Day10

LetsUpgrade class notes

Process of Hypothesis Testing

Formulate the Null Hypothesis and the alternative hypothesis.



Select the appropriate test statistic.



Choose the level of significance, a, and the Degree of Freedom



Compute the calculated test value of the test statistic



Compute the table test value of the test statisitc



Compare the calculated values and table values



Make the statistical decision and state the managerial conclusion.





Press Esc to exit full screen

Step 1: Hypothesis Formulation

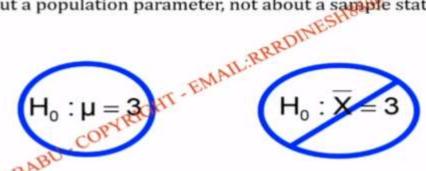
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The Null Hypothesis, Ho

States the claim or assertion to be tested

- Example: The average number of TV sets in U.S. Homes is equal to 010 Is always about a population parameter, not about a sample statistic



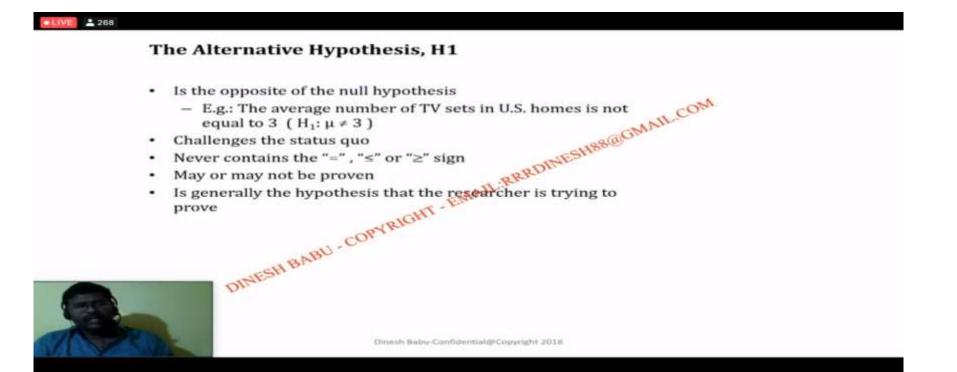
ontains "=", "≤" or "≥" sign



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Null hypothesis: 1.set by us, 2. alws must have three sings shown in fig.



- Alternate: alws opposite to null!.
 Alws not contained signs!
- May or may not b proven

Step2:



Process of Hypothesis Testing

Formulate the Null Hypothesis and the alternative hypothesis.

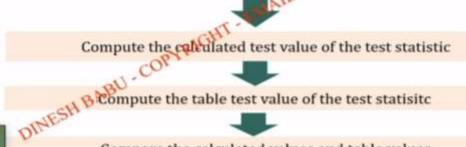


Select the appropriate test statistic.



Choose the level of significance, Confidence Interval, Degree of Freedom







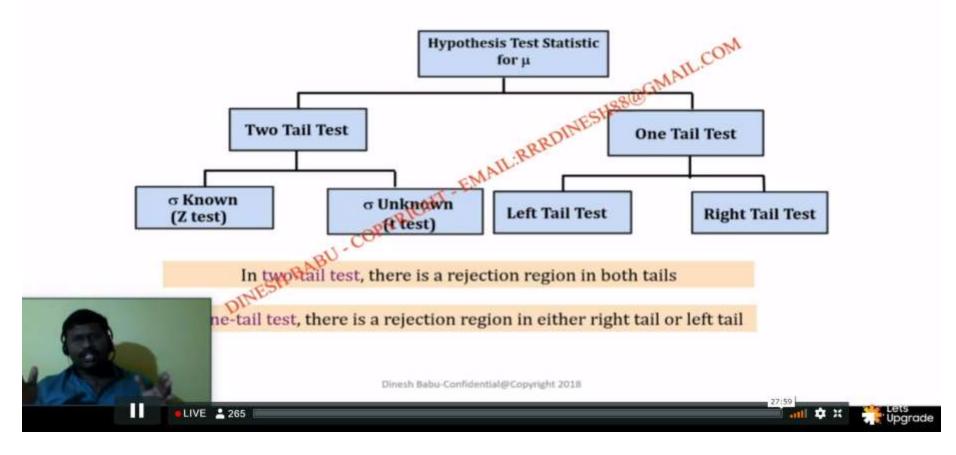
Compare the calculated values and table values



Make the statistical decision and state the managerial conclusion.



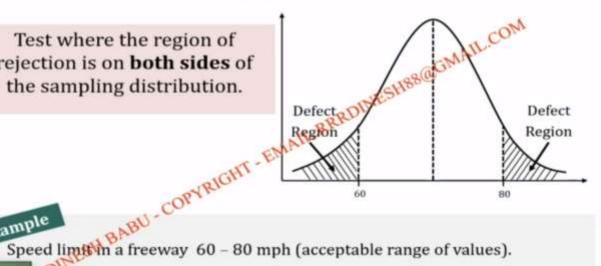
Hypothesis Tests for the Mean



- T test: std devt not kwn, Z tes: when std deviation is given for population.
- LHS / RHS tail: based on side of sampling distribution needed!

Two-Tailed Tests

Test where the region of rejection is on both sides of the sampling distribution.

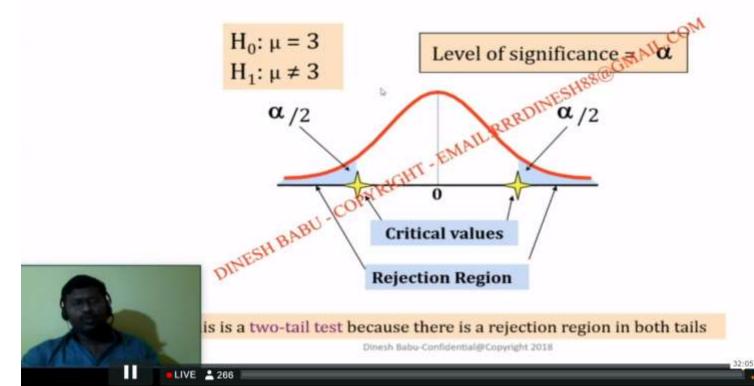


Example

ion of rejection would be numbers from both sides of the distribution, t is, both <60 and >80 are defects.

