

Chapter = 02

Presentation of Data.

- * Frequency distribution :- A mass of statistical data in its original form \rightarrow Raw Data / ungrouped data
- * F.D is a classification according to the no. of processing the same values of the variables. It is simply a table in which data are grouped into classes & the no. of cases which fall in each class is recorded. The no. \rightarrow Frequencies.
They are 2 type \rightarrow
- 1) Discrete Freq D = If we have a large no. of items in the data, it is better to prepare a freq array. It contains the data further. Freq array is prepared by listing once & consequently all the values occurring in the series & not in the no. of times each such value occurs.

e.g. - 1, 4, 3, 2, 1, 2, 0, 2, 1, 2, 3, 2

1, 0, 2, 3, 0, 3, 2, 1, 2, 2, 1, 4, 2

Data	Freq.
0	3
1	6
2	10
3	4
4	2

- 3) Continuous freq. D :- Here the data are classified according to class intervals.
 - following are the rules for forming a freq. table
 i) note the difference b/w largest & smallest value in the given set of observations.
 ii) determine the no. of classes into which difference can be divided.
 iii) classes should be exclusive.
 iv) 3 ~~st~~ columns \rightarrow classes, tally mark & freq.
 v) write class in 1st column.
 vi) put tally marks
 vii) write sum of tally marks of each class.
 viii) sum of freq of all classes = No. of observations.
- \rightarrow Concepts of freq. table :-
- 1) class limits = observations which constitute a class \rightarrow c.limits.
 left hand side observation \rightarrow lower limit
 right " " \rightarrow upper limit
- 2) working class = classes of form 0-9, 10-19, 20-29, ...
 \rightarrow w.cls. / nominal cls.
- 3) Actual cls = If we're leaving either the upper limit / lower limit from each cls \rightarrow exclusive method of classification.
 - we can convert w.cls to Actual cls \rightarrow
- a) note the difference one w.cls \rightarrow the next 1. limit.
 b) \div the difference by 2.

c) Extract that value from L. limit & + same to U. limits.

d) Class boundaries = cls. limits of actual cls \rightarrow C-boundaries (fractional cls. limits)
class mark = Avg of U. limit & L. limit of that cls \rightarrow c.mark / mid values.

e) Class interval = Difference b/w U. limit & L. limit of actual cls.

f) Tally Sheet or entry form = In freq. table, freq are noted by a stroke.

\rightarrow Cumulative Frequency Distribution :-

No. many observations are lying below / above a particular value / in b/w 2 specified values \rightarrow c.freq.
 we get less c.f & c.f \rightarrow greater c.f ($>c.f$)
 c.f give no. of observations falling below the upper limit of a cls & $>c.f \rightarrow$ no. of observations lying above L. limit of cls.
 $<c.f \rightarrow$ + freq of all previous classes.

cls	F	BL	$>c.f$	UL	$<c.f$	
0-10	2	10	2	0	$3+7+10+8+5+2$	35
10-20	5	20	7	10	$7+10+8+5+3$	33
20-30	8	30	15	20	$10+8+5+3$	28
30-40	10	40	25	30	10+7+3	20
40-50	7	50	25	58	$2+5+8+10+7$	32
50-60	3	60	25	58+3	$2+5+8+10+7+3$	35
						3

→ graphical presentation of data :-

2 types of graphs →

i) Frequency distribution ii) Time Series.

- iii) Graph of freq distributions :-
- iv) Histogram :- It has adjacent bars \square erected on X axis. Depending on size of class interval - equal or unequal.

v) If class intervals are not equal on X axis & on Y axis take the freq. Now over each class erect a rectangle whose lengths are proportional to corresponding freq.

It enables the location of mode freq equal class intervals.

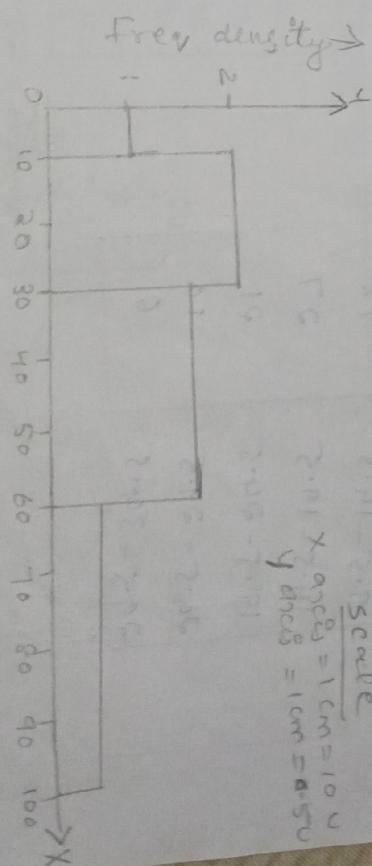
e.g. construct a histogram -

$15 \rightarrow 0-10 \quad 10-20 \quad 20-30 \quad 30-40 \quad 40-50 \quad 50-60$

freq $\rightarrow 4 \quad 10 \quad 21 \quad 9 \quad 4 \quad 2$.

