

Thesis for obtaining the academic degree
Bachelor of Science

Finding optimal hyperparameters for cleaning
algorithms for the Cherenkov Telescope
Array

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Title graphic by Kai Brügge.

¹<https://github.com/maxnoe/tudothesis>

Abstract

In recent years, gamma astronomy has become a vastly studied field of astrophysics. Since then many Imaging Air Cherenkov Telescope (IACT) experiments have been producing insights into sources of high-energy gamma-rays. Continuing this trend, the Cherenkov Telescope Array (CTA), a next-generation IACT, will provide new data at some of the highest energies of the gamma-ray spectrum.

In this thesis, I take a look at the four cleaning algorithms implemented in the low-level data processing software `ctapipe`, currently developed for CTA. Furthermore, I will determine optimized hyperparameters for each algorithm with the aim of improving the performance of the cleaning algorithms. This is achieved with a grid search over a range of reasonable hyperparameters. The data used in this work is diffuse gamma Monte Carlo (MC) simulation data for the Medium-Sized Telescopes (MSTs) at the northern site of CTA on the Canarian island of La Palma.

The hyperparameters determined for the `TimeConstrainedImageCleaner` (TCC) algorithm in `ctapipe` improved its performance over its default parameters w. r. t. to the angular resolution, while the other algorithms were only slightly improved by the respective hyperparameters or at least returned similar results. In terms of metrics, the performance of the TCC algorithm only improved slightly with the new parameters, while `FACTImageCleaner` (FACT) performed worse than with its default values. Overall, however, FACT performed better than the other algorithms.

Kurzfassung

In den vergangenen Jahrzehnten hat sich die Gammaastronomie zu einem viel erforschten Bereich der Astrophysik entwickelt. Seitdem haben bildgebende, atmosphärische Tscherenkow-Teleskope (IACT) zahlreiche neue Erkenntnisse im Bereich der hochenergetischen Gammastrahlen und deren Quellen geliefert. Mit CTA, einem IACT der nächsten Generation, werden neue Daten in einigen der höchsten Energiebereiche der Gammastrahlen erwartet.

In dieser Arbeit schaue ich mir die vier Bildreinigungsalgorithmen an, die in der sich zur Zeit für CTA in Entwicklung befindlichen Software `ctapipe` implementiert sind. Zudem bestimme ich optimierte Hyperparameter für jeden Algorithmus mit dem Ziel, die Leitung der Bildreinigungsalgorithmen zu verbessern. Dies wird mittels einer Grid-Search über eine Auswahl von Hyperparametern durchgeführt. Die Daten, die zu diesem Zweck verwendet werden, bestehen aus diffusen Gammadaten, die mittels einer MC-Simulation für die MSTs des nördlichen Standorts CTAs auf der Kanarischen Insel La Palma erzeugt wurden.

Die Ergebnisse zeigen, dass die in dieser Arbeit gefundenen Hyperparameter die Leistung des TCC-Algorithmus in Bezug auf die Winkelauflösung verbesserten, während die Leistungen der anderen Algorithmen nur ein wenig verbessert wurden oder gleiche Ergebnisse lieferten, wie mit den Standardparametern. In Bezug auf die Metriken konnten die gefundenen Hyperparameter bei TCC eine leichte Verbesserung bewirken, während die Parameter bei FACT sogar eine etwas schlechtere Leistung bewirkten. Insgesamt lieferte FACT allerdings bessere Ergebnisse als die anderen Algorithmen.

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1

Gamma-Ray Astronomy

Astronomy, being one of the oldest sciences, is a vast field of study dating back to the earliest days of civilization, where astronomers have been studying the stars and the planets to understand the universe. It is, therefore, no surprise that astronomy spawned a great number of discoveries throughout the centuries. Whereas first observations were made by eye only, we now have access to a multitude of experiments and telescopes that deepen our understanding of the universe. With the discovery of cosmic rays (CR) by Victor Hess in the early 20th century, the new field of astroparticle physics was born [25].

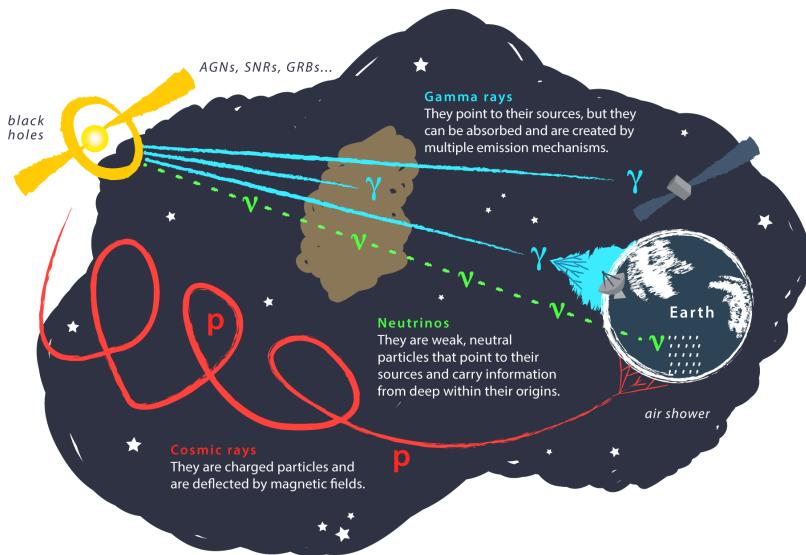


Figure 1.1: Different types of cosmic messengers on their way to Earth. Charged particles like protons and electrons are deflected by magnetic fields, thus making it hard to pinpoint the source. Only the origin of photons and neutrinos can be reconstructed directly since they are uncharged particles and therefore travel in straight lines. However, photons can be absorbed or created in multiple mechanisms. Since neutrinos only rarely interact with matter via the weak force, their detection is significantly harder than that of photons [5].

Only 50 years after Hess' discovery, in 1961, Explorer XI [24], the first satellite experiment to measure gamma rays from space was launched, providing measurements of gamma rays above 50 MeV, thus starting gamma-ray astronomy from space-based experiments. Just a few years earlier neutrinos were already discovered by Cowan and Reines [12], with solar neutrinos being discovered by Davis et. al. [16] in the 1960s at the Homestake experiment. The first detection of neutrinos from a supernova was made

by the Kamiokande experiment in 1987 [22]. The most recent discovery of a cosmic messenger has been that of gravitational waves in 2015 [1].

Cosmic messengers come in different types, that are either charged or uncharged, as shown in Figure 1.1. CR like electrons, protons or atomic nuclei are charged particles making it difficult to trace back their origin as they are deflected by cosmic electromagnetic fields. Uncharged particles like photons or neutrinos, however, travel in straight lines, making it easier to reconstruct their origins.

While photons can be absorbed by dust clouds on their way to Earth, they are easier to detect than neutrinos, the latter having a very small cross-section and interacting only weakly with matter. This means that neutrino detectors and experiments, such as IceCube [4] or Super-Kamiokande [30], have to be large enough to detect neutrinos in sufficient quantities.

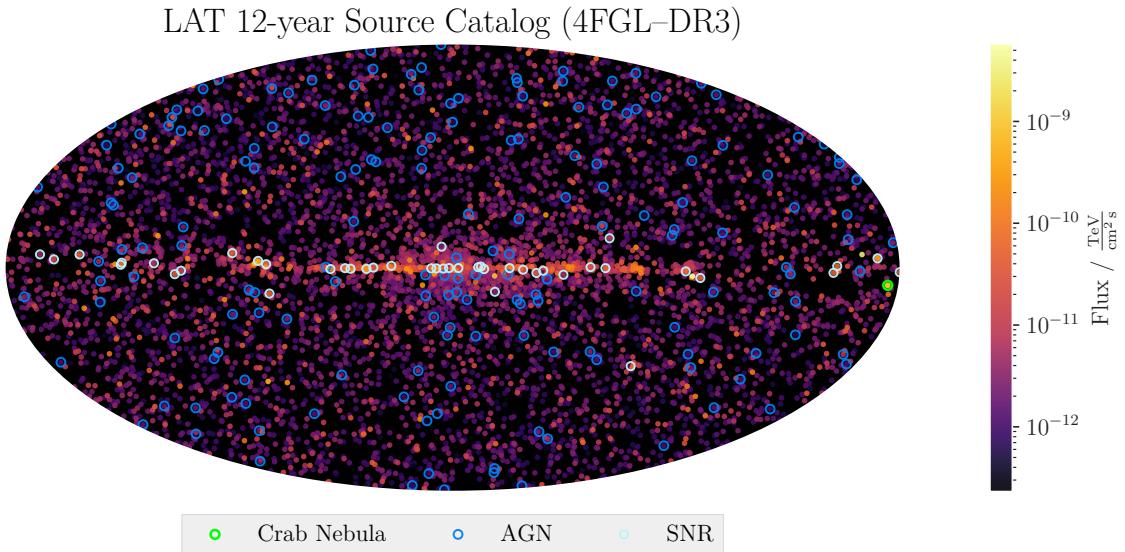


Figure 1.2: Mollweide projection of the *Fermi* Large Area Telescope (*Fermi*-LAT) 4FGL-DR3 catalog data of gamma-ray sources. The sky map shows the flux of gamma-ray sources in $\text{TeV}/(\text{cm}^2 \text{s})$ observed over a span of 12 years from the experiment's launch in 2008. Note the concentration of high-energy (HE) gamma-ray sources around the galactic plane. Additionally, the Crab Nebula (bright green circle, right hand side)—being a standard candle gamma-ray astronomy—is marked along with supernova remnants (SNRs) (ice blue/light blue circles) and active galactic nuclei (AGNs) (blue circles) that *Fermi*-LAT observed [2, 3]. Notice, that the AGNs shown here are but a subset of all AGNs observed by the experiment—the non-blazar active galaxies. They were chosen to show at least some other sources alongside the SNRs without obstructing the plot too much. This figure was adapted from Kai Brügge's Ph.D. thesis [9].

In recent years, gamma-ray astronomy has become an important research field in astroparticle physics. The term gamma ray is generally denoted as photons with energies above 100 keV [18]. Due to this high-energy nature, gamma rays pose some of the most powerful cosmic messengers in the universe and since photons at such energies cannot be produced by thermal processes, their origin has to be described by higher order processes involving charged particles. Some of the brightest sources of gamma rays in our galaxy are supernova remnants (SNRs) such as the Crab Nebula. The Crab Nebula, in particular, poses as a so-called standard candle with its constant flux of high-energy gamma rays (HEGR), allowing

to test the performance of new experiments and telescopes. Other sources for gamma rays include gamma ray bursts (GRBs), Pulsars and active galactic nuclei (AGNs), the latter being one of the most common types of extragalactic gamma-ray sources. AGNs themselves can be classified further depending on the existence of a relativistic jet, the viewing angle of the observer or how bright they are.

Gamma rays can be detected by a variety of experiments, either ground- or space-based. Space-based experiments like the *Fermi*-LAT are usually more sensitive to lower energies, but their performance is lower for higher energies, as their effective collection area is comparatively small. Ground-based experiments, however, are more sensitive to higher energies and rely on the scattering of secondary particles in extensive air showers (EASs) induced by the primary particle in Earth's atmosphere. The gamma-ray sky as observed by *Fermi*-LAT over a span of 12 years is shown in Figure 1.2.

For the past two decades, ground-based Imaging Air Cherenkov Telescope (IACT) experiments like the Major Atmospheric Gamma-Ray Imaging Cherenkov (MAGIC) telescopes, the Very Energetic Radiation Imaging Telescope Array System (VERITAS) and the High Energy Stereoscopic System (H.E.S.S.) have been monitoring these very-high-energy gamma rays (VHE gamma rays) to gain an understanding of their production. This allowed determining different source classes inside and outside our galaxy, with some of the most important source classes inside our galaxy being SNRs such as the Crab Nebula, because of their brightness and the constant flux of CR in the (GeV) energy regime.