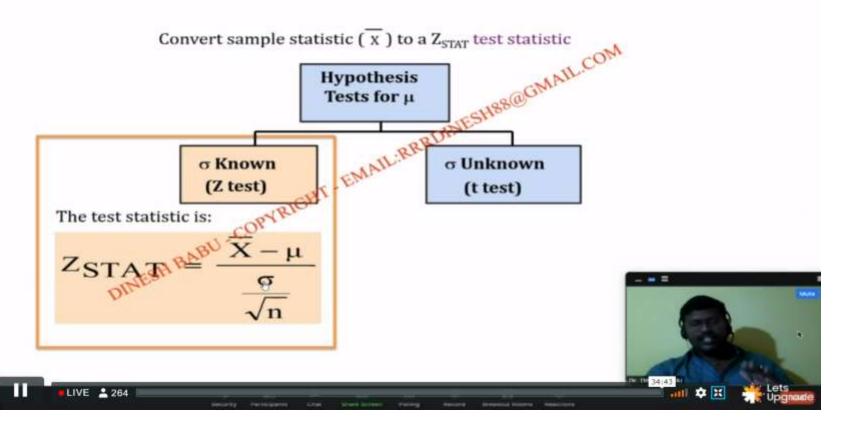
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Level of Significance and the Rejection Region



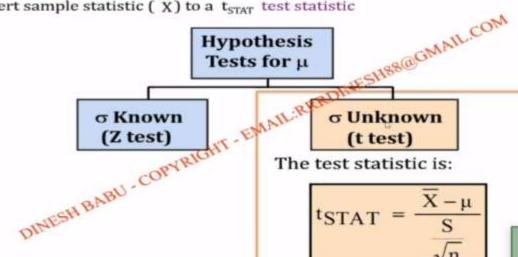
- One tail : < += or >+=
- Two tail : = must there. (rejection at both sides)

Z Test of Hypothesis for the Mean (σ Known)



t Test of Hypothesis for the Mean (σ Unknown) -> Std Deviation unknown

Convert sample statistic (\overline{X}) to a t_{STAT} test statistic



The test statistic is:

$$t_{\text{STAT}} = \frac{\overline{X} - \mu}{\frac{S}{\sqrt{n}}}$$

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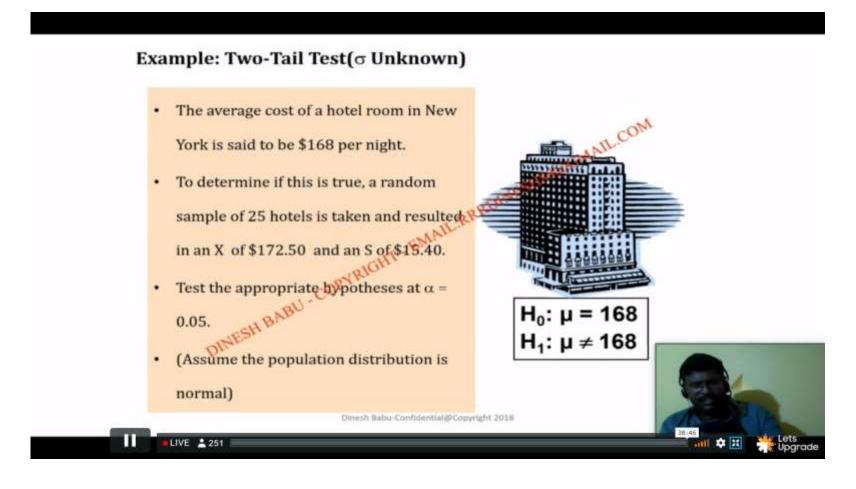






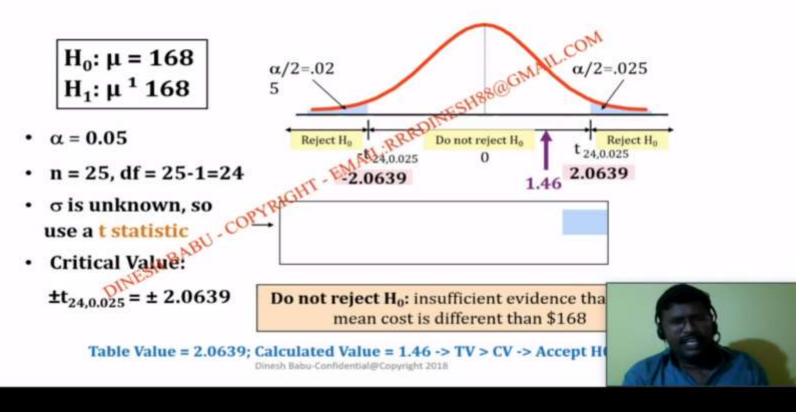






 Its two tail prob(= sing), \(\mathred{\pm} \) is not avbl, only mean is given, hence T-test can be done.

Example Solution: Two-Tail t Test



- $\dot{\alpha}$ = nothing but error rate, it is given, 1.46>TV>CV: -> accept hypothesis.
- A = comes from quality of data, mostly given by customer.
- Rejection area: defined based on table values.

Two-Tail T test (Table Value or Critical Value)

t Table										
cum. prob	£.60	£.76	f.se	t.aa	£.00	f.ns.	t , 175	£.99	f.mm	f ,00
one-tail	0.50	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.00
two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002
df		1,000,000								
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.3
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	28,72
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	11/21
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.17
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4,002	5.89
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	A STATE OF THE PARTY OF THE PAR	5.20
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.78
8	0.000	0.706	0.889	1.108	1.397	1.860	8.306	2 806	3.355	4.50
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.29
10	0.000	0.700	0.879	1.093	1.372	1.812	2.2280	2.764	3.169	4.14
11	0.000	0.697	0.876	1.088	1.363	1.796		2.718	3.106	4.02
12	0.000	0.695	0.873	1.083	1.356	1.782		2.681	3.055	3.93
13	0.000	0.694	0.870	1.079	1.350	17701	2.160	2.650	3.012	3.85
14	0.000	0.692	0.868	1.076	1.345	1.753	2.145	2.624	2.977	3.78
16	0.000	0.690	0.865	1.074	1-337	1.746	2.131	2.602	2.921	3.73
17	0.000	0.689	0.863	1.069	V.333	1.740	2.110	2.567	2.898	3.64
18	0.000	0.688	0.862	1.062	1.330	1.734	2.101	2.552	2.878	3.61
19	0.000	0.688	0.861	1.000	1.328	1.729	2.093	2.539	2.861	3.57
20	0.000	0.687	0.860	0.064	1.325	1.725	2.086	2.528	2.845	3.55
21	0.000	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.52
22	0.000	0.686	0.868	1.061	1.321	1.717	2.074	2.508	2.819	3.50
23	0.000	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.48
24	0.000	0.685	0.857	1.059	1.318	1.711	(2.064)	2.492	2.797	3.46
25	0.000	0.04	0.856	1.058	1.316	1,708	2.060	2.485	2.787	3.45
26	0.000	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.43
27	0.000	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.42
28	0,000	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.40
29	00000	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.39
30	0.000	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.38
40	0.000	0.681	0.851	1.050	1.303	1.684	2.021	2.423	2.704	3.30
60	0.000	0.679	0.848	1.045	1.296	1.671	2.000	2.390	2.660	3.23
80	0.000	0.678	0.846	1.043	1,292	1.664	1.990	2.374	2.639	3.19
100	0.000	0.677	0.845	1.042	1.290	1.660	1.984	2.364	2.626	3.17
1000	0.000	0.675	0.842	1.037	1.282	1.646	1.962	2.330	2.581	3.09
Z	0.000	0.674	0.842	1.036	1.282	1.645	1.960	2.326	2.576	3.09
	0%	50%	60%	70%	80%	90%	.95%	98%	99%	99.89

