

lab1

August 24, 2020

```
[1]: import numpy as np
import matplotlib as mpl
import matplotlib.pyplot as plt
plt.style.use('seaborn-whitegrid')
pi = np.pi

def createSubplot(n):
    fig, ax = plt.subplots(n, figsize=(10, 10))
    fig.tight_layout(pad=3.0)
    return fig, ax
```

1 1 Generating Singnal

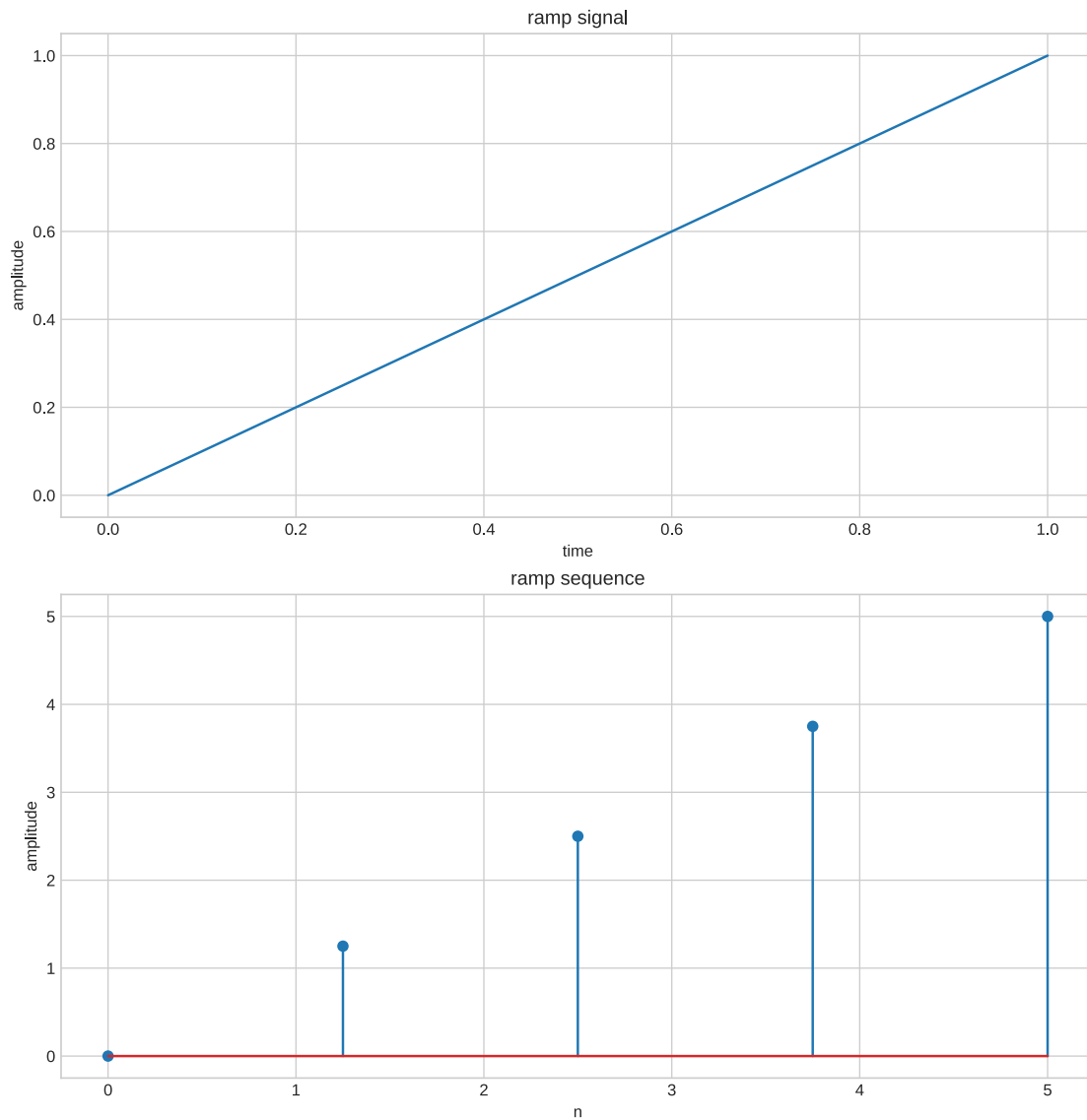
1.1 Ramp signal and Sequence

```
[2]: def ramp(t):
    return t

fs = 5
t = np.linspace(0, 1, fs)
# print(t.shape) #(5,)
fig, ax = createSubplot(2)
ramp_signal = ramp(t)
ax[0].plot(t, ramp_signal)
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('ramp signal')

n = np.linspace(0, fs, fs)
ramp_seq = ramp(n)
ax[1].stem(n, ramp_seq)
ax[1].set_xlabel('n')
ax[1].set_ylabel('amplitude')
ax[1].set_title('ramp sequence')
```

```
[2]: Text(0.5, 1.0, 'ramp sequence')
```



1.2 Impulse signal and Impulse sequence

```
[3]: def impulse(t):
    sig = np.zeros(len(t))
    sig[0] = 1
    return sig

fs = 100
t = np.linspace(0,1,fs)

fig, ax = createSubplot(2)
impulse_signal = impulse(t)
```

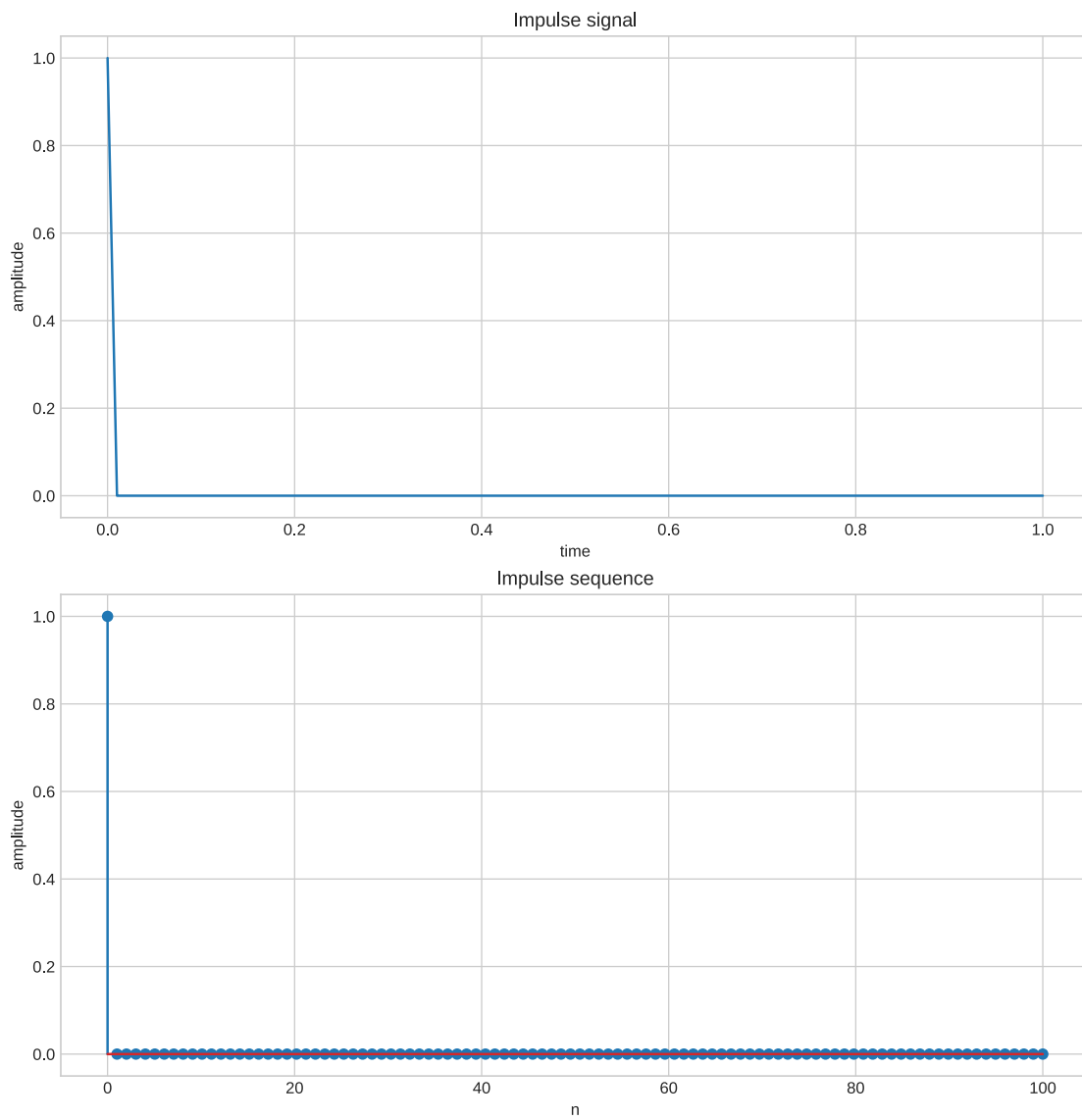
```

ax[0].plot(t,impulse_signal)
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('Impulse signal')

n = np.linspace(0,fs,fs)
impulse_seq = impulse(n)
ax[1].stem(n,impulse_seq)
ax[1].set_xlabel('n')
ax[1].set_ylabel('amplitude')
ax[1].set_title('Impulse sequence')

