Mediation with Repeated-Measures and Multilevel Data

Amanda K. Montoya University of California, Los Angeles

Workshop: 2:15pm - 5:15pm

Please go to https://github.com/akmontoya/SPSP2019Workshop.git, download the folder and open SPSS.

Part I: Intro to Mediation and Basic Repeated-Measures

- · Between Subjects Mediation
 - · Path analytic approach
 - Interpretation
 - Estimation
 - Inference
- · Repeated Measures Data
- Two-Instance Repeated-Measures Mediation
 - Judd Kenny and McClelland (2001)
 - · Path analytic approach
 - · Estimation of Indirect Effects
 - MEMORE
 - · Reporting (Writing and Figures)
 - Common Questions

Workshop Procedures

Download files at

https://github.com/akmontoya/APS2018.git

Assuming some familiarity with:

- · Regression & Multilevel Models
- Mediation
- SPSS

What we will learn:

- · Mediation in Between Subjects Designs
- · Mediation in Two-Instance Within-Participant Designs
- · Introduction to Multilevel Modeling
- · Mediation with Multilevel Data
- Q&A

Short breaks throughout

How we will learn:

- · Combination of theory and practice
- · Follow along with the analysis as we go
 - Use syntax!
 - . Ask questions about concepts or anything that is confusing
- · Make friends, if you have troubles as you go through you can work together.

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Running Example: Group Work in Computer Science (BS)

Montoya, A. K. (2013) Increasing Interest in Computer Science thought Group Work: A Goal Congruity Approach.

Between-Subjects Version (CASC_BS.sav):

Female participants (N = 107) read *one of two* syllabi for a computer science class. One of the syllabi reported the class would have \underline{group} projects throughout (cond = 1), and the other syllabi stated that there would be $\underline{individual}$ projects (cond = 0) throughout the class

Measured Variables:

- Interest in the class ($\alpha = .89$)
 - How interested are you in taking the class you read about?
 - How much would you want to take the class you read about?
 - How likely would you be to choose the class you read about?
 - How interested are you in majoring in computer science?
 - 1 Not at All 7 Very much
- CSComm: Perceptions that computer science is communal ($\alpha = .90$)
 - Computer science would assist me in
 - Helping others, serving the community, working with others, connecting with others, caring for others.
 - 1 Strongly Disagree 7 Strongly Agree

University of Washington Computer Science & Engineering 142: Introduction to Programming I Course Syllabus

Instructor

John Johnson j.johnson@uw.edu CSE 800 office phone: (206)555-1234 office hours: see course website

Course Overview

This course provides an introduction to computer science using the Java programming language. CSE 142 is primarily a programming course that focuses on common computational problem solving techniques. No prior programming experience is assumed, although students should know the basics of using a computer (e.g., using a web browser and word processing program) and should be competent with muth through Algebra 1. The information, concepts, and analytical thinking introduced in lecture provide a unifying framework for the topics covered

Lecture Time MWF 12:00 PM - 1:00 PM, Classroom TBA

Discussion Sections

You will be expected to participate in a weekly discussion section, held on Thursdays (see course website for details). The TA who runs your section will grade your homework assignments. In section, we will answer questions, go over common errors in homework, and discuss sample problems in more detail than

Course Web Site

Textbook

Reges/Stepp, Building Java Programs: A Back to Basics Approach (2nd)

Grading

The primary assessment for your success in this class is exams. There will be 2 midterns and 1 final, and together they make up 85% of your grade. The homework assignments are designed to prepare you for your exams. The exams are designed to assess your ability to utilize the concepts you've learned from your homework and in lecture in new contexts

5% participation

10% weekly homework assignments 25% midterm 1 25% midterm 2

35% final exam

Our exams are closed-book and closed-notes, although each student will be allowed to bring a single index card with hand-written notes (no larger than 5" by 8"). No electronic devices may be used, including calculators. Make-up exams will not be

Homework

Homework consists of weekly assignments done in optional groups and submitted electronically on the course web site. Disputes about homework grading must be made within 2 weeks of receiving the grade. If you don't make an honest effort on the homework, your exam score will reflect it.

Academic Integrity and Collaboration

sure that you thoroughly understand each concept. Homework as completed with other students. You are strongly encouraged to discuss go gas of how to approach an assignment with other students, and may discu pecific details about what to write with other students. Any help you receive provide to classmates should be <u>cited in your assignment</u>. You may seek help om University of Washington CSE 142 TAs, professors, <u>and classmates</u>.

You must abide by the following rules

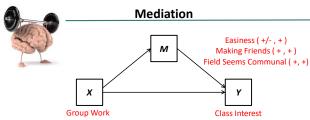
· You are highly encouraged to work with another student on homework

 You may not show another student outside of your class your solution to an assignment, nor look at his/her solution.

• You may not have anyone outside of your class describe in detail how to solve a

assignment or sit with you as you write it.

You may not post online about your homework, other than on the class discuboard, to ask others for help.



A simple mediation model connects an assumed causal variable (X) to an assumed outcome variable (Y), through some mechanism (M).

M is frequently referred to as a mediator, intermediary variable, or surrogate variable.

Many different kind of variables may act as mediators. Emotional variables, situational, individual level variables, cognitive variables, environmental variables, etc.

Mediation can be found throughout the psychology literature and is particularly common in social psychology

A quick example: Name some possible mediators!

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Course Web Site

http://www.cs.washington.edu/142/

Textbook

Reges/Stepp, Building Java Programs: A Back to Basics Approach (2nd Edition).

Grading

The primary assessment for your success in this class is exams. There will be 2 midterms and 1 final, and together they make up 85% of your grade. The homework assignments are designed to prepare you for your exams. The exams are designed to assess your ability to utilize the concepts you've learned from you homework and in lecture in new contexts

25% midterm 2

35% final exam

Our exams are closed-book and closed-notes, although each student will be allowed to bring a single index card with hand-written notes (no larger than 5" by 8"). No electronic devices may be used, including calculators. Make-up exams will not be given except in case of a serious emergency.

Homework

electronically on the course web site. Disputes about homework grading must be made within 2 weeks of receiving the grade. If you don't make an honest effort on the homework, your exam score will reflect it.

Academic Integrity and Collaboration

computer Science is best learned through interacting with the material to ensure as you thoroughly understand each concept. Homework assignments must be unspitaled individually. You may not discuss general ideas of how to approach a signment with other students or discuss specified dealth about what to write with signment with other students or discuss specified dealth about what to write with must always and the students of the students of the students of the mustal. You may such pick secure from or provide to classmates should be mustal. You may such pick secure. limited. You may seek help from University of Washington CSE 142 TAs and

ou must abide by the following rules:

You may not work with another student on homework assignments.
You may not show another student your solution to an assignment, nor look at

You may not have anyone describe in detail how to solve an assignment or si

Mediation: Path Analysis

Consider a, b, c, and c' to be measures of the effect of the variables in the mediation model.

These could be measured using regression coefficients from OLS or path estimates in a structural equation model using maximum likelihood estimation.

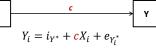
Indirect effect of X on Y (through M) = $a \times b$

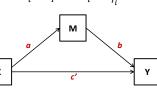
Direct effect of X on Y (not through M) = c'

Indirect effect = total effect - direct effect $a \times b = c$ -

Total effect = direct effect + indirect effect

 $c = c' + a \times b$





$$M_i = i_M + aX_i + e_{M_i}$$

$$Y_i = i_Y + c'X_i + bM_i + e_{Y_i}$$

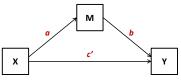
Interpreting the Coefficients

Total Effect (c): The effect of our presumed cause (X) on our outcome (Y), without controlling for any other variables.

a-path: The effect of our presumed cause (X) on our mediator (M).

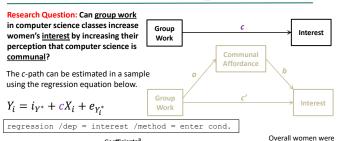
b-path: The effect of our mediator (M) on the outcome (Y) while controlling for X. (i.e. predicted difference in Y for two people with the same score on X but who differ on M by one unit).

Direct effect (c'): The effect of our presumed cause (X) on Y while controlling for M. (i.e. predicted difference in Y for two people who differ by one unit on *X* but with the <u>same score</u> on M)



Indirect Effect (ab): Product of effect of X on M, and effect of M on Y controlling for X. The effect of X on Y through M.

Estimation with CompSci_BS Data



Coefficients^a .462 units more Standardized interested in the Unstandardized Coefficients Coefficients class with group Std. Error Sig. work. 2 701 193 14 002 000 c = .462

.156

1.621

.108

a. Dependent Variable: Interest

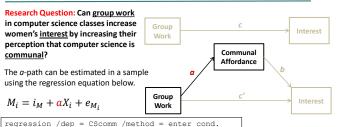
462

.285

(Constant)

Cond

Estimation with CompSci BS Data



Coefficients²

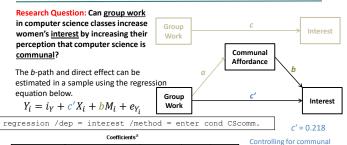
				Standardized			l M
		Unstandardized Coefficients		Coefficients			SC
Mod	lel	В	Std. Error	Beta	t	Sig.	m
1	(Constant)	3.421	.159		21.472	.000	re
	Cond	.488	.237	.198	2.060	.042	gr
a. C	ependent Variab	le: CSComm					•

Vomen saw computer cience as .488 units nore communal after eading a syllabus with roup work.

a = .488

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Estimation with CompSci BS Data

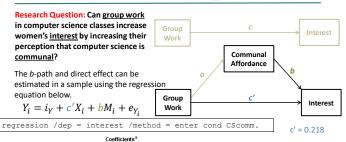


Unstandardized Coefficients Coefficients Std. Error Sig. .964 .413 2.336 .021 Cond .218 .268 .073 .812 .419 CSComm 508 .109 .421 4.663 .000

a. Dependent Variable: Interest

affordance, women in the group work condition were .218 units more interested in the class with group work. b = .508

Estimation with CompSci_BS Data



Standardized Unstandardized Coefficients Coefficients Std. Error Model Beta Sia. (Constant) .964 413 2.336 .021 Cond .218 .268 .073 .812 .419 CSComm .109 .421 4.663 .000

a. Dependent Variable: Interest

For two people in the same condition, a one unit difference in communal goals results in a 0.51 unit difference in interest, on average.

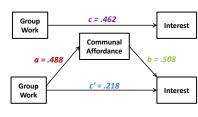
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Interpreting Indirect, Direct, and Total Effects

Indirect Effect

 $a \times b = .488 \times .508 = .249$

Group work increased interest by .249 units indirectly through communal affordance. Where group work increased perceptions of communal affordance by .488 units, and a one unit increase in communal affordance resulted in a .508 unit increase in interest.



Direct Effect

c' = .218

Total Effect c = .462

Group work increased interest by .218 units directly (not through communal affordance).

Group work increased interest by .462 units in total.

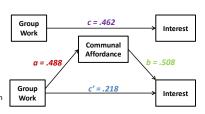
Inference for the direct and total effects can be drawn from the regression results because these are based on a single regression parameter.

p = .419 p = .108

Interpreting the Coefficients

Research Question: Can group work in computer science classes increase women's interest by increasing their perception that computer science is communal?

On average, women were .46 units more interested in the class with group work (p=1.08). Similarly, computer science was perceived as .49 units more communal after reading a syllabus with group work (p=.042). Controlling for condition, a one unit increase in communal affordance resulted in a .508 unit increase in interest (p<.001). Controlling for communal affordance, group work did not predict additional interest (c'=.22, p=.42).



But what about the indirect effect?

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Inference about the Indirect Effect

- How to make proper inference about the indirect effect may be the most active area of research in mediation analysis
- · Some methods you may have heard of
 - · Causal Steps / Baron and Kenny Method / Baron and Kenny Steps
 - · Test of Joint Significance
 - · Sobel Test / Multivariate Delta Method
 - Monte Carlo Confidence Intervals
 - · Distribution of the Product Method
 - · Bootstrap Confidence Intervals
 - · Percentile Bootstrap
 - Bias-Corrected Bootstrap
 - Bias Corrected and Accelerated Bootstrap
- · Why is this so hard?
 - The product of two normal distributions is not necessarily normal. The shape of the distribution of the indirect effect depends on the true indirect effect.
 - There are many instances where the indirect effect could be zero (either a or b could be zero, or both could be zero).

Causal Steps Method

Method

- 1. Test if there is a significant total effect $(c \neq 0)$.
- 2. Test if there is a significant effect of X on M ($a \ne 0$).
- 3. Test if there is a significant effect of M on Y controlling for $X(b \neq 0)$.
- 4. If all three steps are confirmed, test for partial vs. complete mediation.
 - 1. If X still has an effect on Y controlling for $M(c' \neq 0)$, this is partial mediation
 - 2. If X does not have a significant effect on Y controlling for M, complete mediation

Appeal

- · Easy to do, just need regression
- Intuitive

What's wrong with it?

- · No estimate of the indirect effect
- · No quantification of uncertainty about conclusion
 - p-value
 - · Confidence Interval
- · Requirement that the total effect is significant before looking for indirect effect
- · Issues with complete and partial mediation

Bootstrap Confidence Intervals (Percentile)

Empirically estimate sampling distribution of the indirect effect. From this distribution compute confidence intervals which can be used for estimation and hypothesis testing.