IACTs and the Cherenkov Telescope Array

2

Most modern gamma-ray observations are performed with either space-based experiments or with Imaging Air Cherenkov Telescopes (IACTs), which are ground-based telescopes or arrays of telescopes that use the Cherenkov light emitted by EASs in the atmosphere. In the following sections I will introduce IACTs and the Cherenkov Telescope Array (CTA) and explain the mechanisms that make it possible to observe gamma rays with these types of experiments.

2.1 Imaging Air Cherenkov Telescopes

Because of their ground-based setup, IACTs are taking advantage of the Earth's atmosphere to get a larger effective area than any space-based instrument. This is especially helpful for energies above 100 GeV, where the gamma-ray flux is low, whereas lower energies show higher fluxes. At such high energies space-based instruments, experiments such as *Fermi-LAT*, see fewer high-energy events compared to ground-based experiments, due to their comparatively small effective collection area [18, p. 256]. The cosmic ray flux in Figure 2.1 shows this well: The flux decreases rapidly with higher energies, with only one high-energy (>40 GeV) photon per day and square meter reaching Earth from the Crab Nebula [26] and even fewer photons for energies in the EeV domain, where only 1 particle per square kilometer per year reaches Earth.

Earth's atmosphere is opaque to HE gamma rays, so ground-based experiments rely on cascades of sub-particles in so-called EASs. For gamma-ray astronomy, the electromagnetic component of these EASs, shown in Figure 2.2a, is of interest, as these are produced by gamma rays. When a gamma ray interacts with Earth's atmosphere, it decays into an electron and a positron via pair production. These charged particles then emit more photons via bremsstrahlung. These photons, again, produce more charged particles, which in turn emit even more photons. This process continues until any of these processes reaches energies below a certain threshold, i. e. 1022 keV for the pair production process. For these processes to happen, the particles

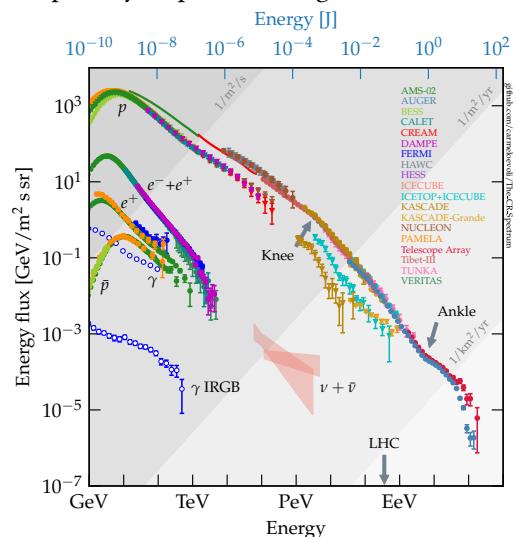
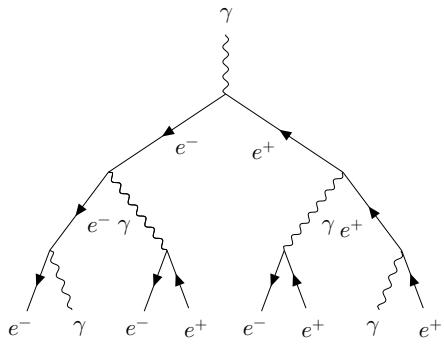


Figure 2.1: The cosmic ray flux as a function of energy. For very high energies the flux becomes very small with only 1 particle per square meter per year reaching Earth. For even higher energies in the domain of EeV this flux becomes 1 particle per square kilometer per year [17].

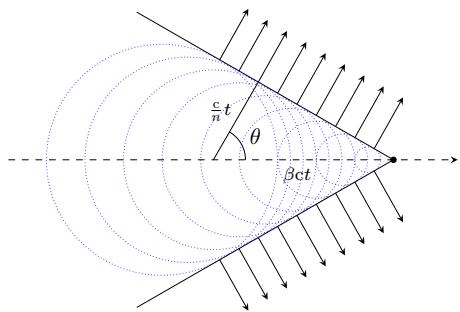
have to be in the fields of the atoms of the Earth's atmosphere. As the particles travel at speeds faster than light in the atmosphere, they emit Cherenkov light at a fixed angle θ with respect to the refraction index n of the atmosphere and the factor $\beta = v/c$. The angle can be determined trigonometrically as

$$\cos \theta = \frac{1}{\beta n}, \quad (2.1)$$

as can be seen in Figure 2.2b.



(a) Simplified first steps of the Heitler model of the electromagnetic component of an extensive air shower. A gamma ray induces an electron and a positron via pair production that then emit more photons via bremsstrahlung.



(b) Cherenkov radiation (outward-pointing arrows) from a charged particle traveling at uniform velocity, faster than the speed of light in the medium. The dashed line shows the path of the particle over time.

Figure 2.2: The electromagnetic component of an extensive air shower (see (a)) is induced by gamma rays that then decay into electrons and positrons via pair production. These charged particles will emit more gammas via bremsstrahlung, which again will produce new electrons and positrons. This will continue until e.g. the energy of the gammas is below the threshold of 1022 keV for pair production. Another process is the production of Cherenkov light from the electrons and positrons, which is shown in (b). The Cherenkov light is the result of the charged particles traveling faster than the speed of light in the atmosphere, thus emitting photons in a fixed angle θ w.r.t. the refraction index n of the medium and the factor β .

Cherenkov light emitted by EASs can then be collected by an IACT's mirrors and detected by its camera within a timeframe of an order of nanoseconds. The resulting image will show the shape of the air shower and can be used to determine the shower's primary particles' properties and reconstruct its origin. As the hadronic component of EASs produce electromagnetic subshowers, IACTs have a dominant hadronic background, which has to be separated from the gamma ray-induced showers, for example with machine learning algorithms. This work, however, does not focus on these algorithms, but instead on cleaning algorithms that are used to separate the signal from the electronic noise coming from the camera as well as from the Night Sky Background (NSB). This is a vital step in the analysis of an event, as only a fraction of all pixels in the camera frame are part of the signal.

2.2 The Cherenkov Telescope Array

CTA is a new generation of IACTs that will consist of two sites, one of which will be built at the Observatorio del Roque de los Muchachos (ORM) on the Canarian island of La Palma while the other will be built in the southern hemisphere at the European Southern Observatorys (ESO) Paranal Observatory in the Atacama desert of northern Chile. In this work, I will focus on the northern array, also called CTA north, on La Palma.

CTA consists of three types of telescopes, shown in Figure 2.3, each being sensitive to a different energy range [13]:

Large-Sized Telescope (LST): The largest telescopes in CTA have a primary deflector diameter of 23 m with a field of view of 4.3 deg and provide full system sensitivity in the energy regime from 20 GeV to 150 GeV.

Medium-Sized Telescope (MST): The MSTs have a primary deflector diameter of 11.5 m with a field of view of 7.7 deg for their NectarCam and provide full system sensitivity in the energy regime from 150 GeV to 5 TeV.

Small-Sized Telescope (SST): Being the smallest telescope type in CTA, the SSTs have a primary deflector diameter of 4.3 m, a secondary deflector diameter of 1.8 m with a field of view of 10.5 deg and provide full system sensitivity in the energy regime from 5 TeV to 300 TeV.

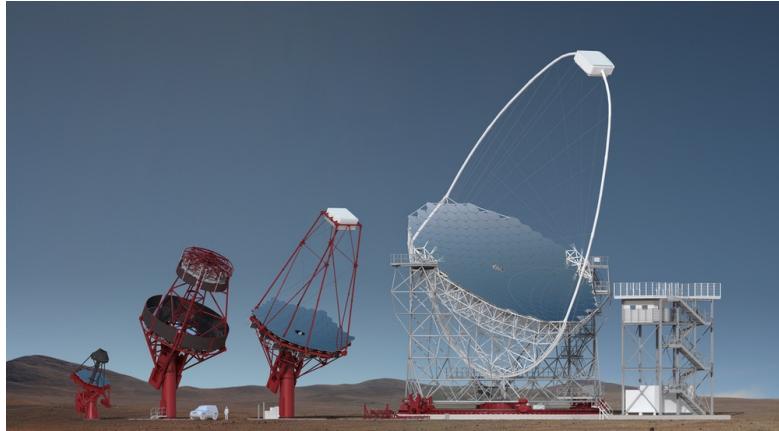


Figure 2.3: A rendered image of the 3 telescope prototypes in CTA. From left to right: The SST, two types of MST (SCT and MST) and the LST. This work will not feature the SCT, as the simulation data used contains only LST and MST data for the northern array. Image credit: Gabriel Pérez Diaz, IAC [34].

Since the southern hemisphere has a better view of the galactic center than the northern hemisphere, only CTA south will feature the SSTs along the other two telescope types. CTA north will only feature MSTs and LSTs. In its full configuration, CTA would feature 70 SSTs, 25 MSTs and 4 LSTs at CTA south, and 15 MSTs and 4 LSTs at CTA north. However, the reduced layout—called Alpha Configuration—is the currently planned layout for both CTA north and south. This work will focus on the northern site, consisting of 9 MSTs and 4 LSTs [14]. Figure 2.4 shows the planned Alpha Configuration layout of both sites of CTA where CTA south is displayed with its 37 SSTs, 14 MSTs and the 4 LSTs in the center [15].

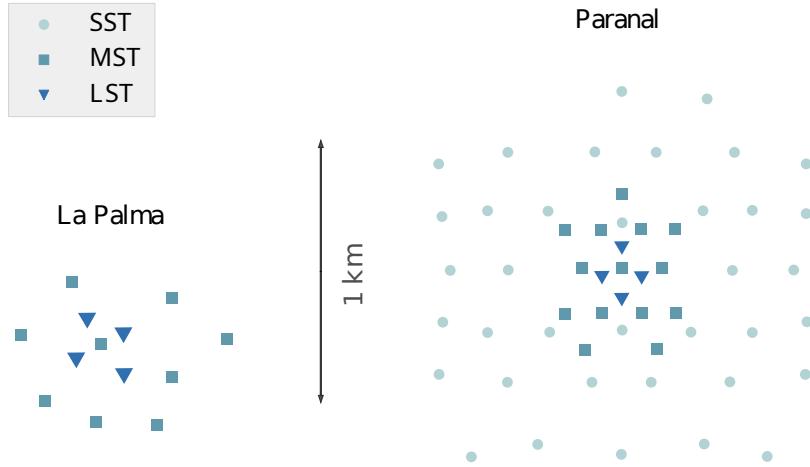


Figure 2.4: Alpha Configuration layout of the CTA north and CTA south site. CTA south would feature 37 SSTs, 14 MSTs and 4 LSTs [15] in its Alpha Configuration, while CTA north would feature 9 MSTs and 4 LSTs [14]. This figure was adapted from Kai Brügge in his Ph.D. thesis [9].

The MST's and LST's cameras are based on photo multiplier tube (PMT) photodetectors, while the SST's camera is based on a silicon photomultiplier (SiPM) photodetector. Both detector types provide fast response times in the order of nanoseconds. PMTs can detect small amounts of electromagnetic radiation due to their amplification process. However, this amplification process also amplifies the noise of the detector and also needs higher voltages than SiPMs. The latter, on the other hand, needs to be cooled, as SiPMs are prone to having a higher dark current at higher temperatures.

With CTA probing the very-high-energy (VHE) gamma-ray sky and a resolution outperforming predecessors, like H. E. S. S. or MAGIC, it will be able to observe a broad variety of sources, allowing insights into interaction processes of VHE gamma rays as well as their origin.

Together with gravitational wave and neutrino observatories as well as with other photon observatories, CTA will probe the universe in its high-energy (HE) domain, allowing to study a broad field of key questions in astrophysics. As such, CTA's scientific goals can be divided into three categories [11]:

Origin and Role of relativistic Cosmic Particles: CTA will try to find the sources of HE cosmic particle acceleration in the universe. This includes the search for the mechanisms that accelerate cosmic particles. Also, CTA will try to answer what role these particles play in feedback on star formation and galaxy evolution.

