

# **ME 620: Fundamentals of Artificial Intelligence**

## **Lecture 4: Problem Solving as State Space Search - II**



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# Production Systems

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To solve a problem using a production system, we must specify the

1. Global Database
2. Rules
3. Control Strategy

Transforming a problem statement into these three components of a production system is called the representation problem in AI

# Production Systems

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- A production system consists of a collection of productions (rules), a working memory of facts (database) and an algorithm for producing new facts from old.
- A rule becomes eligible to "fire" when its conditions match some set of elements currently in working memory.
  - A control strategy determines which of several eligible rules fires next.

# Production Systems vs. Conventional Computations

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- There are **several differences** between Production System Structure and Conventional Computational Systems that use hierarchically organized programs.
  - The global database can be accessed by all of the rules; no part of it is local to any of them in particular.
  - Rules do not 'call' other rules; communication between rules occurs only through the global database.
- Production System Structure is **modular**; changes to any of the components can be made independently.
- Using Conventional Computation in AI applications is difficult, for any change in knowledge base would **require extensive changes** to the program.

# Production Systems

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## Procedure: Production

```
DATA ← initial database
until DATA satisfies the termination condition;
do
begin
    select some rule R, in the set of rules that
    can be applied to DATA
    DATA ← result of applying R to DATA
end
```

# Control

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- Selecting rules and keeping track of those sequence of rules already tried and the database they produce constitute what we call the **control strategy** for production systems.
- Operations of AI production systems can thus be characterized as a search process in which rules are tried until **some sequence** of them is found that produces a database satisfying the **termination condition**.

# Computational Cost

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- An important characteristics for selecting rules is the amount of information or knowledge about the problem.
- At the uninformed extreme the rule selection is made completely arbitrarily.
- At the informed extreme the control strategy is guided by the problem knowledge great enough to select a correct rule every time.

# Computational Cost

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□ Overall computational cost of a AI Production System is in two major categories

■ Rule Application Cost

Uninformed Control System

Try a large number of rules to find a solution;

High Rule Application Cost

■ Control Strategy Cost

Uninformed Control System

Arbitrary rule selection need not depend on costly computation;

Low Control Strategy Cost



# Computational Cost

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- Overall computational cost of a AI Production System is in two major categories

- Rule Application Cost

- Informed Control System

- Guide Production Systems directly to solution;