- 1. Randomly sample *n* cases from your dataset with replacement.
- 2. Estimate the indirect effect using resampled dataset, call this $ab^{(1)}$
- 3. Repeat steps 1 and 2 a total of K times where K is many (10,000 recommended), each time calculated ab(k).
- 4. The sampling distribution of the ab(i)'s can be used as an estimate of the sampling distribution of the indirect effect.
- 5. For a 95% confidence interval the lower and upper bounds will be the 2.5th and 97.5th percentiles of the K estimates of the indirect effect.

- · No assumptions about the sampling distribution of the indirect effect
- · Provides point estimate of indirect effect
- · Can calculate confidence intervals
- · Good method balance Type I Error and Power

What's wrong with it?

- · Most software does not have this functionality built in
- · Requires original data

Joint Significance

Method

- 1. Test if there is a significant effect of X on M ($a \neq 0$).
- 2. Test if there is a significant effect of M on Y controlling for $X(b \neq 0)$.

Appeal

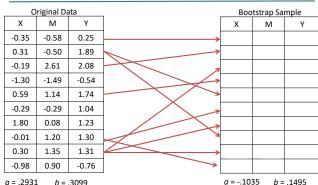
- · Easy to do, just need regression
- · Solves issues of requirement of significant total effect to claim an indirect effect.
- · Good method balance Type I Error and Power

What's wrong with it?

- · No estimate of the indirect effect
- · No quantification of uncertainty about conclusion
 - p-value
 - · Confidence Interval

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Bootstrap Confidence Intervals

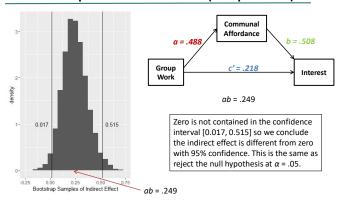


a = .2931b = .3099

ab = .0908

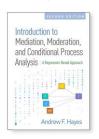
ab = -.0155

Bootstrap Confidence Intervals (CompSci Data)



PROCESS

PROCESS is a macro available for SPSS and SAS written by Andrew F. Hayes, documented in Mediation, Moderation, and Conditional Process Analysis, and available for free online at processmacro.org



Published in January 2018 and available through The Guilford Press, Amazon.com, and elsewhere.

- PROCESS integrates a variety of macros previously developed by Hayes: SOBEL, INDIRECT, MODMED, MODPROBE, MED3C. If you are using any of these now, switch to PROCESS.
- · Current version is 3.0
- PROCESS can assess a variety of models. Find the model you are interested in in the templates file, then use that model number.
- · Appendix A of IMMCPA provides complete documentation of options in PROCESS and how to use them.
- Version 3 allows for specifying your own models (not from templates)

The Monte Carlo interval

Monte Carlo empirically estimate the sampling distribution of the indirect effect and generate a confidence interval (CI) for estimation and hypothesis testing. This simulation based method assumes each individual path (a and b) are normally

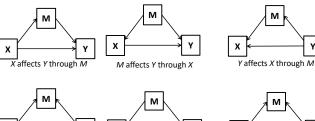
- (1) Generate k samples from a normal distribution with mean a and standard
- (2) Generate k samples from a normal distribution with mean b and standard deviation s_h
- (3) Multiply samples together to get a distribution of k estimates of ab.
- (4) Rank order estimates and select estimates which define the lower percentile of sorted *k* estimates and upper percentile of sorted estimates which define CI of interest.
- (5) For 95% CI lower and upper bounds are 2.5th and 97.5th percentile in k bootstrap estimates of the indirect effect.

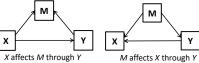
This method performs well (similarly to bootstrapping) in a variety of simulation studies, but is still less popular.

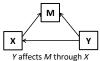
This method makes stronger assumptions than bootstrapping, but does not seem to result in greater power.

A Brief Caution on Causality

There are a number of alternative causal processes that may be occurring when a statistical indirect effect is present:







A Brief Caution on Causality

What you get by manipulating X. X affects Y through M X affects Y through Y X affects M through Y M affects X through Y Y affects M through Y Y affects M through Y

Even when *X* is manipulated, we can not provide evidence for the causal order between *M* and *Y*. This can only be supported using other experiments or previous research. *A statistically significant indirect effect does not lend credence to one model over another.*

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Repeated Measures Data

MEMORE is for **two-instance repeated measures** mediation analysis, where the causal variable of interest is the factor which differs by repeated measures.

X: varies between repeated measurements

M: measured in each of the two instances

Y: measured in each of the two instances

Evamples

- Participants read two scenarios. Interested in how scenario influences Y through M. Measure M and Y in each scenario.
- Pre-post test: Therapist measures certain symptoms and various outcomes before administering some intervention, and after administering the intervention.
- Researcher interested in if male partners in heterosexual relationships believe fights are less severe because they are less perceptive of small "squabbles".
 Measure both male and female partners in relationships, self report number of small "squabbles" and severity of last fight.

Non-Examples:

- Does calorie consumption impact body image through weight gain over time?
- Any instance where repeated-measure factor is a "nuisance" (e.g. studying schools, but not interested in comparing schools directly).

Repeated Measures Data

There are many different kinds of "repeated measures data." What type of data you have will determine what kind of mediation analysis is appropriate.

Types of Repeated Measurements:

- Each person over time
- Nested/Multilevel data (individuals within schools, cohorts, etc)
- Dyadic data (twins, couples, labmates, roommates)
- Each person in a variety of circumstances
- and many more...

What is measured repeatedly?

- Specifically in mediation, it's important to think about how/when/how many times the variables in your mediation model are measured
- Multilevel has a nice system referring to levels (1-1-1 mediation, 2-2-1, mediation etc.
- Is your causal variable measured repeatedly?
- Is your causal variable what differentiates your repeated measurements?

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Running Example: Group Work in Computer Science (WS)

Montoya, A. K. (2013) Increasing Interest in Computer Science thought Group Work: A Goal Congruity Approach (Undergraduate Honors Thesis).

Within-Subjects Version (CompSci_WS.sav):

Female participants (N = 51) read <u>two syllabi</u> for a different computer science classes. One of the syllabi reported the class would have group projects throughout, and the other syllabi stated that individual project would be scheduled throughout.

Syllabi also differed in professor's name (but not gender), and the primary
programming language used in the class.

Measured Variables:

- Interest in each the class (same as BS version)
 - Two measures: int_i int_g
- Perceptions that the class has a communal environment.
- Two measures: comm_i comm_g
- Taking this class would assist me in _____
- Helping others, serving the community, working with others, connecting with others, caring for others.
- How difficult would you rate the class you read about?
 - Two measures: diff i diff g

Judd, Kenny, and McClelland (2001)

Judd, C. M., Kenny, D. A., & McClelland, G. H. (2001). Estimating and testing mediation and moderation in within-subject designs. *Psychological Methods*, *6*, 115-134.



One of the few treatments of mediation analysis in this common research design.

A "causal steps", Baron and Kenny type logic to determining whether M is functioning as a mediator of X's effect on Y when both M and Y are measured twice in difference circumstances but on the same people.

- 1. On average, does Y differ by condition?
- 2. On average, does M differ by condition?
- 3. Does difference in M predict a difference in Y?
- 4. Does the difference in *M* account for all the difference in *Y*?

Analysis using Judd et al. (2001)

1. On average, does Y differ by condition?

Setup a model of the outcome in each condition:

$$Y_{1i} = c_1 + \epsilon_{Y_{1i}^*}$$

 $Y_{2i} = c_2 + \epsilon_{Y_{2i}^*}$ Is c_1 different from c_2 ?

Based on these models, setup a new model where you can directly estimate and conduct inference on what you are interested in (in this case c_2-c_1):

$$Y_{2i} - Y_{1i} = (c_2 - c_1) + (\epsilon_{Y_{2i}^*} - \epsilon_{Y_{1i}^*}) = c + \epsilon_{Y_i^*}$$

Use intercept only regression analysis, or a paired sample t-test, or a one sample t-test on the differences to conduct inference on c_2-c_1

With the data: On average, is class interest higher in the group work condition?

	Paired Samples Test									
				Paired Different						
				Std. Error	95% Confidence Interval of the Difference					
		Mean	Std. Deviation	Mean	Lower	Upper	t	df	Sig. (2-tailed)	
Pair 1	int_G - int_I	.37255	1.99585	.27948	18879	.93389	1.333	50	.189	

Computer Science Within-Subjects Data Example

Montoya, A. K. (2013) Increasing Interest in Computer Science thought Group Work: A Goal Congruity Approach (Undergraduate Thesis).

Research Question: Can group work in computer science classes increase women's interest by increasing their perception that computer science is communal?

Data is in wide form: repeated measurements of the same variables are saved as separate variables (one row per participant). Long form is when there is a variable coding instance of repeated measurements (multiple rows per participant, one for each instance).

	CompSc	i_WS.sav	
int_l	int_G	comm_l	comm_G
1.50	4.00	1.00	6.80
2.75	3.25	2.00	5.40
5.75	2.50	3.20	3.60
3.50	5.75	1.60	5.20
2.25	2.00	4.40	4.60
1.50	1.75	3.00	5.00
2.50	4.25	4.20	4.40
6.00	1.75	4.80	2.40
3.00	2.00	2.60	5.80
4.00	5.25	1.60	5.00
5.00	5.00	4.60	6.20
2.00	1.75	3.80	4.20
1.00	1.75	2.60	3.20
1.25	4.50	1.00	6.00
5.75	4.50	2.60	6.00
3.25	4.75	3.00	6.20
2.75	2.25	4.80	4.60
5.50	2.00	4.00	7.00
1.75	5.25	1.60	5.60
4.00	5.50	1.80	5.40
2.25	4.00	2.20	4.80
4.00	6.50	2.00	6.80
5.00	4.50	3.20	6.00

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Analysis using Judd et al. (2001)

2. On average, does M differ by condition?

Setup a model of the mediator in each condition:

$$M_{1i} = a_1 + \epsilon_{M_{1}i}$$

 $M_{2i} = a_2 + \epsilon_{M_{2}i}$ Is a_1 different from a_2 ?

Based on these models, setup a new model where you can directly estimate and conduct inference on what you are interested in (in this case a_2-a_1):

$$M_{2i} - M_{1i} = (a_2 - a_1) + (\epsilon_{M_{2i}} - \epsilon_{M_{1i}}) = a + \epsilon_{M_i}$$

Use intercept only regression analysis, or a paired sample t-test, or a one sample t-test on the differences to conduct inference on $a_2 - a_1$

With the data: On average, is communal goal affordance higher in the group work condition?

T-TEST PAIRS=comm_G WITH comm_I (PAIRED).

Analysis using Judd et al. (2001)

3. Does difference in M predict a difference in Y? / Does M predict Y controlling for condition?

Setup a model of the outcome in each condition:

$$Y_{1i} = g_{10} + g_{11}M_{1i} + \epsilon_{Y_{1i}}$$
$$Y_{2i} = g_{20} + g_{21}M_{2i} + \epsilon_{Y_{2i}}$$

Note that there are **two estimates** of the effect of M on Y. Let's average them to estimate an average effect of M on Y. Setup a new model where you can directly estimate and conduct inference on what you are interested in (in this case $\frac{1}{2}(g_{21}+g_{11})$):

$$Y_{2i} - Y_{1i} = (g_{20} - g_{10}) + g_{21}M_{2i} - g_{11}M_{1i} + (\epsilon_{Y_{2i}} - \epsilon_{Y_{1i}})$$
 Optional board work
$$Y_{2i} - Y_{1i} = (g_{20} - g_{10}) + \underbrace{\frac{g_{21} + g_{11}}{2}}_{b} (M_{2i} - M_{1i}) + \underbrace{\frac{(g_{21} - g_{11})}{2}}_{d} (M_{2i} + M_{1i}) + (\epsilon_{Y_{2i}} - \epsilon_{Y_{1i}})$$

Analysis using Judd et al. (2001)

4. Does the difference in communal goal affordance account for all the difference in interest?

$$Y_{2i} - Y_{1i} = (g_{20} - g_{10}) + \underbrace{\frac{g_{21} + g_{11}}{2}}_{b} (M_{2i} - M_{1i}) + \underbrace{\frac{(g_{21} - g_{11})}{2}}_{c} (M_{2i} + M_{1i}) + (\epsilon_{Y_{2i}} - \epsilon_{Y_{1i}})$$

Next we center the sum term, so the intercept has the interpretation of the predicted difference in Y for someone with no difference in M's but is average on M's.

$$\begin{split} Y_{2i} - Y_{1i} &= c' + b(M_{2i} - M_{1i}) + d(M_{2i} + M_{1i} - (\overline{M_2 + M_1})) + (\epsilon_{Y_{2i}} - \epsilon_{Y_{1i}}) \\ \text{where} \qquad c' &= (g_{20} - g_{10} + d(\overline{M_2 + M_1})) \end{split}$$

Intercept is predicted *outcome* when all regressors are zero. This means predicted difference in *Y* when there is no difference in *M* and a person is average on the sum of *M*.