Extreme Environments: CTA aims to deepen our understanding of the processes that are at work close to neutron stars and black holes, the characteristics of relativistic jets and pulsar wind nebula (PWN). Also, it will probe how intense radiation fields and magnetic fields are and how these would evolve over cosmic time scales.

Frontiers in Physics: CTA will try to answer questions about the nature of dark matter and its distribution in the universe. As such, the existence of axion-like particles will be probed. Furthermore, CTA will search for quantum gravitational effects on photon propagation.

Data processing with `ctapipe`

3

The analysis in this work was done with the open-source low-level data processing software for CTA, `ctapipe` [23], more specifically, version 0.15.1. The goal of `ctapipe` is to provide a complete analysis framework ranging from data calibration and image extraction to the reconstruction of events and the analysis of their properties. In this chapter, I will first describe how the data was simulated in section 3.1 and then, in section 3.2, explain the different data levels and `ctapipe`'s various analysis steps. In section 3.3 I will explain the full pipeline created for this work.

3.1 Data simulation

In its current in-development state, `ctapipe` is used and tested with simulated data, as the software can only be sufficiently tested when the output is compared to truth data. This data is created with the help of Monte Carlo (MC) simulations. The software used for these simulations is called Cosmic Ray Simulations for Kascade (`CORSIKA`) [21] and allows for detailed simulation of EASs initiated by high-energy cosmic rays (HECRs). The showers are observed by a virtual IACT array, the `sim_telarray` [8], that allows simulating the optics of various mirror and camera geometries via ray-tracing of incoming photons. This also includes simulations of imperfections or misalignments of the mirrors of each telescope. The resulting so-called `simtel` data is used in `ctapipe` and can be processed as described in section 3.2 and Figure 3.1. Some of the data properties are listed in Table 3.1.

This data is the basis for the analysis in this work. A total of around 27 k telescope events (~12 k array events) throughout 20 `simtel` runs of diffuse gamma data were used for the initial analysis, i. e. the testing of different parameters as described in section 4.2. Telescope events are the events that have been observed on a telescope level, while array events are the events where at least two telescopes observed the same EAS. After processing the individual runs and merging them into one large file, this file is processed for the aforementioned parameters.

Once promising parameters are found, a larger dataset, containing around 1.3 M telescope events (~620 k array events) throughout 987 runs, is processed with these selected settings, allowing for more statistics and a better comparison of the cleaning algorithms.

Table 3.1: Simtel data properties of the `CORSIKA` simulation used for the datasets in this works analysis.

Diffuse Gamma data	
Energy range / TeV	0.003–330
Zenith angle / °	20
View cone angle / °	10
Number of showers	50 000
Spectral index	−2.0
Maximum scatter range / m	1900

3.2 Data Levels in *ctapipe*

There are several data levels in *ctapipe*, spanning from the raw data **R0** to the reconstructed events **DL2**, with the raw data levels being denoted by an **R** and the stored data levels by a **D**. Figure 3.1 shows a simplified overview of the data levels and the analysis steps. The raw data level **R0** is the data that comes directly from the photodetectors. The time-resolved signal of the data is calibrated from **R0** to **R1**. The data volume gets reduced (**R1** → **DL0**) by selecting waveform peaks for each pixel.

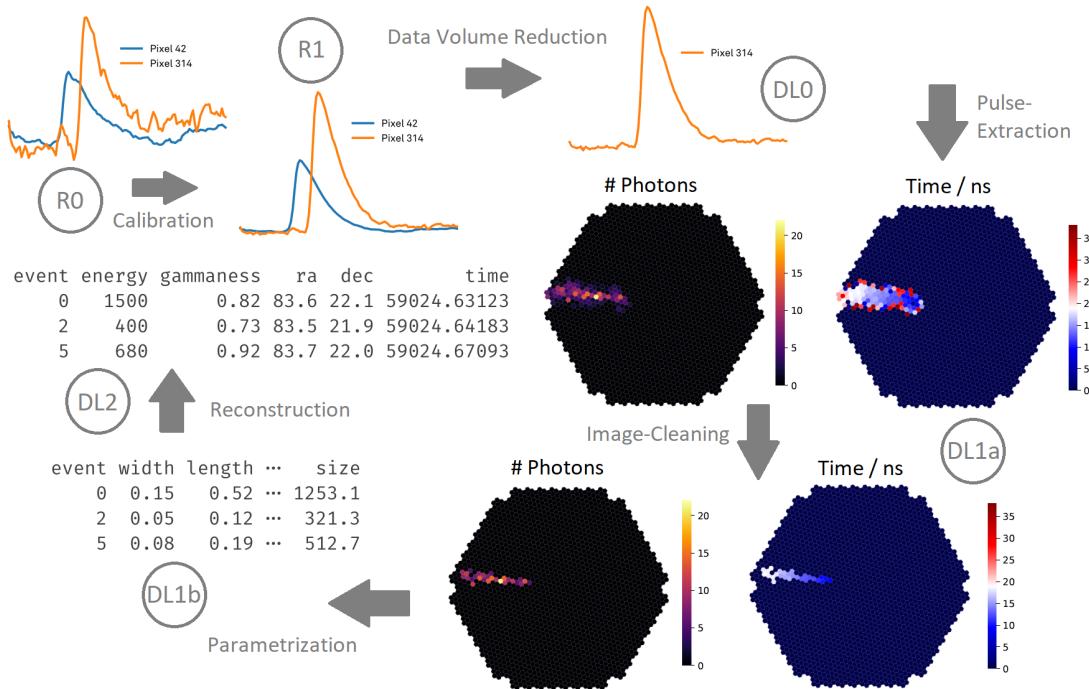


Figure 3.1: Data levels in *ctapipe*. Raw data levels are denoted by an **R** and calibrated data levels by a **D**. The raw data first gets calibrated (**R0** → **R1**) and then reduced in volume by selecting waveforms (**R1** → **DL0**). From there the images are extracted (**DL0** → **DL1a**) and cleaned with a cleaning algorithm. This allows for parametrization of the events (**DL1a** → **DL1b**). The parametrized events can then be reconstructed (**DL1b** → **DL2**) [26, 19].

The **DL0** data level is the first level being stored and also the first level to be processed from the simulation datasets used in this work. From **DL0** to **DL1a**, the photon images are extracted by integrating the waveform peaks of each pixel, whilst the time images ("peak times", compare Figure 3.1) are extracted by finding the rising edge of the pulse. The resulting images are cleaned by cleaning algorithms, to distinguish signal from NSB, which, in turn, allows for a parametrization of the events from **DL1a** to **DL1b**. The cleaning is a necessary step, especially for low-energy events, where the signal count is low compared to the NSB. The cleaning algorithms of *ctapipe* are introduced in section 4.1 and can be roughly categorized into time-based and non-time-based algorithms.

While the latter are selecting pixels based on charge thresholds which subsequently might lead to the need for a higher threshold, the former also takes the arrival times of pixels in the camera frame into

account, allowing for a lower charge threshold.

The advantage of a lower charge threshold allows the selection of more of the signal at lower energies. Once the events are cleaned and parametrized, they can then be reconstructed (**DL1b** → **DL2**) and stored on the **DL2** data level, which consists of an event list with direction, energy and the reconstructed gammaness—a value that predicated how likely an event was produced by a gamma.

3.3 This work’s data processing pipeline

In this work, the data processing pipeline is as follows: First, several simulation data runs are selected and processed with *ctapipe*. Then, the datasets are merged and serve as a basis for a re-run of the combined dataset with various parameter combinations described in chapter 4.

The settings for *ctapipe* are saved in two configuration files: First, a file, that sets up the cleaning process and what data to write to the output file. For the preprocessing step of this work’s pipeline, the cleaning settings are not relevant, as this step only serves to create a merged dataset. The second file contains a list of all the allowed telescope IDs. This allows a selection of the telescopes that are used in the analysis. This is especially helpful if one wants to only analyze MST-related data, like in this work.

For the re-run of the combined dataset, the cleaning settings are used¹, however, since this step is the heart of this work’s search for the optimal hyperparameters. The configuration files used are shown in appendix 1.

Each resulting dataset can then be processed on an array or telescope data level, resulting in **DL1a** image plots, values for the angular resolution and the efficiency as well as metrics for the performance. An in-detail description of how this helps to compare the performance of the different cleaning algorithms can be found in section 4.2. A schematic overview of the data processing pipeline of this work is shown in Figure 3.2.

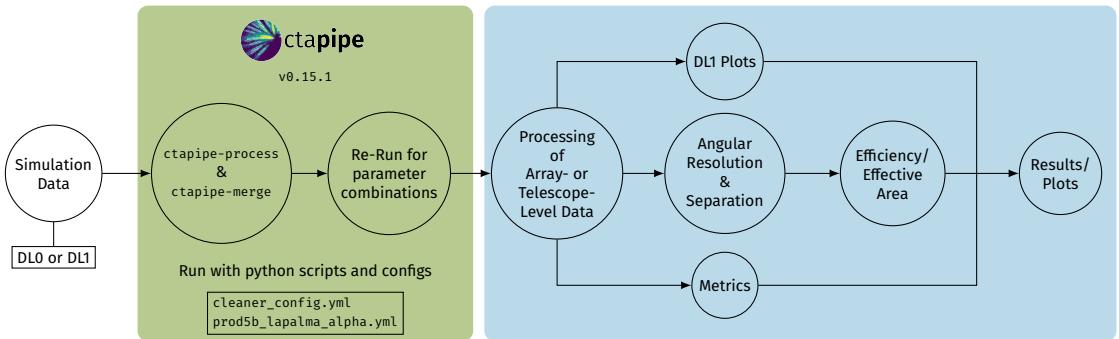


Figure 3.2: Schematic overview of the data pipeline used for this work. Single runs of the simulation data are processed with *ctapipe-process* and then merged via the tool *ctapipe-merge* (green shaded area). The merged data is then processed on the array or telescope data level resulting in scores for metrics as well as **DL1** images and plots for the angular resolution and the effective area (blue shaded area).

¹As opposed to the preprocessing step

Finding Optimal Hyperparameters for the Cleaning Algorithms

4

This work aims to find optimal hyperparameters for the cleaning algorithms used in `ctapipe`. Optimizing the cleaning step of the **DL1** data level in section 3.2 can most certainly lead to a better reconstruction of the events in a dataset. Therefore, a tweaking of the available parameters of each cleaner is necessary. In this chapter, I will first introduce the cleaning algorithms and their parameters in section 4.1 and then describe the procedure to find optimal hyperparameters in section 4.2.

4.1 Cleaning Algorithms

4.1.1 TailcutsImageCleaner

Version 0.15.1 of `ctapipe` features four cleaning algorithms, two of which are time-based. The `TailcutsImageCleaner` (Tailcuts) algorithm is the most basic algorithm of the four and serves as a good starting point for the development of new cleaning algorithms. Its first step is to select all pixels that are above a certain threshold, the core threshold Q_c . These pixels are the core part of the signal and are the brightest. The Tailcuts algorithm then selects all pixels that are above the boundary threshold Q_b and are neighboring the core pixels. A visualization of the algorithm is shown in Figure 4.1 for the default values of the algorithm.

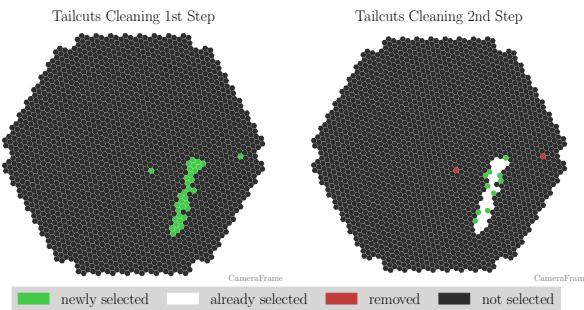


Figure 4.1: Visualization of the Tailcuts algorithm for a MST NectarCam image. First, all pixels above the core threshold are selected. Then, all pixels neighboring the core pixels that are above the boundary threshold are selected.

