

*Unassigned, but suggested: Problems 1, 10, 13, 17, 20 in Section 0.3*

*Unassigned, but suggested: Problems 2, 3, 5, 6, 9 in Section 1.1*

### 1.1 Problem 0.3.3

Finish the proof of Proposition 0.3.15.

*Solution.*



### 1.2 Problem 0.3.4

a) Prove Proposition 0.3.16.

*Solution.*



b) Find an example for which equality of sets in  $f(C \cap D) \subset f(C) \cap f(D)$  fails. That is, find an  $f$ ,  $A$ ,  $B$ ,  $C$ , and  $D$  such that  $f(C \cap D)$  is a proper subset of  $f(C) \cap f(D)$ .

*Solution.*



### 1.3 Problem 0.3.16

Find the smallest  $n \in \mathbb{N}$  such that  $2(n+5)^2 < n^3$  and call it  $n_0$ . Show that  $2(n+5)^2 < n^3$  for all  $n \geq n_0$ .

*Solution.*



### 1.4 Problem 1.1.1

Prove part (iii) of Proposition 1.1.8.

*Solution.*



### 1.5 Problem 1.1.4

Let  $S$  be an ordered set. Let  $B \subset S$  be bounded (above and below). Let  $A \subset B$  be a nonempty subset. Suppose all the inf's and sup's exist. Show that

$$\inf B \leq \inf A \leq \sup A \leq \sup B.$$

*Solution.*