- Minimal Rule Application Cost

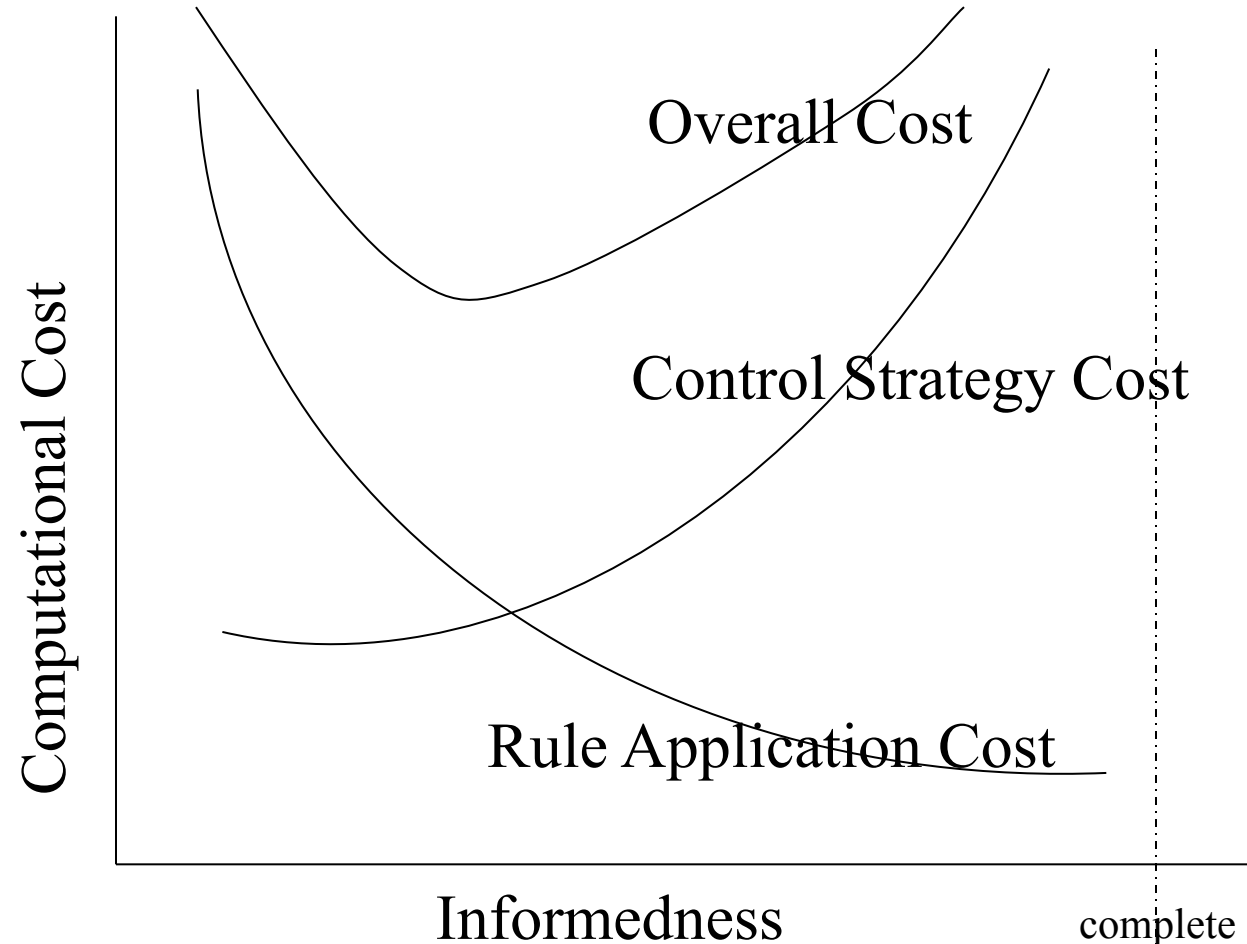
- Control Strategy Cost

- Informed Control System

- To inform about the problem domain, cost in terms of storage and computation;