4.1.2 MARSImageCleaner

The `MARSImageCleaner` (MARS) algorithm [35] is very much based on the Tailcuts algorithm and features an additional step, in that it also selects all neighbors of a neighbor of a core pixel, if they are above the boundary threshold. The three steps for the MARS algorithm are shown in Figure 4.2 for its default values.

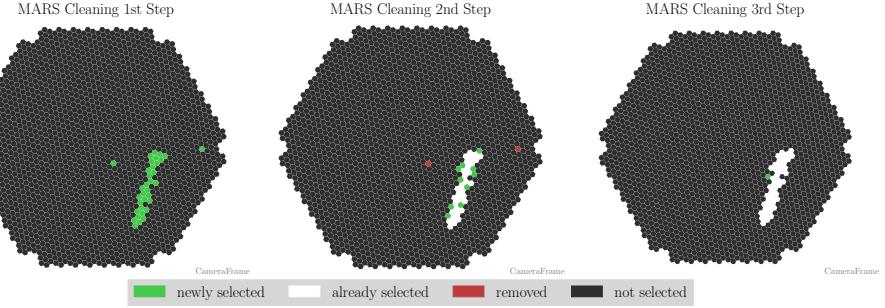


Figure 4.2: Visualization of the MARS algorithm for a MST NectarCam image. The first two steps are identical to the Tailcuts algorithm. The third step selects all neighbors of a neighbor of a core pixel if they are above the boundary threshold Q_b .

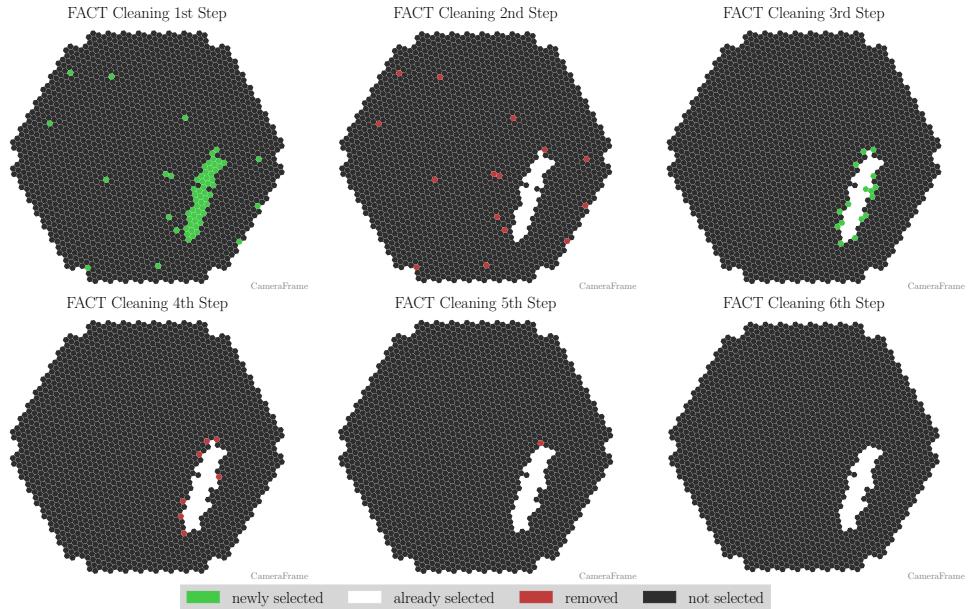


Figure 4.3: Visualization of the FACTImageCleaner (FACT) algorithm for a MST NectarCam image. The first step selects all pixels above the core threshold Q_c . The second step removes all pixels that have less than N neighbors. The third step selects all pixels neighboring the remaining pixels that are above the boundary threshold Q_b . The fourth step removes all pixels that have less than N neighbors, that have arrived within a given timeframe. The fifth and sixth steps are analogous to steps two and four respectively. Notice, that—per default in ctapipe—the values for Q_c and Q_b are lower than for the other cleaners (see Table 4.1), and hence together with the time limit more individual pixels than in the other cleaning algorithms are selected in the first step.

4.1.3 FactImageCleaner

The FACT algorithm [33, 32] is a time-based cleaning algorithm that first selects all pixels that are above Q_c . Then, all pixels that have less than N neighbors are removed. For the third step, all pixels neighboring the remaining pixels that are above Q_b are selected. After that, all pixels that have less than N neighbors and that have arrived within a given timeframe are removed. Again, all pixels with less than N neighbors are removed. The last step once again removes pixels with less than N neighbors, arriving within the given time limit. The visualization of the algorithm is shown in Figure 4.3 for the default values of the algorithm.

4.1.4 TimeConstrainedImageCleaner

The TimeConstrainedImageCleaner (TCC) algorithm is another time-based algorithm, coming from the MAGIC collaboration [29]. It first selects all pixels that are above Q_c . Then, all pixels that have less than N neighbors are removed. A minimum of 1 neighboring pixel is needed in the default settings. After that, all core pixels whose arrival times are within a given timeframe of the average arrival time. As a fourth step, the TCC algorithm finds all pixels above Q_b . Then, all pixels with less than N neighbors arriving within a given timeframe are removed. The visualization of the algorithm is shown in Figure 4.4 for the default values of the algorithm. For a better comparison, the resulting cleaned images are of each cleaner are shown in Figure 1 in appendix 4.

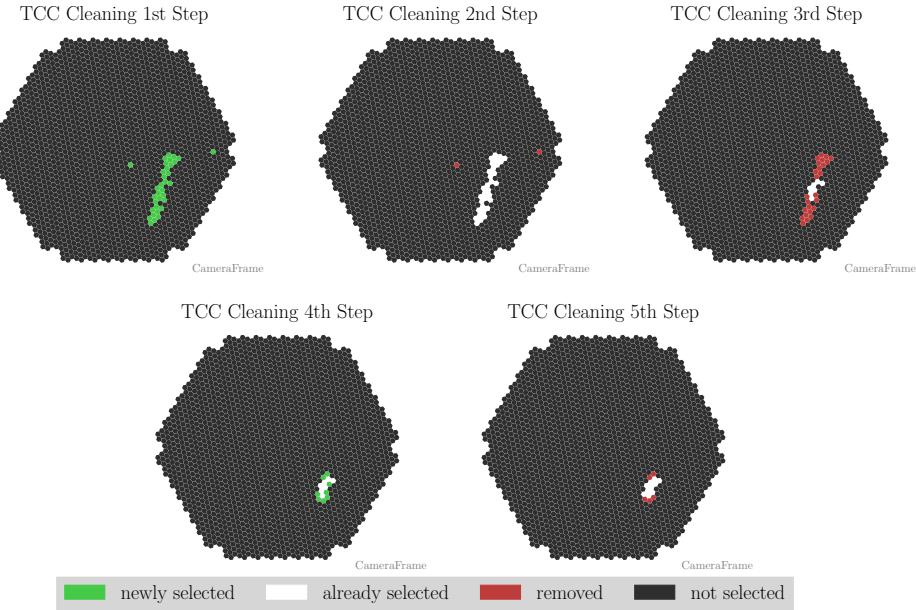


Figure 4.4: Visualization of the TCC algorithm for a MST NectarCam image. The first step selects all pixels above the core threshold Q_c . The second step removes all pixels that have less than N neighbors. The third step selects all pixels whose arrival times are within a given timeframe of the core time limit t_c . The fourth step selects all pixels above the boundary threshold Q_b . The fifth step removes all pixels with less than N neighbors, that have arrived within a given timeframe of the boundary time limit t_b . Notice, that with the default values TCC tends to select fewer pixels than the other algorithms.

4.2 Hyperparameters

The hyperparameters of each cleaning algorithm are set in a specific configuration file. There, the user can set and change the parameters, shown in Table 4.1. Tailcuts and MARS can be set-up with only three parameters: the `picture_threshold`, the `boundary_threshold` and `min_number_picture_neighbors`. The time-based algorithms have additional parameters: First of all a `time_limit` for FACT and then a `time_limit_core` as well as a `time_limit_boundary` for TCC.

Table 4.1: The four cleaning algorithms and their hyperparameters. Being the most basic algorithms, Tailcuts and MARS have only three parameters, while the FACT and TCC algorithms have one and two additional time-based parameters, respectively. This table shows the default values and, if the parameters have them, also their units, as they are implemented in the ctapipe source code for version 0.15.1.

Cleaning Algorithm	Hyperparameter	Default Values
Tailcuts	<code>picture_threshold</code>	7 p.e.
	<code>boundary_threshold</code>	5 p.e.
	<code>min_number_picture_neighbors</code>	0
MARS	<code>picture_threshold</code>	7 p.e.
	<code>boundary_threshold</code>	5 p.e.
	<code>min_number_picture_neighbors</code>	0
FACT	<code>picture_threshold</code>	4 p.e.
	<code>boundary_threshold</code>	2 p.e.
	<code>time_limit</code>	5 ns
	<code>min_number_picture_neighbors</code>	2
TCC	<code>picture_threshold</code>	7 p.e.
	<code>boundary_threshold</code>	5 p.e.
	<code>time_limit_core</code>	4.5 ns
	<code>time_limit_boundary</code>	1.5 ns
	<code>min_number_picture_neighbors</code>	1

The full configuration files for the default settings of each cleaning algorithm are listed in appendix 1. There, the configuration files for the allowed telescopes as described in section 3.3 are shown, too.

To find the optimal hyperparameters, I utilized `scikit-learn` [28] for a grid search. This allows one to manually set subsets of hyperparameters and search for the best combination of these. Table 1 in appendix 2 shows the subsets of hyperparameters used in this work.

I used noise quantiles, i. e. the percentage of all `noise` pixels that are therefore not part of the true signal, to determine the core threshold Q_c . This would mean, that e. g. 99.99 % of the noise pixels would fall under a threshold of 9.50 p.e. for the data used in this work. The quantiles are calculated directly from the images by discriminating the noise pixels from the image with the help of the true image. This approach has the advantage, that the resulting thresholds are more precisely optimized¹. Since the boundary thresholds are calculated as a quotient of Q_c , this benefits here as well. The quantiles used in this work are shown in Figure 4.5.

¹As opposed to setting the thresholds by hand, e. g. 4 to 10 in 0.5 increments.

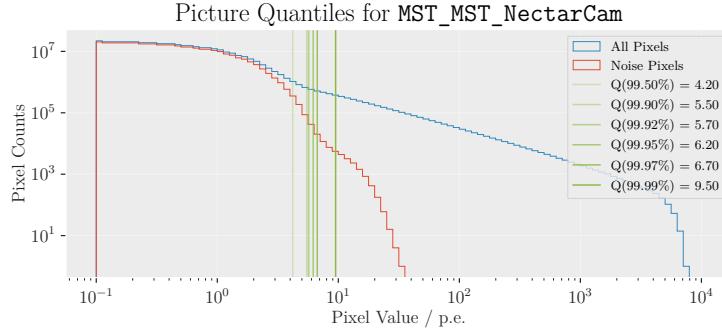


Figure 4.5: Picture noise quantiles for a MST NectarCam dataset. The quantiles are calculated as the percentage of noise pixels in the image. The resulting threshold can then be used as a candidate for the core threshold Q_c in a grid search.

The grid search results in 150 parameter combinations for Tailcuts and MARS each, as well as another 1050 combinations for FACT and further 3000 combinations for TCC. Since it's impossible to find the optimal settings just by looking at the cleaned images of the datasets, a combined metric is necessary to evaluate each cleaner's performance for the parameter combinations.

In this work, I chose to first look at the efficiency

$$\text{Eff} = \frac{n_{\text{reco}}}{n_{\text{total}}}, \quad (4.1)$$

where n_{total} is the total number of events in the dataset and n_{reco} the number of reconstructed events. The latter depends on the cleaning, as only a successfully cleaned event can be parametrized and therefore reconstructed. By first binning the efficiency per energy and then taking the sum over all energy bins, one can sort the datasets by setting upper and lower bounds for the efficiency. The intervals' lengths were chosen as 0.05, i. e. 5 %, resulting in a total of 20 intervals between 0 % and 100 %.