53:55

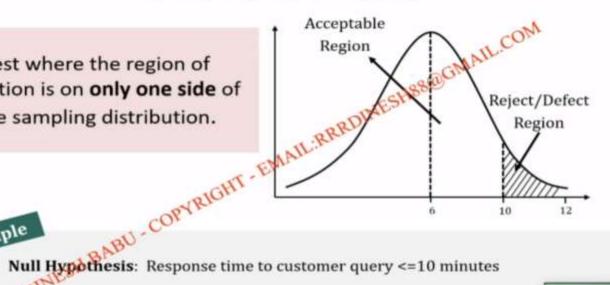
f ,9996 0.0005 0.001 636.62 31,599 12.924 8.610 6.869 5.959 5.408 5.041 4.781 4.587 4.437 4.318 4.221 4.140 4.073 4.015 3.965 3.922 3.883 3.850 3.819 3,792 3.768 3.745 3.725 3.707 3.690 3.674





One-Tailed Tests

Test where the region of rejection is on only one side of the sampling distribution.



Example

Alternative Hypothesis: Response time > 10 minutes Region of rejection would be the numbers greater than 10 (there is no bo the lesser time interval)



One-Tail Tests

In many cases, the alternative hypothesis focuses on a particular direction



 $H_0: \mu \geq 3$ $H_1: \mu < 3$ This is a lower-tail test since the alternative hypothesis is focused on the lower tail below the mean of 3

H₀: μ≤3BU - COPYRIGHT Tail Test

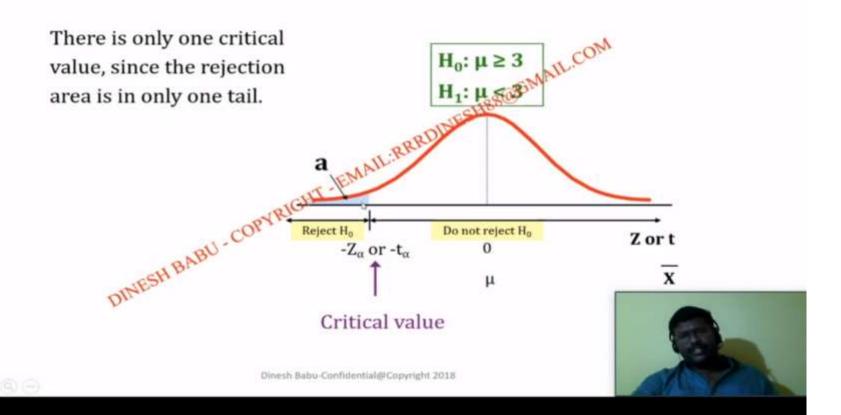
This is an upper-tail test since the alternative hypothesis is focused on the upper tail above the mean of 3

1:04:30

In one-tail test, there is a rejection region in either right tail or left

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Lower-Tail Tests -> One Tail Test -> Left Tail Test



Example: Upper-Tail t Test for Mean (\sigma unknown)

- A phone industry manager thinks that customer monthly cell phone bills have decreased, and now average less than \$52 per month.

 The company wishes to test this claim.
 Assume a normal population

 ypothesis test:

Form hypothesis test:

H₁: μ > 52 Bithe average is not over \$52 per month

(i.e., sufficient evidence exists to support the manager's old in the support the manager's old in th

Process of Hypothesis Testing

Formulate the Null Hypothesis and the alternative hypothesis.



Select the appropriate test statistic.



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Compute the calculated test value of the test statistic



DINESH B compute the table test value of the test statistic





Compare the calculated values and table values



Make the statistical decision and state the managerial conclusion.



Step 3: Choose a Level of Significance α

- If α = 0.05 then 5% error in the sample and remaining 95% accurate
- If α = 0.10 then 10% error in the sample and remaining 90% accurate



Key Terms

Two key terms that you need to understand in Hypothesis Testing are:

Confidence Interval:

Measure for reliability of an estimate; sample is used for estimating a population parameter so we need to know the rehability of that estimate

OHT - EMAIL: PRRDINESH88@GMAIL.COM are free to vary in a study





Confidence Interval

Confidence Interval

- apper boundary) within which the population parameter is included

 Width of the interverse VRIGHT be un Range of values (lower and
- the uncertainty associated with the estimate

Confidence leves

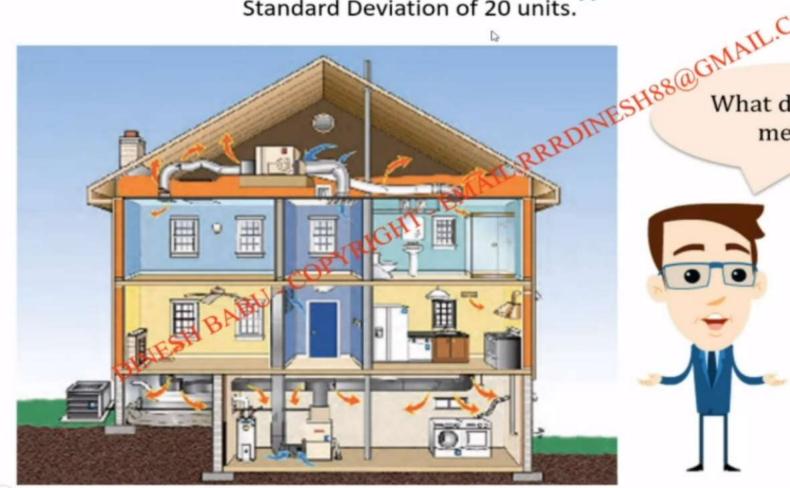
Probability associated with the



Example 1: Confidence Inter

Mean energy consumption of various houses in a colony is 200 units w

Standard Deviation of 20 units.



Discussion (Cont'd)

SOLUTION:

If the mean energy consumption of various houses in a colony is 200 units with a

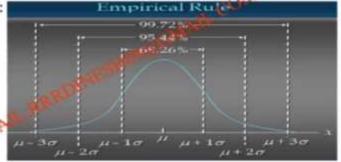
standard deviation of 20 units, it means that:

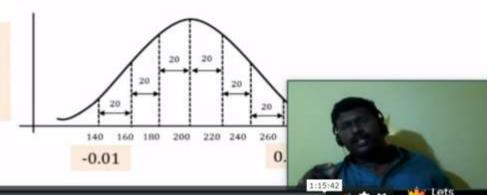


68.2% consume energy between 180 to 220 units

99% have their energy consumption Modern 140 to 260 units Tr

Thus for any given tousehold in the colony, there is a 99% confidence that the energy consumption of the household would be between 140 and 260 units.





