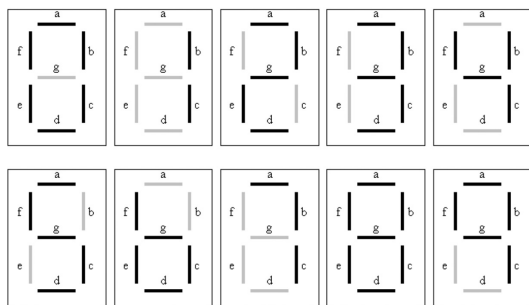


HOMEWORK #3

EE/CS 119a

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①



	input							output						
	a	b	c	d	e	f	g	a	b	c	d	e	f	g
0	1	1	1	1	1	1	0	0	1	1	0	0	0	0
1	0	1	1	0	0	0	0	1	1	0	1	1	0	1
2	1	1	0	1	1	0	1	1	1	1	1	0	0	1
3	1	1	1	1	0	0	1	0	1	1	0	0	1	1
4	0	1	1	0	0	1	1	1	0	1	1	0	1	1
5	1	0	1	1	0	1	1	0	0	1	1	1	1	1
6	0	0	1	1	1	1	1	1	1	1	0	0	0	0
7	1	1	1	0	0	0	0	1	1	1	1	1	1	1
8	1	1	1	1	1	1	1	1	1	1	0	0	1	1
9	1	1	1	0	0	1	1	1	1	1	1	1	1	0



Form:

				a	b	c	d/e
				0	0	0	0
				0	0	0	1
				0	0	1	1
				0	0	1	0
				0	1	1	0
				0	1	1	1
				0	1	0	1
				0	1	0	0
				1	1	0	0
				1	1	0	1
				1	1	1	1
				1	1	1	0
				1	0	1	0
				1	0	1	1
				1	0	0	1
				1	0	0	0

a	b	c	d	e
0	0	0	0	0
0	0	0	0	1
0	0	0	1	0
0	0	0	1	1
0	0	1	0	0
0	0	1	0	1
0	0	1	1	0
0	0	1	1	1
0	1	0	0	0
0	1	0	0	1
0	1	0	1	0
0	1	0	1	1
0	1	1	0	0
0	1	1	0	1
0	1	1	1	0
0	1	1	1	1
1	0	0	0	0
1	0	0	0	1
1	0	0	1	0
1	0	0	1	1
1	0	1	0	0
1	0	1	0	1
1	0	1	1	0
1	0	1	1	1

$$a = \bar{g}\bar{f} + ac\bar{d} + b\bar{f}\bar{e} + ge$$

b	c	d	e
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1
1	1	1	1

$$b = \bar{g}\bar{f} + ab + ge$$

c	d	e
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1

$$c = g + a$$

d	e	f	g
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

$$d = \bar{g}\bar{f} + f\bar{e} + b\bar{e}$$

e	f	g
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1
1	1	1

$$e = \bar{g}\bar{f} + af\bar{e}$$

f	g
0	0
0	1
1	0
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1
1	1

$$f = abc\bar{f} + bgf + ab$$

g
0
1
1
1
1
1
1
1
1
1
1
1
1
1
1
1

$$g = \bar{g}\bar{f} + ab + abdg + ab$$



Final equations:

$$a = \bar{g}\bar{f} + ac\bar{d} + b\bar{f}\bar{e} + ge$$

$$b = \bar{g}\bar{f} + ab + ge$$

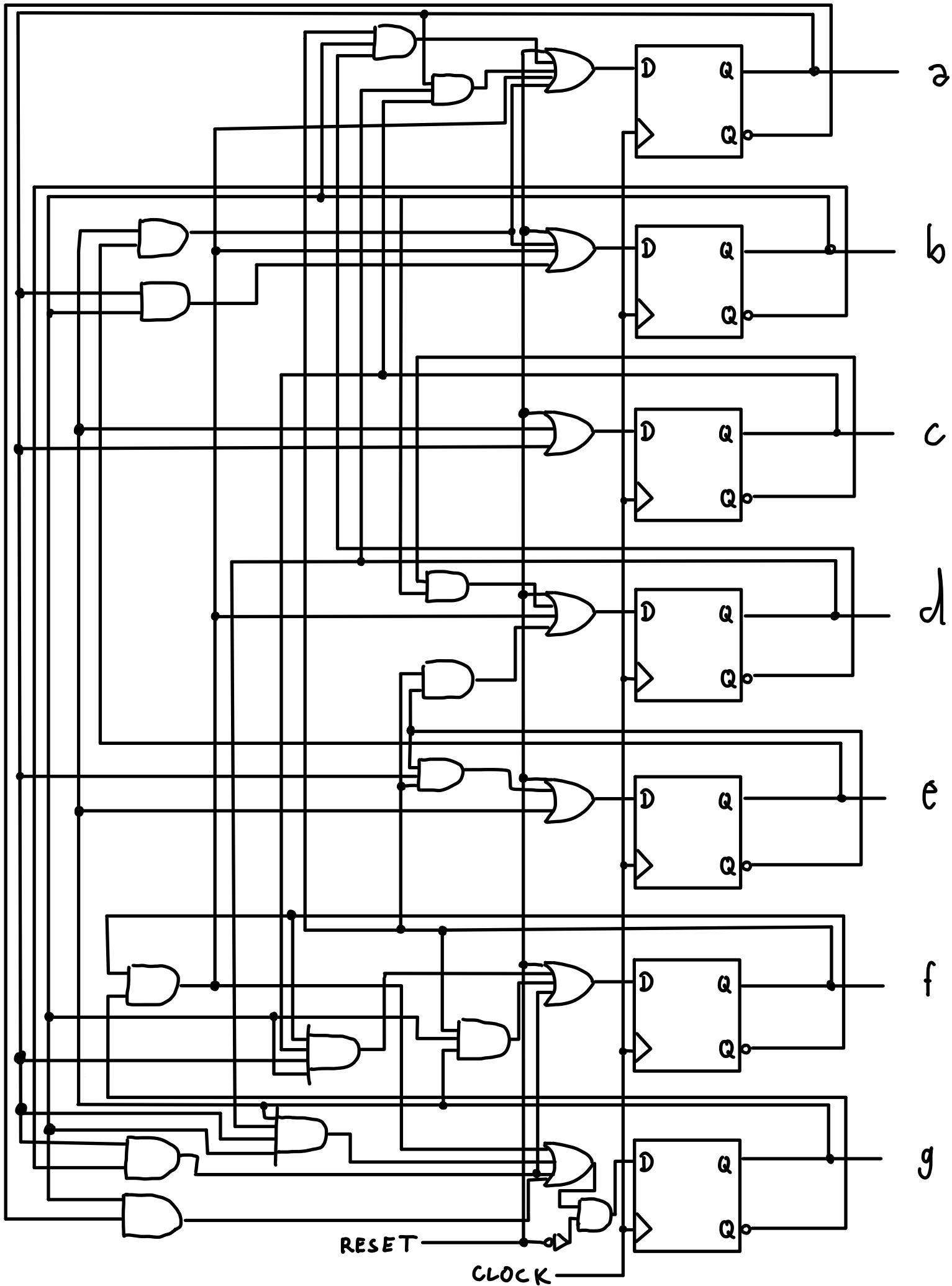
$$c = g + a$$

$$d = \bar{g}\bar{f} + f\bar{e} + b\bar{e}$$

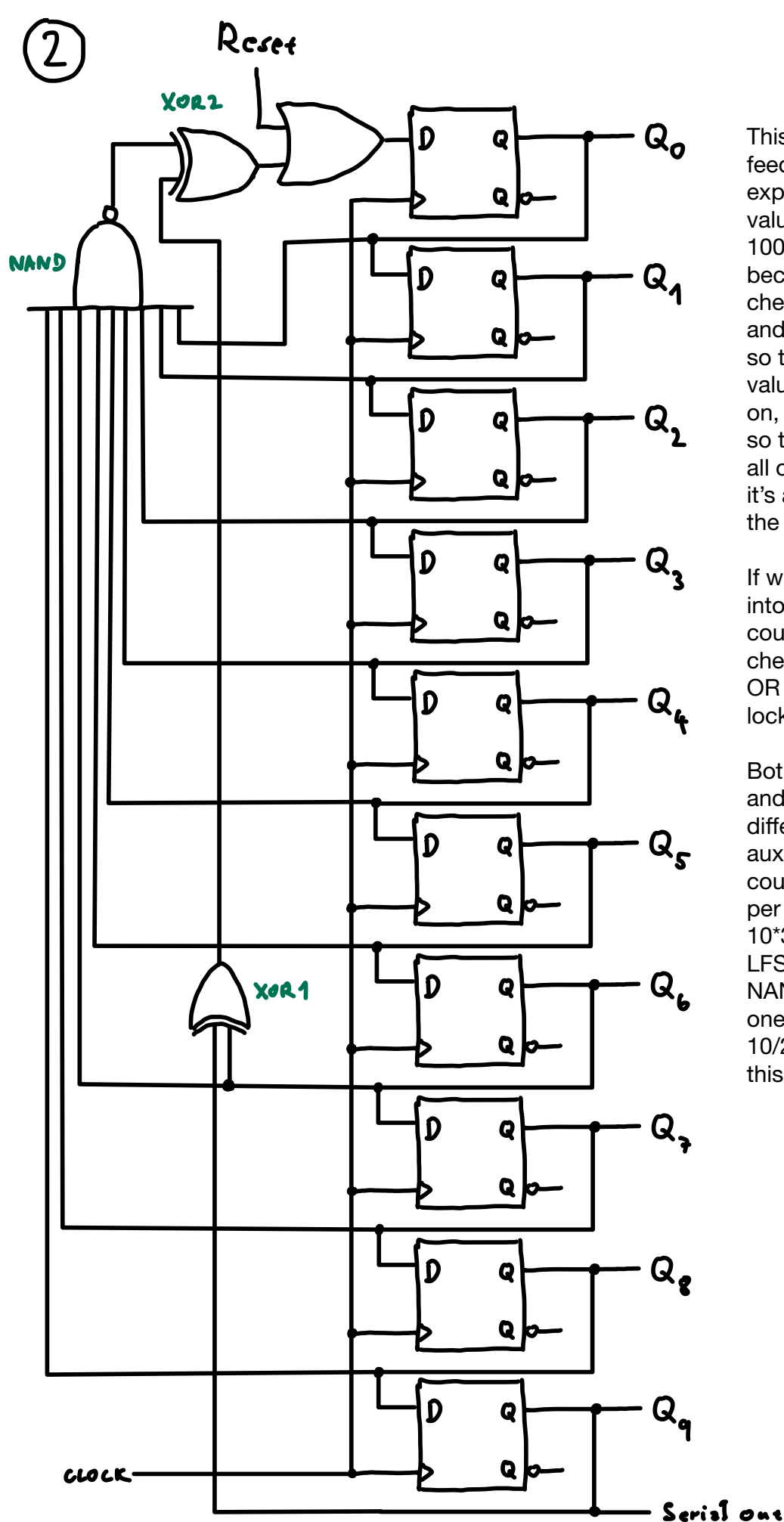
$$e = \bar{g}\bar{f} + af\bar{e}$$

$$f = abc\bar{f} + bgf + ab$$

$$g = \bar{g}\bar{f} + ab + abdg + ab$$



2



This is a standard LFSR with the 9 and 6 feedback bits (as in the lecture notes), expect when the counter reaches the value 0000000001, instead of going to 1000000000, it goes to 0000000000, because the both the NAND gate, which checks for $Q_0Q_1Q_2Q_3Q_4Q_5Q_6Q_7Q_8$, and the XOR1 gate is on, so XOR2 is off, so the next pushed bit is 0. When the value is 0000000000, the NAND gate still on, but XOR1 is now off, so XOR2 is on, so the next pushed bit is 1000000000. In all other cases, the NAND gate is off, so it's as if the XOR2 gate wasn't there and the circuit acts as a standard counter.

If we didn't care about the circuit looping into and back to 0000000000, we could've just added a single AND gate checking for all-zeros going into the main OR gate, which would get us *from* the lock state but never *into* it.