For each interval, the mean angular resolution is calculated by determining the 68 % containment of the angular distance distribution, i. e. the angular distance between the reconstructed origin and the true origin of the shower. The dataset with the lowest mean angular resolution is the best performing for each interval. If more low-energy events are reconstructed, not only will the efficiency be higher, but also the angular resolution, as those events are more likely to include pixels that are part of the NSB. As a result, a trade-off between efficiency and angular resolution is necessary.

For the performance analysis of the algorithms, I calculated metrics such as, but not limited to, the True Positive Rate (TPR) or recall, the False Positive Rate (FPR) or fall-out and the True Negative Rate (TNR) or specificity. A list of all used metrics can be seen in Table 2 in appendix 4.1.

Results

5

In this chapter, the results of the analysis are presented. First, I present the results of the efficiency analysis in section 5.1. The initial tests of parameter combinations are based on a small dataset consisting of 20 runs, i. e. 12 668 events. This is due to the number of parameter combinations that are tested, as more runs would increase the processing time immensely. Furthermore, I show the results of the angular resolution for a combined metric with the efficiency. Then, in section 5.2, the metrics of each resulting combination of hyperparameters are plotted. In section 5.3, the performance of each cleaning algorithm compared to the default settings is shown. Finally, a comparison of the different cleaning algorithms is provided in section 5.4.

5.1 Analysis of the efficiency and the angular resolution

To narrow down possible candidates for the optimal hyperparameters, I first analyzed the efficiency of the different cleaning algorithms. The efficiency is determined by the number of events that are reconstructed after cleaning. For this work I chose 20 intervals within 0 and 1 with a step size of 0.05. The events are binned per energy and the mean efficiency over all energy bins is then calculated as the mean of Equation 4.1. For each interval only those datasets are selected, where the mean efficiency lies between the lower and upper bound of the interval. Then the minimum angular resolution is determined for each interval. The parameters of these datasets are then selected to be the optimal parameters for each cleaning algorithm. This not only allows for a comparison of the cleaners but also a decision on a trade-off between the efficiency and the angular resolution, namely having a better angular resolution, but a lower efficiency or a higher efficiency but a higher and therefore worse angular resolution. The results for the mean efficiency are listed in Table 5.1 and the results for the mean angular resolution in Table 5.2.

As one can see, not all cleaning algorithms have valid values for each interval, peaking at a maximum of around 45 % to 50 % of successfully reconstructed events. This is because not all events are stereo events, i. e. events, where two or more telescopes were triggered, which is a requirement for the reconstruction. The remaining events are therefore mono events and do not contribute to either the efficiency or the angular resolution. The efficiency would be higher, of course, for a full-array analysis, but that would mean also including LSTs data¹, which for this work would not help find the optimal parameters, since it is better to analyze the telescope types separately. The reason for the latter is, that optimizing the telescopes by type would lead to better results for the hyperparameters.

The results listed in the tables show that there is a clear trade-off in choosing between efficiency and angular resolution. As such, for further comparison of the cleaning algorithms, the corresponding datasets for the efficiency and the angular resolution are plotted in Figure 5.1 for the intervals [0.25, 0.30] and [0.45, 0.50]. The reason for this is that these are the minimum and maximum intervals w. r. t. the

¹which was left out due to time limitations, see chapter 6.

Table 5.1: The results of the analysis for the mean efficiency of each cleaning algorithm taken over all energy bins. The efficiency is calculated as the ratio of the number of reconstructed events n_{reco} and the number of total events n_{total} . The table lists the lower and upper limits of each efficiency interval. The efficiency is then calculated as the mean over the whole energy range of the dataset and each listed efficiency is the one where the mean angular resolution is minimal for the given interval. Notice how not all cleaning algorithms have valid results for all efficiency intervals.

Mean Efficiency					
Eff _{lower}	Eff _{upper}	Tailcuts	MARS	FACT	TCC
0.00	0.05			0.034	
0.05	0.10			0.051	
0.10	0.15			0.117	
0.15	0.20			0.163	
0.20	0.25			0.218	0.211
0.25	0.30	0.263	0.265	0.287	0.273
0.30	0.35	0.313	0.315	0.321	0.316
0.35	0.40	0.362	0.364	0.369	0.390
0.40	0.45	0.402	0.403	0.426	0.426
0.45	0.50	0.451	0.463	0.466	0.455
0.50	0.55	0.501			

Table 5.2: The results of the analysis for the mean angular resolution of each cleaning algorithm. The table lists the lower and upper limits of each efficiency interval. The angular resolution listed is the minimum mean angular resolution of the respective efficiency interval. The corresponding efficiency values are listed in Table 5.1. Notice how not all cleaning algorithms have valid results for all efficiency intervals.

Mean Angular Resolution / °					
Eff _{lower}	Eff _{upper}	Tailcuts	MARS	FACT	TCC
0.00	0.05			0.244	
0.05	0.10			0.297	
0.10	0.15			0.420	
0.15	0.20			0.428	
0.20	0.25			0.477	0.413
0.25	0.30	0.358	0.291	0.415	0.396
0.30	0.35	0.308	0.282	0.367	0.340
0.35	0.40	0.334	0.332	0.366	0.386
0.40	0.45	0.357	0.343	0.365	0.383
0.45	0.50	0.395	0.395	0.404	0.390
0.50	0.55	1.301			

5 Results

efficiency, where all cleaners have valid values. Furthermore, the mean angular resolution is plotted against the efficiency in Figure 5.2.

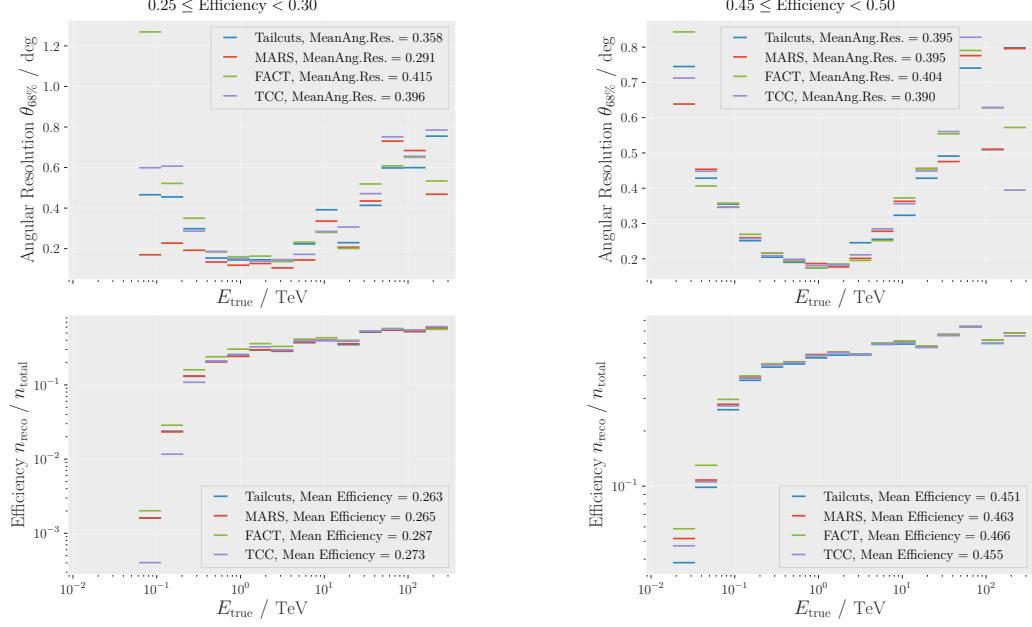


Figure 5.1: Mean angular resolution and efficiency for the MST simulation binned per energy. Notice the decrease in the scattering of the mean angular resolution at medium to medium-high energies at higher efficiencies in the plots on the right.

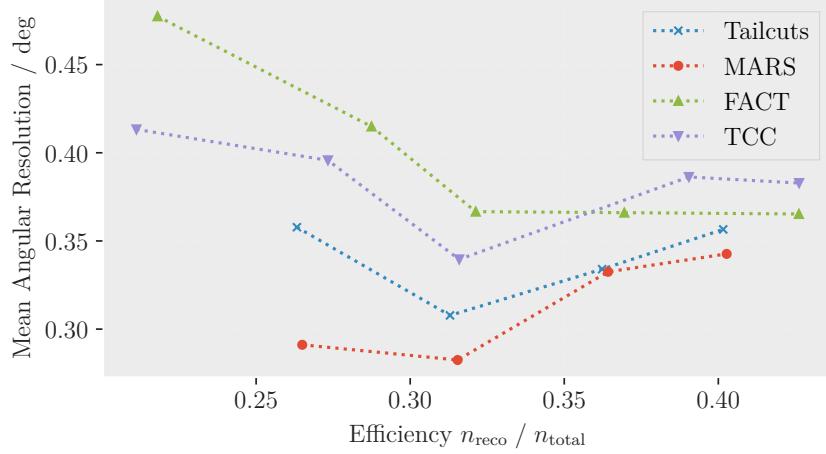


Figure 5.2: Angular resolution plotted against the efficiency between 0.2 and 0.5.

5.2 Metrics of the cleaning algorithms

Concerning the metrics, I first analyzed the parameter combinations of all settings found in section 5.1. First, the number of the True Positive (tp), False Positive (fp), False Negative (fn) and True Negative (tn) values is calculated per event. Then, those values are summed up for each cleaning algorithm and the metrics are calculated as shown in Table 2.

The metrics for each parameter combination are first compared for each cleaning algorithm respectively, to determine the best setting within a set of parameter combinations. The results are then plotted in Figures 5.3, 5.4, 5.5 and 5.6 and are shown with specific IDs they were given when the datasets were processed with ctapipe. This improves readability as opposed to writing out the full settings. The hyperparameters for the best performing IDs of all algorithms are listed in Table 5.7.

While all settings perform well w. r. t., for example, the TNR, one can see from the results, that for all cleaning algorithms—except for MARS—, the best parameter combination is the one where the TPR, the Accuracy (ACC) and the Balanced Accuracy (BA) are the highest. These settings are the ones that correspond to the highest efficiency. While this is true for Tailcuts, FACT and TCC, the metrics for MARS are an exception. The reason for that is, that when looking at the corresponding mean angular resolution for the highest performing setting (ID 10), the value is 1.301° (see Table 5.2) and therefore an order of magnitude worse than the other algorithms. For better comparison, I, therefore, choose the second highest performing setting (ID 15) with a mean angular resolution of 0.395° to be the best candidate for further analysis. The values for each respective metric and cleaning algorithm are listed in Tables 5.3, 5.4, 5.5 and 5.6 respectively, while a comparison of the cleaners against each other is shown in section 5.4.

Table 5.3: Results for the metrics of Tailcuts. One can see, that the best results are obtained for the setting with ID 47.

ID	TPR	TNR	FNR	ACC	BA
118	0.0972	1.0000	0.9028	0.9256	0.5486
51	0.1231	1.0000	0.8769	0.9256	0.5615
140	0.1460	1.0000	0.8540	0.9256	0.5730
81	0.1854	1.0000	0.8146	0.9288	0.5927
47	0.2268	1.0000	0.7732	0.9332	0.6134

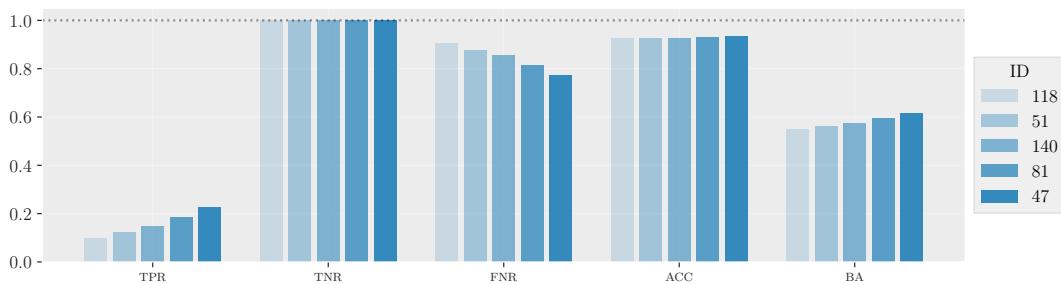


Figure 5.3: Metrics for Tailcuts. It can be seen, that the cleaning setting with ID 47 performs best in terms of the true positive rate, accuracy and balanced accuracy, making it the best setting of the five parameter combinations.