A]

Scale
 $X \text{ axis} = 1 \text{ cm} = 10 \text{ units}$
 $Y \text{ axis} = 1 \text{ cm} = 5 \text{ units}$



classes	freq	f/c.
0-10	10	1 (one)
10-20	40	2 (two)
20-30	45	1.5
30-40	9	0.5
40-50	2	
50-60	1	

classes

classes	freq	f/c.
0-10	10	1 (one)
10-20	40	2 (two)
20-30	45	1.5
30-40	9	0.5
40-50	2	
50-60	1	

scale

$$1 \text{ cm} = 10 \text{ units}$$

$$1 \text{ cm} = 5 \text{ units}$$

classes

(ii) On equal class intervals :- class interval

determine the base of \square . i.e. the height of bars are determined by class densities.

A class density (freq density) is the ratio of class freq to its class interval $\rightarrow \frac{\text{freq}}{\text{class}}$

e.g. construct a histogram.

$$\begin{array}{|c|c|c|c|c|} \hline \text{class} & 0-10 & 10-20 & 20-30 & 30-40 \\ \hline \text{freq} & 10 & 40 & 45 & 9 \\ \hline \end{array}$$

classes

(b) Freq polygon :- It can be constructed by drawing the histogram. If we join the top of \square of histogram using straight line. Freq polygon can be drawn by

consecutive points of x & y joining consecutive points of x & y can be drawn to form a frequency polygon, but it cannot be drawn on the same graph, but histograms cannot.

Not equal intervals

- construct a frequency curve :- The method of drawing frequency curve is similar to the construction of frequency polygon.
- 1st construct the histogram. Then join the mid points & the top of the histogram using a smooth curve by free hand method.

) construct a frequency curve

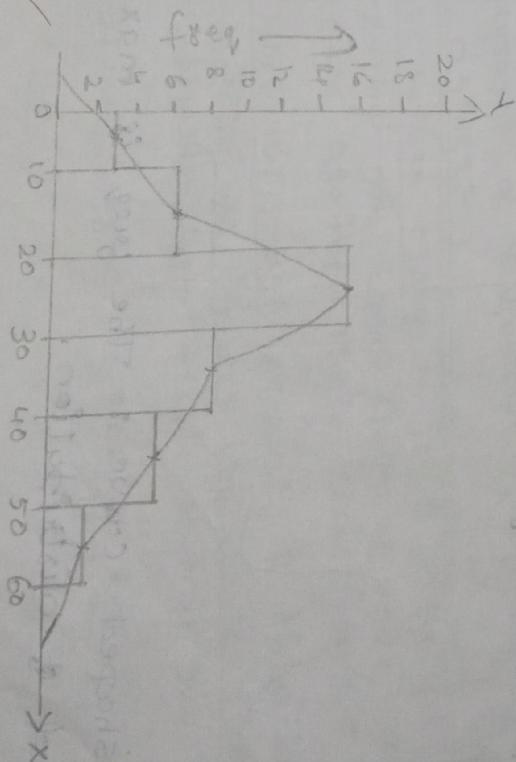
cls	freq
0-10	3
10-20	6
20-30	15
30-40	9
40-50	7
50-60	2

cls	freq
5-9	8
10-14	18
15-19	27
20-24	21
25-29	10
30-34	6

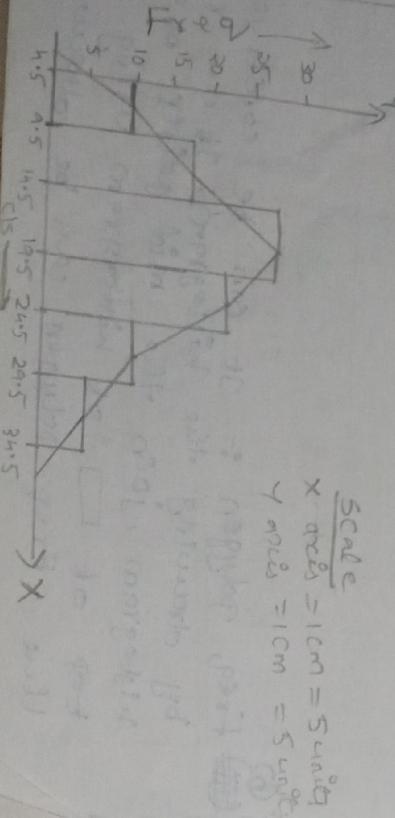
A)

cls	freq
4.5-9.5	8
9.5-14.5	18
14.5-19.5	27
19.5-24.5	21
24.5-29.5	10
29.5-34.5	6

