample size 404 of quadrat percent-cover observations would be easy to do in the field, we found little evidence 405 that it would lead to higher precision of climate coefficient estimates (Fig. 4). 406 We did, however, find evidence that the QBM statistical model failed to identify climate depen-407 dence for some vital rates (Fig. 5). For no species were climate effects from the QBM strongly 408 correlated with all three vital rates (Fig. 5). Freckleton et al. (2011) acknowledge that averaging 409 over complex stage dependence will lead to poorly specified models. This is analogous to our

situation, but instead of averaging over complex life histories, we are averaging over complex climate dependence. Though our work here focused on plant species, this finding is applicable to any species with vital rates that respond uniquely to weather/climate. Our interpretation is that the QBM is "missing" climate signals associated with at least one vital 414 rate for each species. This leads to inaccurate and imprecise forecasts because the QBM statisti-415 cal model struggles to explain variation due to climate variables that have positive and negative 416 impacts on different vital rates. When this is the case, as it is for all our species to varying de-417 grees (Fig. 3), forecasts from models based on population-level data will fail. Our result is consis-418 tent with related work on the importance of individual-level data to forecast population responses 419 to exogenous drivers (Clark et al. 2011a, 2011b, 2012, Galván et al. 2014). 420 Detailed demographic data appears to be necessary to forecast climate change impacts on plant populations when vital rates have unique climate responses. How then can we build models to 422 make forecasts for the landscape and regional scales beyond the scope of traditional population 423 models (Queenborough et al. 2011)? There are alternatives to density-structured models. For 424 example, Clark et al. (2011a) use Forest Inventory and Analysis (FIA) data to parameterize a pop-425 ulation model with multiple vital rates and climate dependence. Distributed efforts such as Plant-426 PopNet (http://plantago.plantpopnet.com) will allow researchers to estimate variation around 427 climate responses for widespread species by taking advantage of spatial variation in climate (e.g. 428 Doak and Morris 2010). Finally, new approaches on the horizon that leverage photo/video of 429 plots and advanced object recognition algorithms (e.g. Liu et al. 2014) will increase the effi-430

The challenge of uncertainty

431

ciency of plant mapping and digitizing efforts.

An important, but unexpected, result of our analysis was the great uncertainty in forecasts, even for our best model. The typical approach in ecology is to use point estimates of model parameters to project populations forward according to the specified model, usually allowing for some vari-

ability around the determinstic process (e.g. Battin et al. 2007, Jenouvrier et al. 2009, Adler et al. 2012). If we follow tradition and calculate the mean response to climate perturbation with only model error and interannual variation included, the IPM and the QBM produce opposing forecasts for three of four species (Fig. D1). It would be tempting to interpret this inconsistency as 439 further evidence for the superiority of the IPM. However, if we introduce parameter uncertainty, 440 the forecasts are actually indistinguishable (Fig. 6), though the IPM projections are generally 441 more precise (consistent with our cross-validation results). The real story is that both models 442 produce highly uncertain forecasts. For all species, the 90% quantiles of predicted changes in 443 population size overlapped zero; we cannot even predict whether a change in precipitation or tem-444 perature will cause populations to increase or decrease. This result held when we tried perturbing 445 climate by 10% and 20% as well. 446 Our results highlight the state of affairs in ecology when it comes to forecasting the impacts of climate change. The analysis we conducted here could be considered at the forefront of ecologi-448 cal forecasting with respect to the statistical approach employed (hierarchical Bayesian), the type of population model we used (density-dependent, stochastic IPM with parameter uncertainty), 450 and the amount of high quality data we had at our disposal (14 years of individual-level data). Yet, model predictions proved so uncertain that any forecast, when bounded with model and parameter uncertainty, would be uninformative. 453 How might we improve on this state of affairs? First, forecasts could be improved by matching 454 the spatial scale of predictor variables with the spatial scale of observations. One of the major 455 limitations of the models we fit here is that the climate data are collected at a larger scale than the 456 individual-level observations of plant size. Climate covariates only vary by year, with no spatial 457 variability within years. Thus, even if we fit models to individual-level data, we are missing the 458 key interaction point between weather and individual plants (Clark et al. 2011b) because all ob-459 servations share the same climate covariates. Demographic studies should be designed with at 460 least plot-level measurements of climate related variables (e.g., soil moisture). Second, accurately detecting climate signals will take even longer time series. Recent theoretical work on detecting

