Do we need demographic data to forecast population responses to climate change?

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Abstract. Rapid climate change has generated growing interest in forecasts of future population trajectories. Traditional population models, typically built using detailed demographic observations from one study site, can address climate change impacts at one location, but are difficult to scale up to the landscape and regional scales relevant to management decisions. An alternative is to build models using population-level data that are much easier to collect over broad spatial scales than individual-level data. However, such models ignore the fact that climate drives population growth through its influence on individual performance. Here, we test the consequences of aggregating individual responses when forecasting climate change impacts on four perennial grass species in a semi-arid grassland in Montana, USA. We parameterized two population models for each species, one based on individual-level data (survival, growth and recruitment) and one on population-level data (percent cover), and compared their accuracy, precision, and sensitivity to climate variables.

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For both models we used Bayesian ridge regression to identify the optimal predictive model in terms of climate covariate strengths. The individual-level model was more accurate and precise than the aggregated model when predicting out-of-sample observations. When comparing climate effects from both models, the population-level model missed important climate effects from at least one vital rate for each species. Increasing the sample size at the population-level would not necessarily reduce forecast uncertainty; the way to reduce uncertainty is to capture unique climate dependence of individual vital rates. Our analysis indicates that there is no shortcut to forecasting climate change impacts on plant populations — detailed demographic data are essential. Despite the superiority of the individual-level model, the forecasts it generated still were too uncertain to be useful for decision-makers. We need new methods to collect demographic data efficiently across environmental gradients in space and time.

Key words: forecasting, climate change, grassland, integral projection model, population model

$_{40}$ Introduction

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- Perhaps the greatest challenge for ecology in the 21st century is to forecast the impacts
- 42 of environmental change (Clark et al. 2001, Petchey et al. 2015). Forecasts require so-
- 43 phisticated modeling approaches that fully account for uncertainty and variability in both
- ecological process and model parameters (Luo et al. 2011, but see Perretti et al. 2013
- for an argument against modeling the ecological process). The increasing statistical so-
- 46 phistication of population models (Rees and Ellner 2009) makes them promising tools for
- 47 predicting the impacts of environmental change on species persistence and abundance.
- But reconciling the scales at which population models are parameterized and the scales at
- 49 which environmental changes play out remains a challenge (Clark et al. 2010, 2012, Freck-
- be leton et al. 2011, Queenborough et al. 2011). The problem is that most population models

tracking the fates of individuals plants, is so difficult. The resulting models cannot be applied to the landscape and regional scales relevant to decision-making without information about how the fitted parameters respond to spatial variation in biotic and abiotic drivers (Sæther et al. 2007). The limited spatial extent of individual-level demographic datasets constrains our ability to use population models to address applied questions about the consequences of climate change. The inability of most population models to address landscape-scale problems may explain why land managers and conservation planners have embraced species distribution models (SDMs) (see Guisan and Thuiller 2005 for a review). SDMs typically rely on easy-to-collect presence/absence data (but see Clark et al. 2014 for new methods) and remotely-sensed environmental covariates that allow researchers to model large spatial extents (e.g., Maiorano et al. 2013). Thus, it is relatively straightforward to parameterize and project SDMs over landscapes and regions. However, the limitations of SDMs are well known (Pearson and Dawson 2003, Elith and Leathwick 2009, Araújo and Peterson 2012). Ideally, researchers would provide managers with landscape-scale population models, combining the extent of SDMs with information about dynamics and species abundances (Schurr et al. 2012, Merow et al. 2014). Aggregate measures of population status, rather than individual performance, offer an intriguing alternative for modeling populations (Clark and Bjørnstad 2004, Freckleton et al. 2011). Population-level data cannot provide inference about demographic mechanisms, 71 but might be sufficient for modeling future population states, especially since such data are feasible to collect across broad spatial extents (e.g., Queenborough et al. 2011). The choice between individual and population-level data involves a difficult trade-off: while individual-level data leads to more mechanistic models, population-level data leads to models that can be applied over greater spatial and temporal extents. An open question is how much forecasting skill is lost when we build models based on population rather than

are built using data from a single study site because collecting those data, which involves

⁷⁸ individual-level data.

attempts to capitalize on population-level measures. An important exception was an effort 80 by Taylor and Hastings (2004) to model the population growth rate of an invasive species to identify the best strategies for invasion control. They used a "density-structured" model 82 where the state variable is a discrete density state rather than a continuous density measure. Such models do not require individual-level demographic data and can adequately describe population dynamics. Building on Taylor and Hastings (2004), Freckleton et al. (2011) showed that density-structured models compare well to continuous models in theory, and Queenborough et al. (2011) provide empirical evidence that density-structured models are capable of reproducing population dynamics at landscape spatial scales, even if some precision is lost when compared to fully continuous models. The appeal of densitystructured approaches is clear. However, none of these models included environmental covariates. Addressing climate change questions with models fit to population-level data is potentially problematic. It is individuals, not populations, that respond to climate variables (Clark 93 et al. 2012). Ignoring this fact amounts to an "ecological fallacy", where inference about the individual relies on statistical inference on the group (Piantadosi et al. 1988). Population growth (or decline) is the outcome of demographic processes such as survival, growth, and recruitment that occur at the level of individual plants. Climate can affect each demographic process in unique, potentially opossing, ways (Dalgleish et al. 2011). These unique climate responses may be difficult to resolve in statistical models based on population-level data where demographic processes are not identifiable. If important climate effects are 100 missed because of the aggregation inherent in in population-level data, then population 101 models built with such data will make uninformative or unreliable forecasts. 102 Here, we compare the forecasting skill of statistical and population models based on aggre-