5 Results

Table 5.4: Results for the metrics of MARS. The last row (ID 10) shows a significant increase in the TPR and therefore decrease in False Negative Rate (FNR) and another significant increase in the BA value. Since this specific parameter combination also corresponds to a mean angular resolution an order higher than the rest, I chose to select the second highest performing setting (ID 15) for further analysis instead.

ID	TPR	TNR	FNR	ACC	BA
54	0.1069	1.0000	0.8931	0.9256	0.5534
59	0.1369	1.0000	0.8631	0.9256	0.5684
76	0.1565	1.0000	0.8435	0.9256	0.5782
135	0.1738	1.0000	0.8262	0.9294	0.5869
15	0.2433	1.0000	0.7567	0.9380	0.6216
10	0.4119	0.9977	0.5881	0.9450	0.7048

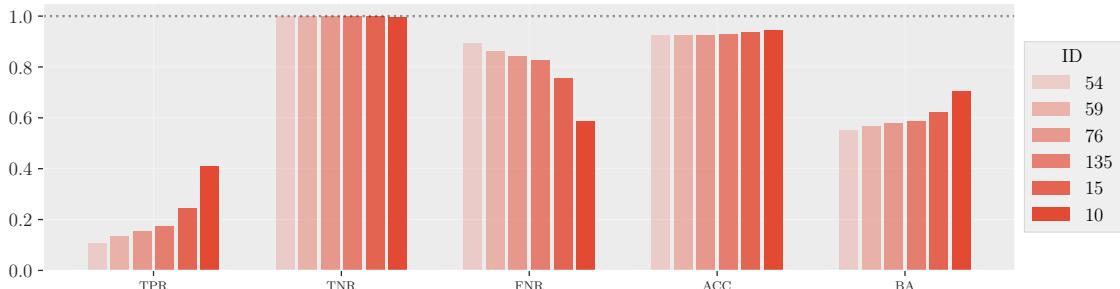


Figure 5.4: Metrics for MARS. While ID 10 arguably performs best at first glance—albeit with a not insignificant decrease in the Positive Predictive Value (PPV) value—, I chose ID 15 for further analysis, as its mean angular resolution is an order of magnitude better.

Table 5.5: Results for the metrics of FACT. One can see, that the best results are obtained for the settings with ID 503.

ID	TPR	TNR	FNR	ACC	BA
553	0.0077	1.0000	0.9923	0.9256	0.5039
833	0.0134	1.0000	0.9866	0.9256	0.5067
549	0.0321	1.0000	0.9679	0.9256	0.5161
271	0.0396	1.0000	0.9604	0.9256	0.5198
12	0.0608	1.0000	0.9392	0.9256	0.5304
767	0.1042	1.0000	0.8958	0.9256	0.5521
722	0.1425	1.0000	0.8575	0.9256	0.5712
691	0.1464	1.0000	0.8536	0.9272	0.5732
608	0.2040	1.0000	0.7960	0.9326	0.6020
503	0.2655	1.0000	0.7345	0.9369	0.6327

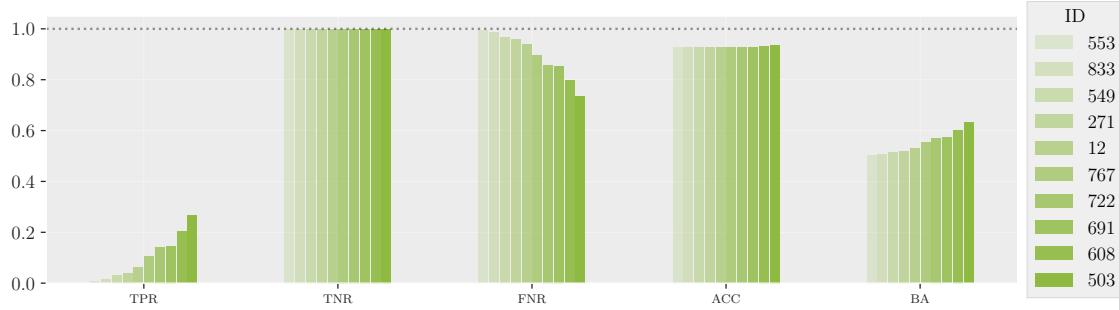


Figure 5.5: Metrics for FACT. The cleaning setting with ID 503 performs best in terms of the number of true positives, accuracy and balanced accuracy, making it the best setting of the ten parameter combinations.

Table 5.6: Results for the metrics of TCC. The best results are obtained for the setting with ID 807.

ID	TPR	TNR	FNR	ACC	BA
11	0.0452	1.0000	0.9548	0.9256	0.5226
367	0.0717	1.0000	0.9283	0.9256	0.5359
399	0.1071	1.0000	0.8929	0.9256	0.5535
171	0.1653	1.0000	0.8347	0.9278	0.5827
1495	0.2088	1.0000	0.7912	0.9321	0.6044
807	0.2314	1.0000	0.7686	0.9364	0.6157

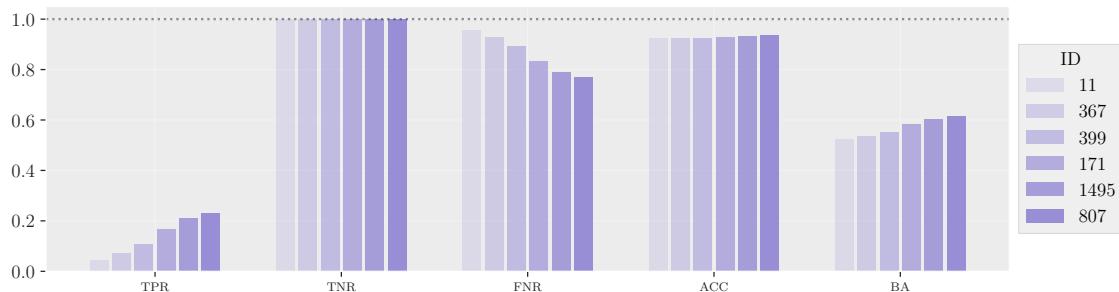


Figure 5.6: Metrics for the TCC. The cleaning setting with ID 807 performs best in terms of the number of true positives, accuracy and balanced accuracy, making it the best setting of the six parameter combinations.

Table 5.7: Best performing IDs and the corresponding hyperparameters for each respective cleaner. Note, that, as discussed above, the best performing ID w.r.t. the metrics for MARS is, in fact, not the best, but the second best. This is because the mean angular resolution is an order of magnitude better for ID 15 than the one for ID 10. For better readability, the names of the algorithms are shortened. Listed are the core threshold Q_c , the boundary threshold Q_b , the minimum number of neighbors and where applicable the time limit t and core and boundary time limits t_c and t_b .

Cleaning Algorithm	ID	Q_c / p.e.	Q_b / p.e.	Min. Neigh.	t / ns	t_c / ns	t_b / ns
Tailcuts	47	6.200	4.650	2			
MARS	15	6.700	4.467	1			
FACT	503	6.700	3.350	1	12.0		
TCC	807	6.700	4.467	1		15.0	12.0

5.3 Performance compared to the default settings

Now, with a setting selected for each cleaner, it is reasonable to compare the performance to the default settings, that are implemented in the `ctapipe` source code (see Table 4.1). First, the relative angular resolution

$$\theta_{\text{rel}} = \frac{\theta_{68\%}}{\theta_{68\%, \text{base}}} \quad (5.1)$$

is computed for the default (base) settings and the selected settings for each cleaner. The results are shown in Figure 5.8 for the same efficiency intervals as in Figure 5.1. One can see, that especially for the interval [0.45, 0.5) and at medium to high energies, TCC performs fairly well compared to the default settings. The other algorithms perform only slightly better than the default settings at a performance gain of about 10 %.

Furthermore, the metrics of the hyperparameters determined in this work can be compared to the metrics of the default settings. The results are shown in Figure 5.7 with the values of the metrics being listed in Table 5.8. The values for the selected settings in this work are listed in Table 5.9. FACT performs worse than its default setting w.r.t. the metrics, especially in terms of TPR and BA. This might be due to the higher core and boundary thresholds compared to the default values, as lower values would allow selecting more pixels. TCC, however, performs significantly better than the default settings, especially in terms of TPR and BA, but also slightly better in terms of the ACC metric.

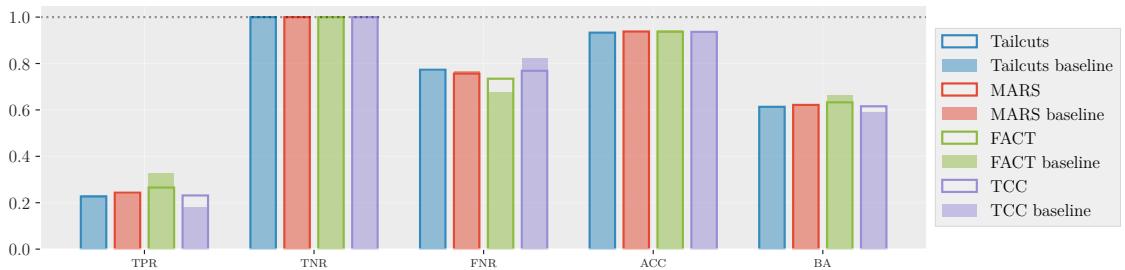


Figure 5.7: Metrics for the default (baseline) settings compared to the settings determined in this work. One can see that an improvement was reached for TCC, especially in terms of TPR and BA, while FACT performs worse than its default implementation.

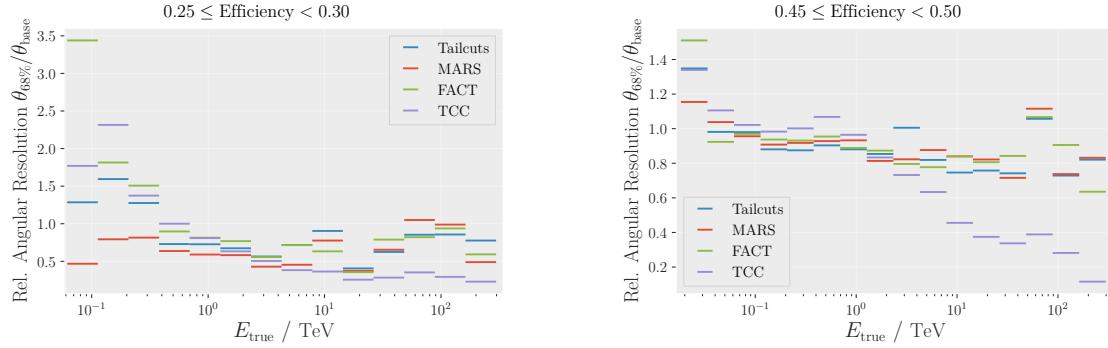


Figure 5.8: Relative angular resolution for the default settings and the selected settings for each cleaner. TCC outperforms the default values with the new settings, while the other algorithms improve only slightly.

Table 5.8: Metrics for the default (baseline) settings. The metrics show that FACT performs well even in its default settings and also better than with the hyperparameters determined in this work. TCC, however, performs better with the hyperparameters listed in Table 5.7 w. r. t. the metrics.

