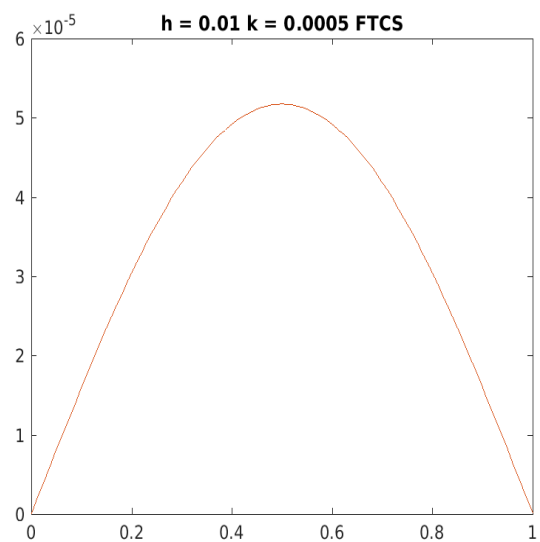


# MA-473 Computational Finance Assignment 1

-Aman Kumar  
200123007

## Question 1

a) **Forward-time and central space (FTCS) discretization scheme** plots look like this -



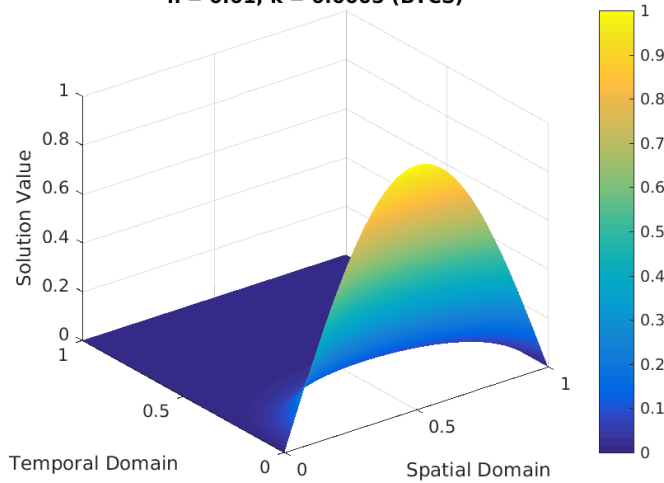
Note – Here the Orange Line in the second plot is of the actual solution and not that of FTCS.

This is because FTCS requires  $dt/dx^2 < 0.5$  for stability whereas in the question we are provided with values of  $dt$  and  $dx$  which results in ratios above 5. Therefore all the FTCS solutions calculated are inaccurate.

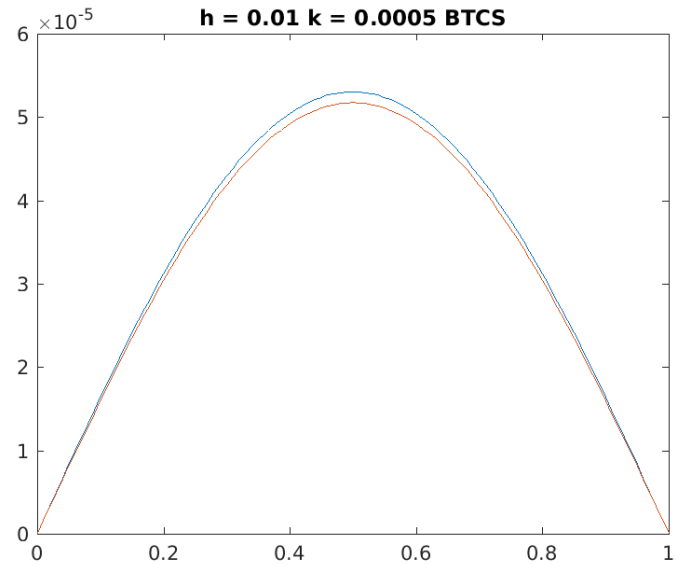
## b) Backward-time and central space (BTCS) discretization scheme