To date, most empirical population modelers have relied on individual-level data, with few

gated, population-level data with models based on individual-level data. We used a unique demographic dataset that tracks the fates of individual plants from four species over 14 105 years to build two kinds of single-species population models, traditional models using indi-106 vidual growth, survival, and recruitment data and alternative models based on basal cover. 107 In both models, interannual variation is explained, in part, by climate covariates. We first 108 quantify forecasting skill using cross-validation. We then performed simulations to quan-100 tify the sensitivities of species' cover to small perturbations in average precipitation and 110 temperature. Based on the cross-validation results, predictions of individual level models 111 were clearly better, but, unfortunately, still too uncertain to inform management decisions. 112

113 Materials and Methods

114 Study site and data

Our demographic data come from the Fort Keogh Livestock and Range Research Labo-115 ratory in eastern Montana's northern mixed prairie near Miles City, Montana, USA (46° 116 19' N, 105° 48' W). The dataset is freely available on Ecological Archives¹ (Anderson et al. 117 2011), and interested readers should refer to the metadata for a complete description. The 118 site is about 800 m above sea level and mean annual precipitation (1878-2009) is 334 mm, with most annual precipitation falling from April through September. The community 120 is grass-dominated and we focused on the four most abundant grass species: Bouteloua 121 gracilis (BOGR), Hesperostipa comata (HECO), Pascopyrum smithii (PASM), and Poa 122 secunda (POSE) (Fig. 1). 123 From 1932 to 1945 individual plants were identified and mapped annually in 44 1-m² 124 quadrats using a pantograph. The quadrats were distributed in six pastures, each as-125 signed a grazing treatment of light (1.24 ha/animal unit month), moderate (0.92 ha/aum), 126 and heavy (0.76 ha/aum) stocking rates (two pastures per treatment). In this analysis 127 ¹http://esapubs.org/archive/ecol/E092/143/

we account for potential differences among the grazing treatments, but do not focus on grazing×climate interactions. The annual maps of the quadrats were digitized and the fates of individual plants tracked and extracted using a computer program (Lauenroth and Adler 2008, Chu et al. 2014). Daily climate data are available for the duration of the data collection period (1932 - 1945) from the Miles City airport, Wiley Field, 9 km from the study site.

We modeled each grass population based on two levels of data: individual and quadrat (Fig. 2). The individual data is the "raw" data. For the quadrat-level we data we simply sum individual basal cover for each quadrat by species. This is equivalent to a near-perfect census of quadrat percent cover because previous analysis shows that measurement error at the individual-level is small (Chu and Adler 2014). Based on these two datasets we can compare population models built using individual-level data and aggregated, quadrat-level data.

All R code and data necessary to reproduce our analysis is archived on GitHub as release v1.0² (http://github.com/atredennick/MicroMesoForecast/releases). That stable release will remain static as a record of this analysis, but subsequent versions may appear if we update this work. We have also deposited the v1.0 release on Dryad (*link here after acceptance*).

146 Stastical models of vital rates

At both levels of inference (individual and quadrat), the building blocks of our population models are vital rate regressions. For individual-level data, we fit regressions for survival, growth, and recruitment for each species. At the quadrat-level, we fit a single regression model for population growth. We describe the statistical models separately since fitting the models required different approaches. All models contain five climate covariates that

²Note to reviewers: so that v1.0 will be associated with the published version of the manuscript, we have released v0.1 to be associated with this review version.

we chose a priori: "water year" precipitation at t-1 (lagppt); April through June precipitation at t-1 and t-2 (ppt1 and ppt2, respectively) and April through June temperature at t-153 1 and t-2 (TmeanSpr1 and TmeanSpr2, respectively), where t is the observation year. We 154 also include interactions among same-year climate covariates (e.g., ppt1 × TmeansSpr1) 155 and climate \times size interactions. Climate \times size interactions are for climate main effects 156 only; we do not include interactions between size and pairs of interacting climate effects. 157 We fit all models using a hierarchical Bayesian approach. The models are fully descibed 158 in Appendix A, so here we focus on the main process and the model likelihood. For the 159 likelihood models, \mathbf{y}^{X} is always the relevant vector of observations for vital rate X (X = 160 S,G,R,orP for survival, growth, recruitment, or population growth). For example, \mathbf{y}^S is a 161 vector of 0's and 1's indicating whether a genet survives from t to t+1, or not.