Analysis using Judd et al. (2001)

3. Does M predict Y controlling for condition?

With the data: Does communal goal affordance predict interest in the class?

```
compute int_diff = int_G - int_I.
compute comm_diff = comm_G - comm_I.
compute comm_sum = comm_G+comm_I.
EXECUTE.
regression dep = int_diff /method = enter comm_diff comm_sum.
```

Coefficients^a

		Unstandardize	d Coefficients	Standardized Coefficients		
Model		В	Std. Error	Beta	t	Sig.
1	(Constant)	1.310	1.877		.698	.489
	comm_diff	.590	.135	.526	4.385	.000
	comm_sum	275	.216	153	-1.272	.210



a. Dependent Variable: int_diff

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Analysis using Judd et al. (2001)

4. Does the difference in communal goal affordance account for all the difference in interest?

With the data: Is there a significance difference in interest predicted when there is no difference in communal goals?

```
compute comm_sumc = comm_G+comm_I- 8.325490.
EXECUTE.
regression dep = int_diff /method = enter comm_diff comm_sumc.
```

Coefficients^a

		Unstandardize	d Coefficients	Standardized Coefficients			
Model		В	Std. Error	Beta	t	Sig.	
1	(Constant)	981	.388		-2.527	.015	
	comm_diff	.590	.135	.526	4.385	.000	
	comm_sum	275	.216	153	-1.272	.210	



a. Dependent Variable: int_diff

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Analysis using Judd et al. (2001)

On average, is interest higher in the group work condition?

On average, is communal goal affordance higher in the group work condition?

Does difference in communal affordance predict a difference in interest?

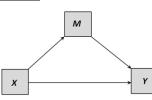
Does the difference in communal goal affordance account for all the difference in interest?

According to Judd, Kenny, and McClelland we do not have a mediated effect!

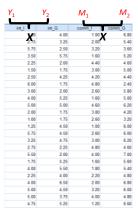
Because there is no evidence that interest is higher in the group work condition, the Judd et al. (2001) method would conclude there is not mediation.

Can we think about it like a path analysis?

Analytic Goal: Can group work in computer science classes increase women's interest by increasing their perception that computer science is communal?



Where is X in the data?



Judd et al. Criticisms and Misuses

All criticisms of the causal steps approach apply to this approach:

- There is no explicit quantification of the indirect effect
 - Inference about an indirect effect should be the result of a test on a quantification of the indirect effect
- · Requiring that there must be a total effect is too restrictive
 - · The direct and indirect effect could be of opposite sign
 - There is greater power to detect the indirect effect than total effect (Judd, Kenny, 2014, Psych Science)

This method has been used by a variety of researchers:

- · Approximately 300 citing papers, with around 140 using this method
- Many researchers do not report or estimate the partial regression coefficient for the sum of the mediators
- Because the estimate of the indirect effect is not made explicit, researchers often misinterpret the coefficients
 - b path is often interpreted as indirect effect
- · Extensions to more complicated models have been poorly implemented

Advantages of a path analytic approach

Provides an estimate of the indirect, total, and direct effects

 Allows us to conduct inferential tests directly on an estimate of the indirect effect

Connects researchers understanding of between-subjects mediation to within-subjects mediation

· Reduce misinterpretation of regression coefficients

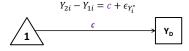
Using a path analytic framework will help extend the simple mediation model to more complicated questions

- · Multiple mediators
- · Moderated mediation
- · Integration of between and within-subjects designs

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Path-Analytic Approach

Total Effect (c): The effect of our presumed cause (X) on our outcome (Y), without controlling for any other variables. (i.e. mean difference in outcome between the two conditions).



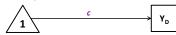
 α -path: The effect of our presumed cause (X) on our mediator (M). (i.e. mean difference in mediator between the two conditions).

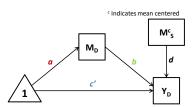
$$M_{2i} - M_{1i} = \mathbf{a} + \epsilon_{M_i}$$



Path-Analytic Approach

Indirect Effect (ab): Product of effect of X on M, and effect of M on Y controlling for X. The effect of X on Y through M.



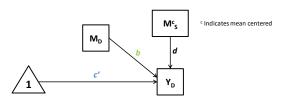


Path-Analytic Approach

b-path: The effect of our mediator (M) on the outcome (Y) while controlling for X. (i.e. predicted difference in Y for two people with the same score on X but who differ on M by one unit).

Direct effect (c'): The effect of our presumed cause (X) on Y while controlling for M. (i.e. predicted difference in Y for two people who differ by one unit on X but with the same score on M)

$$Y_{2i} - Y_{1i} = c' + b(M_{2i} - M_{1i}) + d(M_{2i} + M_{1i} - (\overline{M_2 + M_1})) + \epsilon_{Y_i}$$

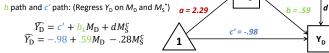


Within Subjects: Path Estimates

Total Effect c: (Regress Y_D on a constant) c = 0.373 \mathbf{Y}_{D} $\widehat{Y_{\rm D}} = c$ $\hat{Y_{\rm D}} = .373$

 α path: (Regress M_D on a constant)

 $\widehat{M_{\rm D}} = a$ $\widehat{M_{\rm D}} = 2.29$



A one unit increase in the difference in communal goal affordance is expected to result in a .59 unit increase in the difference in interest.

People with no difference in communal goal affordance perceptions are expected to be .98 units more interested in the individual class than the group work class.

Note: M, must be mean centered for c' to have intended interpretation

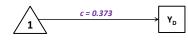
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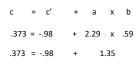
c Indicates mean centered

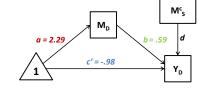
 M_s^c

Data Example: Partitioning effect of X on Y

The effect of X on Y partitions into two components: direct and indirect, in the usual way.







We can conduct inferential tests on the estimate of the indirect effect as in any other mediation analysis.

MEMORE has three methods of inference for the indirect effect available: bootstrapping, Monte Carlo confidence intervals, Sobel Tests

Writing MEMORE Syntax

MEMORE has 2 required arguments: Y and M

MEMORE m= comm_G comm_I /y = int_G int_I /normal=1/samples=10000
/conf = 90 /model = 1.

M is your list of mediators (order matters)

Y is you list of outcomes (order should be matched to the order in the M list)

Arguments:

mode1 specifies the model you are interested. The default is 1, mediation. Moderation models are 2 and 3.

normal = 1 asks for Sobel test

samples corresponds to the number of bootstrap/MC samples you would like
conf specifies level of confidence you want (default is 95)

mc = 1 asks for Monte Carlo confidence intervals

bc = 1 asks for bias corrected bootstrap confidence intervals

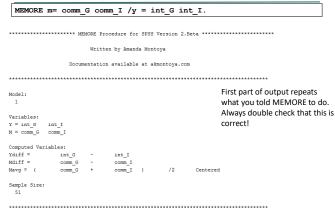
Teaching your package MEMORE

MEMORE is a command which must be taught and re-taught to your statistical package (SPSS) every time you open the package. To teach your program the MEMORE command, open the memore.sps file and run the script exactly as is.



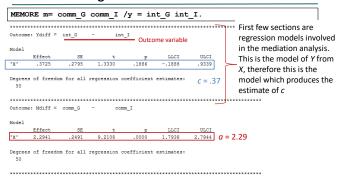
SPSS now knows a new command called MEMORE

Using MEMORE for CASC WS data



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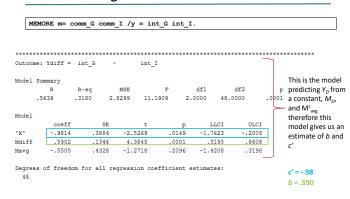
Using MEMORE for CASC WS data



Using MEMORE for CASC WS data

MEMORE m= comm G comm I /y = int G int I. Total effect of X on Y Effect ULCI Important effects .2795 1.3330 50.0000 -.1888 .9339 .3725 .1886 for mediation and Direct effect of X on Y inference about these effects -2.5269 -.9814 .3884 48.0000 .0149 Indirect Effect of X on Y through M Based on a 95% bootstrap Effect BootSE BootLLCI BootULCI 1.3540 1.9653 confidence interval we have evidence of Indirect Key mediation! Ind1 X Mldiff -> Ydiff

Using MEMORE for CASC WS data



Turning off the XM interaction

$$Y_{2i} - Y_{1i} = c' + b(M_{2i} - M_{1i}) + d(M_{2i} + M_{1i} - (\overline{M_2 + M_1})) + \epsilon_{Y_i}$$

When we estimate this regression model, we allow the relationship between *M* and *Y* to differ by instance (*X*). This is like allowing for an interaction between *X* and *M* when estimating *Y*.

We do this by including the sum term in the regression model.

d estimates the difference in the relationship between $M_1 \rightarrow Y_1$ and $M_2 \rightarrow Y_2$. If we fix this coefficient to zero (do not include the sum term in the model) we fix the interaction to zero.

Turning off the XM interaction

	No int	eraction					Interaction
Outco	me: Ydiff =	int_G	- int	_I			
Model							c = .3725 (.2795)
louci	Effect	SE	t	p	LLCI	ULCI	
'X'	.3725	.2795	1.3330	.1886	1888	.9339	
50	es or rreedo		,	oefficient	estimates:	*****	******
50		*****	******	*****	estimates:	******	*******
50	*****	*****	******	*****	estimates:	*****	a = 2.2941 (.249
50 **** Outco	************ me: Mdiff = Effect	**************************************	********** - com	******* m_I P	**************************************		a = 2.2941 (.249)
50 **** outcom	************ me: Mdiff = Effect	**************************************	********* - com	******* m_I P	****		a = 2.2941 (.249)

Writing up a Repeated Measures Mediation Analysis

Tips

- Walk the reader through the steps of the mediation in a way that is intuitive.
- Include interpretations of the results: b.e.g. "The total effect was significant, p < .05"
- Use equations and numbers where helpful.
- · Avoid using computational variable names (e.g. RESPAPPR)
- Avoid causal language if it is not supported by your research design.
- · Pick one inferential method and report it
- · Read the write ups of other's mediation analyses

Is the effect of group work on class interest mediated by communal goal affordance of the class?

Overall there was no evidence of a total effect of group work on interest in computer science classes, we estimate that individuals were .37 units higher on interest in group work than individual work classes (p=.19). The class with group work was rated 2.29 units higher on communal goal affordance than the class with individual work (p <.001). A one unit increase in perception of communal goal affordance increased interest in the class by .59 units (p <.0001), and the relationship between communal goal affordance and interest in a class did not depend on condition (p <.001). The effect of group work on interest through communal goal affordance and interest in a class did not depend on condition (p < 2.1). The effect of group work on interest through communal goal affordance, and the subsequent effect one without group work, through the effect of group work on communal goal affordance, and the subsequent effect of communal goal affordance on interest. There was a significant direct effect between group work and interest (c' = -.98, p = .01). This indicates that there may be some other process, separate from communal goal affordance, which is actually deterring women from computer science classes with group work.

Turning off the XM interaction

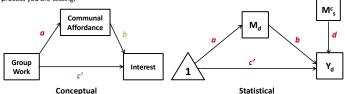
MEMORE m= comm G comm I /y = int G int I /xmint = 0. No interaction Interaction *************** Outcome: Ydiff = int_G Model Summary df2 .5432 .2950 2.8655 20.5060 49.0000 .0000 1.0000 Model coeff SE LLCI ULCI c = -.9814(.2795)'X' -1.0257 .3893 -2.6349 .0112 -1.8079 -.2434 b = .5902 (.1346)Mdiff .6095 .1346 4.5284 .0000 .3390 .8799 Indirect Effect of X on Y through M Effect BootSE BootLLCT BootULCI ab = 1.3540 [.6827, 1.9653].3082 .8034 2.0156

Ultimately results are mostly unchanged, but that is not always the case.

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Visualizations

I suggest using both a conceptual and statistical visualization in order to help the reader understand the process you are testing.



Ting

- Providing a conceptual diagram helps the readers understand the process you are interested in
- Providing a statistical diagram helps readers understand how you estimated the model, and that you did it correctly.
- Provide path estimates on statistical diagram or in a table.
- Don't forget to report the path estimates and statistics for the d path. It's important!

Common Questions

Can this method be used for more than two conditions?

YES! Judd, Kenny, and McClelland (2001) describe a system for setting up contrasts among conditions, and testing the indirect effects of those contrasts.

I recommend reading Hayes & Preacher (2014) on mediation analysis with a multicategorical IV if you want to try this out. I am happy to give instructions on how to trick MEMORE into doing this. There will be functionality (soonish) for MEMORE to do this.

ALTERNATIVES: Some of the other repeated-measures mediation options are more appropriate if you have more than two conditions (especially longitudinal), so take a look at those when thinking about these options.

Can I use multiple mediators?

YESI MEMORE is already set up to do parallel mediation with up to 10 sets of mediators and serial mediation with up to **five** sets of mediators (See Montoya & Hayes 2017 for instructions).

Can we do conditional process models?

VERY SOON!

How do I control for covariates?

All of MEMORE's mediation analyses are within-person models, so you do not need to control for any between subjects variables such as age, gender, big-5.

Sometimes there are covariates which change within a person across conditions that you want to account for, this can be done by treating this additional variable as another set of mediators.