- High Control Strategy Cost

# Computational Cost



# Computational Cost

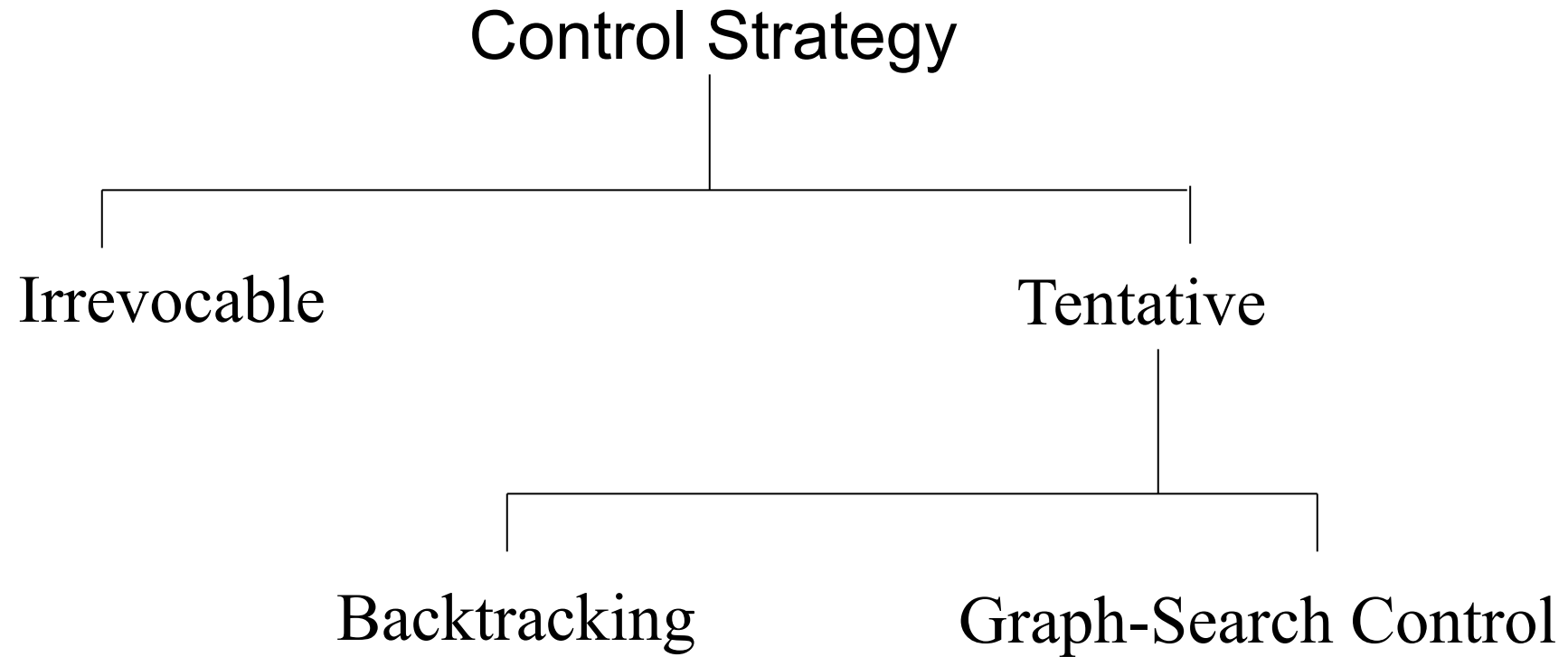
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- Overall computation cost of an AI production system is the combined **rule application cost** and **control strategy cost**.
  - Part of the art of designing efficient AI systems is deciding how to balance the above two costs.
- An important aspect of AI system design involves the use of **techniques** that allow the control strategy to use a **large amount of problem information** without incurring excessive control cost.

# Control Strategy

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# Control Strategy

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**Irrevocable** - Applicable rule is applied without provision for reconsideration later.

**Tentative** - Applicable rule is applied, but provision is made to return later to this point in the computation to apply some other rule.

■ **Backtracking:** Point is established; state of computation can revert to this point.

■ **Graph-Search:** Provision is made for keeping track of effects of several sequences of rules simultaneously.

# Production System

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The production system used for solving the 8-Puzzle worked **from the initial state to a goal state**. Such a production system is called a **forward production system**.

A production system that worked by **starting at the goal state**, applying inverse moves and **reaching the initial state** is a **backward production system**.

# Production System

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Clear States  
and Goals

**State** descriptions as  
the global database.  
**F-rules**

Forward Production  
System

**Goal** descriptions as  
the global database  
**B-rules**

Backward  
Production System

# Specialized Production System

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## Commutative Production Systems

Order in which a set of applicable rules is applied to a database is unimportant.