Vital rate models at the individual level We used logistic regression to model survival probability (S) of genet i from species j in quadrat group Q from time t to t + 1:

$$logit(S_{ijQ,t}) = \gamma_{j,t}^{S} + \phi_{jQ}^{S} + \beta_{j,t}^{S} x_{ij,t} + \omega_{j}^{S} w_{ij,t} + \nu_{j}^{S} w_{ij,t} x_{ij,t} + \theta_{jk}^{S} C_{k,t}$$
(1)

$$y_{ijQ,t}^S \sim \text{Bernoulli}(S_{ijQ,t})$$
 (2)

where $x_{ij,t}$ is the log of genet size, $\gamma_{j,t}^S$ is a year-specific intercept, $\beta_{j,t}^S$ is the year-specific slope parameter for size, ϕ_{jQ}^S is the random effect of quadrat group location, and θ_k^S is the fixed parameter for the effect of the kth climate covariate at time t ($C_{k,t}$). Note that the vector of climate covariates (\mathbf{C}) includes climate variable interactions and climate×size interactions. We include density-dependence by estimating the effect of crowding on the focal individual by other individuals of the same species. ω is the effect of crowding and $w_{t,Q}$ is the crowding experienced by the focal individual at time t in quadrat group Q. We include a size×crowding interaction effect (ν^S). We modeled growth as a Gaussian process describing genet size at time t+1 as a function of size at t and climate covariates:

$$x_{ijQ,t+1} = \gamma_{j,t}^G + \phi_{jQ}^G + \beta_{j,t}^G x_{ij,t} + \omega_j^G w_{ij,t} + \nu_j^S w_{ij,t} x_{ij,t} + \theta_{jk}^G C_{k,t}$$
(3)

$$y_{ijQ,t}^G \sim \text{Normal}(x_{ijQ,t+1}, \varepsilon_{ij,t})$$
 (4)

where x is log genet size and all other parameters are as described for the survival regression. We capture non-constant error variance in growth by modeling the variance around the growth regression (ε) as a nonlinear function of predicted genet size:

$$\varepsilon_{ij,t} = ae^{bx_{ijQ,t+1}} \tag{5}$$

Our data allows us to track new recruits, but we cannot assign a specific parent to new genets. Therefore, we model recruitment at the quadrat level: the number of new individuals of species j in quadrat q recruiting at time t+1 as a function of quadrat "effective cover" (A') in the previous year (t). Effective cover is a mixture of observed cover (A) in the focal quadrat (q) and the mean cover across the entire group (\bar{A}) of Q quadrats in which q is located:

$$A'_{jq,t} = p_j A_{jq,t} + (1 - p_j) \bar{A}_{jQ,t}$$
(6)

where p is a mixing fraction between 0 and 1 that is estimated within the model.

We assume the number of individuals, y^R , recruiting at time t+1 follows a negative binomial distribution:

$$y_{jq,t+1}^R \sim \text{NegBin}(\lambda_{jq,t+1}, \zeta)$$
 (7)

where λ is the mean intensity and ζ is the size parameter. We define λ as:

$$\lambda_{jq,t+1} = A'_{jq,t} e^{(\gamma_{j,t}^R + \phi_{jQ}^R + \theta_{jk}^R C_{k,t} + \omega^R \sqrt{A'_{q,t}})}$$
(8)

where A' is effective cover (cm²) of species j in quadrat q and all other terms are as in the survival and growth regressions.

Population model at the quadrat level The statistical approach used to model aggregated data depends on the type of data collected. We have percent cover data, which 191 can easily be transformed to proportion data. We first considered fitting three vital rate 192 models analogous to those we fit at the individual level: one for probability of extirpation 193 within a quadrat (analogous to survival), one for cover change within a quadrat (analogous 194 to growth), and one for probability of colonization within a quadrat (analogous to recruit-195 ment). However, within-quadrat extirpation and colonization events were rare in our time 196 series (N = 9 and N = 10, respectively, across all species). Given the broad spatial distri-197 bution of the quadrats we are studying, it is safe to assume that these events are in fact 198 rare enough to be ignored for our purposes. So we constrained our statistical modeling 199 of vital rates at the population level to change in percent cover within quadrats. For the 200 remaining discussion of statistical modeling, we refer to proportion data, which is simply 201 percent cover divided by 100. 202 An obvious choice for fitting a linear model to proportion data is beta regression because 203 the support of the beta distribution is [0,1], not including true zeros or ones. However, when we used fitted model parameters from a beta regression in a quadrat-based pop-205 ulation model, the simulated population tended toward 100% cover for all species. We

therefore chose a more constrained modeling approach based on a truncated log-normal likelihood. The model for quadrat cover change from time t to t+1 is

$$x_{jq,t+1} = \gamma_{j,t}^{P} + \phi_{jQ}^{P} + \beta_{j,t}^{P} x_{jq,t} + \theta_{jk}^{P} C_{k,t}$$
(9)

$$y_{jq,t+1}^P \sim \text{LogNormal}(x_{jq,t+1}, \tau_j) T[0, 1]$$
 (10)

where $x_{jq,t}$ is the log of species' j proportional cover in quadrat q at time t and all other parameters are as in the individual-level growth model (Eq. 3). Again, note that the climate covariate vector (\mathbf{C}) includes the climate×cover interaction. The log normal likelihood includes a truncation (T[0,1]) to ensure that predicted values do not exceed 100% cover.