Example 2: Confidence Interval

Consider mean demand for computers during assembly lead time is 350 units. our

operations manager wants to know whether the mean is different from 350 units. Null Hypothesis - > H_0 : = 350

Thus, our research hypothesis becomes: H_1 : \neq 350 SH88(a) GMAIL: REPORT SH88(a) Recall that the standard deviation [σ] was assumed to be 75, the sample size [n] was 25, and the sample mean was calculated to be 370.16





B. Common confidence levels and their critical values

You don't have to perform the above calculations every time. This list of critical values and their associated twotailed test confidence levels were calculated using the above steps:

		M.COM				
Confidence Level	Critical Value (Z-score) 1.645 1.70 1.75 1.8 F.MAIL.: RRRDINE SH88 (0) GMAIL. COM 1.75 2.8 F.MAIL.: RRRDINE SH88 (0) GMAIL. COM 1.70 1.75 2.70 2.33 2.575					
0.90	1.645					
0.91	170 ROINI					
0.92	1.75 ALL: RR					
0.93	Latimir					
0.94	RIGHTISS					
0.95	COPY L96					
0.96 QABU	2.05					
0.97 JESH B	2.17					
0.98 DIA	2.33					
0.99	2.575					

https://www.statisticshowto.datasciencecentral.com/probability-and-statistics/find-critical-values/



Critical Value Approach

- If we define the guts as the center 95% of the distribution [this 0.05], then the critical values that define the guts will be 1.96 st deviations of X-Bar on either side of the mean of the sampling distribution [350], or distribution [350], or
- Upper Confidence Interval = Mean + (Table Value) * Std Dev.

- Lower Confidence Interval = Mean (Table Value) * Std Dev. LCV = 350 - 1.96*15 = 350 - 29.4 = 320.6Table Value ($\alpha = 0.05$, Df = 24) = 1.96

Degrees of Freedom

Degrees of Freedom is the measure of number of values in a study that are free to vary.

For example, if you have to take ten different courses to graduate, and only ten different courses are offered, then you have nine degrees of freedom.

In nine semesters, you will be able to choose which class to take. In the tenth semester, there will only be one class left to take – there is no choice.

DINES





Degrees of freedom = No. of Rows - No. of Columns = 10 -1 = 9

Process of Hypothesis Testing

Formulate the Null Hypothesis and the alternative hypothesis.



Select the appropriate test statistic.



Choose the level of significance, Confidence Interval, Degree of Freedom



Compute the calculated test value of the test statistic



Compute the table test value of the test statistic



Compare the calculated values and table values



Make the statistical decision and state the managerial conclusion.



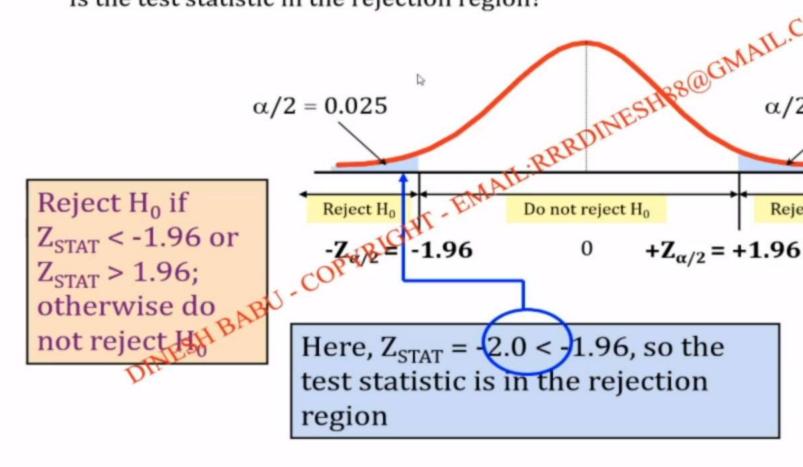




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Hypothesis Comparison

Is the test statistic in the rejection region?



Critical Value Approach to Testing

Test the claim that the true mean # of TV sets in US homes is equ (Assume $\sigma = 0.8$)

- State the appropriate null and alternative hypotheses All.
 H₀: μ = 3 H₁: μ ≠ 3 (This is a two-tail test) (This is a two-tail test).
 Specify the desired level of significance and the sample size
- - Suppose that $\alpha = 0.05$ and n = 100 are chosen for this te
 - σ is assumed known so this is a Z test.
- 3. Collect the data and compute the test statistic
 - Suppose the sample results are

100, X = 2.84 ($\sigma = 0.8$ is assumed known)

So the test statistic is:

$$Z_{\text{STAT}} = \frac{\overline{X} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{2.84 - 3}{\frac{0.8}{\sqrt{100}}} = \frac{-.16}{.08} = -$$

Process of Hypothesis Testing

Formulate the Null Hypothesis and the alternative hypothesis.



Select the appropriate test statistic.



Choose the level of significance, Confidence Interval, Degree of Freedom



Compute the calculated test value of the test statistic

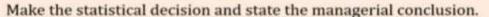


Compute the table test value of the test statistic



Compare the calculated values and table values









Type here to search











































P-Value Approach to Testing

- P-value is the probability of obtaining a test statistic at least as extreme as the one that was actually observed, assuming that the Null Hypothesis is true
- When P-value is less than a certain significance level (often 0.05), you reject

When P-value is less than a certain significance level (often 0.05), you reject the null hypothesis". This result indicates that the observed result is not due to a random occurrence but a true difference.

Result is due to a true difference

Result is due to a true difference

REJECT

Compare the p-value with $\alpha = 0.05$

- Compare the p-value with $\alpha = 0.05$
 - If p-value < 0.05, reject H₀
 - If p-value ≥ 0.05, do not reject H₀







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Possible Scenarios in Hypothesis

Four possible scenarios: Truth about the population Ho true Ha true Reject Ho Type I Correct decision error Decision based on sample Correct Type II Accept Hodecision error

Type I Error (α): Reject the Null Hypothesis when it is true

Type II Error (β): Accept the Null Hypothesis when it is false



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Example

- · A criminal trial is an example of hypothesis testing without the statistics.
- · In a trial a jury must decide between two hypotheses. The null hypothesis is:

Ho: The defendant is innocent

The alternative hypothesis or research hypothesis is:

H₁: The defendant is guilty

The jury does not know which hypothesis is true. They must make a
decision on the basis of evidence presented.









Justice

Null Hypothesis = "Person is innocent"

		Dec	ision
		Prison	Set free
True State	Innocent	Type I error	Correct decision
	Guilty	Correct decision	Type II error













Testing of hypotheses

Type I and Type II Errors. Example

Suppose there is a test for a particular disease.