```

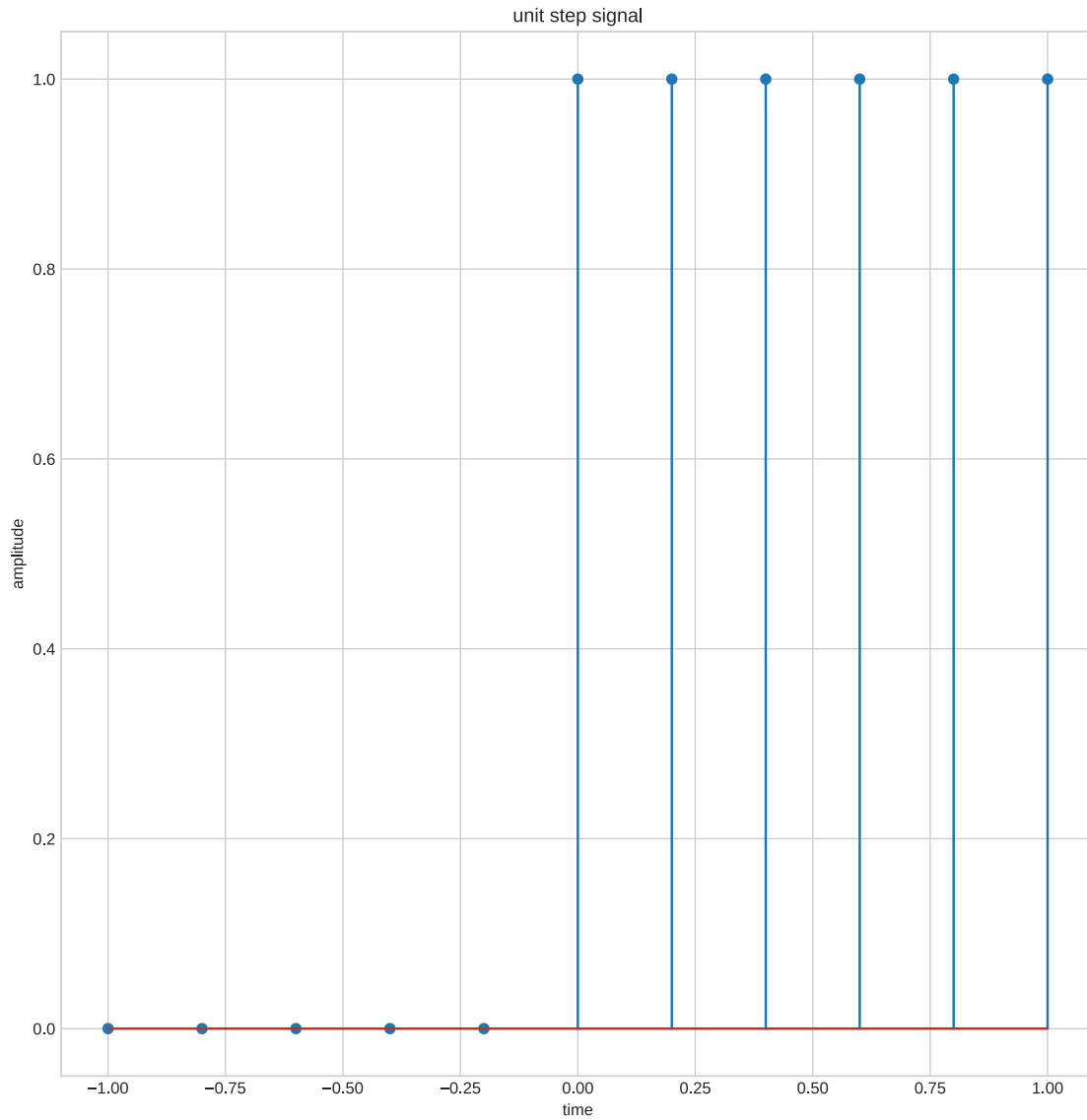
[3]: Text(0.5, 1.0, 'Impulse sequence')



1.3 unit step signal

```
[4]: def unit(t):  
    # sig = np.concatenate(np.zeros(len(t)//2),np.ones(len(t)//2))  
    s = t.copy()  
    s[s>=0] = 1  
    s[s<0] = 0  
    return s  
  
fs = 5  
t = np.linspace(-1,1,(fs*2)+1)  
  
fig, ax = createSubplot(1)  
unit_signal = unit(t)  
ax.stem(t,unit_signal)  
ax.set_xlabel('time')  
ax.set_ylabel('amplitude')  
ax.set_title('unit step signal')
```

```
[4]: Text(0.5, 1.0, 'unit step signal')
```