climate signals in noisy data suggests that even advanced approaches to parameter fitting require 20-25 year time series (Teller et al. n.d.). Third, ecologists need a stronger commitment to reporting uncertainty. Although most modeling studies explicitly consider model uncertainty, parameter 465 uncertainty is often ignored. In some cases this is because the most convenient statistical methods 466 make it difficult to propogate parameter uncertainty. Yet even Bayesian approaches that allow 467 integration of model fitting and forecasting (Hobbs and Hooten 2015) are not simple when using 468 modeling approaches like integral projection models that separate the model fitting and simula-469 tion stages (Rees and Ellner 2009). However, as we have done here, it is still possible to include 470 parameter uncertainty by drawing parameter values from MCMC iterations, taking care to draw 471 all parameters from the same chain and iteration to account for their correlations. Only by being 472 honest about our forecasts can we begin to produce better ones, and forecasts reported without 473 parameter error are disingenuous. Ignoring parameter error may be justifiable when the goal is 474 investigating basic processes, but it is indefensible when forecasting is the goal.

476 Conclusions

This work is not a critique of density-structured population models. We are confident that densitystructured models will prove to be a valuable tool for many applications. However, our analysis 478 represents the first comparison, to our knowledge, of population models based on individual and 479 aggregated forms of the same data in a climate change context. Our results confirm theoretical 480 arguments (Clark et al. 2011b) and empirical evidence (Clark et al. 2011a, 2012) that individual 481 responses are critical for predicting species' responses to climate change. It seems there is no 482 short cut to producing accurate and precise population forecasts: we need detailed demographic 483 data to forecast the impacts of climate change on populations. Given the importance of demo-484 graphic data and its current collection cost, we need modern methods to collect demographic data 485 more efficiently across environmental gradients in space and time. 486

Our results also offer a cautionary tale because forecast uncertainty was large for both model

types. Even with 14 years of detailed demographic data and sophisticated modeling techniques,
our projections contained too much uncertainty to be informative. Uncertainty in demographic
responses to climate can be reduced by collecting (1) longer time series and (2) climate covariates
that match the scale of inference (e.g., plot rather than landscape level climate/weather metrics).

92 Acknowledgments

This work was funded by the National Science Foundation through a Postdoctoral Research Fellowship in Biology to ATT (DBI-1400370) and a CAREER award to PBA (DEB-1054040). We
thank the original mappers of the permanent quadrats in Montana and the digitizers in the Adler
lab, without whom this work would not have been possible. Informal conversations with Stephen
Ellner, Giles Hooker, Robin Snyder, and a series of meetings between the Adler and Weecology labs at USU sharpened our thinking. Brittany Teller provided comments that improved our
manuscript. Compute, storage and other resources from the Division of Research Computing
in the Office of Research and Graduate Studies at Utah State University are gratefully acknowledged.