214 Model fitting and stastical regularization

Model fitting Our Bayesian approach to fitting the vital rate models required choos-215 ing appropriate priors for unknown parameters and deciding which, if any, of those pri-216 ors should be hierarchical. We decided to fit models where all terms were fit by species. 217 Within a species, we fit yearly size effects and yearly intercepts hierarchically where year-218 specific coefficients were drawn from global distributions representing the mean size effect 219 and intercept. Quadrat random effects were also fit hierarchically, with quadrat offsets 220 being drawn from distributions with mean zero and a shared variance term (independent 221 Gaussian priors, Appendix A). Climate effects were not modeled hierarchically, and each 222 was given a diffuse prior distribution. We used standard diffuse priors for all unknown 223 parameters (Appendix A). 224 All of our analyses (model fitting and simulating) were conducted in R (R Core Team 225 2013). We used the 'No-U-Turn' MCMC sampler in Stan (Stan Development Team 2014a)

to estimate the posterior distributions of model parameters using the package 'rstan' (Stan Development Team 2014b). We obtained posterior distributions for all model parameters from three parallel MCMC chains run for 1,000 iterations after discarding an initial 229 1,000 iterations. Such short MCMC chains may surprise readers more familiar with other 230 MCMC samplers (i.e. JAGS or WinBUGS), but the Stan sampler is exceptionally efficient, 231 which reduces the number of iterations needed to achieve convergence. We assessed con-232 vergence visually and made sure scale reduction factors for all parameters were less than 233 1.01. For the purposes of including parameter uncertainty in our population models, we 234 saved the final 1,000 iterations from each of the three MCMC chains to be used as ran-235 domly drawn values during population simulation. This step alleviates the need to reduce 236 model parameters by model selection since sampling from the full parameter space in the 237 MCMC ensures that if a parameter broadly overlaps zero, on average the effect in the pop-238 ulation models will also be near zero. We report the posterior mean, standard deviation, 239 and 95% Bayesian Credible Intervals for every parameter of each model for each species in 240 Appendix B. 241

Statistical regularization: Bayesian ridge regression Our objective is to model 242 the response of our focal grass species to interannual variation in climate, even if those 243 responses are weak. Therefore, we avoid selecting among models with all possible com-244 binations of climate covariates, and instead use Bayesian ridge regression to regulate, or 245 constrain, the posterior distributions of each climate covariate (Hooten and Hobbs 2015). 246 Ridge regression is a specific application of statistical regularization that seeks to opti-247 mize model generality by trading off bias and variance. As the name implies, statistical 248 regularization involves the use of a regulator that constrains an optimization. The natural regulator in a Bayesian application is the prior on the coefficient of interest. Each of our statistical models includes the effects of climate covariates via the term $c'\theta$ with prior $\boldsymbol{\theta} \sim \text{Normal}(\boldsymbol{\mu}_{\theta}, \sigma_{\theta}^2)$. Since we standardized all climate covariates, including interaction

terms, to have mean zero and variance one we can set $\mu_{\theta} = 0$, letting σ_{θ}^2 serve as the regulator that can shrink covariates toward zero – the smaller the prior variance, the more θ is 254 shrunk toward zero, and the stronger the penalty (Hooten and Hobbs 2015). 255 To find the optimal penalty (i.e., optimal value of the hyperparameter σ_{θ}^2), we fit each 256 statistical model with a range of values for σ_{θ}^2 and compared predictive scores from leave-257 one-year-out cross-validation. We performed the grid search over 24 evenly-spaced values 258 of σ_{θ}^2 , ranging from $\sigma_{\theta}^2 = 0.01$ to $\sigma_{\theta}^2 = 2.25$. For each statistical model and each species 259 we fit $13 \times 24 = 312$ models (13 years to leave out for cross-validation and 24 values of 260 σ_{θ}^2) – a total of 4992 models. We calculated the log pointwise predictive density (lppd) to 261 score each model's ability to predict the left-out data. Thus, for training data y_{train} and 262 held-out data y_{hold} at a given value of σ_{θ}^2 across all MCMC samples s=1,2,...,S and all hold outs of data from year t to year T, lppd is

$$lppd_{CV} = \sum_{t=1}^{T} log_e \int [y_{t,hold}|\theta] [\theta|y_{train}] d\theta,$$
(11)

265 and computed as

$$\sum_{t=1}^{T} \log_e \left(\frac{1}{S} \sum_{s=1}^{S} (y_{t,hold} | \theta_{ts}) \right). \tag{12}$$

We chose the optimal prior variance for each species-statistical model combination as the one that produced the highest lppd and then fit each species-statistical model combination using the full data set for each species and the optimal prior variance. In some cases lppd was highest at the highest (most vague) value of prior variance, in which case we explored a slightly expanded range of prior variances (e.g., $\sigma_{\theta}^2 > 2.25$).

Population models

With the posterior distribution of the vital rate statistical models in hand, it is straightforward to simulate the population models. We used an Integral Projection Model (IPM) to
model populations based on individual-level data (Ellner and Rees 2006) and a quadratbased version of an individually-based model (Quadrat-Based Model, QBM) to model
populations based on quadrat-level data. We describe each in turn.