1.4 square wave signal and square wave sequence

```
[5]: from scipy import signal
def square(t,f):
    return signal.square(2 * pi * f * t)
    # s = t.copy()
    # T = 1/f
    # s[s%T < T/2] = 1
    # s[s%T > T/2] = 0
    # return s
```

```

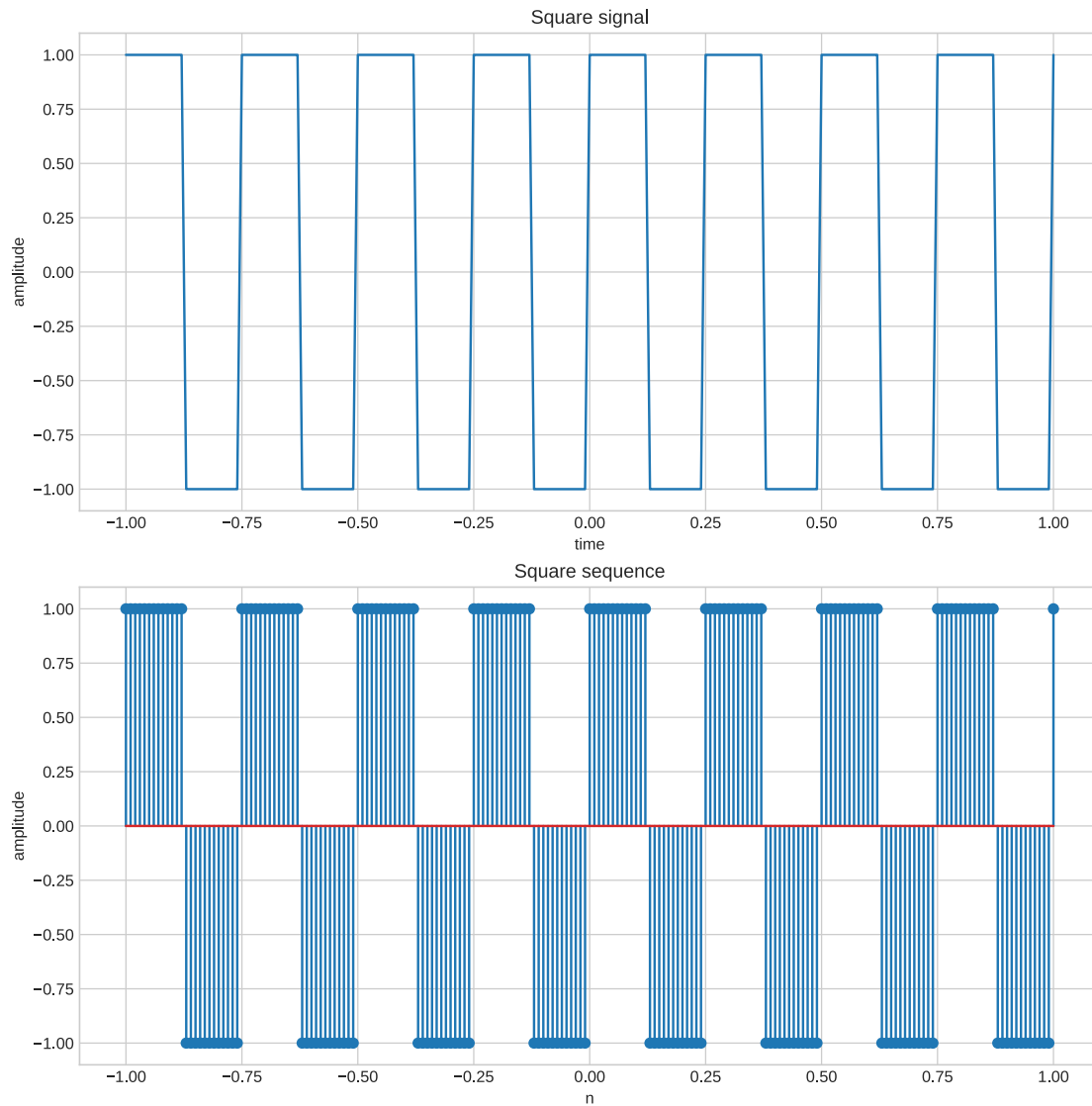
f = 4 #Hz
fs = 100
t = np.linspace(-1,1,(fs*2)+1)

fig, ax = createSubplot(2)
square_signal = square(t,f)
ax[0].plot(t,square_signal)
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('Square signal')

ax[1].stem(t,square_signal)
ax[1].set_xlabel('n')
ax[1].set_ylabel('amplitude')
ax[1].set_title('Square sequence')

```

```
[5]: Text(0.5, 1.0, 'Square sequence')
```



1.5 saw tooth signal and saw tooth sequence

```
[6]: def saw(t,f):
    s = t.copy()
    T = 1/f
    s[s%T < T] = s[s%T < T]%(T)
    return s

f = 4 #Hz
fs = 100
t = np.linspace(-1,1,(fs*2)+1)
```

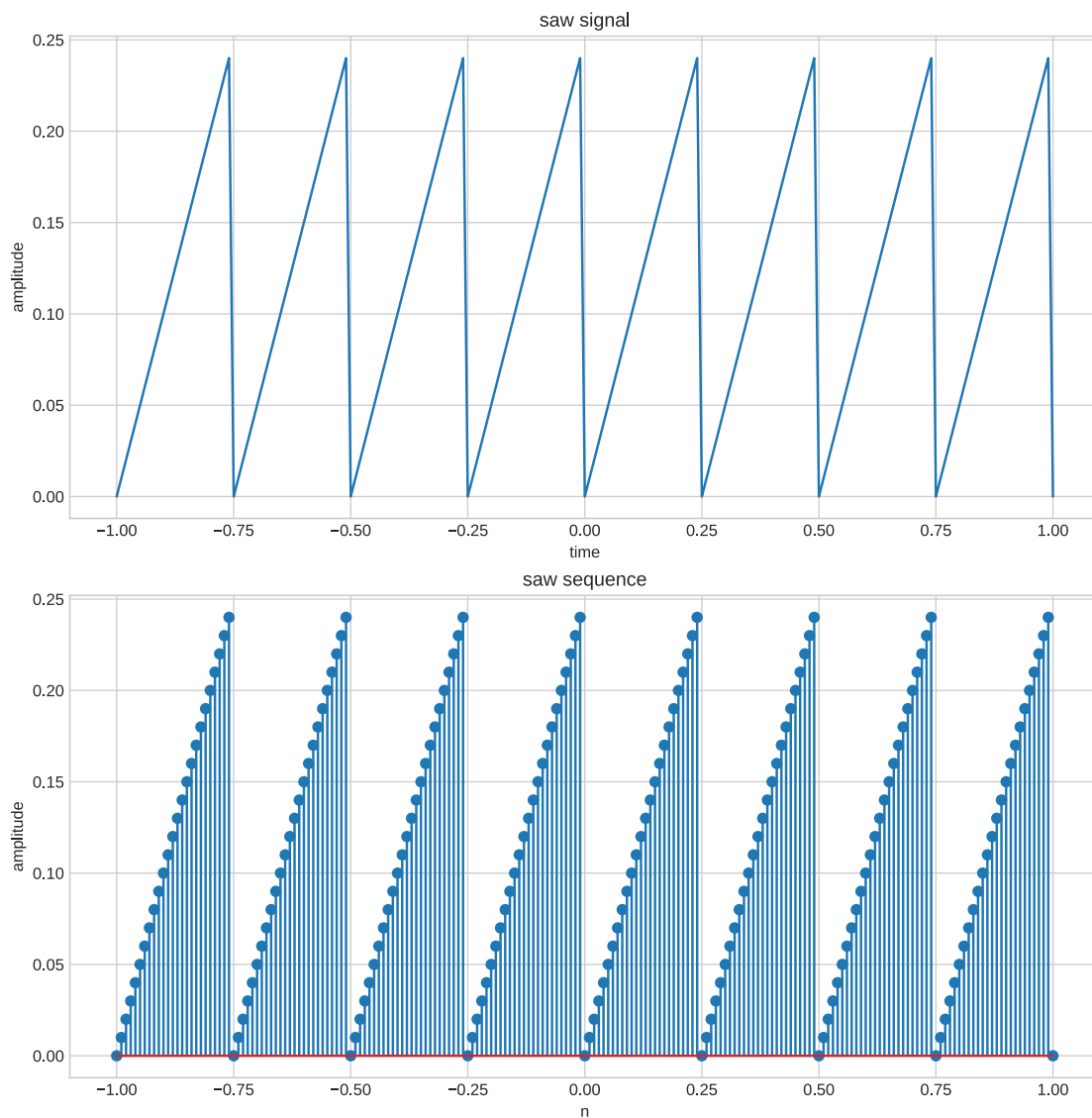
```

fig, ax = createSubplot(2)
saw_signal = saw(t,f)
ax[0].plot(t,saw_signal)
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('saw signal')

ax[1].stem(t,saw_signal)
ax[1].set_xlabel('n')
ax[1].set_ylabel('amplitude')
ax[1].set_title('saw sequence')

```

[6]: Text(0.5, 1.0, 'saw sequence')