The plots are -

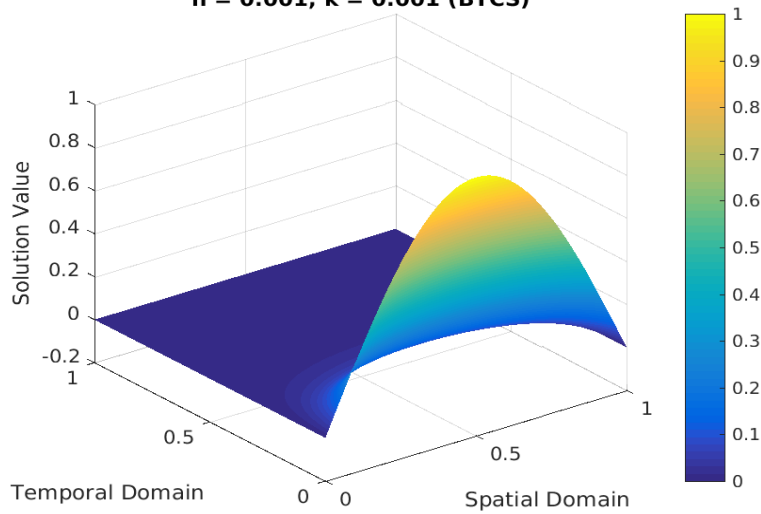
**$h = 0.01, k = 0.0005$  (BTCS)**



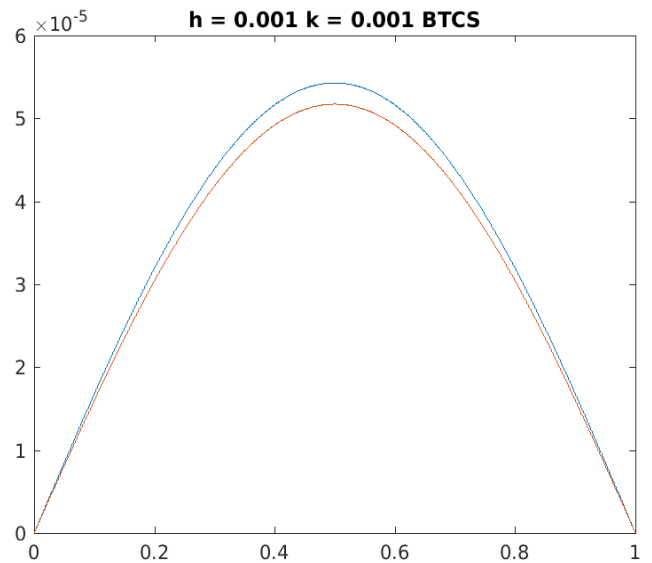
**$h = 0.01, k = 0.0005$  BTCS**



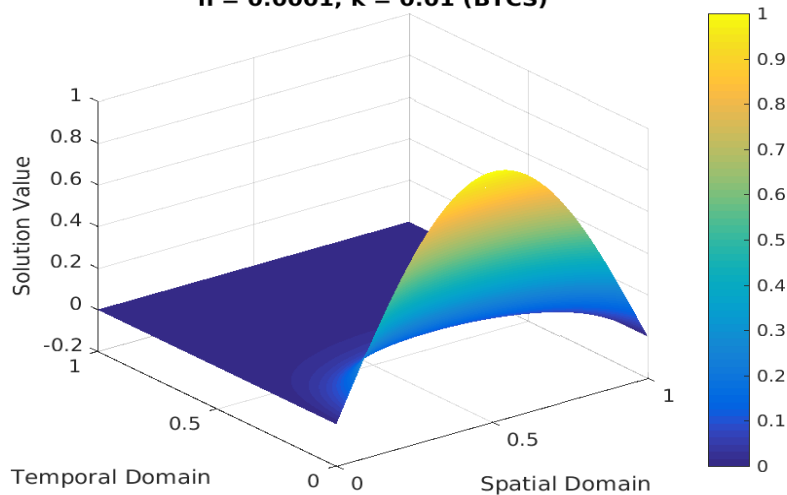