Integral projection model We use a stochastic IPM (Rees and Ellner 2009) that includes the climate covariates from the vital rate statistical models. In all simulations we ignore the random year effects so that interannual variation is driven solely by climate. We fit the random year effects in the vital rate regressions to avoid over-attributing variation to climate covariates. Our IPM follows the specification of Chu and Adler (2015) where the population of species j is a density function $n(u_j, t)$ giving the density of sized-u genets at time t. Genet size is on the natural log scale, so that $n(u_j, t)du$ is the number of genets whose area (on the arithmetic scale) is between e^{u_j} and e^{u_j+du} . The density function for any size v at time t+1 is

$$n(v_j, t+1) = \int_{L_j}^{U_j} k_j(v_j, u_j, \bar{w}_j(u_j)) n(u_j, t)$$
(13)

where $k_j(v_j, u_j, \bar{w}_j)$ is the population kernel that describes all possible transitions from size u to v and \bar{w}_j is a scalar representing the average intraspecific crowding experienced by a genet of size u_j and species j. The integral is evaluated over all possible sizes between predefined lower (L) and upper (U) size limits that extend beyond the range of observed genet sizes.

Since the IPM is spatially-implicit, we cannot calculate neighborhood crowding for specific genets (w_{ij}) . Instead, we use an approximation (\bar{w}_j) that captures the essential features of neighborhood interactions (Adler et al. 2010). This approximation relies on a

'no-overlap' rule for conspecific genets to approximate the overdispersion of large genets in space (Adler et al. 2010).

The population kernel is defined as the joint contributions of survival (S), growth (G), and recruitment (R):

which means we are calculating growth (G) for individuals that survive (S) from time

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$$k_j(v_j, u_j, \bar{w}_j) = S_j(u_j, \bar{w}_j(u_j))G_j(v_j, u_j, \bar{w}_j(u_j)) + R_j(v_j, u_j, \bar{w}_j), \tag{14}$$

t to t+1 and adding in newly recruited (R) individuals of an average sized one-year-old 299 genet for the focal species. Our stastical model for recruitment (R, described above) re-300 turns the number of new recruit produced per quadrat. Following previous work (Adler 301 et al. 2012, Chu and Adler 2015), we assume that fecundity increases linearly with size 302 $(R_j(v_j,u_j,\bar{w}_j)=e^{u_j}R_j(v_j,\bar{w}_j))$ to incorporate the recruitment function in the spatially-303 implicit IPM. 304 We used random draws from the final 1,000 iterations from each of three MCMC chains 305 to introduce stochasticity into our population models. At each time step, we randomly 306 selected climate covariates from one of the 14 observed years. Then, we drew the full pa-307 rameter set (climate effects and density-dependence fixed effects) from a randomly selected MCMC iteration. Using this approach, rather than simply using coefficient point 309 estimates, captures the effect of parameter uncertainty. Relatively unimportant climate 310 covariates (those that broadly overlap 0) will have little effect on the mean of the simula-311 tion results, but can contribute to their variation. Since our focus was on the contribution 312 of climate covariates to population states, we set the random year effects and the random 313 group effects to zero. 314

Quad-based model To simulate our quad-based model (QBM), we simply iterate the quadrat-level statistical model (Eqs. 9-10). We use the same approach for drawing pa-

rameter values as described for the IPM. After drawing the appropriate parameter set,
we calculate the mean response (population cover at $t+1 = x_{t+1}$) according to Eq. 9. We
then make a random draw from a [0,1] truncated lognormal distribution with mean equal
to x_{t+1} from Eq. 9 and the variance estimate from the fitted model. We can then project
the model forward by drawing a new parameter set (unique to climate year and MCMC
iteration) at each timestep. As with the IPM, random year effects are ignored for all simulations.

Model validation

To test each model's ability to forecast population state, we made out-of-sample predic-325 tions using leave-one-year-out cross validation. For both levels of modeling, we fit the 326 vital rate models using observations from all years except one, and then used those fitted 327 parameters in the population models to perform a one-step-ahead forecast for the year 328 whose observations were withheld from model fitting. Within each observation year, sev-320 eral quadrats were sampled. We made predictions for each observed quadrat in the focal 330 year, initializing each simulation with cover in the quadrat the previous year. Since we 331 were making quadrat-specific predictions, we incorporated the group random effect on the 332 intercept for both models. We repeated this procedure for all 13 observation years, making 333 100 one-step-ahead forecasts for each quadrat-year combination with parameter uncer-334 tainty included via random draw from the MCMC chain as described above. Random year effects were set to zero since year effects cannot be assigned to unobserved years. 336 This cross-validation procedure allowed us to compare accuracy and precision of the two 337 modeling approaches (IPM versus QBM). We first calculated the median predicted cover 338 across the 100 simulations for each quadrat-year and then calculated the absolute error as 339 the absolute value of the difference between the observed cover for a given quadrat-year 340 and the median prediction. To arrive at mean absolute error (MAE), we then averaged the absolute error within each species across the quadrat-year specific errors. We use MAE
as our measure of accuracy. To measure precision we calculated the distance between
the upper and lower 90th quantiles of the 100 predictions and averaged this value over
quadrat-years for each species.