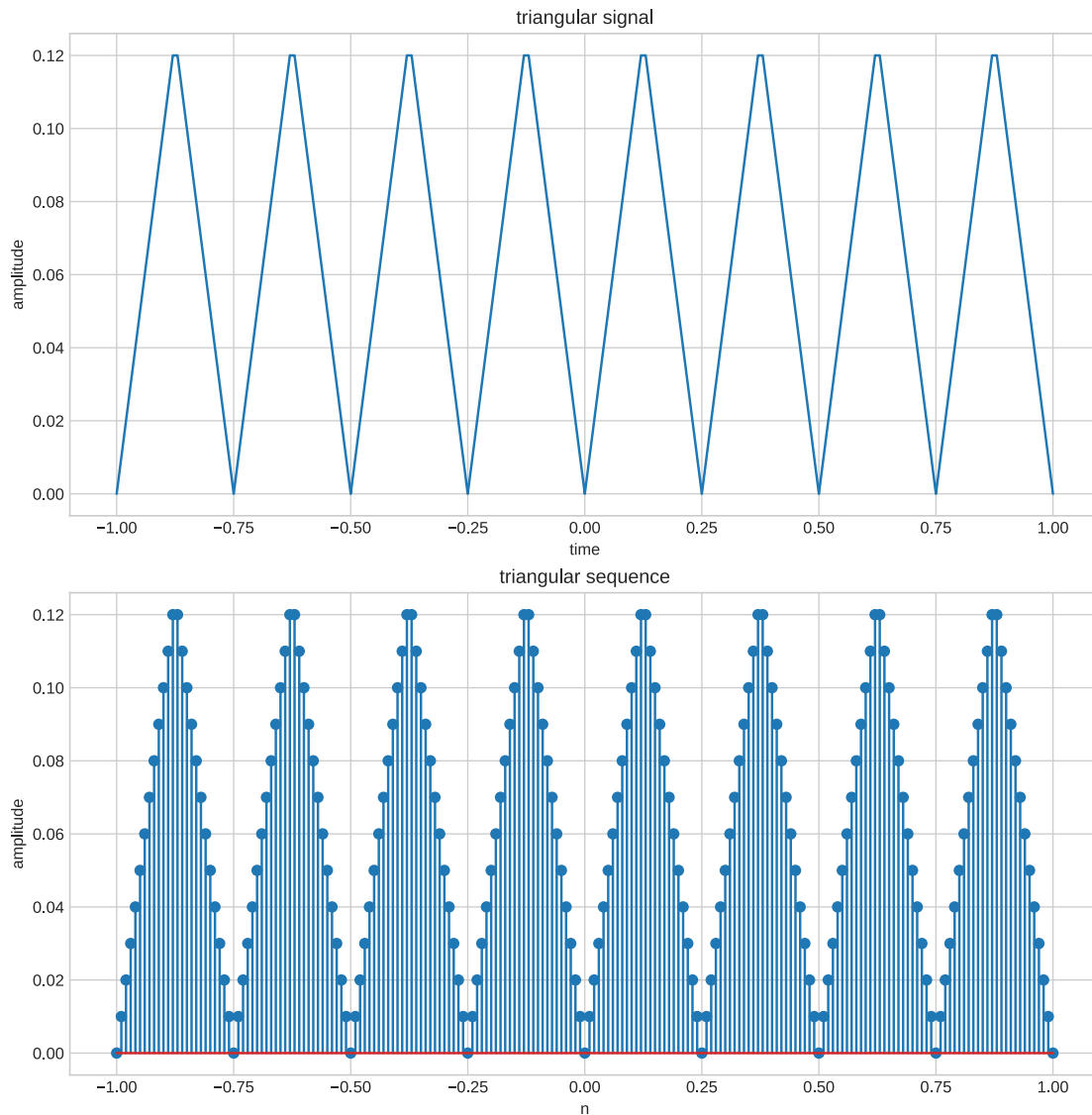


1.6 triangular signal and triangular sequence

```
[7]: def triangular(t,f):  
    s = t.copy()  
    T = 1/f  
    s[s%T < T/2] = s[s%T < T/2]%(T/2)  
    s[s%T > T/2] = (T/2) - s[s%T > T/2]%(T/2)  
    return s
```

```
f = 4 #Hz  
fs = 100  
t = np.linspace(-1,1,(fs*2)+1)  
  
fig, ax = createSubplot(2)  
triangular_signal = triangular(t,f)  
ax[0].plot(t,triangular_signal)  
ax[0].set_xlabel('time')  
ax[0].set_ylabel('amplitude')  
ax[0].set_title('triangular signal')  
  
ax[1].stem(t,triangular_signal)  
ax[1].set_xlabel('n')  
ax[1].set_ylabel('amplitude')  
ax[1].set_title('triangular sequence')
```

```
[7]: Text(0.5, 1.0, 'triangular sequence')
```



1.7 sinusoidal wave signal and sinusoidal wave sequence

```
[8]: def sinusodial(t,f):
    s = t.copy()
    T = 1/f
    s = np.sin(t * pi * f * 2)
    return s

f = 4 #Hz
fs = 100
t = np.linspace(-1,1,(fs*2)+1)
```