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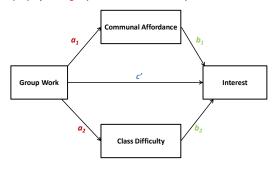
Using MEMORE for CASC WS data

Do people just like group work classes because they are easier?

														cont	ce that rolling	for dif	ficul
Outcome			= int_	I	-	int_G	;							estin	nating munal	the eff	
		R	R-sq		MSE		F		df1		df2		р	affor	rdance	on into	erest
	. 630	7	.3978	2	.6073	7.5	978	4.0	000	46.0	000	.00)1				
Model																	
		coe	ff	SE		t		df		р	LI	CI	1	ULCI			
'x'		.91	72	.3815	2	.4042	46.	0000		203	.14	193	1.	6851			
Mldiff		.48	47	.1448	3	.3460	46.	0000		016	.19	931		7762]		
M2diff		41	23	.1878	-2	.1952	46.	0000		332	79	904		0342			
Mlavg		.51	60	.4157	1	.2411	46.	0000		2209	32	209	1.	3528			
M2avg		37	81	.2879	-1	.3133	46.	0000		1956	95	577		2014			

Using MEMORE for CASC WS data

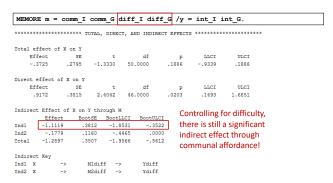
Do people just like group work classes because they are easier?



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Using MEMORE for CASC WS data

Do people just like group work classes because they are easier?





Example: Drug Name Fluency

Dohle, S., & Montoya, A. K. (2017). The dark side of fluency: Fluent names increase drug dosing. Journal of Experimental Psychology: Applied, 23(3), 231 – 239.

- 1. Estimate the proposed model (Fluency -> Hazardousness -> Dosage) using MEMORE
- 2. Turn off the XM interaction
- 3. Find estimates of the following paths: a, b, c, c'
- 4. Of the following inferential methods, which support the hypothesized mediation model (use $\alpha=0.05$ or 95% confidence intervals): Percentile bootstrap CIs, bias corrected CIs, Monte Carlo CIs, Sobel Test / Normal
 - Percentile bootstrap Cls, bias corrected Cls, Monte Carlo Cls, Sobel Test / Norma Theory
- 5. Practice writing up some of the results explored above.

Raise your hand with Questions!

Example: Drug Name Fluency

Dohle, S., & Montoya, A. K. (2017). The dark side of fluency: Fluent names increase drug dosing. Journal of Experimental Psychology: Applied, 23(3), 231 – 239.

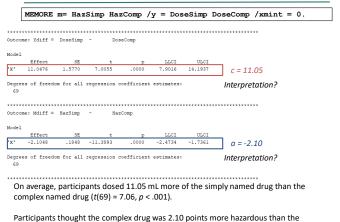
Participants (N = 70) were asked to imagine they had the flu, and 6 different drugs were provided to treat the drug. Participants poured the dose they would feel comfortable taking at maximum into a plastic cup. Each person judged drugs with simple or complex names (3 of each). Responses on the measured variables were averaged across the 3 drugs (but later we'll look at what happens when we treat these separately).

Measured Variables:

- Dosage in mL
 - Variable name: Dose
 - 0 mL 200mL
- Hazardousness of drug
 - Variable name: Haz
 - Average of two questions:
 - Hazardousness (1-9)
 - Dangerousness (1-9)

<table-cell-rows> *FluencyE</table-cell-rows>	FluencyData_Avg.sav [DataSet1] - IBM SPSS Statistics Data Editor								
<u>F</u> ile <u>E</u> dit	<u>V</u> iew <u>D</u> ata	Transform Anal	yze Direct <u>M</u> ark	eting <u>G</u> raphs					
⊜ ⊩	1 🖨 🗔		E						
		1							
	HazSimp	HazComp	DoseComp	DoseSimp					
1	2.50	7.50	46.00	58.33					
2	7.00	7.00	84.33	86.67					
3	6.50	6.50	68.67	70.00					
4	3.00	5.67	118.00	152.00					
5	6.50	5.17	45.00	48.33					
6	2.83	4.83	40.33	53.00					
7	2.67	4.50	153.67	139.00					
8	5.00	5.00	5.00 140.67						
9	4.67	6.67	71.67	69.67					
10	2.50	6.67	53.00	91.67					
11	4.67	5.00	142.00	143.00					
		7.00	70.07	01.00					

Using MEMORE for Drug Fluency data



simply named drug, on average (t(69) = 11.39, p < .001).

Using MEMORE for Drug Fluency data

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp.

Outcome: Ydiff = DoseSimp - DoseComp

Model Summary R-sq MSE dfl .1616 148.1029 13.1047 1.0000 68.0000 .0006 .4020

c' = 3.83 Interpretation? .1256 -1.0978 8.7537 b = -3.43 Interpretation?

Degrees of freedom for all regression coefficient estimates:

Mode1

After controlling for hazardousness, participants were expected to dose 3.8 mL more of the simple drug. This effect was not significantly different than zero (t(68) = 1.55, p= .13).

A one unit increase in the difference in perceived hazardousness between conditions results in a 3.43 unit decrease in the difference in dosage (t(68) = 3.62, p < .001).

A one unit increase in perceived hazardousness results in a 3.43 unit decrease in dosage, averaged across fluency conditions (t(68) = 3.62, p < .001).

Using MEMORE for Drug Fluency data

Methods of Inference

Percentile Bootstrap CI

Bias Corrected Bootstrap CI

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp /xmint = 0.

Indirect Effect of X on Y through M Effect BootSE BootLLCT BootULCT

7.2197 Indl 1.8940 3.8590

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp /xmint = 0 /bc = 1.

Indirect Effect of X on Y through M Effect BootSE BootLLCI BootULCI Indl 7.2197 1.9274 3.6702

Monte Carlo CI

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp /xmint = 0 /mc = 1.

Indirect Effect of X on Y through M Effect MCSE MCLLCI Ind1 7.2197 2.0916 3.2369 11.3834 **Using MEMORE for Drug Fluency data**

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp. Total effect of X on Y 11.0476 1.5770 7.0055 69.0000 .0000 7.9016 14.1937 df 2.4684 1.5508 68.0000 .1256 -1.0978 Indirect Effect of X on Y through M Effect BootSE BootLLCI BootULCI ab = 7.22 Interpretation? Indirect Kev Mldiff -> Indl 'X'

Participants were dosed simple drugs 7.22 mL more, through the effect of simple drugs on hazardousness and the subsequent effect of hazardousness on dosage (Percentile CI = [3.86,

Drug name fluency increased dosage indirectly effect through hazardousness by 7.22 mL (Percentile CI = [3.86, 11.16]).

Simple names were perceived as less hazardous, which then increased dosage, resulting in an indirect effect of 7.22 mL on dosage (Percentile CI = [3.86, 11.16]).

Using MEMORE for Drug Fluency data

Methods of Inference

Sobel Test / Normal Theory

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp /xmint = 0 /normal = 1. Normal Theory Tests for Indirect Effect

Effect 7.2197 2.0927 3.4500 JKM Causal Steps

MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp.

Outcome: Ydiff = DoseSimp -Model Summary df1 MSE

SE

.1616 148.1029 13.1047 1.0000 68.0000 .4020 Model

coeff .1256 .0978 3.8280 2.4684 1.5508 Mdiff -3.4302 .9475 -3.6200

Degrees of freedom for all regression coefficient estimates:

Mediation

- Between Subjects Mediation
 - · Path analytic approach
 - Interpretation
 - Estimation
 - Inference
- · Repeated Measures Data
- Two-Instance Repeated-Measures Mediation
 - Judd Kenny and McClelland (2001)
 - · Path analytic approach
 - · Estimation of Indirect Effects
 - MEMORE
 - Reporting (Writing and Figures)
 - Common Questions



New York Elegance

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Part II: Mediation and Multilevel Modeling

One of the primary assumptions of Ordinary least squares (OLS) regression is that each observation is independent of all other observations.

Ordinary least squares (OLS) regression is not directly applicable when data are nested.

- · Students nested within classrooms
- · Employees nested within companies
- · Repeated measurements nested within individuals

Responses from employees within the same company tend to be more related to each other than responses from employees in different companies.

This violates the assumption of independence.

Several methods are available for accounting for this dependence, but today we will focus on multilevel/mixed modeling.

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Multilevel Modeling

What's a level?

Students (Level 1) within classrooms (Level 2)
Employees (Level 1) within companies (Level 2)
Repeated measurements (Level 1) within individuals (Level 2)

Multilevel models are often expressed either as separate equations for the different levels of the model, or as one combined model.

Let i denote Level 1 units and j denote Level 2 units

 X_{ij} : Person i in group j's observation on X

 Y_{ij} : Person i in group j's observation on Y

 W_j : Group j's observation on W (Level 2 characteristics (e.g., Company size))

Two-Level Unconditional Model

Let's predict an outcome at Level 1 using a predictor from Level 1

$$Y_{ij} = b_{0j} + b_{1j}X_{ij} + e_{ij}$$

 b_{0j} : The expected value of Y for someone in group j with $X_{ij} = 0$. Notice this is allowed to vary by group! This is the **intercept** for group j.

 b_{1j} : The expected difference in Y for two people in the same group j that differ by 1 unit on X_{ij} . This is the **slope** for group j.

 e_{ij} : The error in estimating Y_{ij} . $e_{ij} \sim N(0, \sigma^2)$

Even if you're not familiar with multilevel models, this should look familiar to what we do in regression. Except the intercept and slope are allowed to randomly vary across groups. We call these *random effects*.

Two-Level Unconditional Model

We also create a Level 2 Model, for the intercept and slope:

$$Y_{ij} = b_{0j} + b_{1j}X_{ij} + e_{ij}$$

 $b_{0i} = b_0 + u_{0i}$

Notice that it's the u's that make the "random effects" random. By allowing the intercept and slope to vary across groups, we soak up all the "dependence" in the data.

 $b_{1j} = b_1 + u_{1j}$

 b_0 is the grand-mean intercept (i.e., the average intercept across groups)

 b_1 is the grand-mean slope (i.e., the average slope across groups)

We assume that $(u_{0j},u_{1j})\sim MVN(0,T)$ where $T=\begin{bmatrix} au_{00} & au_{01} \\ au_{01} & au_{11} \end{bmatrix}$

The random effects are not individually estimated, but rather we estimate their covariance matrix as well as the grand-mean intercept and slope.

Simplifying the Model

Not all coefficients need to be random. For example the intercept could be random but the slope could vary across groups:

$$Y_{ij} = b_{0j} + b_1 X_{ij} + e_{ij}$$

$$b_{0j} = b_0 + u_{0j}$$

$$b_1 = b_1$$

 b_0 is the grand-mean intercept (i.e., the average intercept across groups)

 b_1 is the slope (assumed to be the same for all groups)

This is like a special case where we assume $au_{11}=0$

We will mostly use the case where we have random-slopes as this is what adds complexity to mediation in multilevel models.

The Combined Model

Sometimes it's clearer to represent both the Level 1 and Level 2 equations together in a *combined model*. We plug in the Level 2 equations in their spots in the Level 1 model

$$Y_{ij} = b_{0j} + b_{1j}X_{ij} + e_{ij}$$

$$Y_{ij} = (b_0 + u_{0j}) + (b_1 + u_{1j})X_{ij} + e_{ij}$$

We can combine and rearrange terms to separate the parts of the model which are random and those which are not random (i.e., fixed).

$$Y_{ij} = \left(b_0 + b_1 X_{ij}\right) + u_{0j} + u_{1j} X_{ij} + e_{ij}$$
 Fixed: does not vary Random: varies by

by group group

You can see how each individual's response is a function of the **overall intercept** the **overall slope** as well as their **group's deviations** from the overall intercept and slope and a **individual-specific error**.

Adding Level 2 Predictors

We can explain variability in the group intercept or slope using characteristics of the Level 2 units.

$$Y_{ij} = b_{0j} + b_{1j}X_{ij} + e_{ij}$$

$$b_{0j} = b_0 + g_{01}W_j + u_{0j}$$

$$b_{1j} = b_1 + g_{11}W_j + u_{1j}$$

 b_0 is the expected group intercept when W_i is zero.

 b_1 is the expected group slope when W_i is zero.

 g_{01} is how much we expect the intercept to change with a one unit change in W_i

 g_{11} is how much we expect the slope (relationship between X and Y) to change with a one unit change in W_i

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E

Adding Level 2 Predictors

We can rewrite the model as a *combined* model, by combining Level 1 and Level 2 equations:

You can see in the combined equation that by including W_j as a predictor of the *slope* we include an <u>interaction</u> between W_i and X_{ij} .

This means the effect of X on Y depends on the value of W.

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Fluency Data

We can use the SPSS MIXED procedure to fit a multilevel model.

Let's look at the relationship between Dosage and Hazardousness using a model with a random intercept and a random slope.

```
MIXED Dose WITH Hazard

/Fixed = Hazard | SSTYPE(3)

/Method = REML

/Print = G Solution Testcov

/Random = INTERCEPT Hazard | Subject(id) COVTYPE(UN).
```

$$Y_{ij} = (b_0 + b_1 X_{ij}) + u_{0j} + u_{1j} X_{ij} + e_{ij}$$

 Y_{ij} : Dosage for observation i for person j X_{ij} : Hazardousness for observation i for person j

Give it a try!

