

# Sum-of-Pairs

# Motivation

- Multiple sequence alignment
- Solves problem with score function  $S_c$ .

# Problem with $S_c$

- In PAM:  $S_c(a,b) = \frac{Pr[\text{alignments are related}]}{Pr[\text{unrelated random sequences}]} = \prod \frac{p_{a_i,b_i}}{q_{a_i}q_{b_i}}$
- Use instead of multiplication the sum over logs
- What if  $S_c(a,\dots,n)$ ?
- Not enough data available to compute probabilities

# Sum-of-Pairs

- align every sequence pairwise
- sum over the scores
- Example:

$$S_C(x, y, z) = S_C(x, y) + S_C(x, z) + S_C(y, z)$$

# Problem

- Scoring can be incorrect:  $S_C(x, y, z) = \log\left(\frac{p_{xyz}}{q_x q_y q_z}\right)$
- but:

$$S_C(x, y, z) = S_C(x, y) + S_C(x, z) + S_C(y, z)$$

$$\log\left(\frac{p_{xyz}}{q_x q_y q_z}\right) \neq \log\left(\frac{p_{xy}}{q_x q_y}\right) + \log\left(\frac{p_{xz}}{q_x q_z}\right) + \log\left(\frac{p_{yz}}{q_y q_z}\right)$$

# List of references

- Lecture “Multiples Sequence Alignment - Basics”  
Bioinformatics I, Prof. Backofen

URL: [http://www.bioinf.uni-freiburg.de//Lehre/Courses/2014\\_SS/V\\_Bioinformatik\\_1/multiple-alignment.pdf](http://www.bioinf.uni-freiburg.de//Lehre/Courses/2014_SS/V_Bioinformatik_1/multiple-alignment.pdf), visited: 13/11/2014