If the disease really exists and is diagnosed early, it can be successfully treated

If it is not diagnosed and treated, the person will become severely disabled

If a person is erroneously diagnosed as having the disease and treated, no physical damage is done.









Testing of hypotheses

Type I and Type II Errors. Example.

Decision	No disease	Disease
Not diagnosed	OK	Type II error
Diagnosed	Type I error	ОК
ated but not harr		irreparable damage would be done

Decision:

to avoid Type error II, have high level of significance



How Do We Control Type I Errors?

- The Type I error rate is controlled by the researcher.
- · It is called the alpha rate, and corresponds to the probability cutoff that one uses in a significance test.
- By convention, researchers use an alpha rate of .05. In other words, they will only reject the null hypothesis when a statistic is likely to occur 5% of the time or less when the null hypothesis is true.
- In principle, any probability value could be chosen for making the accept/reject decision. 5% is used by convention.









Type I & II Error Relationship

Type I and Type II errors cannot happen at the same time

- A Type I error can only occur if H₀ is true
- A Type II error can only occur if H₀ is false

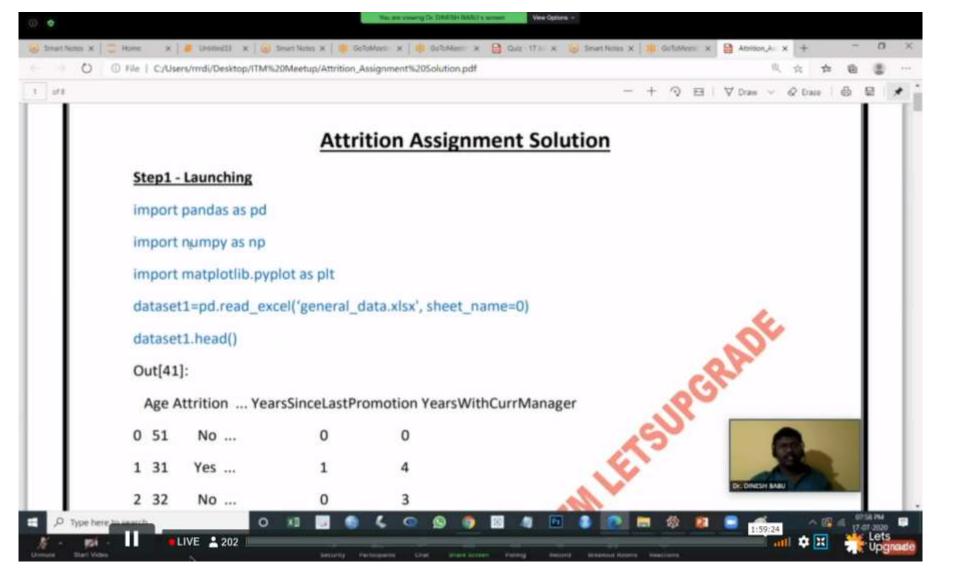
If Type I error probability (α), then
Type II error probability (β)



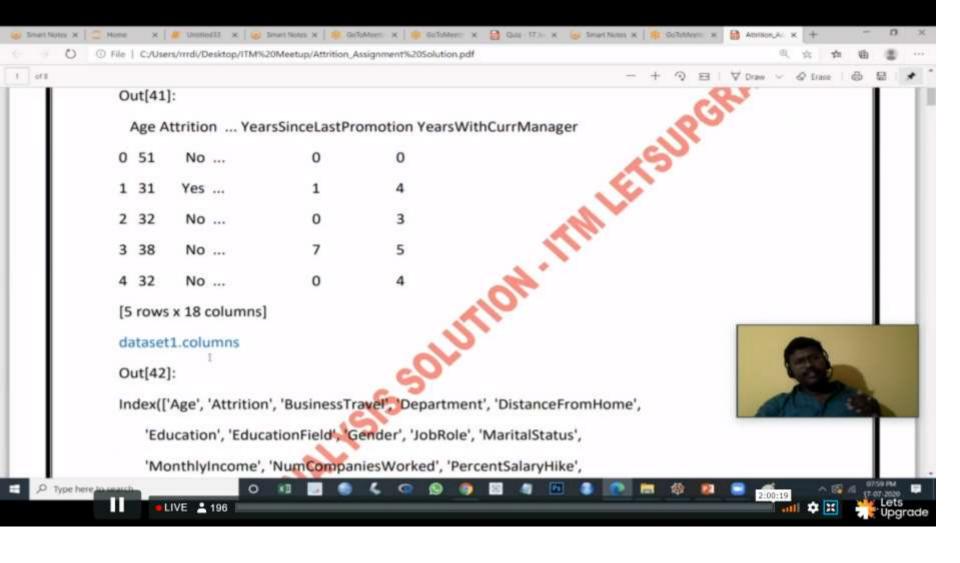
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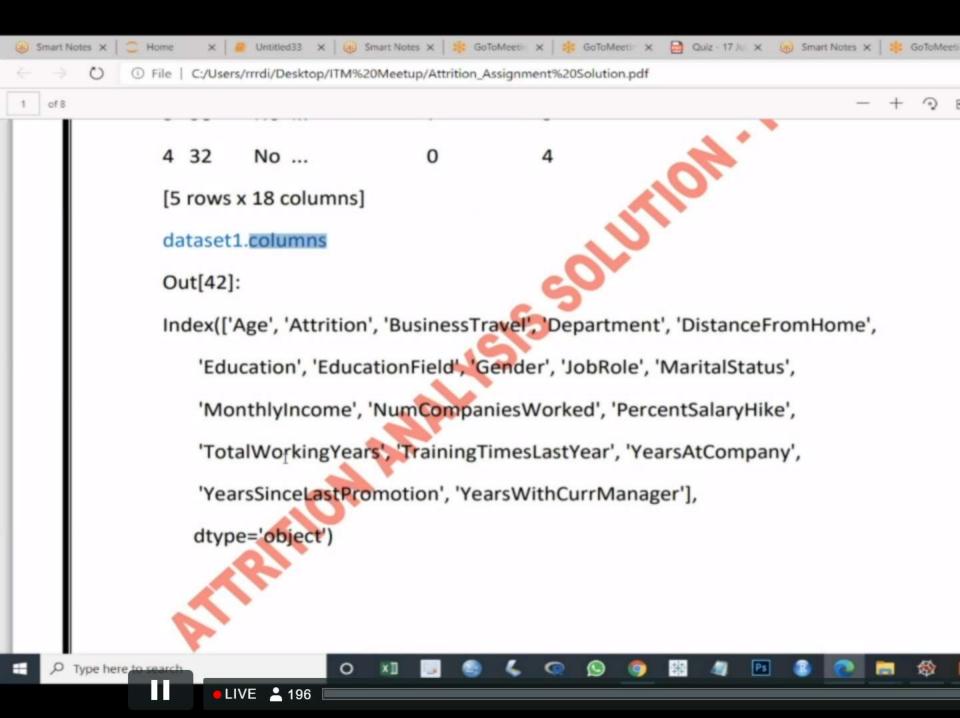