502 Tables

503 Figure Legends

Figure 1. Time series of average percent cover over all quadrats for our four focal species: Bouteloua gracilis (BOGR), Hesperostipa comata (HECO), Pascopyrum smithii (PASM), and Poa secunda (POSE). Light grey lines show trajectories of individual quadrats. Note the different 506 y-axis scales across panels. 507 Figure 2. Work flow of the data aggregation, model fitting, and population simulating. 508 Figure 3. Sensitivity of equilibrium cover simulated from the IPM to each climate scenario applied to individual and combined vital rates. For example, the points associated with G show the 510 median cover from IPM simulations where a climate perturbation is applied only to the growth 511 regression climate covariates. These simulations use mean parameter values for clarity. 512 Figure 4. Effect of quadrat sample size on the precision (standard deviation) of main climate 513 effect estimates in the QBM. Increasing the number of quadrats results in diminishing returns in 514 terms of parameter certainty. Light dashed lines show individual climate effects at five quadrat 515 sample sizes. Thick dark lines are inverse gaussian fits showing the mean effect of increasing 516 quadrat sample size on parameter precision. 517 Figure 5. Correlations (r) between QBM and IPM estimates of climate effects. We ignore sizeX-518 climate interactions since these are not directly comparable across model types. The QBM does 519 not have multiple vital rates, so its values are repeated across panels within each species. Across 520 top panels, 'growth' = growth regression, 'rec' = recruitment regression, 'surv' = survival regres-521 sion. 522 Figure 6. Mean (points) and 90% quantiles (errorbars) for the proportional difference between 523 baseline simulations (using observed climate) and the climate pertubation simulation on the 524 x-axis. We calculated proportional difference as log(perturbed climate cover) - log(observed 525 climate cover), where 'perturbed' and 'observed' refer to the climate time series used to drive 526 interannual variation in the simulations. Model error and parameter uncertainty were propagated 527

through the simulation phase. Climate simulations are as in Figure 3.

529 Figures

References

- Adler, P. B., H. J. Dalgleish, and S. P. Ellner. 2012. Forecasting plant community impacts of
- climate variability and change: when do competitive interactions matter? Journal of Ecology
- 533 100:478–487.
- Adler, P. B., S. P. Ellner, and J. M. Levine. 2010. Coexistence of perennial plants: An embarrass-
- ment of niches. Ecology Letters 13:1019–1029.
- Anderson, J., L. Vermeire, and P. B. Adler. 2011. Fourteen years of mapped, permanent quadrats
- in a northern mixed prairie, USA. Ecology 92:1703.
- Araújo, M. B., and A. T. Peterson. 2012. Uses and misuses of bioclimatic envelope modeling.
- 539 Ecology 93:1527–1539.
- Battin, J., M. W. Wiley, M. H. Ruckelshaus, R. N. Palmer, E. Korb, K. K. Bartz, and H. Imaki.
- ⁵⁴¹ 2007. Projected impacts of climate change on salmon habitat restoration. Proceedings of the
- National Academy of Sciences of the United States of America 104:6720–6725.
- ⁵⁴³ Chu, C., and P. B. Adler. 2014. When should plant population models include age structure?
- Journal of Ecology 102:531–543.
- ⁵⁴⁵ Chu, C., and P. B. Adler. 2015. Large niche differences emerge at the recruitment stage to stabi-
- lize grassland coexistence. Ecological Monographs 85:373–392.
- Chu, C., K. M. Havstad, N. Kaplan, W. K. Lauenroth, M. P. McClaran, D. P. Peters, L. T. Ver-
- meire, and P. B. Adler. 2014. Life form influences survivorship patterns for 109 herbaceous
- perennials from six semi-arid ecosystems. Journal of Vegetation Science 25:947–954.
- ⁵⁵⁰ Clark, J. S., and O. N. Bjørnstad. 2004. Population time series: Process variability, observation
- errors, missing values, lags, and hidden states. Ecology 85:3140–3150.
- ⁵⁵² Clark, J. S., D. M. Bell, M. H. Hersh, and L. Nichols. 2011a. Climate change vulnerability of
- ⁵⁵³ forest biodiversity: Climate and competition tracking of demographic rates. Global Change
- 554 Biology 17:1834–1849.