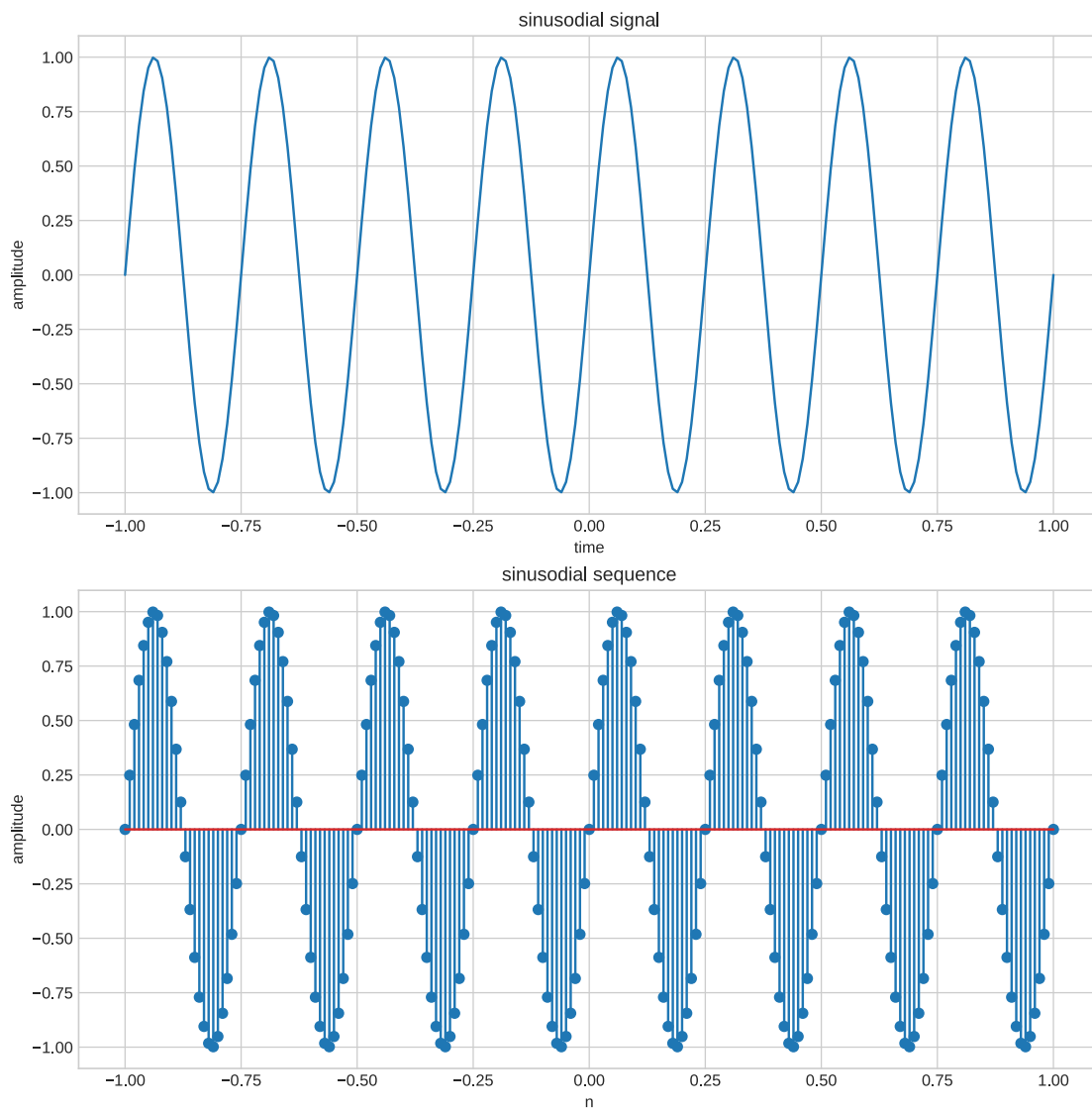
```

fig, ax = createSubplot(2)
sinusodial_signal = sinusodial(t,f)
ax[0].plot(t,sinusodial_signal)
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('sinusodial signal')

ax[1].stem(t,sinusodial_signal)
ax[1].set_xlabel('n')
ax[1].set_ylabel('amplitude')
ax[1].set_title('sinusodial sequence')

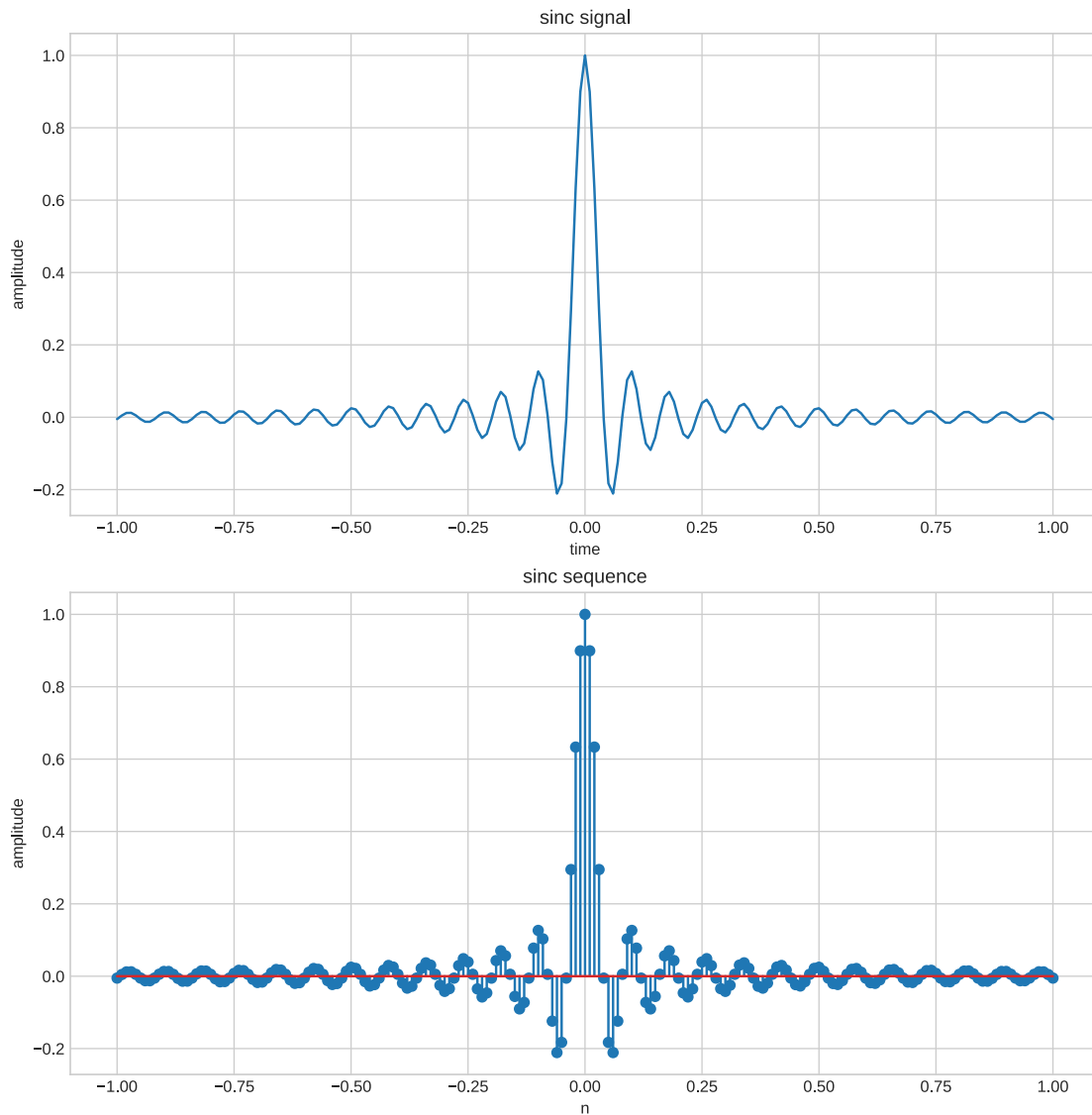
```

[8]: Text(0.5, 1.0, 'sinusodial sequence')



1.8 sinc signal and sinc sequence

```
[9]: def sinc(t,f):  
    s = t.copy()  
    T = 1/f  
    s = np.sinc(t * pi * f * 2)  
    return s  
  
f = 4 #Hz  
fs = 100  
t = np.linspace(-1,1,(fs*2)+1)  
  
fig, ax = createSubplot(2)  
sinc_signal = sinc(t,f)  
ax[0].plot(t,sinc_signal)  
ax[0].set_xlabel('time')  
ax[0].set_ylabel('amplitude')  
ax[0].set_title('sinc signal')  
  
ax[1].stem(t,sinc_signal)  
ax[1].set_xlabel('n')  
ax[1].set_ylabel('amplitude')  
ax[1].set_title('sinc sequence')  
  
[9]: Text(0.5, 1.0, 'sinc sequence')
```



2 2 Operations on a continuous signal

```
[10]: # 1. Generate two sine waves with frequency 4Hz and 8Hz from the below signal
      ↪ in Matlab
      # for 0 to 1s with 0.01 increments and plot both of them.  $A = \sin(2\pi f t)$ 
      fs = 100
      t = np.linspace(0,1,fs)
      s1 = np.sin(t * 2 * pi * 4) #4Hz
      s2 = np.sin(t * 2 * pi * 8) #8Hz
      fig, ax = createSubplot(4)
      ax[0].plot(t,s1, color='blue')
```

```

ax[0].plot(t,s2, color='red')
ax[0].set_xlabel('time')
ax[0].set_ylabel('amplitude')
ax[0].set_title('4Hz and 8Hz')

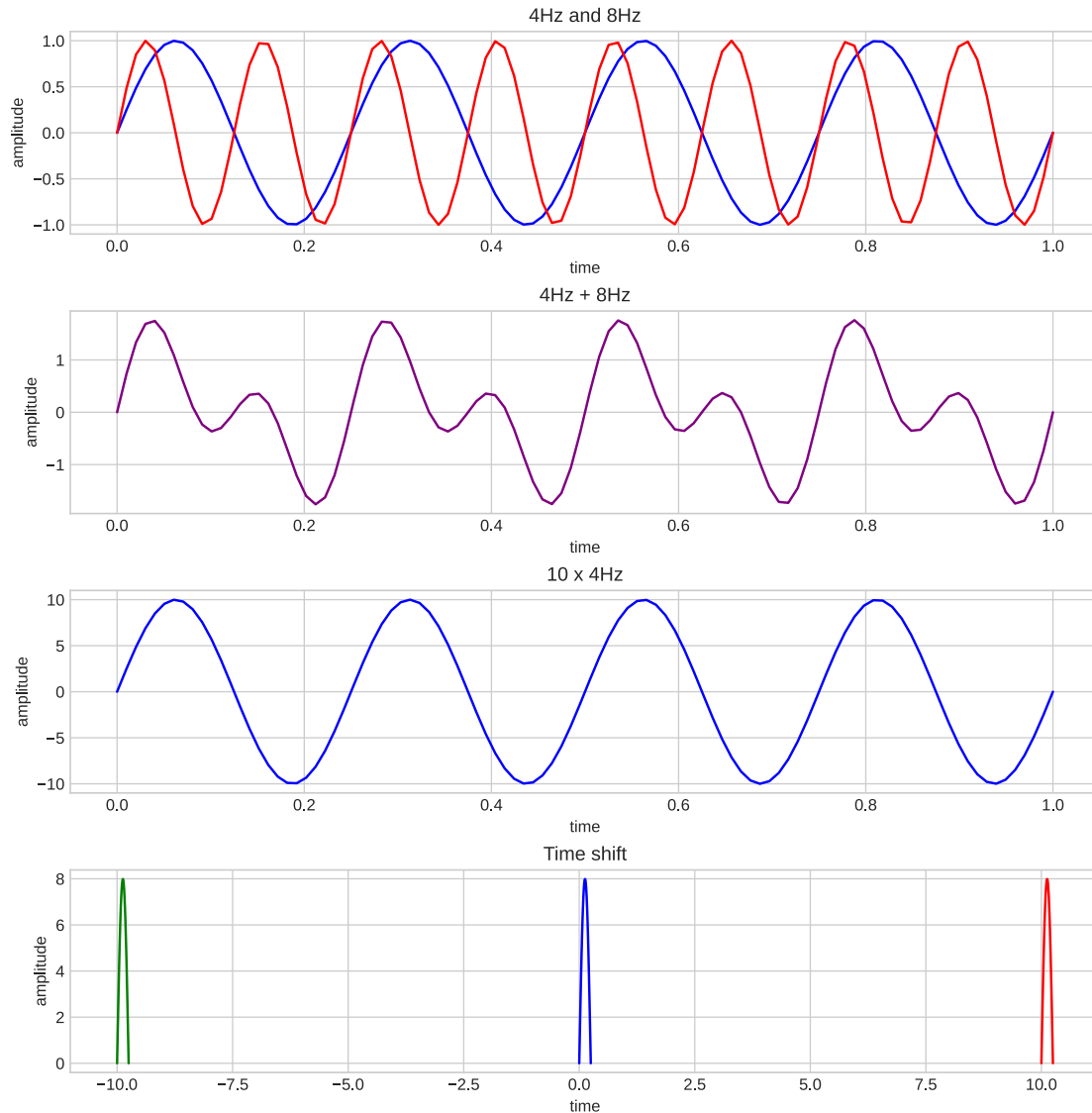
# 2. Plot the addition and multiplication of these signals with each other.
ax[1].plot(t,s1 + s2, color='purple')
ax[1].set_xlabel('time')
ax[1].set_ylabel('amplitude')
ax[1].set_title('4Hz + 8Hz')

# 3. Plot the amplified signal for 4Hz if the scaling factor k is 10.
ax[2].plot(t,10*s1, color='blue')
ax[2].set_xlabel('time')
ax[2].set_ylabel('amplitude')
ax[2].set_title('10 x 4Hz')

# 4. Plot these time shifted signals for 0 to 0.26 with 0.01 increments with 2Hz.
↳  $A = 8\sin(2\pi f t)$   $B = 8\sin(2\pi f(t + 10))$   $C = 8\sin(2\pi f(t - 10))$ 
t = np.arange(0,0.26,0.01)
# print(t)
f = 2 #Hz
A = 8 * np.sin(2 * pi * f * t)
B = 8 * np.sin(2 * pi * f * (t+10))
C = 8 * np.sin(2 * pi * f * (t-10))
ax[3].plot(t,A, color='blue')
ax[3].plot(t+10,B, color='red')
ax[3].plot(t-10,C, color='green')
ax[3].set_xlabel('time')
ax[3].set_ylabel('amplitude')
ax[3].set_title('Time shift')