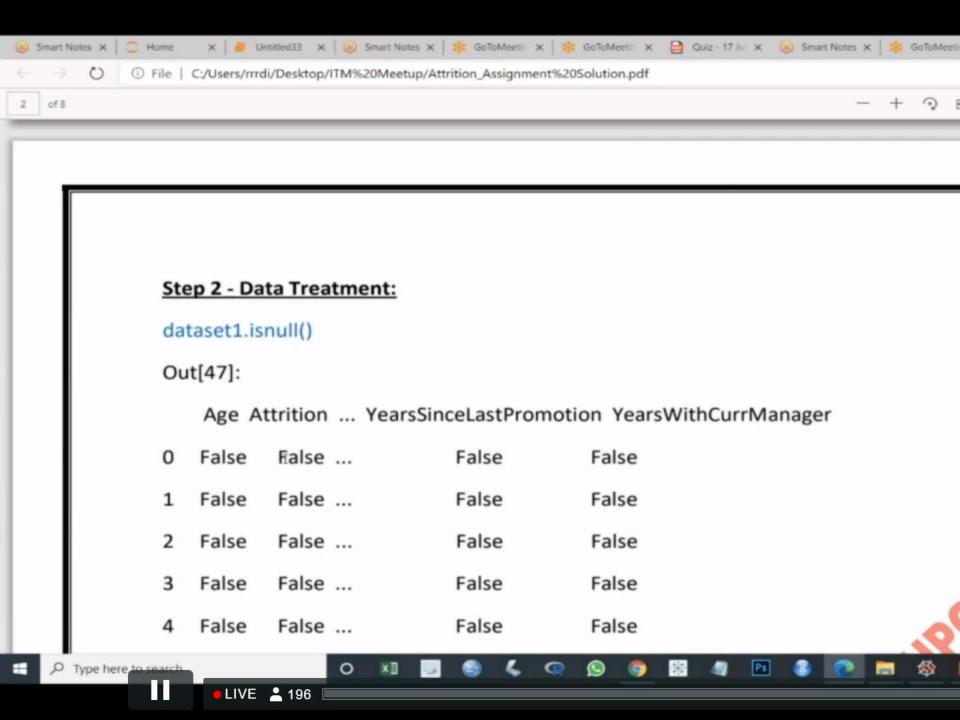


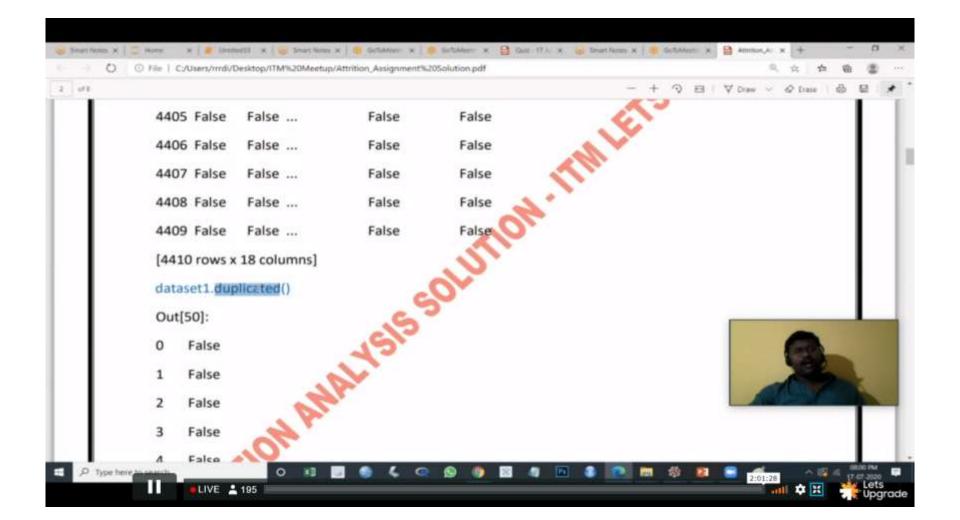


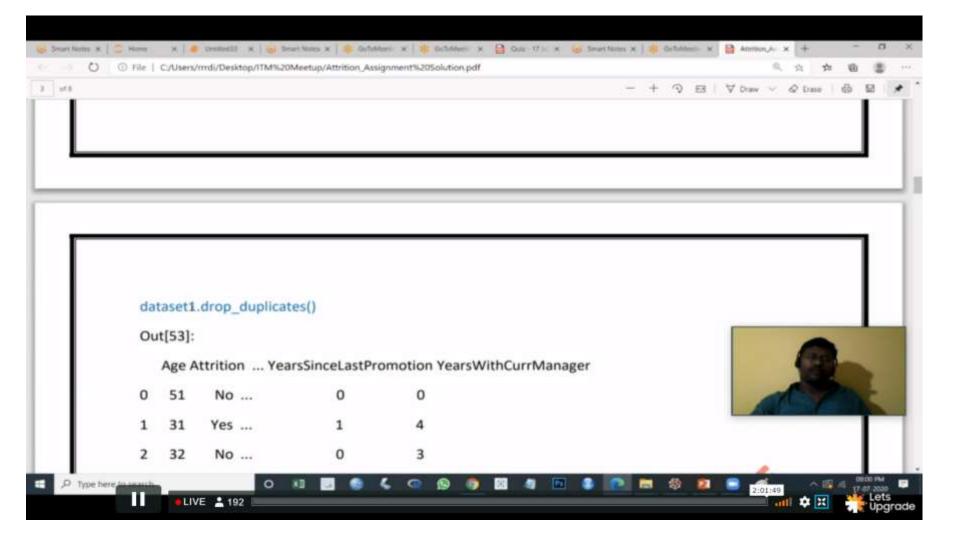
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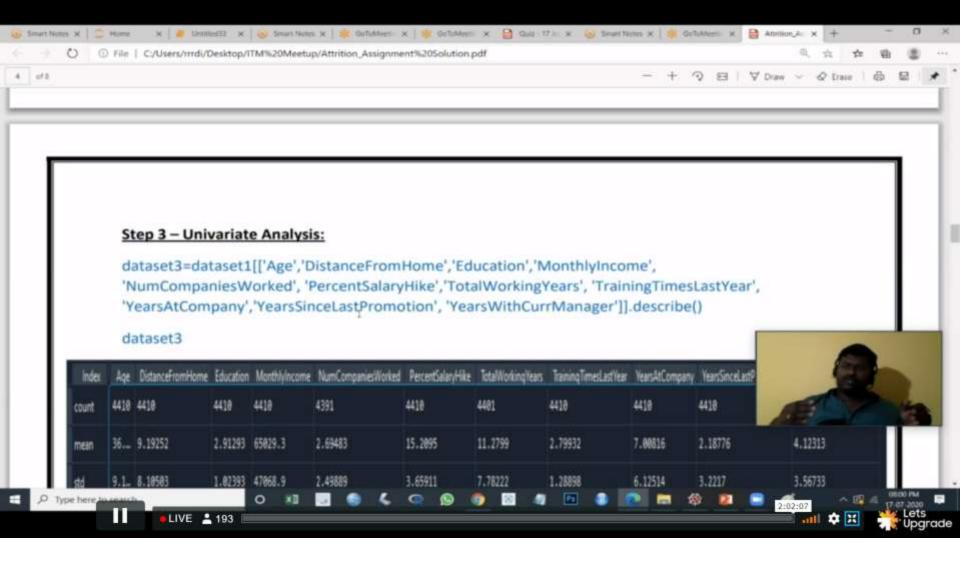