Both the regular synchronous counter and the LFSR use 10 D-flip-flops, so the difference in the gate count will be in the auxiliary gates. A regular synchronous counter uses 1 AND gate and 1 OR gate per bit, so for a 10-bit counter that's $10 \times 3 = 30$ gates. In our extended 10-bit LFSR counter, we have one 10 input NAND gate, two 2 input XOR gates and one 2 input OR gate, which is $10/2 + 2 \times 1 + 1.5 = 8.5$ gates. We can see that this is much less.

3

decimals

99 1100011
 ↓ 10 0001010

$$RST_{HELPER} = RST + Q_0 Q_1 Q_5 Q_6$$

$$Q_0' = \overline{RST_{HELPER}} \cdot \overline{Q_0}$$

$$Q_1' = RST_{HELPER} + (Q_0 \oplus Q_1)$$

$$Q_2' = \overline{RST_{HELPER}} \cdot Q_0 Q_1 \oplus Q_2$$

$$Q_3' = RST_{HELPER} + (Q_0 Q_1 Q_2 \oplus Q_3)$$

$$Q_4' = \overline{RST_{HELPER}} \cdot Q_0 Q_1 Q_2 Q_3 \oplus Q_4$$

$$Q_5' = \overline{RST_{HELPER}} \cdot Q_0 Q_1 Q_2 Q_3 Q_4 \oplus Q_5$$

$$Q_6' = \overline{RST_{HELPER}} \cdot Q_0 Q_1 Q_2 Q_3 Q_4 Q_5 \oplus Q_6$$