```

[10]: Text(0.5, 1.0, 'Time shift')



3 4.3 Operations on a discrete signal

```
[11]: # 1. Plot  $x[n1] = 1\ 3\ 4\ 6\ 0\ 3\ 8\ 0\ 3$  and  $x[n2] = 1\ 2\ 2\ 6\ 4\ 9\ 4\ 0\ 6$  sequence.
fig, ax = createSubplot(4)

x1 = np.array([1,3,4,6,0,3,8,0,3])
x2 = np.array([1,2,2,6,4,9,4,0,6])
n = np.arange(0,len(x1))
ax[0].stem(n,x1,linewidth='--',markerfmt='o')
ax[0].stem(n,x2,linewidth=':',markerfmt='x')
ax[0].set_xlabel('time')
```

```

ax[0].set_ylabel('amplitude')
ax[0].set_title('x[n1] and x[n2]')

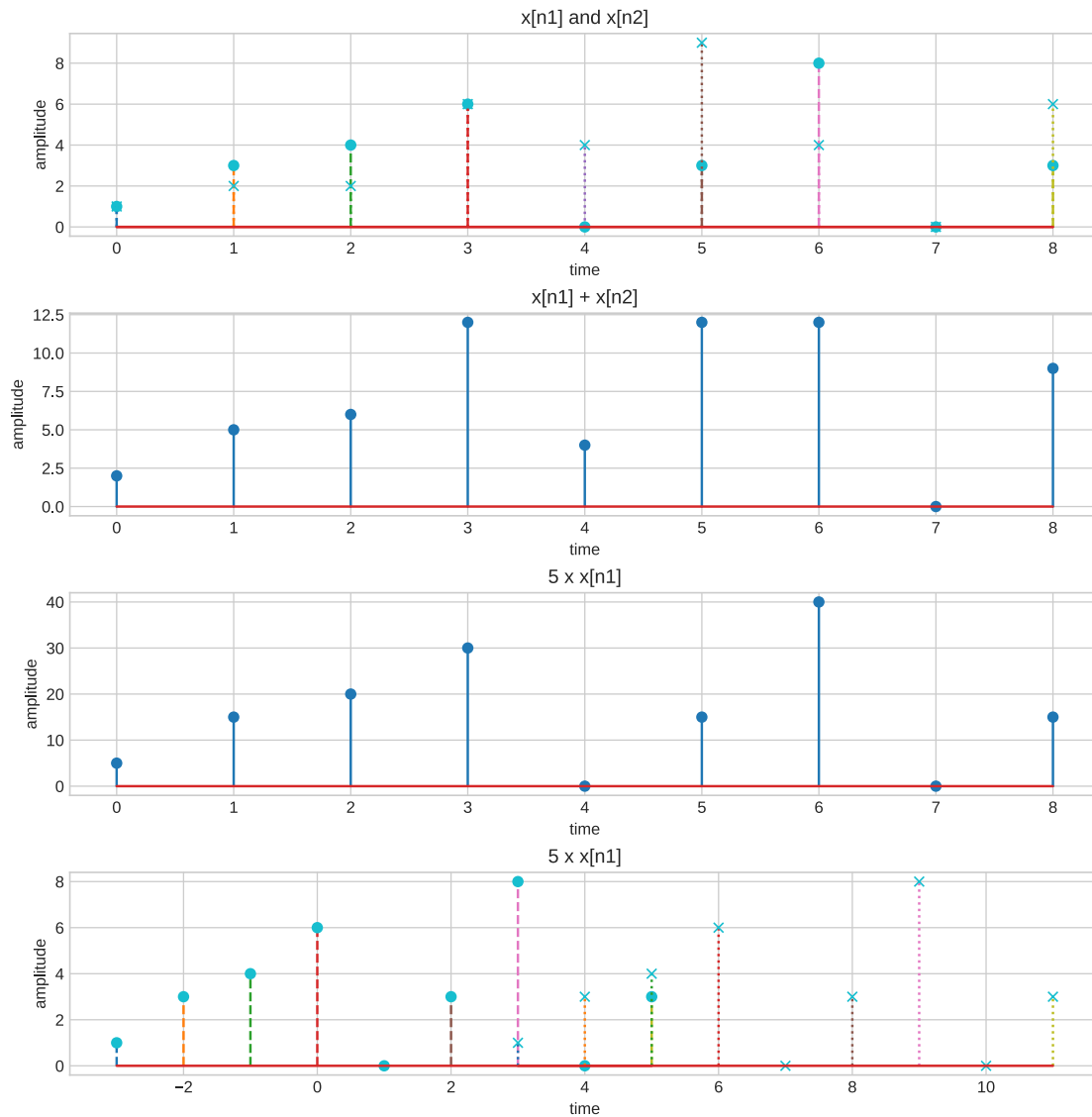
# 2. Plot the addition and multiplication of these signals with each other.
ax[1].stem(n,x1+x2)
ax[1].set_xlabel('time')
ax[1].set_ylabel('amplitude')
ax[1].set_title('x[n1] + x[n2]')

# 3. Plot the amplified signal for x[n1] if the scaling factor k is 5.
ax[2].stem(n,5 * x1)
ax[2].set_xlabel('time')
ax[2].set_ylabel('amplitude')
ax[2].set_title('5 x x[n1]')

# 4. Plot the time shifted signal x[n1 - 3] and x[n1+3].
ax[3].stem(n-3,x1,linewidth='--',markerfmt='o')
ax[3].stem(n+3,x1,linewidth=':',markerfmt='x')
ax[3].set_xlabel('time')
ax[3].set_ylabel('amplitude')
ax[3].set_title('5 x x[n1]')