## Decomposable Production Systems

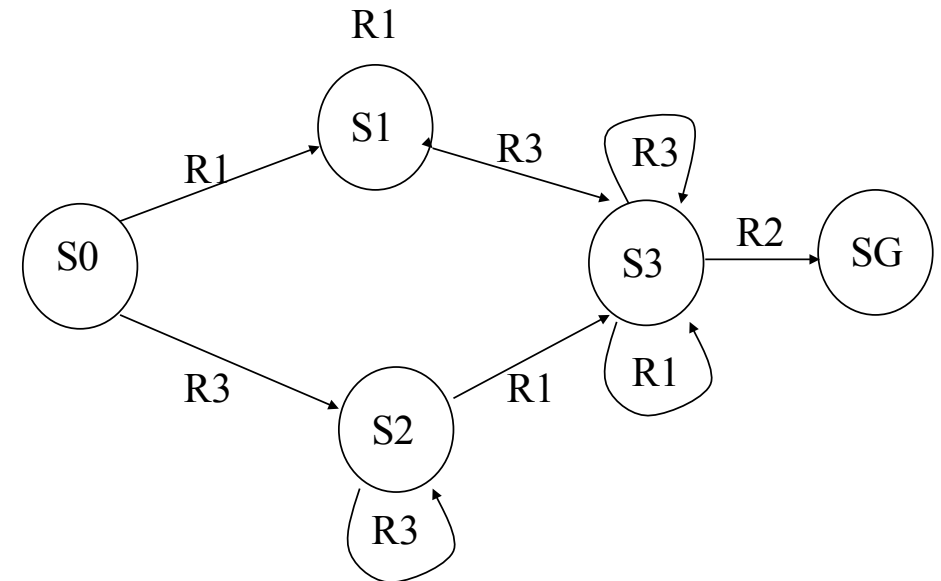
Initial database can be decomposed or split into separate components that can be processed independently.



# Commutative Production System

A production system is commutative if it has the following properties with respect to a database  $D$

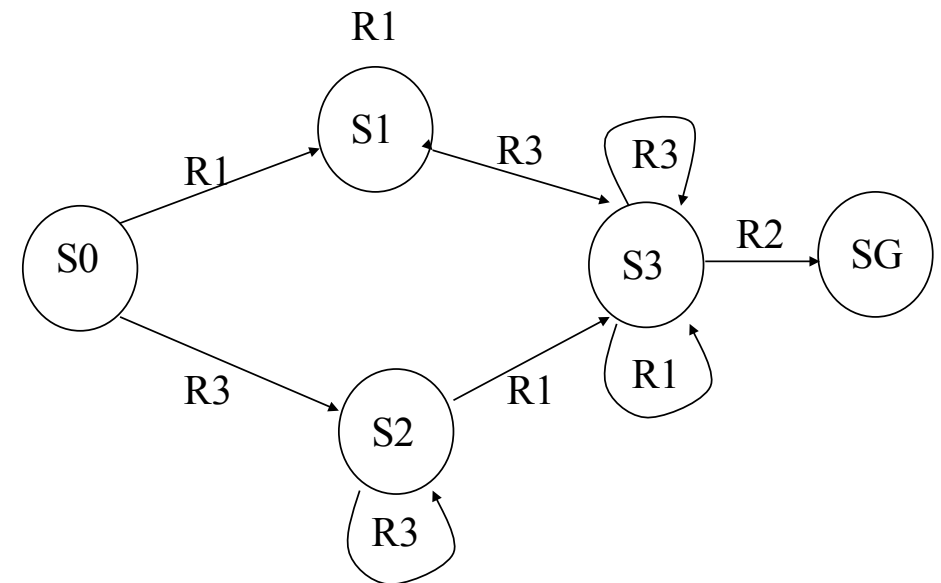
Each member of the set of rules applicable to  $D$  is also applicable to any database produced by applying an applicable rule to  $D$ .