Fluency Data

The Fluency data we used for within-subjects mediation (FluencyData_Avg.sav) is in wide form and we must convert it to long-form for multilevel modeling (FluencyData_Avg_long.sav).

```
VARSTOCASES
/ID=id
/MAKE Hazard FROM HazSimp HazComp
/MAKE Dose FROM DoseSimp DoseComp
/INDEX=Simple(2)
/KEEP=
/NULL=KEEP.

RECODE Simple (2=0) (1=1).
EXECUTE.
```

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Fluency Data: Fixed Effects

```
MIXED Dose WITH Hazard

/Fixed = Hazard | SSTYPE(3)

/Method = REML

/Print = G Solution Testcov

/Random = INTERCEPT Hazard | Subject(id) COVTYPE(UN).
```

Estimates of Fixed Effects^a

						95% Confidence Interval	
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	109.484321	4.932038	52.923	22.199	.000	99.591570	119.377072
Hazard	-4.838863	.615111	33.198	-7.867	.000	-6.090033	-3.587694

a. Dependent Variable: Dosing Simple.

The expected dose administration of drugs is 109.48 mL given a hazardousness rating of zero $(X_{ij}=0)$. But remember this is the "grand-mean" across groups.

For each one unit increase in harazardousness, dose administration of drugs is expected to decrease by 4.84 mL. Remember this is a "grand-mean" across groups.

Fluency Data: Random Effects

$$(u_{0j}, u_{1j}) \sim MVN(0, T)$$
 where $T = \begin{bmatrix} \tau_{00} & \tau_{01} \\ \tau_{01} & \tau_{11} \end{bmatrix}$

Estimates of Covariance Parameters

						95% Confid	ence Interval
Parameter		Estimate	Std. Error	Wald Z	Sig.	Lower Bound	Upper Bound
Residual		58.509962	18.167383	3.221	.001	31.836928	107.529709
Intercept + Hazard	UN (1,1)	1062.426086	309.657876	3.431	.001	600.074242	1881.015899
[subject=id]	UN (2,1)	-30.092244	35.454856	849	.396	-99.582485	39.397997
	UN (2,2)	5.018740	5.501233	.912	.362	.585545	43.015932

a. Dependent Variable: Dosing Simple.

There is substantial between-person variability ($au_{00}=1062.43$) in dosage of drugs with a hazardousness rating of zero.

The relationship between hazardousness and dos age varies across individuals ($au_{11} = 5.02$)

Those with higher-than-average dose values at $X_{ij}=0$ (hazardousness is zero) have lower-than-average slopes for the relationship between hazardousness and dosage $(\tau_{01}=-30.09)$

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Within-Group Centering

Typically variables at Level 1 contain information about Level 1 and Level 2.

Consider the hazardousness ratings: X_{ii}

Part of X_{ij} has to do with how hazardous **that specific drug** is compared to other drugs. (Level 1)

But another part has to do with how hazardous the person sees **drugs in general**. (Level 2)

$$X_{ij} = X_{ij} - \overline{X}_{j} + \overline{X}_{j}$$

Within-group/ Between-group/
Level 1 Level 2

 $\overline{X}_{.j}$ is the group j's mean of X_{ij}

Within-group centering divides these two pieces of information, so we can see what is predicted by Level 1 variance and what is predicted by Level 2 variance, separately.

The within and between group pieces are uncorrelated.

Centering Variables

There is substantial between-person variability ($\tau_{00}=1062.43$) in dosage of drugs with a hazardousness rating of zero.

When we interpret τ_{00} we condition of the predictor being zero (i.e., Hazardousness is zero).

In this data a score of zero is impossible for hazardousness because it's the average of two items scored 1-9. So the intercept and probably it's variance are not interpretable.

For multilevel models, there are two common centering options (grand mean centering and **group mean centering**).

The choice of centering has a big impact on the parameter estimates and their substantive meaning.

Enders, C. K. & Tofighi, D. (2007). Centering predictor variables in cross-sectional multilevel models: a new look at an old issue. *Psychological Methods*, 12(2), 121-138.

Within-Group Centering

To group mean center we subtract the group's mean of *X* from each observation on that predictor.

Person 1

Simple	Hazard	Hazard_Centered
0	7.50	2.50
1	2.50	-2.50
Group mean->	5	

Person 34

Simple	Hazard	Hazard_Centered
0	3.83	.58
1	2.67	58
Group mean->	3.25	

Within-Group Centering

AGGREGATE /OUTFILE = * MODE = ADDVARIABLES /BREAK = id /Hazard_m = MEAN(Hazard). COMPUTE Hazard_groupc = Hazard - Hazard_m. Execute.

Compute a new variable called Hazard_m, which will be the group mean of hazard.

Next we compute the group-mean centered hazard ratings, and call these Hazard_groupc.

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		*	id	🖧 Simple		i	∅ Dose		ırd_m 🏽 🛷	Hazard_	groupc
	1		1	1	2	.50	58.33	3	5.00		-2.50
	2		- 1	0	7	.50	46.00)	5.00		2.50
	3		2	- 1	7	.00	86.67	7	7.00		.00
	4		2	0	7	.00	84.33	3	7.00		.00
	5		3	1	6	.50	70.00)	6.50		.00

Contextual Effects

Sometimes we are interested in the within-group relationship between a Level 1 predictor and an outcome as well as the between-group relationship.

When the between-group effect is different from the within-group effect, we call this a contextual effect (Raudenbush & Bryk, 2002).

The within-group relationship is tested by including the group-mean centered Level 1 predictor.

The between-group relationship can be tested by adding the group mean of the Level1 predictor as a Level 2 predictor for the random intercept.

$$Y_{ij} = b_{0j} + b_{1j}(X_{ij} - \bar{X}_{.j}) + e_{ij}$$

$$b_{0j} = b_0 + g_{01}\bar{X}_{.j} + u_{0j}$$

$$b_{1i} = b_1 + u_{1i}$$

Within-Group Centering

Thinking about within and between group variance, we can see how there may be **two relationships** of interest:

- (1) How does within-group variance in X predict variance in Y?
- (2) How does between-group variance in X predict variance in Y?

$$\begin{split} Y_{ij} &= b_{0j} + b_{1j} X_{ij} + e_{ij} \\ \\ Y_{ij} &= b_{0j} + b_{1j} (X_{ij} - \bar{X}_{.j} + \bar{X}_{.j}) + e_{ij} \\ \\ Y_{ij} &= b_{0j} + b_{1j} (X_{ij} - \bar{X}_{.j}) + b_{1j} \bar{X}_{.j} + e_{ij} \end{split}$$

When we don't use any centering (or use grand mean centering) we're fixing the relationship between the within-group part of *X* and *Y* to be equal to the relationship between the between-group part of *X* and *Y*.

Ultimately this makes these coefficients difficult to interpret because they're a blend of these two relationship s(Raudenbush & Bryk, 2002).

Contextual Effects

The combined contextual effects model:

$$Y_{ij} = (b_0 + g_{01}\bar{X}_{.j} + u_{0j}) + (b_1 + u_{1j})(X_{ij} - \bar{X}_{.j}) + e_{ij}$$

$$Y_{ij} = b_0 + g_{01}\bar{X}_{.j} + b_1(X_{ij} - \bar{X}_{.j}) + u_{1j}(X_{ij} - \bar{X}_{.j}) + u_{0j} + e_{ij}$$
Fixed
Random

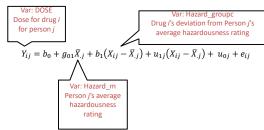
 b_1 represents the **average within-group effect** of X_{ij} on Y_{ij} . The variance in the **within-group effect** is $Var(b_{1j}) = Var(u_{1j}) = \tau_{11}$

 g_{01} represents the **between group effect** of X_{ij} on Y_{ij} .

When b_1 and g_{01} differ from each other, this means there is a contextual effect.

Contextual Effects

```
MIXED Dose WITH Hazard_groupc Hazard_m
    /Fixed = Hazard_groupc Hazard_m | SSTYPE(3)
    /Method = REML
    /Print = G Solution Testcov
    /Random = INTERCEPT Hazard_groupc |
Subject(id) COVTYPE(UN).
```



Mediation Modeling with Multilevel Data

Multilevel mediation processes are often labeled by the level at which each variable varies

- 1-1-1 implies that X, M, and Y are all measured at Level 1.
 Example: Measuring individuals on a variety of days, we may wonder if number of calories eaten before noon each day (X) predicts daily stress (Y) through improved productivity in the afternoon (M).
- 2-1-1 implies that X is measured at Level 2, but M and Y are at Level 1
 Example: Individuals are randomly assigned to either a healthy breakfast supplement (X) and tracked over a variety of days to see if their daily stress (Y) is improved through improved through afternoon productivity (M).
- 2-2-1 implies X and M are Level 2, but Y is measured at Level 1.
 Example: Perhaps individuals were randomly assigned to either a healthy breakfast supplement (X) and asked at the end of the week whether they felt able accomplish what they needed to in the afternoon this week (M) and we track their daily stress (Y).

Contextual Effects

```
 \begin{aligned} Y_{ij} &= b_0 + g_{01} \overline{X}_{,j} + b_1 (X_{ij} - \overline{X}_{,j}) + u_{1j} (X_{ij} - \overline{X}_{,j}) + u_{0j} + e_{ij} \\ \text{MIXED Dose WITH Hazard groupe Hazard m} & | \text{Fixed} &= \text{Hazard groupe Hazard m} | \text{SSTYPE (3)} \\ \text{/Method} &= \text{REML} \\ \text{/Print} &= \text{G Solution Testcov} \\ \text{/Random} &= \text{INTERCEPT Hazard groupe} \mid \text{Subject (id)} \\ \text{COVTYPE (UN)}. \end{aligned}
```

Estimates of Fixed Effects^a

						95% Confid	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	115.262328	19.454675	68.013	5.925	.000	76.441268	154.083388
Hazard_groupc	-4.827233	.669329	22.424	-7.212	.000	-6.213817	-3.440649
Hazard_m	-5.939038	3.603082	68.013	-1.648	.104	-13.128853	1.250776

a. Dependent Variable: Dosing Simple.

For drugs at each individual's group mean the expected dosage is 115.26 mL.

For two drugs that differ by 1 unit on hazardousness, the more hazardous drug is expected to be dosed 4.83 mL less, controlling for average hazardousness rating.

Individuals 1 unit higher on average rating of hazardousness, are expected to dose drugs 5.94 units less, controlling for deviation of the drug from the individual's average.

Mediation Modeling with Multilevel Data

You may notice that when some variables are at Level 2, they should not be able to predict Level 1 variability.

For example, knowing whether someone is in the breakfast supplement condition, should help us predict their average daily stress, but none of the deviation of day-to-day stress from the person's average.

As such we'll focus on the 1-1-1 model, as it is the most general multilevel mediation model that exists when all variables are measured at Level 1.

We can explore between-group and within-group variability. **Indirect effects** can occur at both levels!

General 1-1-1 Mediation Model

Recall the single-level (between-subjects) mediation model:

$$M_i = a_0 + a_1 X_i + e_{M_i}$$

 $Y_i = b_0 + c' X_i + b_1 M_i + e_{Y_i}$

Let's make it multilevel, where X, M, and Y are Level 1 variables:

$$M_{ij} = a_{0j} + a_{1j}X_{ij} + e_{M_{ij}}$$

$$Y_{ij} = b_{0j} + c'_{j}X_{ij} + b_{1j}M_{ij} + e_{Y_{ij}}$$

Let's use group-mean centering, because we're interested in differentiating within and between effects:

$$\begin{split} M_{ij} &= a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_{0j} + c'_{j}(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}} \end{split}$$

1-1-1 Mediation Model: Between-Group Effects

$$\begin{split} M_{ij} &= a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_{0j} + c_j'(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}} \end{split}$$

BUT WAIT! We haven't included between-group effects. How did we do that before?

Include \overline{X}_i as a Level 2 predictor of the intercept.

$$a_{0j} = a_M + a_B \, \bar{X}_{.j} + u_{a_0 j}$$

 $b_{0j} = b_Y + c'_B \, \bar{X}_{.j} + b_B \, \bar{M}_{.j} + u_{b_0 j}$

 a_B , b_B , and c_B' are the **between-group effects** of X and M, M on Y controlling for X, and X and Y controlling for M respectively.

1-1-1 Mediation Model: Within-Group Effects

$$M_{ij} = a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}}$$

$$Y_{ij} = b_{0j} + c'_{j}(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}}$$

 $a_{1j} = a_W + u_{a_1j}$ This is the within-group effect of X on M for group j

 $b_{1j} = b_W + u_{b_1j}$ This is the within-group effect of M on Y, controlling for X in group j

 $c_j' = c'_W + u_{c'j}$ This is the within-group effect of X on Y, controlling for M in group j

 a_W , b_W , and c_W' are the **average within-group effects** of X and M, M on Y controlling for X, and X and Y controlling for M respectively.