346 Testing sensitivity to climate covariates

With our fitted and validated models in hand, we ran simulations for each model type (IPM and QBM) under four climate perturbation scenarios: (1) observed climate, (2) pre-348 cipitation increased by 1%, (3) temperature increased by 1%, and (4) precipitation and 349 temperature increased by 1%. We ran the simulations for 2,500 time steps, enough to 350 estimate equilibrium cover after discarding an initial 500 time steps as burn-in. Each simu-351 lation was run under two parameter scenarios: (1) using mean parameter estimates and (2) 352 using randomly drawn parameters from the MCMC chain. We use (1) to detect the overall 353 sensitivity of equilibrium cover to climate, and we use (2) to show the impact of model 354 and parameter uncertainty on forecast precision. 355 As an effort to identify potential discrepencies between IPM and QBM forecasts, we also 356 ran simulations designed to quantify the sensitivities of individual and combined vital rates to climate for the IPM. Specifically, we ran simulations for the above climate scenarios, but applied the perturbed climate covariates to survival, growth, or recruitment vital 359 rates individually and in pairwise combinations. This allowed us to isolate the vital rate(s) most sensitive to climate. For this analysis, we used mean parameter estimates to reduce 361 the sources of uncertainty in the sensitivity estimates. 362 We expected the IPM to produce more accurate and precise forecasts due to either (1) 363 the smaller sample size of the quadrat level data sets compared to the individual level 364 data sets, leading to larger parameter uncertainty for the QBM, or (2) the QBM climate 365 effects being weakly associated with one or more vital rate climate effects at the individual

level. To assess the impact of sample size on QBM parameter uncertainty we refit the QBM statistical model (Eqs. 9-10) after removing sets of 2, 5, 10, and 15 quadrats. We fit 10 models at each level of quadrat removal (2, 5, 10, 15 quadrats), removing a different 369 randomly selected set of quadrats for each fit. We calculated the standard deviation of 370 climate main effects (pptLag, ppt1, ppt2, TmeanSpr1, and TmeanSpr2) for each model 371 and averaged those over replicates within each set of quadrat removals. This allowed us to 372 regress parameter uncertainty against sample size. 373 To deterime if the QBM climate effects are correlated with climate effects for each vital 374 rate model in the IPM, we simply regressed the QBM climate coefficients against each 375 vital rate model's climate coefficients and calculated Pearson's ρ . Strong correlations indi-376 cate the QBM is capable of detecting climate effects associated with individual vital rates. A weak correlation indicates the QBM "misses" the climate effect on a particular vital rate.

380 Results

381 Comparison of forecast models

382 Sensitivity of models to climate

The response of a population to climate change is a result of the aggregate effects of climate on individual vital rates. Since the IPM approach relies on vital rate regressions, we
were able to quantify the sensitivity of each vital rate in isolation and in pairwise combinations. Across all species, climate covariates can have opposing effects on different vital
rates (Fig. 3). Growth was the most sensitive vital rate for all species, showing a negative
response to increased precipitation, and stronger positive response to increased temperature, and a mostly positive response when both climate factors are increased (Fig. 3). B.

gracilis survival rates were sensitive to temperature, resulting in an increase in plant cover

under increased temperature (Fig. 3a). In isolation, recruitment and survival were insensitive to climate factors for *H. comata* (Fig. 3b). Survival and recruitment of *P. smithii* were both sensitive, negatively, to temperature and precipitation (Fig. 3c). *P. secunda* equilibrium cover was sensitive to the climate effects on survival and recruitment, showing a negative effect on both vital rates for increased precipition, but a strong positive effect on survival with increased temperature (Fig. 3d). Equilibrium cover responded negatively when increased precipitation and temperature affect recruitment (Fig. 3d). At least two of three vital rates were sensitive to climate for each species (Fig. 3).

399 Sources of uncertainty in the QBM

Sample size had a relatively weak effect on QBM climate parameter uncertainty after 400 the number of quadrats used in fitting exceeded about 10 (Fig. 5). Inverse-gaussian fits 401 show that increasing sample size beyond the number of quadrats we used would result in 402 diminishing returns in terms of parameter certainty (Fig. 5). 403 Climate effects estimated from the QBM are most correlated with climate effects from 404 the growth regression at the individual level (Fig. 6). In no case does the QBM statistical 405 model have strong correlations across all three vital rates (Fig. 6). QBM climate effects were most weakly correlated with those from individual-level recruitment models for B. gracilis, H. comata, and P. secunda (Fig. 6a,b,d). For P. smithii, QBM climate effects 408 showed no correlation with the survival model effects (Fig. 6c).

410 Model forecasts

Forecasts based on 1% climate changes were extremely uncertain when we considered model error and parameter uncertainty (Fig. 6; simulations with mean parameters are in Appendix D for comparison). As expected based on model validation (Table 1), QBM projections were more uncertain than IPM projections for all species except *P. smithiii* (Fig. 6). IPM forecasts for *P. smithiii* were very uncertain due to a very high instrinsic rate of recruitment combined with uncertainty in climate coefficients which lead to high recruitment boom years and subsequent busts when young plants suffer high mortality (Appendx C). When we included model error and parameter uncertainty, forecast changes in proportional cover always spanned a wide range of negative to positive values. In other words, neither model could predict whether a climate perturbation would increase or decrease equilibrium population size.