Scale
 x scale = 1 cm = 5 units
 y scale = 1 cm = 5 units

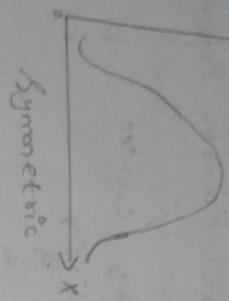


cls →



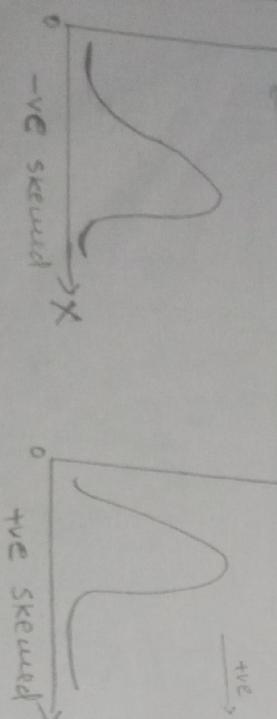
→ Different shapes of freq. curve :-

a) Symmetrical distribution :- freq. uses equally on either side of the central value during the max freq.

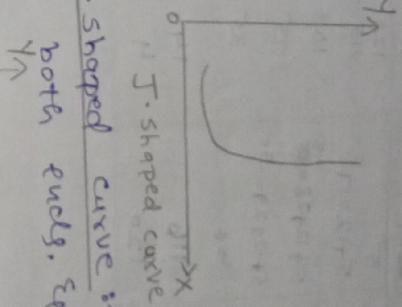


b) Moderate skewed / slightly Asymmetrical distri:-

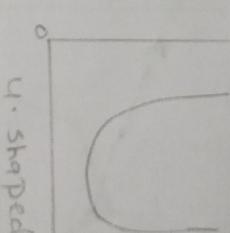
The rate of use of frequencies on 1 side at the max value is huge than the corresponding rate on the other side.



c) J-shaped curve :- The freq. is max at both ends. e.g. min at centre.



d) U-shaped curve :- The freq. is max at both ends. e.g. min at centre.



e) Graphs of cumulative freq. distribution / Ogives :-

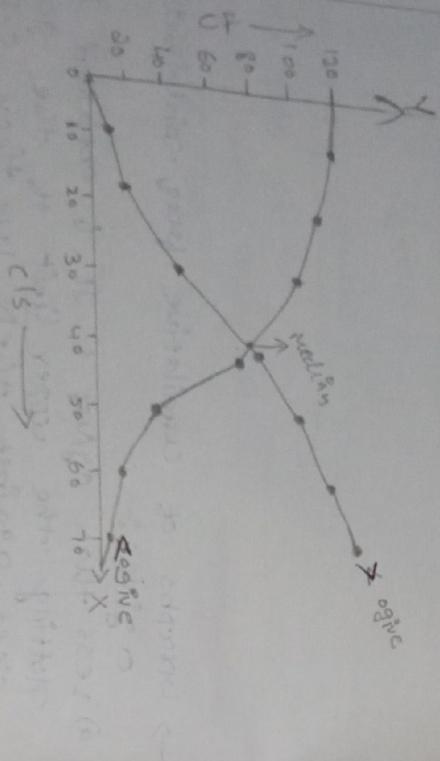
a) Less than ogive :- It is obtained by plotting the upper limit of the actual classes against their less than C.F.

b) More than ogive :- It is obtained by plotting the lower limit of the actual classes against their >C.F.

c) Draw < ogive & > ogive for the data.

c) J-shaped curve :- The freq. is max at both ends of distribution.

	OGIVE	CDF ($F(x)$)	CCF ($(1-F)$)
0-10	5	5	120 115 (approx)
10-20	12	5+12=17	103
20-30	28	5+12+28=45	75
30-40	40	59+24=83	35
40-50	21	106	
50-60	10	116	
60-70	4	120	



Note :-
ogives for more than 50 less than type
distribution intersect at median

→ Graph of Time Series :- It is a set of values of a variable collected & recorded in chronological order (i.e. base) & time intervals, i.e. the data depending on time.
It is also called historical Series.

Plot the time values against the corresponding values in Jain & Rao points by a smooth line → Time Series graph by a moving average.

Draw a time series graph.

Given : 1991 1992 1993 1994 1995 1996 1997
1998 : 100 98 96 94 92 90 92
1999 : 80 90 92 83 94 99 92