**$h = 0.001, k = 0.001$  (BTCS)**



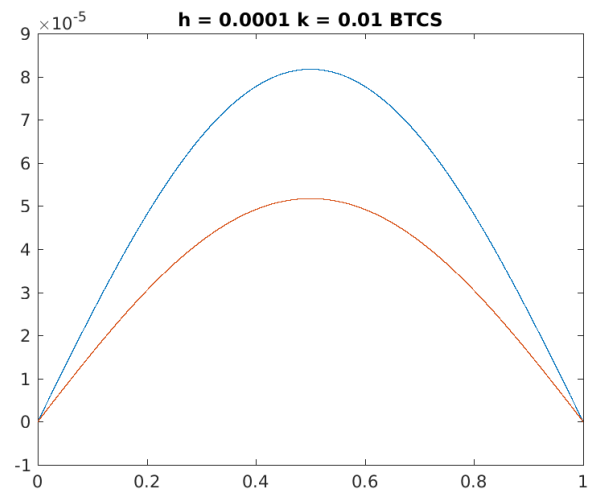
**$h = 0.001, k = 0.001$  BTCS**



**$h = 0.0001, k = 0.01$  (BTCS)**

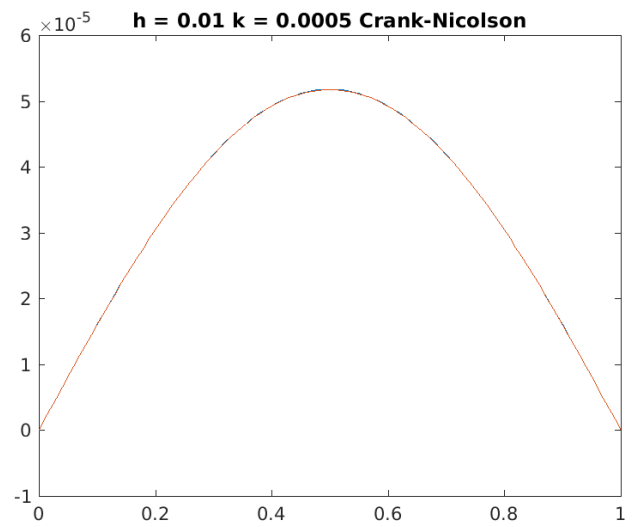
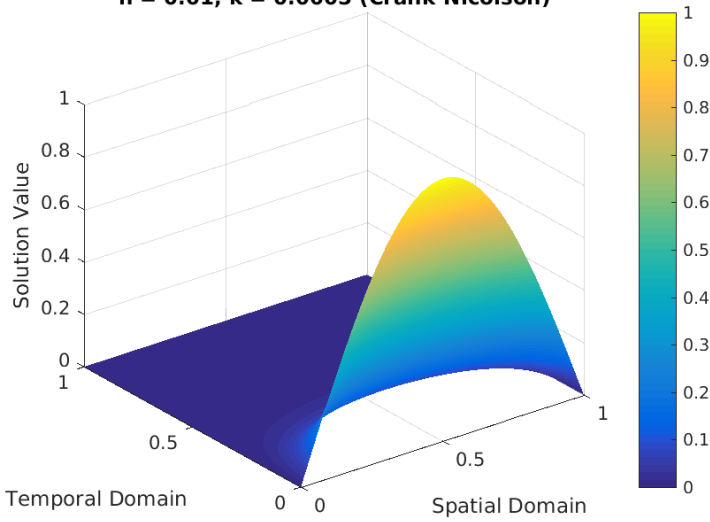