422 Discussion

Population models built using individual-level data allow inference on demographic pro-423 cesses, but they can only forecast future population states across the (typically limited) 424 spatial extent of the observations. Population-level data are much easier to collect across 425 broad spatial extents, so models built using such data offer an appealing alternative to 426 traditional population models (Queenborough et al. 2011). However, density-structured 427 models rely on the aggregation of individual-level data. This creates a potential problem if 428 such models are to be used in a climate change context because it is individuals, not pop-429 ulations, which respond to climate (Clark et al. 2012). Are models based on populationlevel metrics as sensitive to climate as models based on individual-level metrics? Do these 431 two types of models produce consistent forecasts? Do we need detailed demographic data 432 to forecast the impacts of climate change?

The importance of demographic data

Our comparison of a traditional, demographic population model (the IPM) with a model inspired by density-structured models (the QBM) showed that the IPM outperformed the QBM: the IPM was more accurate and precise than the QBM in out-of-sample cross validation (Table 1). The superiority of the IPM could reflect either differences in sample

size or the effect of averaging over unique effects of climate on each individual-level vital rate. Although increasing sample size of quadrat percent-cover observations would be easy to do in the field, we found little evidence that it would lead to higher precision of climate coefficient estimates (Fig. 4). 442 We did, however, find evidence that the QBM statistical model failed to identify climate 443 dependence for some vital rates (Fig. 5). For no species were climate effects from the 444 QBM strongly correlated with all three vital rates (Fig. 5). Freckleton et al. (2011) ac-445 knowledge that averaging over complex stage dependence will lead to poorly specified 446 models. This is analogous to our situation, but instead of averaging over complex life his-447 tories, we are averaging over complex climate dependence. Though our work here focused on plant species, this finding is applicable to any species with vital rates that respond uniquely to weather/climate. Our interpretation is that the QBM is "missing" climate signals associated with at least 451 one vital rate for each species. This leads to inaccurate and imprecise forecasts because 452 the QBM statistical model struggles to explain variation due to climate variables that have 453 positive and negative impacts on different vital rates. When this is the case, as it is for all 454 our species to varying degrees (Fig. 3), forecasts from models based on population-level 455 data will fail. Our result is consistent with related work on the importance of individual-456 level data to forecast population responses to exogenous drivers (Clark et al. 2011a, 2011b, 457 2012, Galván et al. 2014). 458 Detailed demographic data appears to be necessary to forecast climate change impacts on plant populations when vital rates have unique climate responses. How then can we build 460 models to make forecasts for the landscape and regional scales beyond the scope of traditional population models (Queenborough et al. 2011)? There are alternatives to density-462 structured models. For example, Clark et al. (2011a) use Forest Inventory and Analysis 463 (FIA) data to parameterize a population model with multiple vital rates and climate dependence. Distributed efforts such as PlantPopNet (http://plantago.plantpopnet.com) will allow researchers to estimate variation around climate responses for widespread species by taking advantage of spatial variation in climate (e.g. Doak and Morris 2010). Finally, new approaches on the horizon that leverage photo/video of plots and advanced object recognition algorithms (e.g. Liu et al. 2014) will increase the efficiency of plant mapping and digitizing efforts.

The challenge of uncertainty

An important, but unexpected, result of our analysis was the great uncertainty in fore-472 casts, even for our best model. The typical approach in ecology is to use point estimates 473 of model parameters to project populations forward according to the specified model, usu-474 ally allowing for some variability around the determinatic process (e.g. Battin et al. 2007, 475 Jenouvrier et al. 2009, Adler et al. 2012). If we follow tradition and calculate the mean 476 response to climate perturbation with only model error and interannual variation included, 477 the IPM and the QBM produce opposing forecasts for three of four species (Fig. D1). It 478 would be tempting to interpret this inconsistency as further evidence for the superiority of 479 the IPM. However, if we introduce parameter uncertainty, the forecasts are actually indis-480 tinguishable (Fig. 6), though the IPM projections are generally more precise (consistent 481 with our cross-validation results). The real story is that both models produce highly un-482 certain forecasts. For all species, the 90% quantiles of predicted changes in population size overlapped zero; we cannot even predict whether a change in precipitation or temperature 484 will cause populations to increase or decrease. This result held when we tried perturbing 485 climate by 10% and 20% as well. Our results highlight the state of affairs in ecology when it comes to forecasting the im-487 pacts of climate change. The analysis we conducted here could be considered at the fore-488 front of ecological forecasting with respect to the statistical approach employed (hierarchi-

cal Bayesian), the type of population model we used (density-dependent, stochastic IPM with parameter uncertainty), and the amount of high quality data we had at our disposal 491 (14 years of individual-level data). Yet, model predictions proved so uncertain that any 492 forecast, when bounded with model and parameter uncertainty, would be uninformative. 493 How might we improve on this state of affairs? First, forecasts could be improved by 494 matching the spatial scale of predictor variables with the spatial scale of observations. One 405 of the major limitations of the models we fit here is that the climate data are collected 496 at a larger scale than the individual-level observations of plant size. Climate covariates 497 only vary by year, with no spatial variability within years. Thus, even if we fit models 498 to individual-level data, we are missing the key interaction point between weather and 499 individual plants (Clark et al. 2011b) because all observations share the same climate co-500 variates. Demographic studies should be designed with at least plot-level measurements of 501 climate related variables (e.g., soil moisture). Second, accurately detecting climate signals will take even longer time series. Recent theoretical work on detecting climate signals in 503 noisy data suggests that even advanced approaches to parameter fitting require 20-25 year time series (Teller et al. 2016). Third, ecologists need a stronger commitment to reporting 505 uncertainty. Although most modeling studies explicitly consider model uncertainty, param-506 eter uncertainty is often ignored. In some cases this is because the most convenient sta-507 tistical methods make it difficult to propagate parameter uncertainty. Yet even Bayesian 508 approaches that allow integration of model fitting and forecasting (Hobbs and Hooten 509 2015) are not simple when using modeling approaches like integral projection models that 510 separate the model fitting and simulation stages (Rees and Ellner 2009). However, as we 511 have done here, it is still possible to include parameter uncertainty by drawing parameter 512 values from MCMC iterations, taking care to draw all parameters from the same chain 513 and iteration to account for their correlations. Only by being honest about our forecasts 514 can we begin to produce better ones, and forecasts reported without parameter error are 515 disingenuous. Ignoring parameter error may be justifiable when the goal is investigating 516