# Commutative Production System

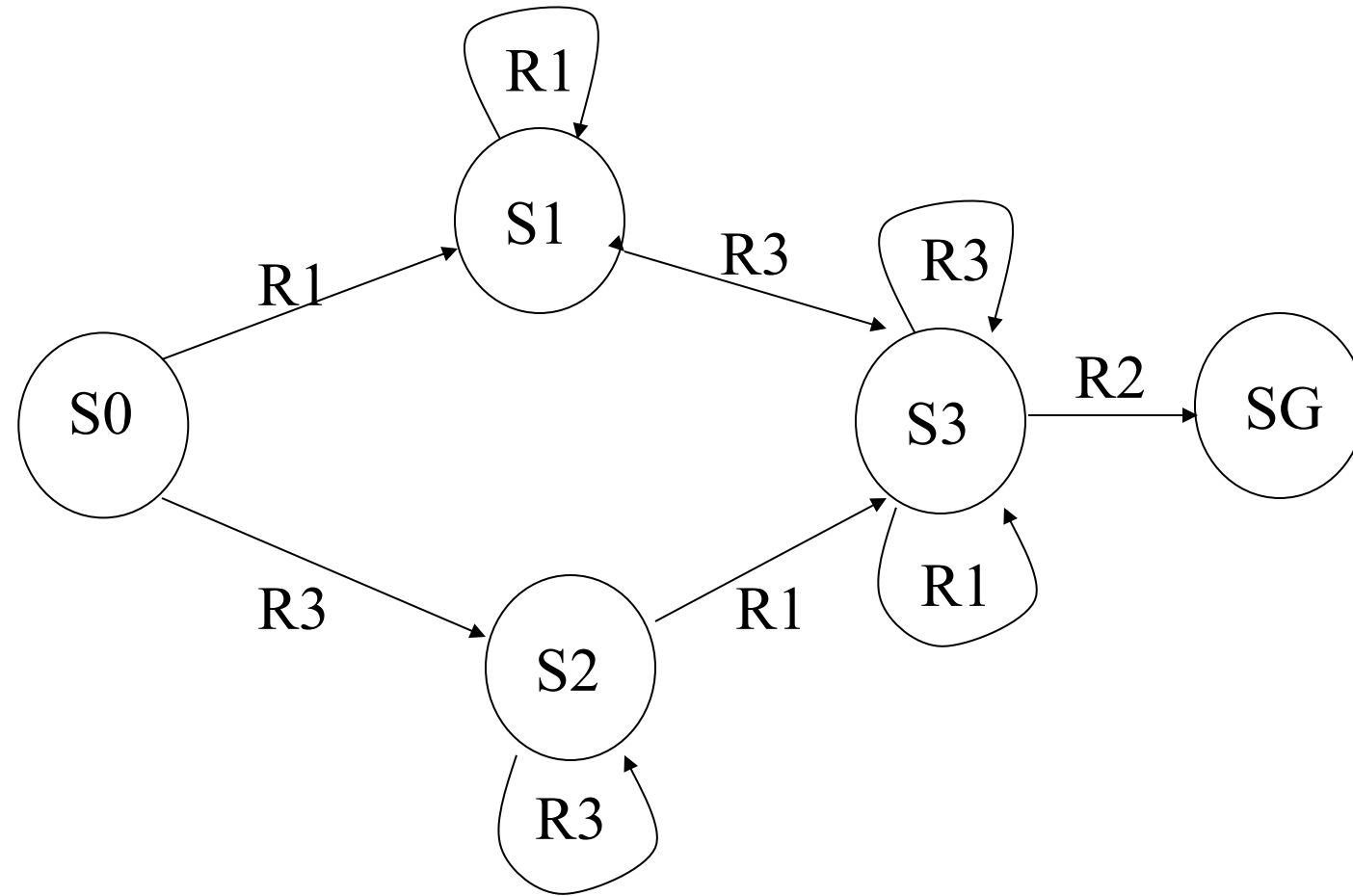
A production system is commutative if it has the following properties with respect to a database D

If the **goal condition is satisfied by D**, then it is also satisfied by any database produced by applying any applicable rule to D.





# Commutative Production System



# Commutative Production System

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Commutative production systems are an important subclass and have the following properties

An **irrevocable control regime** can always be **used** in a commutative system because the application of a rule never needs to be taken back or undone.

No need of a mechanism for applying **alternative sequence of rules**. Rule that is applicable to an earlier DB is applicable to the current one.

Applying an **inappropriate rule delays**, but never prevents termination.

# Decomposable Production System

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Consider a system - initial database is  $(C, B, Z)$ .