1-1-1 Mediation Full Model

$$M_{ij} = a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}}$$

$$Y_{ij} = b_{0j} + c'_{j}(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}}$$

$$a_{0j} = a_M + a_B \, \bar{X}_{.j} + u_{a_0 j}$$

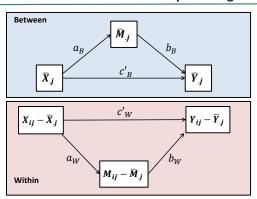
$$b_{0j} = b_Y + c'_B \, \bar{X}_{.j} + b_B \, \bar{M}_{.j} + u_{b_0 j}$$

$$a_{1j} = a_W + u_{a_1j}$$

$$b_{1j} = b_W + u_{b_1j}$$

$$c_j^\prime = c^\prime_W + u_{c\prime j}$$

1-1-1 Mediation Model: Conceptual Diagram

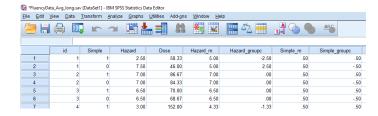


Estimating the M Equation

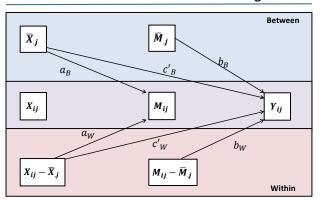
First we have to group-mean center Simple and create a variable which is the group mean of Simple.

```
AGGREGATE
/OUTFILE = * MODE = ADDVARIABLES
/BREAK = id
/Simple_m = MEAN(Simple).

COMPUTE Simple_groupc = Simple - Simple_m.
EXECUTE.
```



1-1-1 Mediation Model: Statistical Diagram



Estimating the M Equation

Next we predict Hazard from the group-mean centered Simple (Simple_groupc) and the group means of Simple (Simple_m)

```
MIXED Hazard WITH Simple_groupc Simple_m

/FIXED = Simple_groupc Simple_m | SSTYPE(3)

/METHOD = REML

/PRINT = G SOLUTION TESTCOV

/RANDOM = Intercept Simple groupc| Subject(id) COVTYPE(UN).
```

Estimates of Fixed Effects^b

						95% Confide	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	5.304762	.121182	69.000	43.775	.000	5.063010	5.546513
Simple_groupc	-2.104762	.184802	69.000	-11.389	.000	-2.473433	-1.736091
Simple_m	0ª	0		<u>. </u>			
- This second		on the course of	Ale or alcorde				

a. This parameter is set to zero because it is redundant. b. Dependent Variable: Hazardousness Simple.

UH OH! Something went wrong? What happened?

Simple_m

Estimating the *M* Equation

"Redundant" group-mean for simple

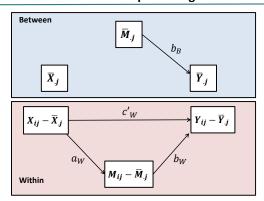
Person 1

Simple	Simple_Centered
0	50
1	.50
Group mean-> 0.5	

Person 34

Simple	Hazard_Centered
0	50
1	.50
Group mean-> 0.5	

Revised: Conceptual Diagram



Estimating the M Equation

"Redundant" group-mean for simple!

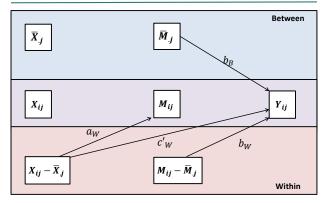
Because each participant complete both levels of Simple (0 and 1) one time each, all participants have a person-level mean of 0.5 (see Simple m)

This means there is no between-person variability on Simple, so the group means and the intercept are linear combinations of one another (Intercept = $2*Simple_m$; , the model is not identified).

We can remove the between-person effect of X from the model, meaning there will not be a between-person indirect effect.

$$\begin{split} a_{0j} &= a_M + \frac{1}{a_B \, \bar{X}_{.j}} + u_{a_0 j} = a_M + u_{a_0 j} \\ b_{0j} &= b_Y + \frac{1}{c_B' \, \bar{X}_{.j}} + b_B \, \bar{M}_{.j} + u_{b_0 j} = b_Y + b_B \, \bar{M}_{.j} + u_{b_0 j} \end{split}$$

Revised: Statistical Diagram



Estimating the M Equation (Again)

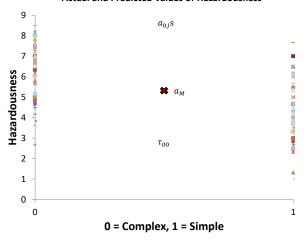
						95% Confide	ence Interval
Parameter		Estimate	Std. Error	Wald Z	Sig.	Lower Bound	Upper Bound
Residual		.653447	.203505	3.211	.001	.354910	1.203101
Intercept +	UN (1,1)	.701233	.202258	3.467	.001	.398426	1.234173
Simple_groupc [subject = id]	UN (2,1)	.071440	.188917	.378	.705	298830	.441710
	UN (2,2)	1.0837444	.000000				

This covariance parameter is redundant. The test statistic and confidence interval cannot be computed b. Dependent Variable: Hazardousness Simple.

Something has gone wrong with the variance for the slope!



Actual and Predicted Values of Hazardousness

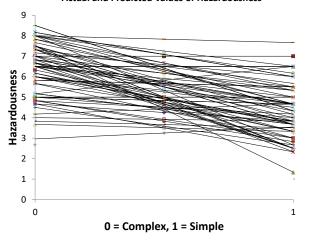


1-1-1 Mediation Full Model

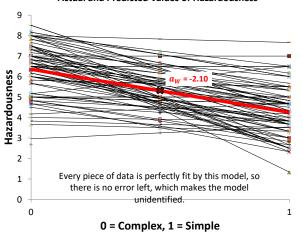
$$\begin{split} M_{ij} &= a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ a_{0j} &= a_M + u_{a_0j} \\ a_{1j} &= a_W + u_{a_1j} \\ M_{ij} &= (a_M + u_{a_0j}) + (a_W + u_{a_1j})(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ & \text{Each person get's their Each person get's their own intercept} & \text{own slope} \end{split}$$

We only have two observations per person, so giving each person their own intercept and their own slope would perfectly fit the data, and there will be no error left over!

Actual and Predicted Values of Hazardousness



Actual and Predicted Values of Hazardousness



Estimating the Y Equation

$$\begin{split} Y_{ij} &= b_{0j} + c_j'(X_{ij} - \bar{X}_{,j}) + b_{1j}(M_{ij} - \bar{M}_{,j}) \ + e_{Y_{ij}} \\ b_{0j} &= b_Y + \frac{c_B'}{B} \bar{X}_{,j} + b_B \ \bar{M}_{,j} + \ u_{b_0j} \\ c_j' &= c_W' + \frac{u_{crj}}{B} \end{split} \qquad \text{Cut out terms involving group mean of } X, \text{ remove random slopes} \\ b_{1j} &= b_W + u_{b_1j} \end{split}$$
 Why do we keep the term involving group mean of M ?

MIXED Dose WITH Hazard_groupc Hazard_m Simple_groupc /FIXED = Hazard_groupc Hazard_m Simple_groupc | SSTYPE(3) /METHOD = REML /PRINT = G SOLUTION TESTCOV /RANDOM = Intercept | Subject(id) COVTYPE(VC).

Estimating the M Equation (Again, Again)

Get rid of the random slope, assuming there is no variance in a_W

```
MIXED Hazard WITH Simple_groupc
/FIXED = Simple_groupc | SSTYPE(3)
/METHOD = REML
/PRINT = G SOLUTION TESTCOV
/RANDOM = Intercept | Subject(id) COVTYPE(VC).
```

Estimates of Fixed Effects^a

						95% Confide	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	5.304762	.121182	69.000	43.775	.000	5.063010	5.546513
Simple_groups	-2.104762	.184802	69.000	-11.389	.000	-2.473433	-1.736091

a. Dependent Variable: Hazardousness Simple.

An one unit increase in Simple_groupc (i.e., moving from the complex to simple condition) predicts a 2.10 unit decrease in perceptions of hazardousness averaged across individuals. $a_W=-2.10$

Estimating the Y Equation

$$\begin{split} Y_{ij} &= b_Y + b_B \; \overline{M}_{.j} + \; u_{b_0j} + c_W'(X_{ij} - \overline{X}_{.j}) + b_W \; (M_{ij} - \overline{M}_{.j}) \; + e_{Y_{ij}} \\ \text{MIXED Dose WITH Hazard_groupe Hazard_m Simple_groupe} \\ \text{/FIXED = Hazard_groupe Hazard_m Simple_groupe} \; | \; \text{SSTYPE(3)} \\ \text{/METHOD = REML} \\ \text{/PRINT = G SOLUTION TESTCOV} \\ \text{/RANDOM = Intercept} \; | \; \text{Subject(id) COVTYPE(VC)} \; . \end{split}$$

Estimates of Fixed Effects^a

						95% Confid	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	115.420197	19.457732	68	5.932	.000	76.592897	154.247498
Hazard_groups	-3.430154	.947546	68.000	-3.620	.001	-5.320953	-1.539354
Hazard_m	-5.968798	3.603669	68	-1.656	.102	-13.159807	1.222211
Simple_groups	3.827962	2.468446	68.000	1.551	.126	-1.097745	8.753670

a. Dependent Variable: Dosing Simple.

A one unit increase in deviation from the group mean on hazardousness, predicts a 3.43 mL decrease in dosage, controlling for group mean hazardousness and name complexity. $b_W=-3.43\,$

Estimating the Y Equation

$$Y_{ij} = b_Y + b_B \overline{M}_{.j} + u_{b_0j} + c'_W (X_{ij} - \overline{X}_{.j}) + b_W (M_{ij} - \overline{M}_{.j}) + e_{Y_{ij}}$$

MIXED Dose WITH Hazard_groupc Hazard_m Simple_groupc /FIXED = Hazard_groupc Hazard_m Simple_groupc | SSTYPE(3) /METHOD = REML

/PRINT = G SOLUTION TESTCOV

/RANDOM = Intercept | Subject(id) COVTYPE(VC).

Estimates of Fixed Effects^a

						95% Confid	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	115.420197	19.457732	68	5.932	.000	76.592897	154.247498
Hazard_groupc	-3.430154	.947546	68.000	-3.620	.001	-5.320953	-1.539354
Hazard_m	-5.968798	3.603669	68	-1.656	.102	-13.159807	1.222211
Simple_groups	3.827962	2.468446	68.000	1.551	.126	-1.097745	8.753670

a. Dependent Variable: Dosing Simple

A one unit increase in the group-mean hazard rating predicts a 5.97 mL decrease in dosage, controlling for deviation from the group-mean in hazard rating and name complexity. $b_R=-5.97$

Indirect Effects in Multilevel Modeling

$$\begin{split} M_{ij} &= a_M + u_{a_0j} + a_W(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_Y + b_B \, \bar{M}_{.j} + \, u_{b_0j} + c_W'(X_{ij} - \bar{X}_{.j}) + b_W(M_{ij} - \bar{M}_{.j}) \, + e_{Y_{ij}} \end{split}$$

Now we have estimates of everything needed for a mediation model.

There's a lot more coefficients here than when we did between-subjects or two instance repeated-measures.

Generally there are going to be two types of indirect effects in MLMs:

Within-Indirect Effects Between-Indirect Effects

Because there is no group-mean variation in *X* in this data, we'll only look at the within-indirect effect.

Estimating the Y Equation

$$\overline{Y_{ij}} = b_Y + b_B \, \overline{M}_{.j} + u_{b_0j} + \overline{c'_W}(X_{ij} - \overline{X}_{.j}) + b_W(M_{ij} - \overline{M}_{.j}) + e_{Y_{ij}}$$

MIXED Dose WITH Hazard_groupc Hazard_m Simple_groupc /FIXED = Hazard_groupc Hazard_m Simple_groupc | SSTYPE(3) /METHOD = REML

/PRINT = G SOLUTION TESTCOV

/RANDOM = Intercept | Subject(id) COVTYPE(VC).

Estimates of Fixed Effects^a

						95% Confid	ence Interval
Parameter	Estimate	Std. Error	df	t	Sig.	Lower Bound	Upper Bound
Intercept	115.420197	19.457732	68	5.932	.000	76.592897	154.247498
Hazard_groups	-3.430154	.947546	68.000	-3.620	.001	-5.320953	-1.539354
_Hazard_m	-5.968798	3.603669	68	-1.656	.102	-13.159807	1.222211
Simple_groups	3.827962	2.468446	68.000	1.551	.126	-1.097745	8.753670

a. Dependent Variable: Dosing Simple

A one unit increase simplicity rating (i.e., going from a complex to simple name) increases dosage by 3.83 mL, controlling for hazardousness ratings $c'_W = 3.83$

Within-Indirect Effects

$$\begin{split} M_{ij} &= a_M + u_{a_0j} + a_W(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_Y + b_B \; \bar{M}_{.j} + \; u_{b_0j} + c_W'(X_{ij} - \bar{X}_{.j}) + b_W(M_{ij} - \bar{M}_{.j}) \; + e_{Y_{ij}} \end{split}$$

A within-group indirect effect quantifies the expected difference in Y through M for two Level 1 units in the same Level 2 unit who differ by one unit on X.

When a_{1j} and b_{1j} don't randomly vary the indirect effect is: $a_W b_W$

From our data
$$a_W = -2.1048$$
, $b_W = -3.4301$, $a_W b_W = (2.1048)(-3.4301) = 7.2197$

Within a given Level 2 unit (within a specific person), we expect dosage to be 7.22 mL higher in the simple name condition as compared to the complex name condition, through the specific mechanism where name complexity influences perceived hazardousness which then in turn affects dosage.