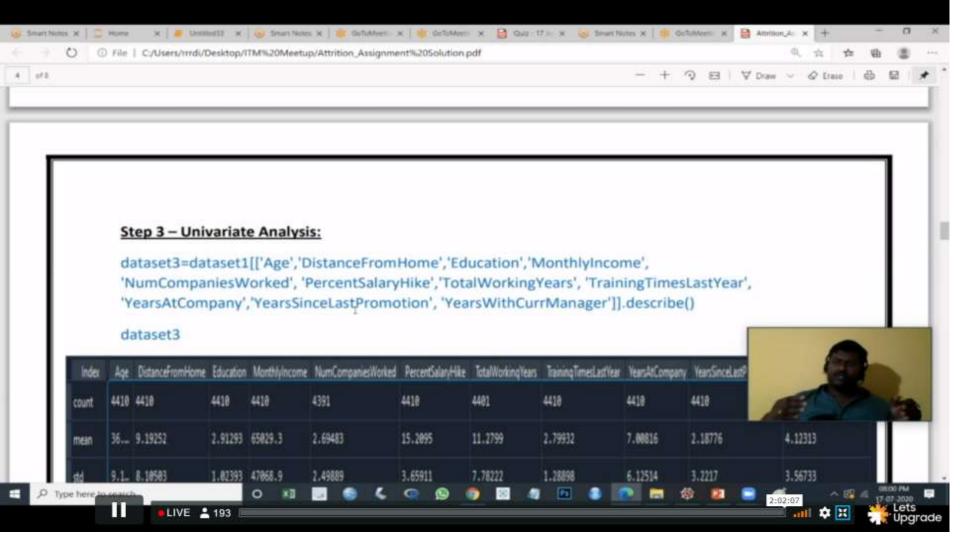


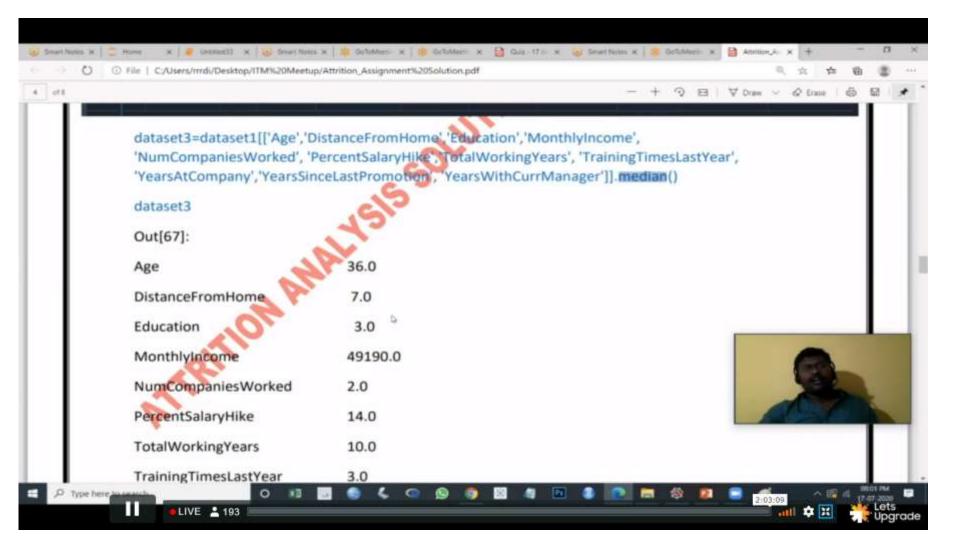


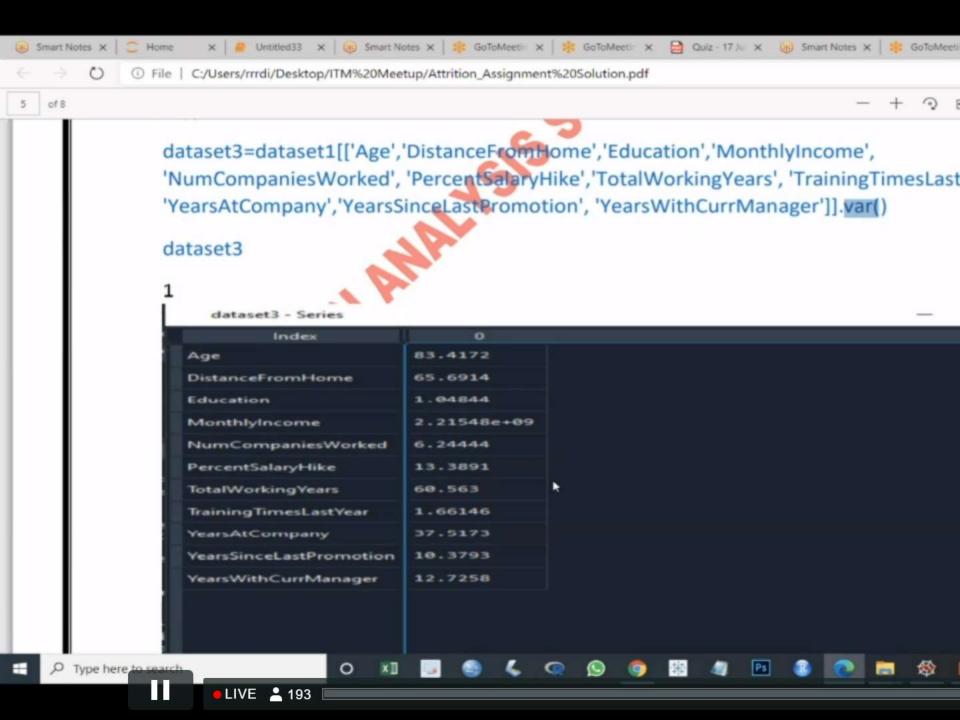


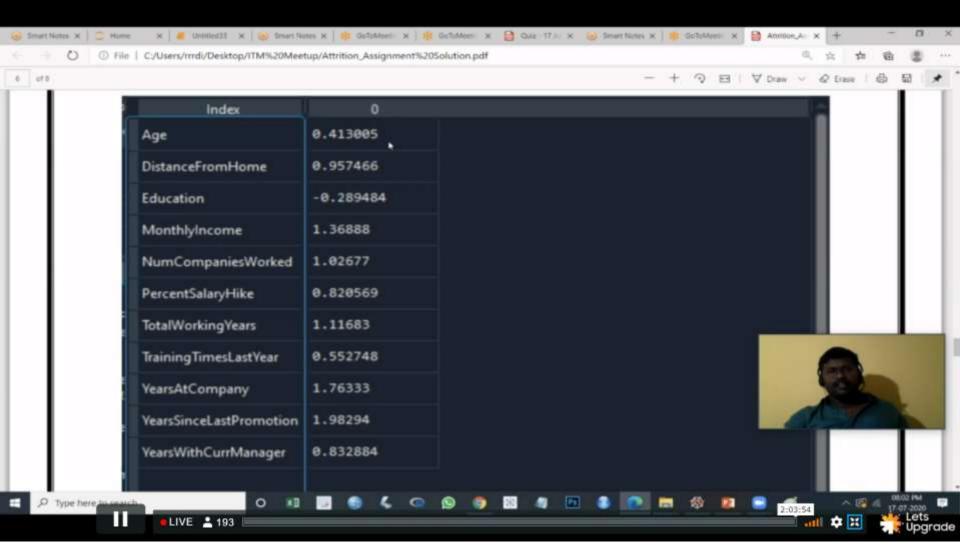