```

```
[11]: Text(0.5, 1.0, '5 x x[n1]')
```

4 4.4 Energy and Power of a Signal

[12]: # Write down a Matlab program to compute the energy and power of a discrete_
 ↳ signal taking the user input sequence. Eg - for sequence 1 3 5 6 you should_
 ↳ get the energy as 71 and power as 17.75

```
# Energy = sum of signal**2
# Power = Energy / num
```

```
def disEnergy(sig):
    return sig @ sig
```

```
def disPower(sig):
    energy = disEnergy(sig)
    return energy/(len(sig))

s = np.array([1,3,5,6])
print("Energy: ", disEnergy(s))
print("Power: ", disPower(s))
```

Energy: 71
Power: 17.75

5 4.5 Magnitude spectrum in frequency domain

```
[13]: from numpy.fft import fft
fig, ax = createSubplot(7)
# 1. Sin(100 t) with sampling frequency Fs=1500 Hz and for a duration of 10s
fs = 1500 # Hz
duration = 10 # second
sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = np.sin(100*pi*t)
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[0].plot(f1,z1/(sampling/2))
ax[0].set_xlabel('Frequency (Hz)')
ax[0].set_ylabel('Magnitude')
ax[0].set_title('Frequency Spectrum Sin(100 t)')

# 2. Cos(200 t) with sampling frequency Fs=3000 Hz and for a duration of 10s
fs = 3000 # Hz
duration = 10 # second
sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = np.cos(200*pi*t)
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[1].plot(f1,z1/(sampling/2))
ax[1].set_xlabel('Frequency (Hz)')
ax[1].set_ylabel('Magnitude')
ax[1].set_title('Frequency Spectrum Cos(200 t)')

# 3. Cos(160 t + /3) with sampling frequency Fs=1500 Hz and for a duration of 10s
fs = 1500 # Hz
duration = 10 # second
```

```

sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = np.cos((160*pi*t) + (pi/3))
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[2].plot(f1,z1/(sampling/2))
ax[2].set_xlabel('Frequency (Hz)')
ax[2].set_ylabel('Magnitude')
ax[2].set_title('Frequency Spectrum Cos(160 t + /3)')

# 4. Square(10 t) with sampling frequency Fs=150 Hz and for a duration of 1s
fs = 150 # Hz
duration = 1 # second
sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = signal.square(10 * pi * t)
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[3].plot(f1,z1/(sampling/2))
ax[3].set_xlabel('Frequency (Hz)')
ax[3].set_ylabel('Magnitude')
ax[3].set_title('Frequency Spectrum Square(10 t)')

# 5. A square pulse with width = 0.2 and Fs = 150Hz
# width = T/2 = 0.2 => T = 4/10
# f = 2.5
fs = 150 # Hz
duration = 1 # second
sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = signal.square(5 * pi * t)
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[4].plot(f1,z1/(sampling/2))
ax[4].set_xlabel('Frequency (Hz)')
ax[4].set_ylabel('Magnitude')
ax[4].set_title('Frequency Spectrum square pulse with width = 0.2')

# 6. A Gaussian pulse Fs = 60Hz
fs = 60 # Hz
duration = 50 # second
sampling = fs*duration
t = np.linspace(-50,duration,sampling)
s1 = []
for i in t:
    s1.append((1/np.sqrt(2*pi*0.01)) * np.exp((-1 * (i * i))/2*0.01 ))
z1 = np.abs(fft(s1))[0:(sampling)//2]

```

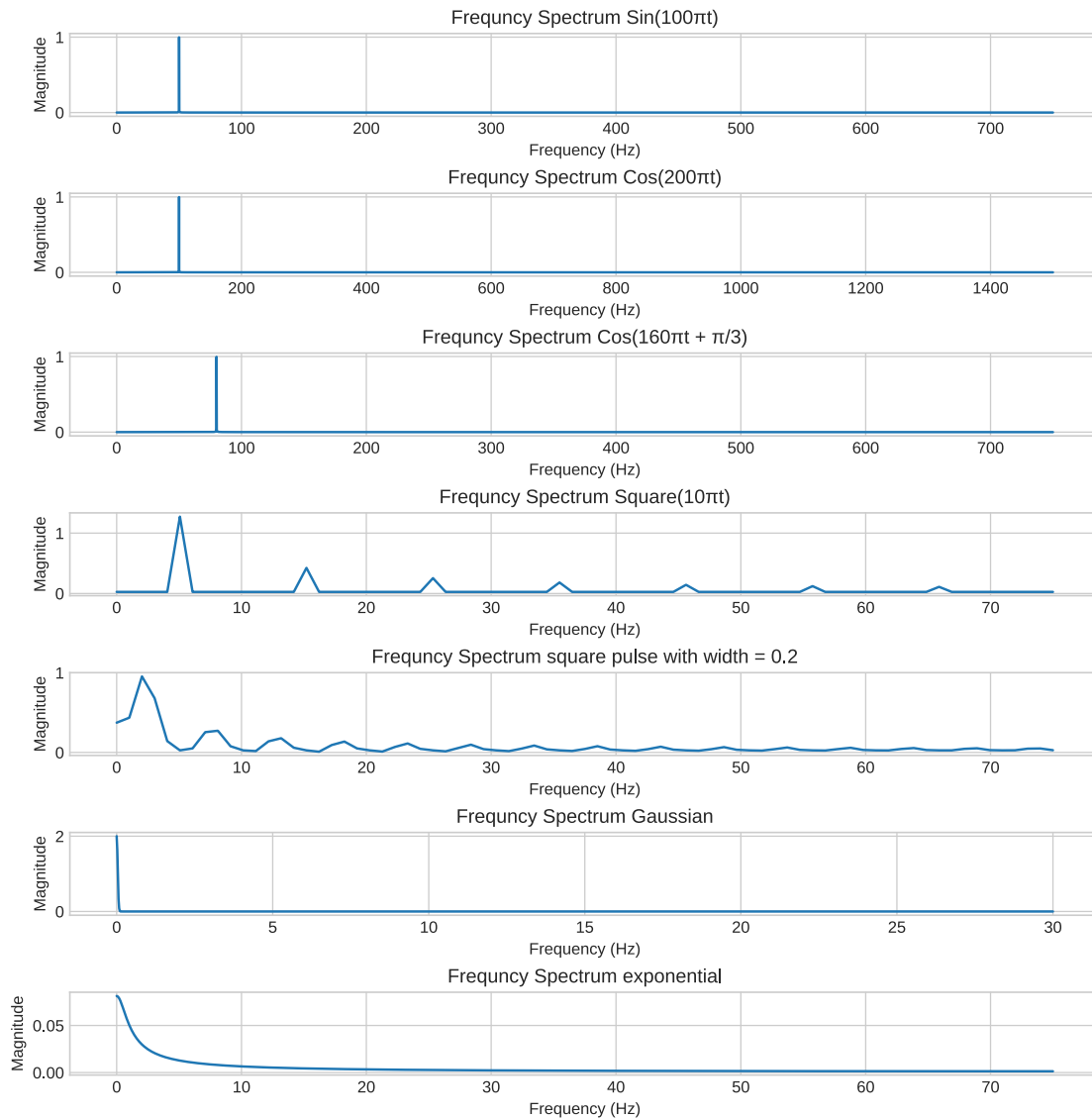
```

f1 = np.linspace(0,fs/2, sampling//2)
# ax[5].plot(t,s1)
ax[5].plot(f1,z1/(sampling/2))
ax[5].set_xlabel('Frequency (Hz)')
ax[5].set_ylabel('Magnitude')
ax[5].set_title('Frequency Spectrum Gaussian')

# 7. An exponential function with  $x = 2e^{-5t}$  and  $F_s = 150\text{Hz}$ 
fs = 150 # Hz
duration = 10 # second
sampling = fs*duration
t = np.linspace(0,duration,sampling)
s1 = []
for i in t:
    s1.append( 2 * np.exp(-5*i) )
z1 = np.abs(fft(s1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
# ax[6].plot(t,s1)
ax[6].plot(f1,z1/(sampling/2))
ax[6].set_xlabel('Frequency (Hz)')
ax[6].set_ylabel('Magnitude')
ax[6].set_title('Frequency Spectrum exponential')