Between-Indirect Effects

$$\begin{split} M_{ij} &= a_M + a_B \, \bar{X}_{.j} + u_{a_0j} + a_W (X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_Y + c'_B \, \bar{X}_{.j} + b_B \, \bar{M}_{.j} + \, u_{b_0j} + c'_W (X_{ij} - \bar{X}_{.j}) + b_W (M_{ij} - \bar{M}_{.j}) \, + e_{Y_{ij}} \end{split}$$

We don't have a between indirect effect in the model that we estimated.

But we could think of a similar study where some people saw lots of complex drugs and a few simple drugs and others saw lots of simple drugs and a few complex ones.

The between-indirect effect quantifies the expected difference in the group-mean of Y through the group-mean of M for two Level 2 units that differ by 1 unit on the average of X.

In the above example this would be the expected difference in average dosage through average hazardousness for two individuals two differ by 1 on the average simple exposure.

The estimate of the between indirect effect is always $a_B b_B$

Inference about Indirect Effects

As with single-level mediation models, the Sobel/normal theory methods are not appropriate due to the non-normal sampling distribution of the indirect effect.

Bootstrapping in multilevel models can be very difficult, as we want to bootstrapping to mimic the way data is collected from the population. It's unclear if we should be resampling at the group level, or resampling groups and then sample level 1 units from the group.

For inference in multilevel models, we'll rely on Monte Carlo Confidence Intervals

Monte Carlo Confidence Intervals (MCCIs) are constructed by simulating data from the estimated sampling distribution of the model parameters and constructing an estimate of the sampling distribution of the indirect effect(s) using the simulated distribution of each part of the indirect effect.

Between-Indirect Effects

$$\begin{split} M_{ij} &= a_M + a_B \, \bar{X}_{.j} + u_{a_0j} + a_W (X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_Y + c'_B \, \bar{X}_{.j} + b_B \, \bar{M}_{.j} + \, u_{b_0j} + c'_W (X_{ij} - \bar{X}_{.j}) + b_W (M_{ij} - \bar{M}_{.j}) \, + e_{Y_{ij}} \end{split}$$

Often the between-indirect effect can be difficult to interpret, as the meaning of the group-aggregate of a variable may differ from the meaning of the variable at the individual level.

Example by Preacher et al. (2010) on differentiating individual efficacy and collective efficacy of a group:

- The aggregate individual efficacy for a given group is a group-level variable (in that it only varies between groups).
- But the focus is still at the individual level and the meaning of such a variable is likely to differ from the meaning of a variable characterizing the dynamics of the self efficacy of the group as a collective.

It's okay not to estimate or be interested in the between-indirect effect, often times in psychology we're interested is within-individual change.

Inference about Indirect Effects

Monte Carlo Confidence Intervals (MCCIs) are constructed by simulating data from the estimated sampling distribution of the model parameters and constructing an estimate of the sampling distribution of the indirect effect(s) using the simulated distribution of each part of the indirect effect.



- Consider two vectors: f is a vector containing all of the FIXED effect estimates.
 r is a vector containing all of the RANDOM effect estimates.
- If we did the study again we would get different estimates for \hat{f} and \hat{r} so let's represent their sampling covariance matrices as $\hat{\Sigma_f}$ (estimated sampling variances and covariances among fixed effects) and $\hat{\Sigma_F}$ (estimated sampling variances and covariances among random effects)
- We know that both random and fixed effects are normally distributed and we know they are independent of each other.
- We generate f* and r* to have a multivariate normal distribution with means, variances, and covariances set by the estimates from the model.

Inference about Indirect Effects

$$\begin{bmatrix} f^* \\ r^* \end{bmatrix} \sim MVN \left(\begin{bmatrix} \widehat{f} \\ \widehat{r} \end{bmatrix}, \begin{bmatrix} \widehat{\Sigma_f} & \mathbf{0} \\ \mathbf{0} & \widehat{\Sigma_f} \end{bmatrix} \right)$$

We generate a large number of samples of f^* and r^* (e.g., 10,000)

For each sample we calculate the within-indirect effect (and/or between-indirect effect), giving us 10,000 estimates of the indirect effect, which approximates the sampling distribution of the indirect effect.

A $100(1-\alpha)\%$ confidence interval is obtained by using the $100\left(\frac{\alpha}{2}\right)$ and $100\left(1-\frac{\alpha}{2}\right)$ percentiles of the simulated sampling distribution.

This method has some similarities to bootstrapping, and is sometimes called the **parametric bootstrap**.

Doing it in SPSS: MLmed

```
Mlmed data = dataset1
/x = Simple
/xB = 0
/m1 = Hazard
/y = Dose
/cluster = id
/covmat = UN
/folder = /Users/Akmontoya/Desktop/
```

WARNING: When you run the code, some windows may pop up on your screen. Let everything resolve, and don't try to interact with those windows.

.50			
50			
.50			
	BM SPSS Statis	 	

Application in SPSS: MLmed

Mlmed is a package for SPSS which can do all of the analysis for you. It does all the recentering, estimates the indirect effects, and does the MCCI on your behalf.

MLmed is written and maintained by Nick Rockwood (PhD Candidate at Ohio State working with Dr. Andrew Hayes). It can be found at njrockwood.com. You also have a copy in your folder.



Just like MEMORE, you need to open the MLmed.sps file, select run all, and now SPSS knows what to do when you use an MLmed command.

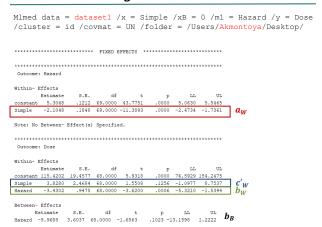
The macro does much more than what I describe here today. Check out the User Guide as well as Rockwood & Hayes (2018).

I'll explain the syntax as we go along.

Doing it in SPSS: MLmed

```
Mlmed data = dataset1 /x = Simple /xB = 0 /m1 = Hazard /y = Dose
/cluster = id /covmat = UN /folder = /Users/Akmontoya/Desktop/
 Written by Nicholas J. Rockwood
          Documentation available at www.njrockwood.com
          Please report any bugs to rockwood.19@osu.edu
 ************************
Model Specification
Rand(L1)
Rand (L2)
Total
Model Fit Statistics
 -2LL 1669.977
AIC 1677.977
AICC 1678.126
CAIC 1696.430
BTC 1692,430
```

Doing it in SPSS: MLmed



Doing it in SPSS: MLmed

Doing it in SPSS: MLmed

```
Mlmed data = dataset1 / x = Simple / xB = 0 / m1 = Hazard / y = Dose
/cluster = id /covmat = UN /folder = /Users/Akmontoya/Desktop/
Level-1 Residual Estimates
      Estimate
               S.E.
                     Wald Z
Dose 74.0515 12.6997 5.8310
                             .0000 52.9120 103.6367
Hazard 1.1953
              .2035 5.8737
                            .0000
                                   .8562 1.6688
Random Effect Estimates
  Estimate S.E. Wald Z
                            р
1 .4303 .2024 2.1255
                          .0335
                                .1711 1.0820
2 884.0882 158.0973 5.5921
                         .0000 622.7006 1255.197
Random Effect Key
1 Int
             Hazard
    Int
             Dose
```

A Comparison: MEMORE vs. MLmed Mlmed data = dataset1 /x = Simple /xB = 0 /m1 = Hazard /y = Dose

/cluster = id /covmat = UN /folder = /Users/Akmontoya/Desktop/

```
MLmed
            -2.1048
                     .1848 69.0000 -11.3893
                                             .0000 -2.4734 -1.7361
   Simple
                    2.4684 68.0000 1.5508
                                             .1256 -1.0977 8.7537
   Simple
            3.8280
                     .9475 68.0000 -3.6200
   Hazard
            -3.4302
                                             .0006 -5.3210 -1.5394
   Within- Indirect Effect(s)
                                     p MCLL MCUL
          Effect
                     SE
                             Z
   Hazard 7.2197 2.1000 3.4379 .0006 3.2952 11.4551
MEMORE m= HazSimp HazComp /y = DoseSimp DoseComp /xmint = 0.
   MEMORE
```

```
ULCI
           Effect
                         SE
                                                      LLCI
          -2.1048
                      .1848
                             -11.3893
                                                   -2.4734
                                                             -1.7361
                                           .0000
    'X'
                                                              8.7537
            3.8280
                      2.4684
                                1.5508
                                            .1256
                                                   -1.0978
   Mdiff -3.4302
                       .9475
                               -3.6200
                                           .0006
                                                   -5 3210
                                                             -1 5393
    Indirect Effect of X on Y through M
             Effect
                       BootSE BootLLCI
                                           BootULCI
ab Indl
            7.2197
                       1.8940
                                3.8590
                                           11.1609
```

A Comparison: MEMORE vs. MLmed

The model MEMORE fits is equivalent to a random intercept only 1-1-1 mediation model:

- · when we have 2 observations per person
- X is dichotomous
- each person is observed once for each level of X

MLmed is a more general multilevel mediation tool

- · Syntax is more verbose
- · Much more flexible
- · Can fit 1-1-1 or 2-1-1 mediations
- · Can include covariates, multiple mediators, Level 2 moderators
- · Can include random slopes

Random slopes: Indirect Effect

$$\begin{split} M_{ij} &= a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_{0j} + c_j'(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}} \end{split}$$

When the slopes have random variance what does this do to the indirect effect?

Between Indirect Effect: unchanged Within Indirect Effect

When a_{1j} and b_{1j} vary across groups, we may want to estimate the **average** within-group indirect effect and it's variance.

Expected Value (i.e. average) of group j's indirect effect

$$\left(E(a_jb_j)\right) = a_Wb_W + \sigma_{a_j,b_j}$$

Even when both a_W and b_W are zero, the average within-group indirect effect can be non-zero if the two random effects covary.

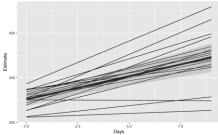
This is also true when one or more slope is fixed, but in that case the covariance is zero, so the equation simplifies to a_Wb_W

Adding random slopes

One of the major benefits of multilevel modeling is the ability to incorporate random slopes

We can allow the relationship between two variables to vary across groups.

This often more closely resembles the reality of the world as we understand it, where a relationship is not constant but rather has some variance around a mean slope.



Random slopes: Indirect Effect

$$\begin{split} M_{ij} &= a_{0j} + a_{1j}(X_{ij} - \bar{X}_{.j}) + e_{M_{ij}} \\ Y_{ij} &= b_{0j} + c_j'(X_{ij} - \bar{X}_{.j}) + b_{1j}(M_{ij} - \bar{M}_{.j}) + e_{Y_{ij}} \end{split}$$

If a_i and b_i is random, the within-group indirect effect is also random.

We can calculate the variance of the within-group indirect effect across groups as:

$$Var(a_jb_j) = b^2\sigma_{a_j}^2 + a^2\sigma_{b_j}^2 + \sigma_{a_j}^2\sigma_{b_j}^2 + 2ab\sigma_{a_j,b_j} + \sigma_{a_j,b_j}^2$$

This tells us how much we can expect the within-group indirect effect to vary across groups.

When a_i or b_i is fixed, this variance is zero.

The way we do inference for the indirect effect is unchanged, we continue to use the MCCI and MLmed will include the relevant factors.

Random slopes: Indirect Effect

$$E(a_j b_j) = a_W b_W + \sigma_{a_j, b_j}$$

$$Var(a_{j}b_{j}) = b^{2}\sigma_{a_{j}}^{2} + a^{2}\sigma_{b_{j}}^{2} + \sigma_{a_{j}}^{2}\sigma_{b_{j}}^{2} + 2ab\sigma_{a_{j},b_{j}} + \sigma_{a_{j},b_{j}}^{2}$$

When we estimate the M equation and Y equation separately we do not estimate the covariance σ_{a_l,b_l}

In these circumstances, it is not possible to estimate the average within group indirect effect.

Instead the equations need to be estimated simultaneously.

Some SEM packages (e.g., Mplus) can estimate multilevel models simultaneously.

Bauer, Preacher, and Gil (2006) demonstrate how the equations can be estimated simultaneously using traditional (univariate) multilevel modeling software.

MLmed utilizes this method when estimating mediation models with random slopes

Doing it in SPSS: MLmed

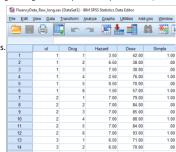
```
\label{eq:main_section} \begin{split} &\text{Mlmed data} = \frac{\text{dataset1}}{\text{/x} = \text{Simple}} \\ &\text{/xB} = 0 \\ &\text{/randx} = 01 \\ &\text{/m1} = \frac{\text{Hazard}}{\text{Hazard}} \\ &\text{/randm} = 1 \\ &\text{/y} = \text{Dose} \\ &\text{/cluster} = \text{id} \\ &\text{/covmat} = \text{UN} \\ &\text{/folder} = \text{/Users/Akmontoya/Desktop/} \end{split}
```

Example: Drug Name Fluency

Dohle, S., & Montoya, A. K. (2017). The dark side of fluency: Fluent names increase drug dosing. Journal of Experimental Psychology: Applied, 23(3), 231 – 239.