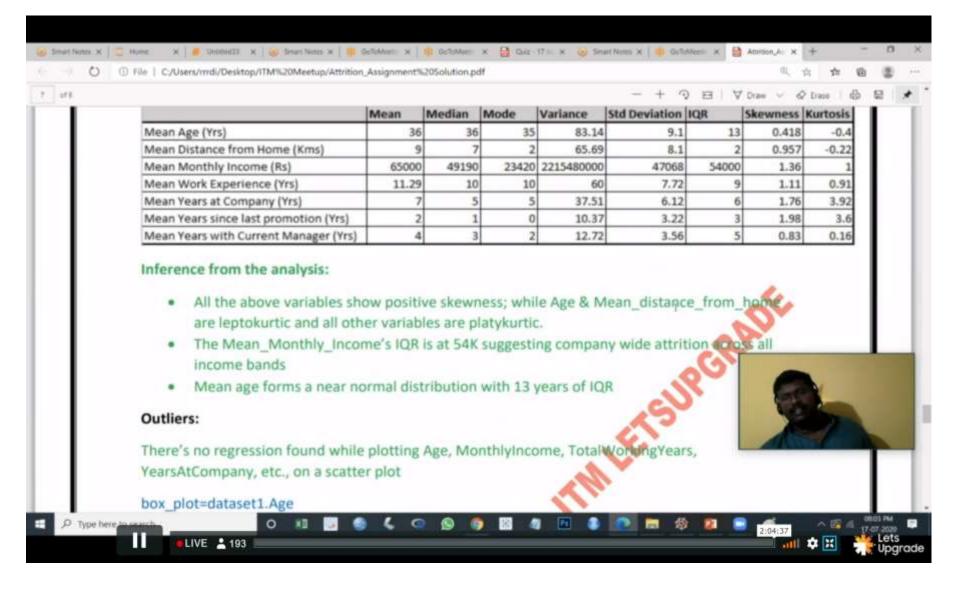


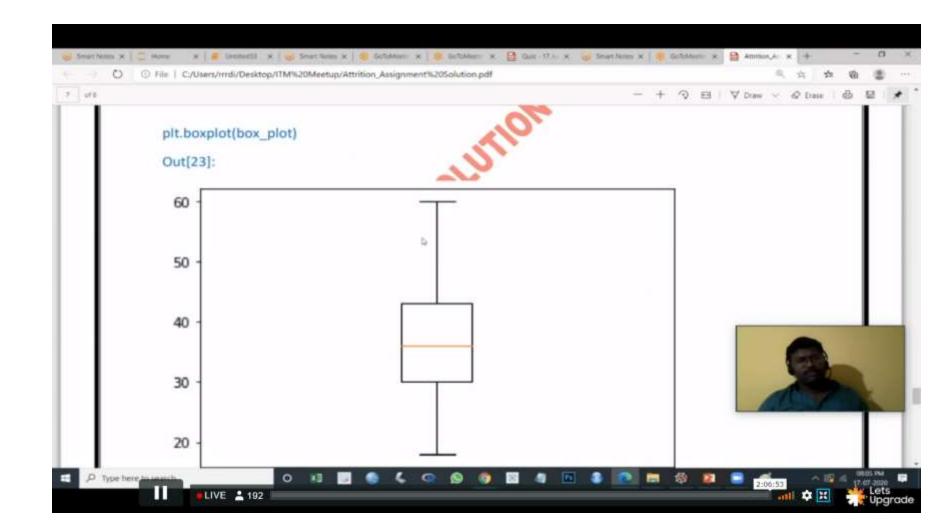


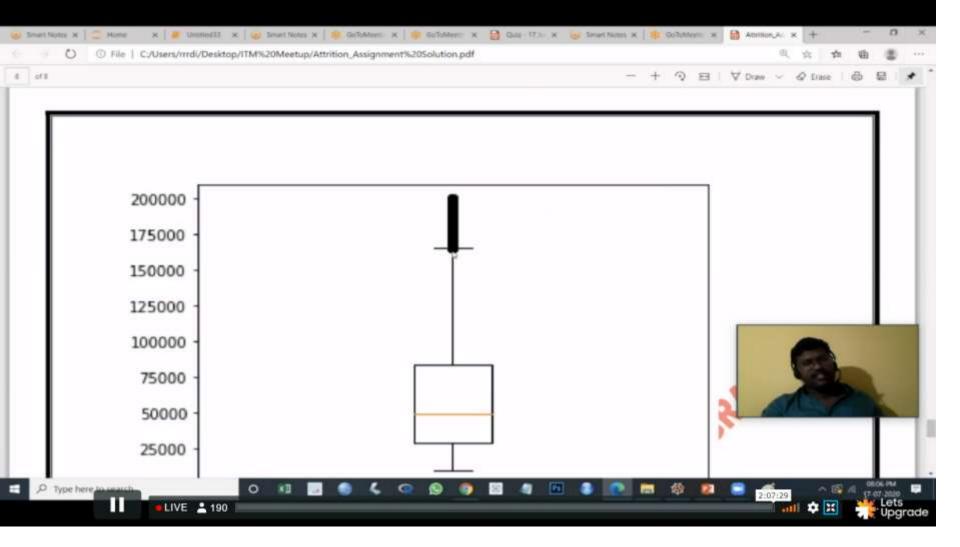




Skewness







Monthly income