```

[13]: Text(0.5, 1.0, 'Frequency Spectrum exponential')



6 Identify string

- high E – 330 Hz
- B – 247 Hz
- G – 196 Hz
- D – 147 Hz
- A – 110 Hz
- low E – 82 Hz

[14]: # Note: Each signal is acquired by playing single string from guitar and then
 ↳ recording through microphone using a sampling rate of 8000 samples/sec and
 ↳ for the duration of 5 seconds

```

fs = 8000 # Hz
duration = 5 # s

fig, ax = createSubplot(6)

# signal1
signal1 = np.loadtxt('signal1.txt', dtype='double')
sampling = fs * duration
z1 = np.abs(fft(signal1))[0:(sampling)//2]
f1 = np.linspace(0,fs/2, sampling//2)
ax[0].plot(f1,z1/(sampling/2))
ax[0].set_xlabel('Frequency (Hz)')
ax[0].set_ylabel('Magnitude')
ax[0].set_title(f'Signal 1 = {f1[np.argmax(z1)]}')

signal2 = np.loadtxt('signal2.txt', dtype='double')
sampling = fs * duration
z2 = np.abs(fft(signal2))[0:(sampling)//2]
f2 = np.linspace(0,fs/2, sampling//2)
ax[1].plot(f2,z2/(sampling/2))
ax[1].set_xlabel('Frequency (Hz)')
ax[1].set_ylabel('Magnitude')
ax[1].set_title(f'Signal 2 = {f2[np.argmax(z2)]}')

signal3 = np.loadtxt('signal3.txt', dtype='double')
sampling = fs * duration
z3 = np.abs(fft(signal3))[0:(sampling)//2]
f3 = np.linspace(0,fs/2, sampling//2)
ax[2].plot(f3,z3/(sampling/2))
ax[2].set_xlabel('Frequency (Hz)')
ax[2].set_ylabel('Magnitude')
ax[2].set_title(f'Signal 3 = {f3[np.argmax(z3)]}')

signal4 = np.loadtxt('signal4.txt', dtype='double')
sampling = fs * duration
z4 = np.abs(fft(signal4))[0:(sampling)//2]
f4 = np.linspace(0,fs/2, sampling//2)
ax[3].plot(f4,z4/(sampling/2))
ax[3].set_xlabel('Frequency (Hz)')
ax[3].set_ylabel('Magnitude')
ax[3].set_title(f'Signal 4 = {f4[np.argmax(z4)]}')

signal5 = np.loadtxt('signal5.txt', dtype='double')
sampling = fs * duration
z5 = np.abs(fft(signal5))[0:(sampling)//2]
f5 = np.linspace(0,fs/2, sampling//2)
ax[4].plot(f5,z5/(sampling/2))

```

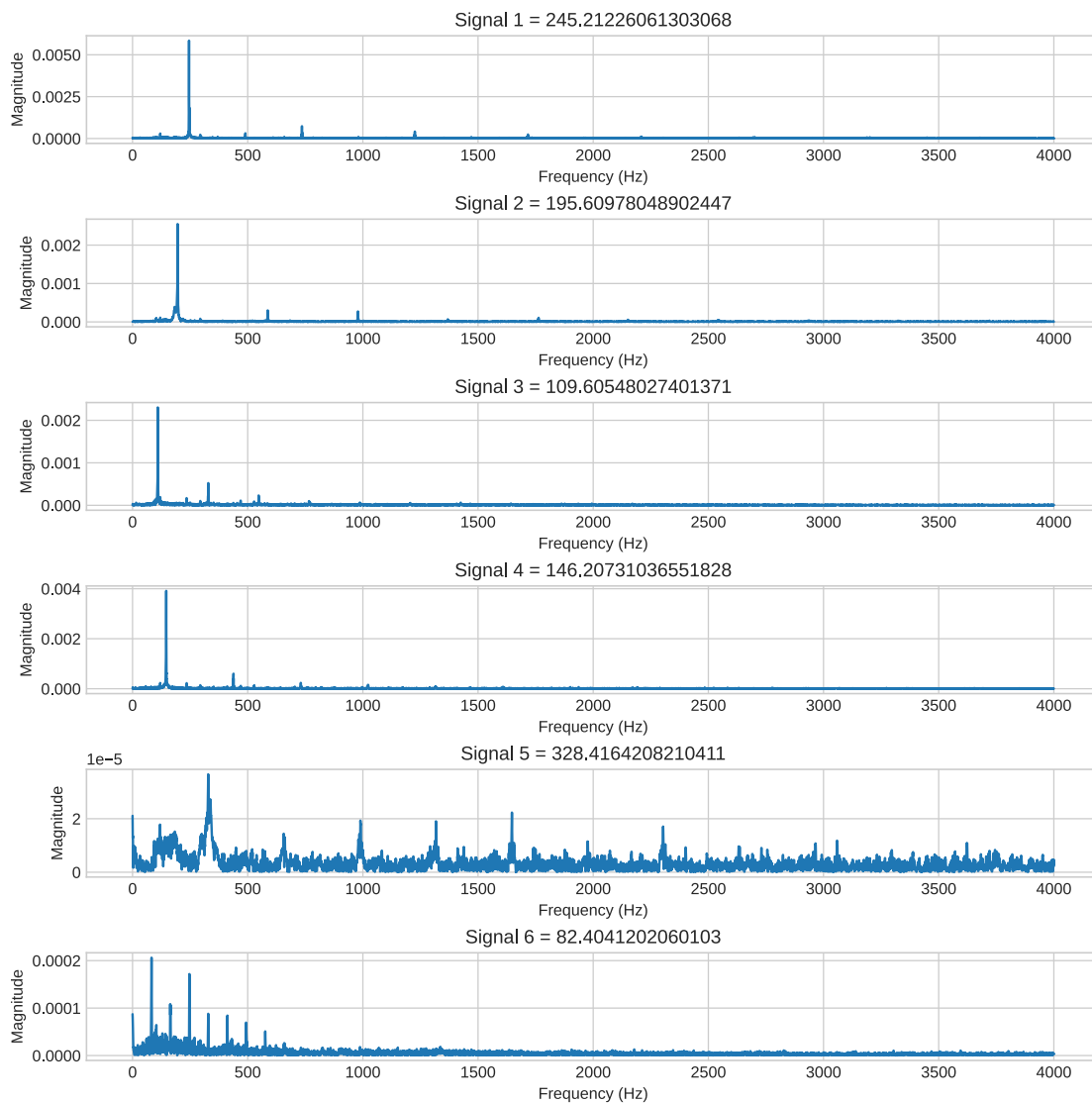
```

ax[4].set_xlabel('Frequency (Hz)')
ax[4].set_ylabel('Magnitude')
ax[4].set_title(f'Signal 5 = {f5[np.argmax(z5)]}')

signal6 = np.loadtxt('signal6.txt', dtype='double')
sampling = fs * duration
z6 = np.abs(fft(signal6))[0:(sampling)//2]
f6 = np.linspace(0,fs/2, sampling//2)
ax[5].plot(f6,z6/(sampling/2))
ax[5].set_xlabel('Frequency (Hz)')
ax[5].set_ylabel('Magnitude')
ax[5].set_title(f'Signal 6 = {f6[np.argmax(z6)]}')

```

[14]: Text(0.5, 1.0, 'Signal 6 = 82.4041202060103')



- Signal 1 is B
- Signal 2 is G
- Signal 3 is A
- Signal 4 is D
- Signal 5 is high E
- Signal 6 is low E