- ⁵⁵⁵ Clark, J. S., D. M. Bell, M. H. Hersh, M. C. Kwit, E. Moran, C. Salk, A. Stine, D. Valle, and K.
- Zhu. 2011b. Individual-scale variation, species-scale differences: Inference needed to understand
- 557 diversity.
- ⁵⁵⁸ Clark, J. S., D. M. Bell, M. Kwit, A. Stine, B. Vierra, and K. Zhu. 2012. Individual-scale infer-
- ence to anticipate climate-change vulnerability of biodiversity. Philosophical Transactions of the
- 560 Royal Society B: Biological Sciences 367:236–246.
- ⁵⁶¹ Clark, J. S., D. Bell, C. Chu, B. Courbaud, M. Dietze, M. Hersh, J. HilleRisLambers, I. Ibáñez, S.
- LaDeau, S. McMahon, J. Metcalf, J. Mohan, E. Moran, L. Pangle, S. Pearson, C. Salk, Z. Shen,
- D. Valle, and P. Wyckoff. 2010. High-dimensional coexistence based on individual variation: a
- synthesis of evidence. Ecological Monographs 80:569–608.
- ⁵⁶⁵ Clark, J. S., S. R. Carpenter, M. Barber, S. Collins, A. Dobson, J. A. Foley, D. M. Lodge, M.
- Pascual, R. Pielke, W. Pizer, C. Pringle, W. V. Reid, K. A. Rose, O. Sala, W. H. Schlesinger, D.
- H. Wall, and D. Wear. 2001. Ecological forecasts: an emerging imperative. Science (New York,
- 568 N.Y.) 293:657–660.
- ⁵⁶⁹ Clark, J. S., A. E. Gelfand, C. W. Woodall, and K. Zhu. 2014. More than the sum of the parts:
- Forest climate response from joint species distribution models. Ecological Applications 24:990–
- ₅₇₁ 999.
- Dalgleish, H. J., D. N. Koons, M. B. Hooten, C. A. Moffet, and P. B. Adler. 2011. Climate influ-
- ences the demography of three dominant sagebrush steppe plants. Ecology 92:75–85.
- Doak, D. F., and W. F. Morris. 2010. Demographic compensation and tipping points in climate-
- induced range shifts. Nature 467:959–962.
- 576 Elith, J., and J. R. Leathwick. 2009. Species Distribution Models: Ecological Explanation and
- 577 Prediction Across Space and Time.
- Ellner, S. P., and M. Rees. 2006. Integral projection models for species with complex demogra-
- phy. The American naturalist 167:410–428.

- Freckleton, R. P., W. J. Sutherland, A. R. Watkinson, and S. A. Queenborough. 2011. Density-
- structured models for plant population dynamics. American Naturalist 177:1–17.
- 582 Galván, J. D., J. J. Camarero, and E. Gutiérrez. 2014. Seeing the trees for the forest: Drivers of
- individual growth responses to climate in Pinus uncinata mountain forests. Journal of Ecology
- ₅₈₄ 102:1244–1257.
- Guisan, A., and W. Thuiller. 2005. Predicting species distribution: Offering more than simple
- 586 habitat models.
- Hobbs, N. T., and M. B. Hooten. 2015. Bayesian Models: A Statistical Primer for Ecologists.
- Princeton University Press, Princeton.
- Hooten, M. B., and N. T. Hobbs. 2015. A guide to Bayesian model selection for ecologists. Eco-
- 1590 logical Monographs 85:3–28.
- Jenouvrier, S., H. Caswell, C. Barbraud, M. Holland, J. Stroeve, and H. Weimerskirch. 2009.
- Demographic models and IPCC climate projections predict the decline of an emperor penguin
- population. Proceedings of the National Academy of Sciences of the United States of America
- 106:1844-1847.
- Lauenroth, W. K., and P. B. Adler. 2008. Demography of perennial grassland plants: Survival,
- life expectancy and life span. Journal of Ecology 96:1023–1032.
- Liu, Y., Y. Jang, W. Woo, and T.-K. Kim. 2014. Video-Based Object Recognition Using Novel
- 598 Set-of-Sets Representations.
- Luo, Y., K. Ogle, C. Tucker, S. Fei, C. Gao, S. LaDeau, J. S. Clark, and D. S. Schimel. 2011.
- 600 Ecological forecasting and data assimilation in a data-rich era. Ecological Applications 21:1429–
- 601 1442.
- Maiorano, L., R. Cheddadi, N. E. Zimmermann, L. Pellissier, B. Petitpierre, J. Pottier, H.
- Laborde, B. I. Hurdu, P. B. Pearman, A. Psomas, J. S. Singarayer, O. Broennimann, P. Vittoz, A.
- Dubuis, M. E. Edwards, H. A. Binney, and A. Guisan. 2013. Building the niche through time:

- using 13,000 years of data to predict the effects of climate change on three tree species in Europe.
- 606 Global Ecology and Biogeography 22:302–317.
- Merow, C., A. M. Latimer, A. M. Wilson, S. M. McMahon, A. G. Rebelo, and J. A. Silander.
- 2014. On using integral projection models to generate demographically driven predictions of
- species' distributions: development and validation using sparse data. Ecography 37:1167–1183.
- Pearson, R. G., and T. P. Dawson. 2003. Predicting the impacts of climate change on the distri-
- bution of species: Are bioclimate envelope models useful? Global Ecology and Biogeography
- 612 12:361-371.
- Perretti, C. T., S. B. Munch, and G. Sugihara. 2013. Model-free forecasting outperforms the
- 614 correct mechanistic model for simulated and experimental data. Proceedings of the National
- 615 Academy of Sciences of the United States of America 110:5253–5257.
- Petchey, O. L., M. Pontarp, T. M. Massie, S. Kéfi, A. Ozgul, M. Weilenmann, G. M. Palamara, F.
- Altermatt, B. Matthews, J. M. Levine, D. Z. Childs, B. J. McGill, M. E. Schaepman, B. Schmid,
- P. Spaak, A. P. Beckerman, F. Pennekamp, and I. S. Pearse. 2015. The ecological forecast hori-
- zon, and examples of its uses and determinants. Ecology Letters 18:597–611.
- Piantadosi, S., D. P. Byar, and S. B. Green. 1988. The Ecological Fallacy. American Journal of
- 621 Epidemiology 127:893-904.
- Queenborough, S. A., K. M. Burnet, W. J. Sutherland, A. R. Watkinson, and R. P. Freckleton.
- 2011. From meso- to macroscale population dynamics: A new density-structured approach.
- Methods in Ecology and Evolution 2:289–302.
- R Core Team. 2013. R: A language and environment for statistical computing.
- Rees, M., and S. P. Ellner. 2009. Integral projection models for populations in temporally varying
- environments. Ecological Monographs 79:575–594.
- Schurr, F. M., J. Pagel, J. S. Cabral, J. Groeneveld, O. Bykova, R. B. O'Hara, F. Hartig, W. D.
- Kissling, H. P. Linder, G. F. Midgley, B. Schröder, A. Singer, and N. E. Zimmermann. 2012.

- How to understand species' niches and range dynamics: A demographic research agenda for
- biogeography. Journal of Biogeography 39:2146–2162.
- 632 Stan Development Team. 2014a. Stan: A C++ Library for Probability and Sampling, Version
- 633 2.5.0.
- Stan Development Team. 2014b. Rstan: the R interface to Stan, Version 2.5.0.
- Sæther, B. E., S. Engen, V. Grøtan, W. Fiedler, E. Matthysen, M. E. Visser, J. Wright, A. P.
- 636 Møller, F. Adriaensen, H. Van Balen, D. Balmer, M. C. Mainwaring, R. H. McCleery, M. Pampus,
- and W. Winkel. 2007. The extended Moran effect and large-scale synchronous fluctuations in the
- size of great tit and blue tit populations. Journal of Animal Ecology 76:315–325.
- Taylor, C. M., and A. Hastings. 2004. Finding optimal control strategies for invasive species: a
- density-structured model for Spartina alterniflora. Journal of Applied Ecology 41:1049–1057.
- Teller, B. J., P. B. Adler, C. B. Edwards, G. Hooker, R. E. Snyder, and S. P. Ellner. (n.d.). Linking
- demography with drivers: climate and competition. Methods in Ecology and Evolution.