Participants (N = 70) were asked to imagine they had the flu, and 6 different drugs were provided to treat the drug. Participants poured the dose they would feel comfortable taking at maximum into a plastic cup. Each person judged drugs with simple or complex names (3 of each)

Open the dataset FluencyData_Raw_long.sav
There are six drugs (Drug = 1 - 6)
Each person saw 3 simple and 3 complex drugs.
We will treat each of these as repeated
observations of the same person (6 instead
of 2).



Doing it in SPSS: MLmed

```
Mlmed data = dataset1 / x = Simple / xB = 0 / randx =
01 /m1 = Hazard /randm = 1 /y = Dose /cluster = id
/covmat = UN /folder = /Users/Akmontoya/Desktop/
Outcome: Hazard
                                                Fixed effects are not
                                               different from when we
                  df
                                               used the averaged data.
           .1212 69.0000 43.7751 .0000 5.0630 5.5465
Simple -2.1048 .1848 69.0000 -11.3893 .0000 -2.4734 -1.7361
Note: No Between- Effect(s) Specified.
Outcome: Dose
Within- Effects
     Estimate
            S.E.
constant 115,4202 19,4577 68,0000 5,9318 .0000 76,5929 154,2475
Simple 3.8946 2.0466 342.6421 1.9029 .0579 -.1309 7.9201
Hazard -3.0849 .6996 76.2642 -4.4094 .0000 -4.4782 -1.6916
Between- Effects
                df +
    Estimate S.E.
Hazard -5.9688 3.6037 68.0000 -1.6563 .1023 -13.1598 1.2222
```

Doing it in SPSS: MLmed

```
Mlmed data = \frac{dataset1}{x} = \frac{datase
 Hazard /randm = 1 /y = Dose /cluster = id
  /covmat = UN /folder = /Users/Akmontoya/Desktop/
 Level-1 Residual Estimates
                   Estimate S.E. Wald Z
Dose 245.4574 20.2443 12.1247 .0000 208.8202 288.5225
Hazard 1.3619 .1151 11.8322 .0000 1.1540 1.6073
Random Effect Estimates
               Estimate S.E. Wald Z
(1.1) .8010 .1761 4.5494 .0000 .5206 1.2323
(2,2) 880.2044 158.0058 5.5707
                                                                                                    .0000 619.1332 1251.362
(3,3) 1.4827 .4142 3.5799
                                                                                                   .0003 .8576 2.5635
                   .6696 .8673 .7720
                                                                                                   .4401 -1.0303 2.3695
(4,4) 3.9093 3.5234 1.1095 .2672 .6682 22.8701
             .0000 880.2044 .0000 .0000
           .0000 .0000 1.4827
          .0000 .0000 .6696 3.9093
Random Effect Correlation Matrix
                                                                                                                                                                           Random Effect Kev
                                                                                                                                                                          1 Int
                                                                                                                                                                                                                        Hazard
1 1.0000
                                   .0000 .0000 .0000
                                                                                                                                                                          2 Int
                                                                                                                                                                                                                        Dose
         .0000 1.0000 .0000 .0000
            .0000 .0000 1.0000 .2781
                                                                                                                                                                          4 Slope
4 .0000 .0000 .2781 1.0000
```

Tutor Data

This example uses a simulated dataset (tutor_data.sav) based on an educational experiment.

Suppose 48 classrooms were randomly sampled where no classrooms were in the same school.

Next, students within each classroom were randomly sampled to participate in an after-school tutoring program throughout the school year.

The total number of students is 450, where 223 students are assigned to tutoring and 227 are assigned to control (no tutoring program).



Doing it in SPSS: MLmed

On average, within an individual, the difference in dosage between sample drugs and complex drugs that operates indirect through perceived hazardousness is estimated to be 7.16 (MCCI = [3.68, 10.89]), where simple drugs are administered at higher dosages than complex drugs. However there is substantial between-person variability in this indirect effect (SD = 6.81).

Tutor Data

The **tutor** variable in the dataset codes the assignment of each student (0 = control, 1 = tutoring)

Before completing an end of year mathematics exam (**post**), the students' academic motivation was measured (**motiv**)

There is also data on the students' test scores from the previous year (pre).



Tutor Data

We are interested in testing whether there is evidence that the participation in afterschool tutoring program (X = tutor) results in higher mathematics post-test scores (Y = post), on average, due to an increase in student motivation (M = motiv).

Further we are interested in whether this effect is consistent across classrooms, or whether there is between-classroom variability in the effect.

Throughout, we will use the previous year's math test score (Q = pre) as a covariate.

All variables are level-1 (student level).

The proportion of students assigned to tutoring in each class is not constant, so there is between-class variability in *X*. Additionally there will be between class variability in *M*, *Q*, and *Y*.

We will use group-mean centering to remove between-class variability and add this back into the model using the classroom means as predictors of the random intercepts to that within-class and between-class effect can be estimated separately.

Doing it in SPSS: MLmed

```
Mlmed data = dataset1 /x = tutor /m1 = motiv /y = post /cov1 = pre
/cluster = classid /covmat = UN /folder = Users/Akmontoya/Desktop/
Outcome: motiv
     Estimate S.E. df
constant 1.2844 .5128 46.8208 2.5049 .0158 .2528 2.3160
tutor 1.3517 .0462 398.0015 29.2783 .0000 1.2610 1.4425
        .0194 .0022 398.0015 8.7609 .0000 .0151 .0238
Between- Effects
   Estimate S.E. df t
tutor .8443 .5654 47.1328 1.4933 .1420 -.2930 1.9817
     .0039 .0058 45.9489 .6771 .5017 -.0077 .0156
Outcome: post
Within- Effects
      Estimate
              S.E. df t
constant 50.3689 7.2512 43.9803 6.9463 .0000 35.7548 64.9830
tutor
      -3.2913 1.4885 394.8792 -2.2112 .0276 -6.2176 -.3649
       4.4675 .9097 394.8792 4.9112 .0000 2.6791 6.2559
motiv
       .3746 .0440 394.8792 8.5215 .0000 .2882 .4611
Between- Effects
   Estimate S.E. df
tutor -24.6103 7.7505 48.0227 -3.1753 .0026 -40.1935 -9.0271
motiv 12.3961 1.9524 43.5166 6.3490 .0000 8.4600 16.3323
     .0119 .0775 44.9123 .1532 .8789 -.1443 .1680
```

Doing it in SPSS: MLmed

```
Mlmed data = dataset1
/x = tutor
/ml = motiv
/y = post
/cov1 = pre
/cluster = classid
/covmat = UN
/folder = /Users/Akmontoya/Desktop/
```

Doing it in SPSS: MLmed

```
Mlmed data = dataset1 /x = tutor /m1 = motiv /y = post /cov1 = pre
/cluster = classid /covmat = UN /folder = Users/Akmontoya/Desktop/
Within- Indirect Effect(s)
      E(ab) Var(ab) SD(ab)
motiv 6.0388 .0000 .0000
Within- Indirect Effect(s)
      Effect SE
motiv 6.0388 1.2475 4.8408 .0000 3.6273 8.5073
Between- Indirect Effect(s)
      Effect
                              p MCLL MCUL
motiv 10.4665 7.2843 1.4368 .1508 -3.3701 25.5751
Test of Indirect Contextual Effect(s): Between - Within
        Dif MCLL MCIII.
motiv 4.4276 -9.5305 19.8116
```

Doing it in SPSS: MLmed

Within a given classroom, there is a significant indirect effect of tutoring on posttest through motivation controlling for pretest $(E(a_jb_j) = 6.04, MCCI = [3.53,8.50])$, where students who participated in tutoring performed better on the post test.

There was not significant evidence that between classroom variability in proportion of students assigned to tutoring influenced average classroom performance through average motivation ($a_Bb_B=10.47$ MCCI = $[-3.42\ 25.32]$). There's not significant evidence that the within and between indirect effects significantly different.

2-1-1 Models

The 1-1-1 model is for the general data design where X-M-Y all contain within and between group variability.

In the dosage data, the model we fit only had within group variability in X.

MLmed can also be used to fit models where X only contains information about between-group variability (2-1-1 models). This type of model is useful for cluster-randomized designs (each group assigned to a condition).

MLmed does not fit 2-2-1 models but these can be fit piecewise, where $X \to M$ is an OLS regression and the Y equation is fit using MLM.

Models with "upward effects" (e.g., 1-2-1) cannot be fit in MLM software and require multilevel structural equation modeling.

Exercise: Adding random slopes

In addition to being interested in the average within-class indirect effect, we are also interested in determining if that within-class indirect effect varies across classrooms.

- Using MLmed, expand the model to include a random a_j and b_j , as well as the covariance between these paths
- Interpret the individual coefficients and their variances making up the mediation model
- Interpret the average and variance of the within-group indirect effect in the context
 of the specific example.

2-1-1 Example

Suppose that rather than students assigned to tutoring, teachers completed a training program deisgned to teach a number of skills focused on engaging their students through the use of interactive real-world applications.

It is thought that students who are exposed to the interactive real-world applications will see the utility of the content being taught and they will be more motivatted, leading to an increase in their post-test scores.

The variable **train** is a teacher-level (Level 2) training identifier (1 = completed training, 0 = control)

2-1-1 Example

In the tutor dataset we may be interested in testing if the average amount of student motivation mediates the relationship between the teacher's completion of a training program and the average post-test score of their students.

This is a 2-1-1 model since training (X) is a Level 2 variable (classroom level), motivation and posttest scores are both at Level 1 (student level).

There can only be a between-group indirect effect.

```
MLmed data = dataset4

/x = train

/xW = 0

/m1 = motiv

/y = post

/cov1 = pre

/cluster = classid

/folder = /Users/Akmontoya/Desktop/
```

2-1-1 Example

```
MLmed data = dataset4 /x = train /xW = 0 /m1 = motiv /y = post
/cov1 = pre /cluster = classid /folder = /Users/Akmontoya/Desktop/
Level-1 Residual Estimates
    Estimate
            S.E. Wald Z
                             p
                                   LL
post 75.1677 5.3404 14.0754
                          .0000 65.3968 86.3983
motiv .7104 .0503 14.1178
                          .0000
                               .6184
                                       .8162
Random Effect Estimates
                          p
  .0818 .0358 2.2833
                       .0224
                             .0347
2 26.8186 7.9874 3.3576
                       .0008 14.9596 48.0784
Random Effect Key
1 Int
           motiv
2 Int
           post
```

2-1-1 Example

```
MLmed data = dataset4 / x = train / xW = 0 / m1 = motiv / y = post
/cov1 = pre /cluster = classid /folder = /Users/Akmontoya/Desktop/
Outcome: motiv
Within- Effects
     Estimate
constant 2.2615 .4840 56.7024 4.6724 .0000 1.2921 3.2308
       .0295
            .0039 398,6255 7,6001 .0000 .0219 .0372
Between- Effects
   Estimate S.E.
                  df
train .3489 .1743 46.2330 2.0014 .0512 -.0019 .6997
pre -.0065 .0078 55.2377 -.8368 .4063 -.0220 .0090
Outcome: post
Within- Effects
     Estimate
constant 48.8441 8.4186 45.1925 5.8019 .0000 31.8902 65.7980
motiv 2.8059 .5150 396.2348 5.4481 .0000 1.7934 3.8185
       .3991 .0427 396.2348 9.3352 .0000 .3150 .4831
Between- Effects
   Estimate S.E. df t
train 5.2720 2.6375 43.0894 1.9989 .0520 -.0467 10.5907
motiv 9.8785 2.1110 43.3758 4.6796 .0000 5.6224 14.1346
pre -.0992 .1109 47.9342 -.8953 .3751 -.3221 .1236
```

2-1-1 Example

There is a significant between-group indirect effect of teacher training on student posttest, by way of student motivation $(a_Bb_B=3.45,MCCI=[0.05,7.47])$. Specifically, the students of teachers who participated in the training had higher motivation on average, than students of teachers who did not participate in the training, and higher average motivation led to higher average posttest scores.

Other Types of Repeated Measures Mediation

- Latent Growth Curve Models (Longitudinal Processes M-Y measured over time)
 - Choeng, MacKinnon, Khoo (2003) Structural Equation Modeling
- Structural Equation Modeling (Can be used for a variety of data types)
 - Cole & Maxwell (2003) Journal of Abnormal Psychology
 - X, M, and Y all measured over time
 - Newsom (2009) Structural Equation Modeling
 - Dyadic data using LGMs
 - Selig & Little (2012) Handbook of Developmental Research Methods
 Autoregressive models and cross-lagged panel models for longitudinal data X, M, and Y all measured over time.
- Multilevel SEM
 - · Preacher, Zyphyr, Zhang, 2010
 - · Preacher, Zhang, Zyphur, 2011

Selig & Preacher (2009) Research in Human Development

 Longitudinal Models X, M, and Y measured across time. Cross-lagged panel models, latent growth models, latent difference score models

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Wrapping Up

Where to learn more:

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MLMED and MEMORE both have many features not described here

MLMED does moderated mediation

MEMORE does moderation and (coming soon) moderated mediation

Andrew F. Hayes

Undered Hayes

Look for MEDYAD for SPSS and SAS in April

2019

afhayes.com/spss-sas-and-m ... 7:11 AM - 26 Jan 2019

Github.com/akmontoya/SPSP2019workshop