Cleaning Algorithm	TPR	FPR	TNR	FNR	PPV	ACC	BA
Tailcuts	0.2316	0.0000	1.0000	0.7684	0.9971	0.9358	0.6158
MARS	0.2346	0.0000	1.0000	0.7654	0.9970	0.9358	0.6173
FACT	0.3261	0.0002	0.9998	0.6739	0.9864	0.9429	0.6629
TCC	0.1790	0.0000	1.0000	0.8210	0.9995	0.9299	0.5895

5.4 Comparison of the cleaning algorithms

As of writing this thesis, the cleaning algorithms discussed in this thesis are the only ones implemented in the `ctapipe` source code. With the determined hyperparameters, I decided to compare the performance of all four cleaners. I once again decided to use the settings selected in section 5.2 for each algorithm and look at the metrics. The metrics of all four algorithms are shown in Figure 5.9. The corresponding values are listed in Table 5.9.

One can see, that FACT performs best in terms of TPR and BA, while MARS and Tailcuts perform well on ACC and PPV respectively. Overall, however, FACT seems to be a good choice for cleaning since it performs reasonably well even on ACC and PPV.

Table 5.9: Metrics for the selected settings of each cleaning algorithm. Out of these four algorithms, FACT performs best in terms of TPR and BA, while MARS and Tailcuts perform well on ACC and PPV respectively. FACT, however, performs reasonably well in the scope of the resulting metrics of this work and is, therefore, a good overall choice for cleaning.

Cleaning Algorithm	TPR	FPR	TNR	FNR	PPV	ACC	BA
Tailcuts	0.2268	0.0000	1.0000	0.7732	0.9994	0.9332	0.6134
MARS	0.2433	0.0000	1.0000	0.7567	0.9985	0.9380	0.6216
FACT	0.2655	0.0000	1.0000	0.7345	0.9968	0.9369	0.6327
TCC	0.2314	0.0000	1.0000	0.7686	0.9989	0.9364	0.6157

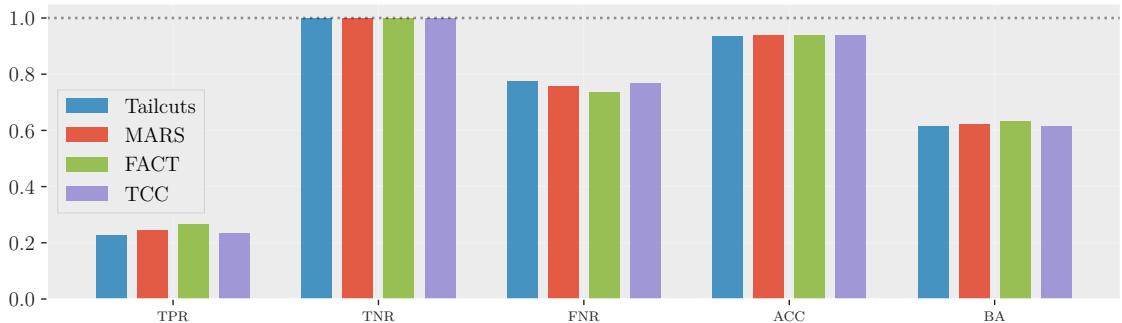


Figure 5.9: Bar plot visualizing the metrics for the selected settings of all four cleaning algorithms. FACT performs best out of all cleaning algorithms, followed by MARS and TCC. The latter, however performs well w. r. t. the angular resolution, as shown in Figure 5.8 and can therefore be considered a viable alternative to FACT.

6

Conclusions and Outlook

In the scope of this work, the hyperparameters for each of the four currently (as of writing this thesis) implemented cleaning algorithms were searched via a grid search. The resulting hyperparameters were then probed w. r. t. a combined metric of the angular resolution and the efficiency. These results led to a subset consisting of the best-performing hyperparameters for each cleaning algorithm. Furthermore, a comparison between the optimized algorithms and the default algorithms, as well as a comparison between each respective cleaner was performed.

Most of the data (pre-)processing in this work was done with CTA’s open-source low-level data processing pipeline software `ctapipe`, version 0.15.1. The data used was PROD5 MC simulations consisting of 1.3 M telescope events (~ 620 k array events) throughout 987 runs. The data was processed from raw `simtel` data (**R0**) up to cleaned (**DL1a**) and parametrized (**DL1b**) levels for the metrics as well as reconstructed (**DL2**) data for the efficiency and angular resolution. Further high-level processing was done with this works pipeline as described in section 3.3.

The four implemented cleaning algorithms can be roughly categorized into time-based (FACT and TCC) and non-time-based algorithms (Tailcuts and MARS). While the non-time-based algorithms only take thresholds of the photon count of each pixel into account, the time-based algorithms also set limits on the arrival time of each pixel. This allows for a lower core threshold Q_c for the photon count per pixel, which in turn can lead to better results in the cleaning process. A good cleaning not only reduces data size—as a majority of the pixels in the image are made up by NSB—but it also allows for a better parameterization and in turn a better reconstruction of the events.

The main results of this thesis are the hyperparameters for the cleaning algorithms. Due to the long runtimes of the grid searches and the time limitation of this thesis, however, the hyperparameters for cleaning algorithms could only optimized for MSTs. The optimal hyperparameters of each cleaning algorithm for the MSTs are listed in Table 5.7. A further grid search with only LST data would be necessary to find the remaining core and boundary thresholds Q_c and Q_b as well as the time limits for the LST data.

The comparison of the performance of the optimized algorithms with the default algorithms has shown that the optimized algorithms performed better than the default algorithms w. r. t. the angular resolution. This means that the found hyperparameters could help with origin reconstructions. When looking at the metrics, however, only TCC really improved, while FACT even performed worse than its default implementation. The reason might be, that the higher core threshold Q_c —compared to the default value—would select fewer pixels. Additionally, a comparison between the optimized algorithms themselves was performed. This led to FACT being the best performing algorithm overall w. r. t. the metrics, with only a slight advantage over the other algorithms, however.

All in all, one can say, that the hyperparameters determined at a higher efficiency return better results, albeit resulting in a higher angular resolution. This is due to the fact that a higher efficiency means that more events got reconstructed and therefore better overall statistics. Nevertheless, further analysis and a broader grid search might be necessary to find better hyperparameters and therefore better the performance of all algorithms. This will also be necessary for the LST data.

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Glossary

ACC Accuracy. 19–24, 37

AGN active galactic nucleus. 2, 3

BA Balanced Accuracy. 19–24, 37

CORSIKA Cosmic Ray Simulations for Kascade. 8

CR cosmic rays. 1–3

CTA Cherenkov Telescope Array. iii, 4, 6–8, 25

EAS extensive air shower. 3–5, 8

ESO European Southern Observatory. 6

FACT FACTImageCleaner. iii, 12–15, 19–25, 33, 36, 38

Fermi-LAT *Fermi* Large Area Telescope. 2–4

fn False Negative. 19, 37

FNR False Negative Rate. 19–21, 23, 24, 37

fp False Positive. 19, 37

FPR False Positive Rate. 15, 23, 24

GRB gamma ray burst. 3

HE high-energy. 2, 4, 7

HECR high-energy cosmic ray. 8

HEGR high-energy gamma rays. 2

H.E.S.S. High Energy Stereoscopic System. 3, 7

IACT Imaging Air Cherenkov Telescope. iii, 3–6, 8

LST Large-Sized Telescope. 6, 7, 16, 25, 35

Glossary

MAGIC Major Atmospheric Gamma-Ray Imaging Cherenkov. 3, 7, 13

MARS MARSIImageCleaner. 11, 12, 14, 15, 19, 20, 22–25, 32, 38

MC Monte Carlo. iii, 8, 25

MST Medium-Sized Telescope. iii, 6, 7, 10–13, 15, 25, 35

NSB Night Sky Background. 5, 9, 15, 25

ORM Observatorio del Roque de los Muchachos. 6

PMT photo multiplier tube. 7

PPV Positive Predictive Value. 20, 23, 24

PWN pulsar wind nebula. 7

SiPM silicon photomultiplier. 7

SNR supernova remnant. 2, 3

SST Small-Sized Telescope. 6, 7

Tailcuts TailcutsImageCleaner. 11, 12, 14, 15, 19, 23–25, 32, 38

TCC TimeConstrainedImageCleaner. iii, 13–15, 19, 21–25, 34, 36, 38

tn True Negative. 19, 37

TNR True Negative Rate. 15, 19–21, 23, 24, 37

tp True Positive. 19, 37

TPR True Positive Rate. 15, 19–24, 37

VERITAS Very Energetic Radiation Imaging Telescope Array System. 3

VHE very-high-energy. 7

VHE gamma rays very-high-energy gamma rays. 3, 7

Appendix

1 Configurations for ctapipe

The listing below shows the configuration file used for preprocessing the datasets, i. e. before the application of the different cleaning settings.

```
DataWriter:  
    transform_image: true  
    transform_peak_time: true  
    write_images: true  
    write_parameters: false  
    write_raw_waveforms: false  
    write_showers: true  
  
ProcessorTool:  
    progress_bar: true  
  
CameraCalibrator:  
    image_extractor_type: NeighborPeakWindowSum  
  
ImageProcessor:  
    image_cleaner_type: TailcutsImageCleaner  
  
TailcutsImageCleaner:  
    picture_threshold_pe:  
        - [type, "LST*", 8.5]  
        - [type, "MST*NectarCam", 9.0]  
    boundary_threshold_pe:  
        - [type, "LST*", 4.75]  
        - [type, "MST*NectarCam", 4.5]  
    keep_isolated_pixels: false  
    min_picture_neighbors: 2  
  
ImageQualityQuery:  
    quality_criteria:  
        - ["enough_pixels", "np.count_nonzero(image) > 2"]  
        - ["enough_charge", "image.sum() > 50"]  
  
ShowerProcessor:  
    reconstructor_type: HillasReconstructor  
    HillasReconstructor:  
        StereoQualityQuery:  
            quality_criteria:  
                - [enough intensity, "parameters.hillas.intensity > 50"]  
                - [Positive width, "parameters.hillas.width.value > 0"]  
                - [enough pixels, "parameters.morphology.num_pixels > 3"]  
                - [not clipped, "parameters.leakage.intensity_width_2 < 0.5"]
```

Appendix

```
SimTelEventSource:  
    focal_length_choice: effective  
    skip_calibration_events: true
```

The listings below show the contents of the default configuration files used with ctapipe for each cleaning algorithm respectively.