basic processes, but it is indefensible when forecasting is the goal.

518 Conclusions

This work is not a critique of density-structured population models. We are confident that 519 density-structured models will prove to be a valuable tool for many applications. However, 520 our analysis represents the first comparison, to our knowledge, of population models based 521 on individual and aggregated forms of the same data in a climate change context. Our 522 results confirm theoretical arguments (Clark et al. 2011b) and empirical evidence (Clark 523 et al. 2011a, 2012) that individual responses are critical for predicting species' responses 524 to climate change. It seems there is no short cut to producing accurate and precise pop-525 ulation forecasts: we need detailed demographic data to forecast the impacts of climate 526 change on populations. Given the importance of demographic data and its current collec-527 tion cost, we need modern methods to collect demographic data more efficiently across 528 environmental gradients in space and time. 529 Our results also offer a cautionary tale because forecast uncertainty was large for both model types. Even with 14 years of detailed demographic data and sophisticated modeling 531 techniques, our projections contained too much uncertainty to be informative. Uncertainty 532 in demographic responses to climate can be reduced by collecting (1) longer time series 533 and (2) climate covariates that match the scale of inference (e.g., plot rather than land-534 scape level climate/weather metrics). 535

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Data accessibility

Chart-quadrat data available from *Ecological Archives* at http://esapubs.org/archive/
ecol/E092/143/. All code to reproduce our work is available on Dryad (link) and GitHub
(https://github.com/atredennick/MicroMesoForecast).

550 Tables

551 Figure Legends

Figure 1. Time series of average percent cover over all quadrats for our four focal species: 552 Bouteloua gracilis (BOGR), Hesperostipa comata (HECO), Pascopyrum smithii (PASM), 553 and Poa secunda (POSE). Light grey lines show trajectories of individual quadrats. Note 554 the different y-axis scales across panels. 555 Figure 2. Work flow of the data aggregation, model fitting, and population simulating. Figure 3. Sensitivity of equilibrium cover simulated from the IPM to each climate scenario 557 applied to individual and combined vital rates. For example, the points associated with G 558 show the median cover from IPM simulations where a climate perturbation is applied only 550 to the growth regression climate covariates. These simulations use mean parameter values 560 for clarity. 561 Figure 4. Effect of quadrat sample size on the precision (standard deviation) of main cli-562 mate effect estimates in the QBM. Increasing the number of quadrats results in diminish-563 ing returns in terms of parameter certainty. Light dashed lines show individual climate 564 effects at five quadrat sample sizes. Thick dark lines are inverse gaussian fits showing the 565 mean effect of increasing quadrat sample size on parameter precision. 566 Figure 5. Correlations (r) between QBM and IPM estimates of climate effects. We ignore 567 sizeXclimate interactions since these are not directly comparable across model types. The 568 QBM does not have multiple vital rates, so its values are repeated across panels within 569 each species. Across top panels, 'growth' = growth regression, 'rec' = recruitment regres-570 sion, 'surv' = survival regression. 571 Figure 6. Mean (points) and 90% quantiles (errorbars) for the proportional difference 572 between baseline simulations (using observed climate) and the climate pertubation simula-573 tion on the x-axis. We calculated proportional difference as log(perturbed climate cover) 574 - log(observed climate cover), where 'perturbed' and 'observed' refer to the climate time series used to drive interannual variation in the simulations. Model error and parameter

 $_{577}\,$ uncertainty were propagated through the simulation phase. Climate simulations are as in $_{578}\,$ Figure 3.

Figures 579

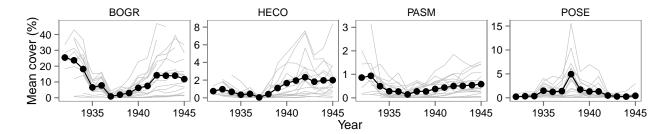


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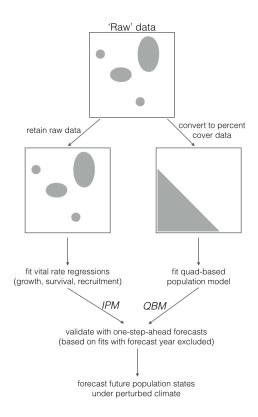


Figure 2: Work flow of the data aggregation, model fitting, and population simulating.

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