**$h = 0.0001, k = 0.01$  BTCS**

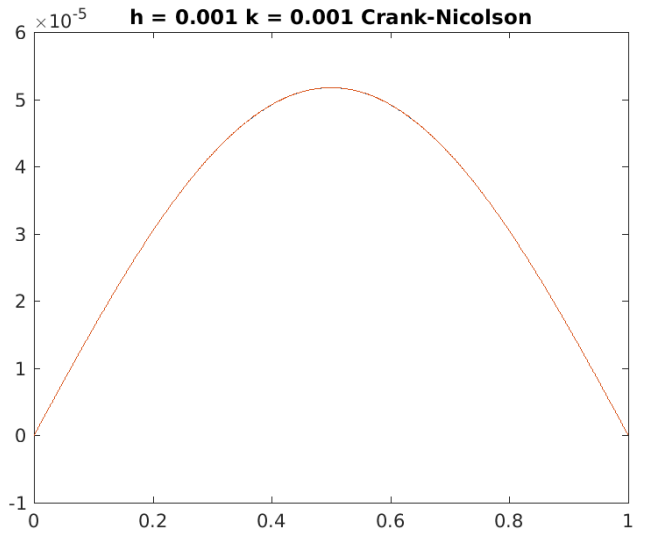
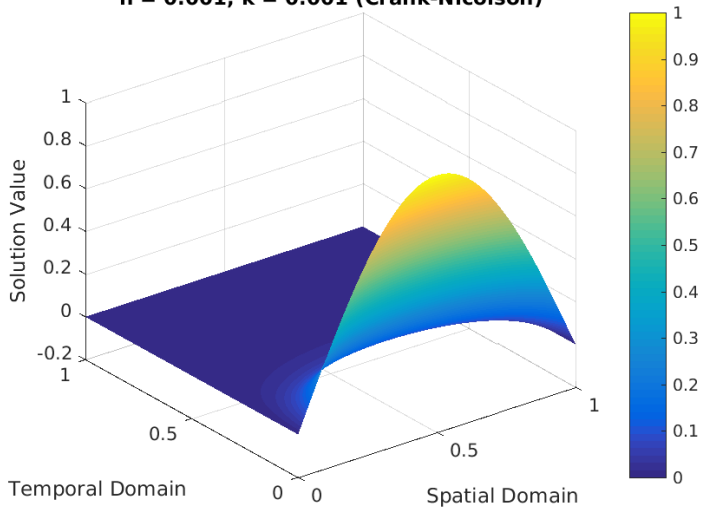


### c) Crank–Nicolson scheme

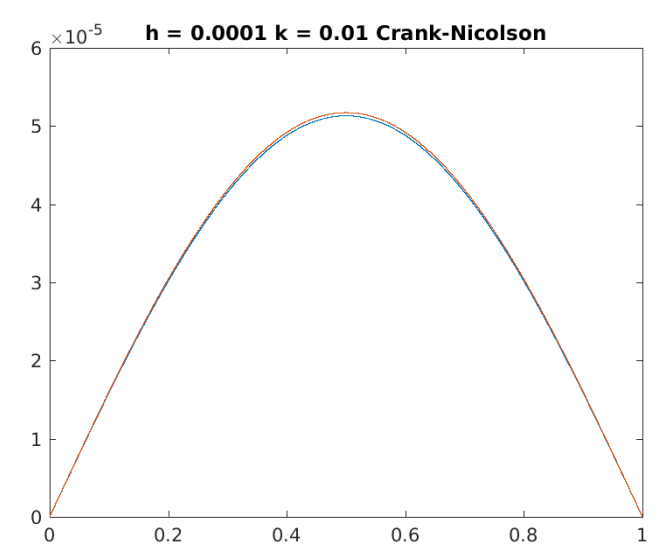
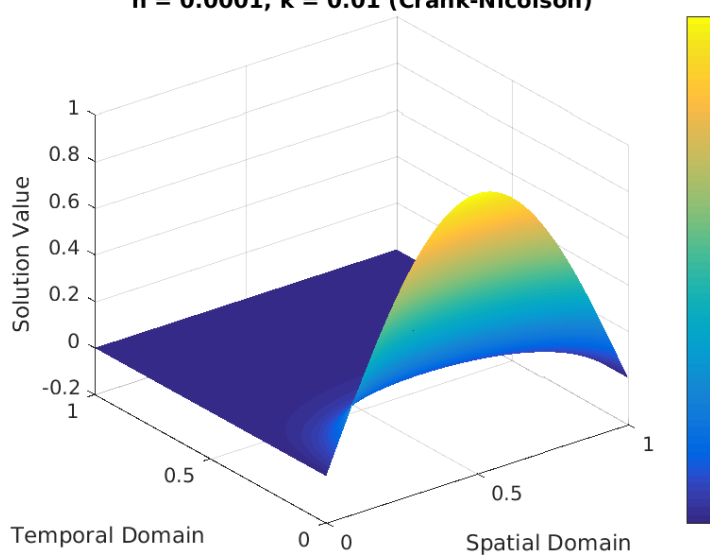
**$h = 0.01, k = 0.0005$  (Crank-Nicolson)**



**$h = 0.001, k = 0.001$  (Crank-Nicolson)**



**$h = 0.0001, k = 0.01$  (Crank-Nicolson)**



**Observation -**

The BTCS plots are close to the actual solution but the plots of CN literally overlaps with the actual solution. For FTCS the given parameters were not good enough to get a stable solution.