TailcutsImageCleaner (Tailcuts):

```
DataWriter:  
    transform_image: true  
    transform_peak_time: true  
    write_images: false  
    write_parameters: true  
    write_raw_waveforms: false  
    write_showers: true  
  
ProcessorTool:  
    progress_bar: true  
  
CameraCalibrator:  
    image_extractor_type: NeighborPeakWindowSum  
  
ImageProcessor:  
    image_cleaner_type: TailcutsImageCleaner  
  
TailcutsImageCleaner:  
    picture_threshold_pe:  
        - [type, "LST*", 7.0]  
        - [type, "MST*NectarCam", 7.0]  
    boundary_threshold_pe:  
        - [type, "LST*", 5.0]  
        - [type, "MST*NectarCam", 5.0]  
    keep_isolated_pixels: false  
    min_picture_neighbors: 0  
  
ImageQualityQuery:  
    quality_criteria:  
        - ["enough_pixels", "np.count_nonzero(image) > 2"]  
        - ["enough_charge", "image.sum() > 50"]  
  
ShowerProcessor:  
    reconstructor_type: HillasReconstructor  
    HillasReconstructor:  
        StereoQualityQuery:  
            quality_criteria:  
                - [enough intensity, "parameters.hillas.intensity > 50"]  
                - [Positive width, "parameters.hillas.width.value > 0"]  
                - [enough pixels, "parameters.morphology.num_pixels > 3"]  
                - [not clipped, "parameters.leakage.intensity_width_2 < 0.5"]
```

MARSImageCleaner (MARS):

```
DataWriter:  
    transform_image: true  
    transform_peak_time: true  
    write_images: false
```

```

write_parameters: true
write_raw_waveforms: false
write_showers: true

ProcessorTool:
  progress_bar: true

CameraCalibrator:
  image_extractor_type: NeighborPeakWindowSum

ImageProcessor:
  image_cleaner_type: MARSImageCleaner

  MARSImageCleaner:
    picture_threshold_pe:
      - [type, "LST*", 7.0]
      - [type, "MST*NectarCam", 7.0]
    boundary_threshold_pe:
      - [type, "LST*", 5.0]
      - [type, "MST*NectarCam", 5.0]
    keep_isolated_pixels: false
    min_picture_neighbors: 0

  ImageQualityQuery:
    quality_criteria:
      - ["enough_pixels", "np.count_nonzero(image) > 2"]
      - ["enough_charge", "image.sum() > 50"]

ShowerProcessor:
  reconstructor_type: HillasReconstructor
  HillasReconstructor:
    StereoQualityQuery:
      quality_criteria:
        - [enough intensity, "parameters.hillas.intensity > 50"]
        - [Positive width, "parameters.hillas.width.value > 0"]
        - [enough pixels, "parameters.morphology.num_pixels > 3"]
        - [not clipped, "parameters.leakage.intensity_width_2 < 0.5"]

```

FACTImageCleaner (FACT):

```

DataWriter:
  transform_image: true
  transform_peak_time: true
  write_images: false
  write_parameters: true
  write_raw_waveforms: false
  write_showers: true

ProcessorTool:
  progress_bar: true

CameraCalibrator:
  image_extractor_type: NeighborPeakWindowSum

ImageProcessor:
  image_cleaner_type: FACTImageCleaner

  FACTImageCleaner:
    picture_threshold_pe:

```

```
- [type, "LST*", 7.0]
- [type, "MST*NectarCam", 7.0]
boundary_threshold_pe:
- [type, "LST*", 5.0]
- [type, "MST*NectarCam", 5.0]
keep_isolated_pixels: false
min_picture_neighbors: 2
time_limit_ns: 5.0

ImageQualityQuery:
quality_criteria:
- ["enough_pixels", "np.count_nonzero(image) > 2"]
- ["enough_charge", "image.sum() > 50"]

ShowerProcessor:
reconstructor_type: HillasReconstructor
HillasReconstructor:
StereoQualityQuery:
quality_criteria:
- [enough intensity, "parameters.hillas.intensity > 50"]
- [Positive width, "parameters.hillas.width.value > 0"]
- [enough pixels, "parameters.morphology.num_pixels > 3"]
- [not clipped, "parameters.leakage.intensity_width_2 < 0.5"]
```

TimeConstrainedImageCleaner (TCC):

```
DataWriter:
transform_image: true
transform_peak_time: true
write_images: false
write_parameters: true
write_raw_waveforms: false
write_showers: true

ProcessorTool:
progress_bar: true

CameraCalibrator:
image_extractor_type: NeighborPeakWindowSum

ImageProcessor:
image_cleaner_type: TimeConstrainedImageCleaner

TimeConstrainedImageCleaner:
picture_threshold_pe:
- [type, "LST*", 7.0]
- [type, "MST*NectarCam", 7.0]
boundary_threshold_pe:
- [type, "LST*", 5.0]
- [type, "MST*NectarCam", 5.0]
keep_isolated_pixels: false
min_picture_neighbors: 1
time_limit_core_ns: 4.5
time_limit_boundary_ns: 1.5

ImageQualityQuery:
quality_criteria:
```

```

    - ["enough_pixels", "np.count_nonzero(image) > 2"]
    - ["enough_charge", "image.sum() > 50"]

ShowerProcessor:
  reconstructor_type: HillasReconstructor
  HillasReconstructor:
    StereoQualityQuery:
      quality_criteria:
        - [enough intensity, "parameters.hillas.intensity > 50"]
        - [Positive width, "parameters.hillas.width.value > 0"]
        - [enough pixels, "parameters.morphology.num_pixels > 3"]
        - [not clipped, "parameters.leakage.intensity_width_2 < 0.5"]

```

The following listing shows the contents of the `prod5b_lapalma_alpha.yml` configuration file, which is used to set the allowed telescope IDs for `ctapipe-process`.

```

# telescope ids of the 4 LST + 9 MST La Palma alpha configuration in Prod5b
# (out of 84 telescopes total)
EventSource:
  allowed_tels: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 19, 35]

```

Since the comparison of the cleaning algorithms also required differentiating between Medium-Sized Telescopes (MSTs) and Large-Sized Telescopes (LSTs), the following two listings show the contents of the `prod5b_lapalma_mst.yml` and `prod5b_lapalma_lst.yml` configuration files, respectively:

MSTs:

```

# telescope ids of the 9 MST of the La Palma alpha configuration
# in Prod5b
EventSource:
  allowed_tels: [5, 6, 7, 8, 9, 10, 11, 19, 35]

```

LSTs:

```

# telescope ids of the 4 LST of the La Palma alpha configuration
# in Prod5b
EventSource:
  allowed_tels: [1,2,3,4]

```

2 Hyperparameters

The following table shows the subsets of hyperparameters used in the grid search:

Table 1: Hyperparameters for the cleaning algorithms used in the grid search. The picture quantiles determine what percent of all pixels per event will be below the core threshold Q_c . The boundary threshold is calculated by multiplying the core threshold by the boundary threshold ratio. The time limit t is the parameter for FACT, while the time limits t_c and t_b are the time limits for TCC.

Picture Quantiles	Boundary Threshold Ratio	Minimum Neighbors	t / ns	t_c / ns	t_b / ns
0.995	0.25	1	1.0	9.0	4.5
0.999	0.33	2	2.0	12.0	9.0
0.9992	0.5	3	4.0	15.0	12.0
0.9995	0.66	4	5.0	18.0	15.0
0.9997	0.75	5	6.0	20.0	
0.9999			10.0		
			12.0		

3 Software used

This work was written and built with L^AT_EX and LuaT_EX from TeXLive 2021 on both the Windows Subsystem for Linux (WSL, Ubuntu 20.04) on Windows 10 and Ubuntu 20.04. Also, I relied heavily on the python programming language, of which the most important libraries used for this work are listed below.

- numpy [20]
- pandas [31]
- matplotlib [10]
- astropy [6, 7]
- pyirf [27]
- scikit-learn [28]

For the processing of the datasets, I used the development version of ctapipe, more specifically, version 0.15.1.dev166+gf26107f. A complete listing of all used python libraries can be found below:

```

name: cta-dev
channels:
- anaconda
- defaults
- conda-forge
dependencies:
- sphinx_rtd_theme=1.0.0
- sphinx=3.5.4
- jupyter=1.0.0
- matplotlib=3.5.1
- iminuit=2.11.2
- tqdm=4.64.0
- traitlets=5.1.1
- joblib=1.1.0
- sphinx-autodocapi=0.14.1
- pytest-runner=6.0.0
- pytables=3.7.0
- tomli=2.0.1
- psutil=5.9.0
- pytest-cov=3.0.0
- python=3.8.13
- pyyaml=6.0
- numba=0.55.1
- pytest=7.1.2
- pip=22.0.4
- jinja2=3.0.3
- xz=5.2.5
- nbsphinx=0.8.8
- scipy=1.8.0
- cython=0.29.28
- eventio=1.9.1
- pandas=1.4.2
- zlib=1.2.11
- black=22.3.0
- h5py=3.6.0
- numpydoc=1.2.1
- vitables=3.0.2
- wheel=0.37.1
- ipywidgets=7.7.0
- scikit-learn=1.0.2
- graphviz=3.0.0
- bokeh=2.4.2
- zstandard=0.17.0
- pre-commit=2.18.1
- numpy=1.21.6
- astropy=5.0.4
- setuptools=62.1.0
- ipython=8.2.0
- jupyterlab=3.3.4
- seaborn=0.11.2
- ipympl=0.9.1
- ca-certificates=2022.6.15
- certifi=2022.6.15
- openssl=3.0.5
- gammamap=0.20
- pylint=2.14.3
- ctapipe=0.15.1
- colour=0.1.5
- flake8=4.0.1
- pip:
  - pyirf==0.7.0
  - pytimedinput==2.0.1
  - runipy==0.1.5
  - setuptools-scm==6.4.2

```

4 Additional plots and tables

4.1 Metrics

Table 2 below shows the metrics used in this work as well as their formulas. Also shown is a confusion matrix for a binary (positive/negative) classification problem.

Table 2: The metrics used for this works analysis as well as their calculation. Right: Confusion matrix for a binary (positive/negative) classification.

Metric	Calculation	Prediction			
		positive	negative		
Label	pos.	True Positive (tp)	False Negative (fn)	neg.	True Negative (tn)
True Positive Rate (TPR)	$\frac{tp}{tp + fn}$				
True Negative Rate (TNR)	$\frac{tn}{tn + fp}$				
False Negative Rate (FNR)	$\frac{fn}{tp + fn}$				
Accuracy (ACC)	$\frac{tp + tn}{tp + fp + tn + fn}$				
Balanced Accuracy (BA)	$\frac{tp + tn}{2}$				

4.2 A comparison of the last steps of the cleaning algorithms

Figure 1 below shows the last steps of the cleaning algorithms Tailcuts, MARS, FACT and TCC for the default parameters set in `ctapipe`.

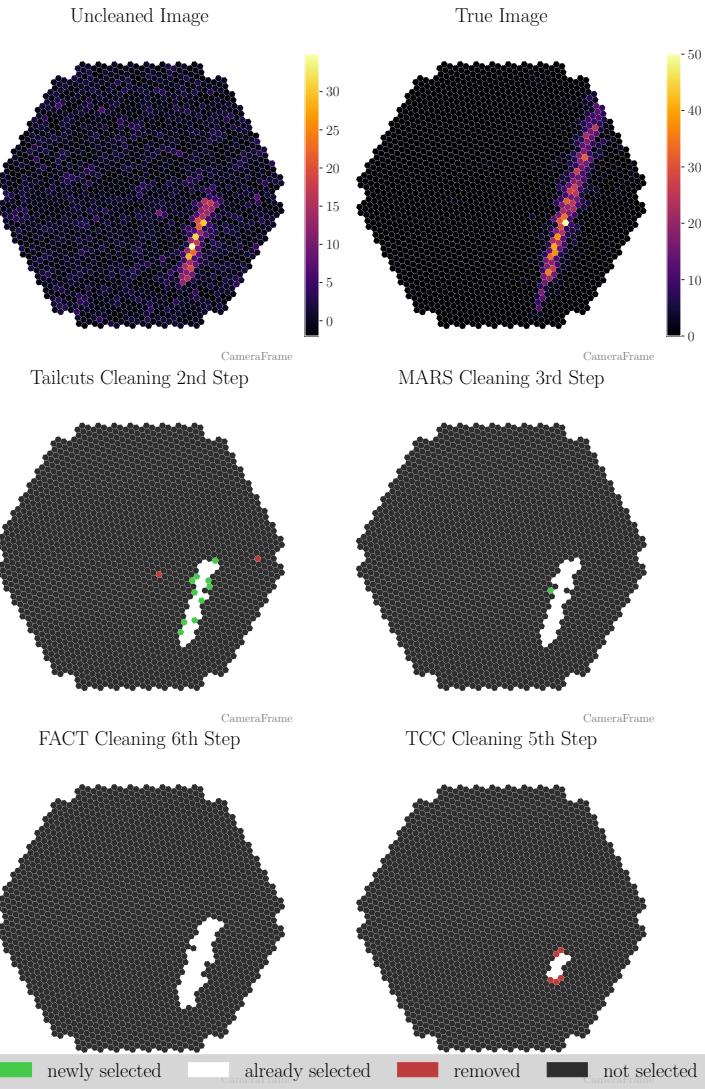


Figure 1: The last steps of the cleaning algorithms Tailcuts, MARS, FACT and TCC for the default parameters set in `ctapipe`. Also shown are the uncleaned image and the true image for better comparison.