The production rules are based on following rewrite rules

R1:  $C \longrightarrow (D, L)$

R2:  $C \longrightarrow (B, M)$

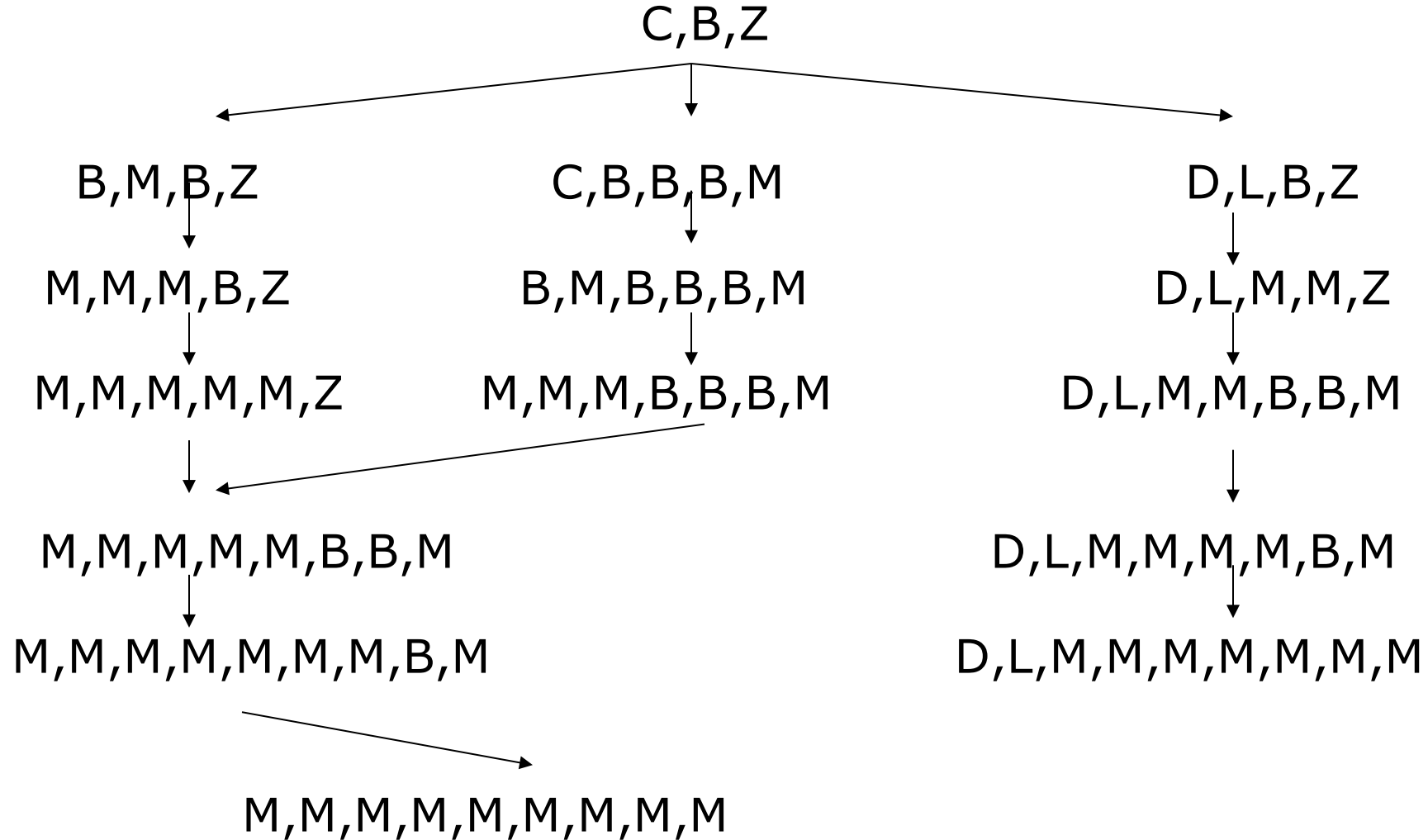
R3:  $B \longrightarrow (M, M)$

R4:  $Z \longrightarrow (B, B, M)$

Termination condition is that the database contains only Ms

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# Decomposable Production System



# Decomposable Production System

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A graph-search control strategy might **explore many equivalent paths** in producing a database containing only Ms.

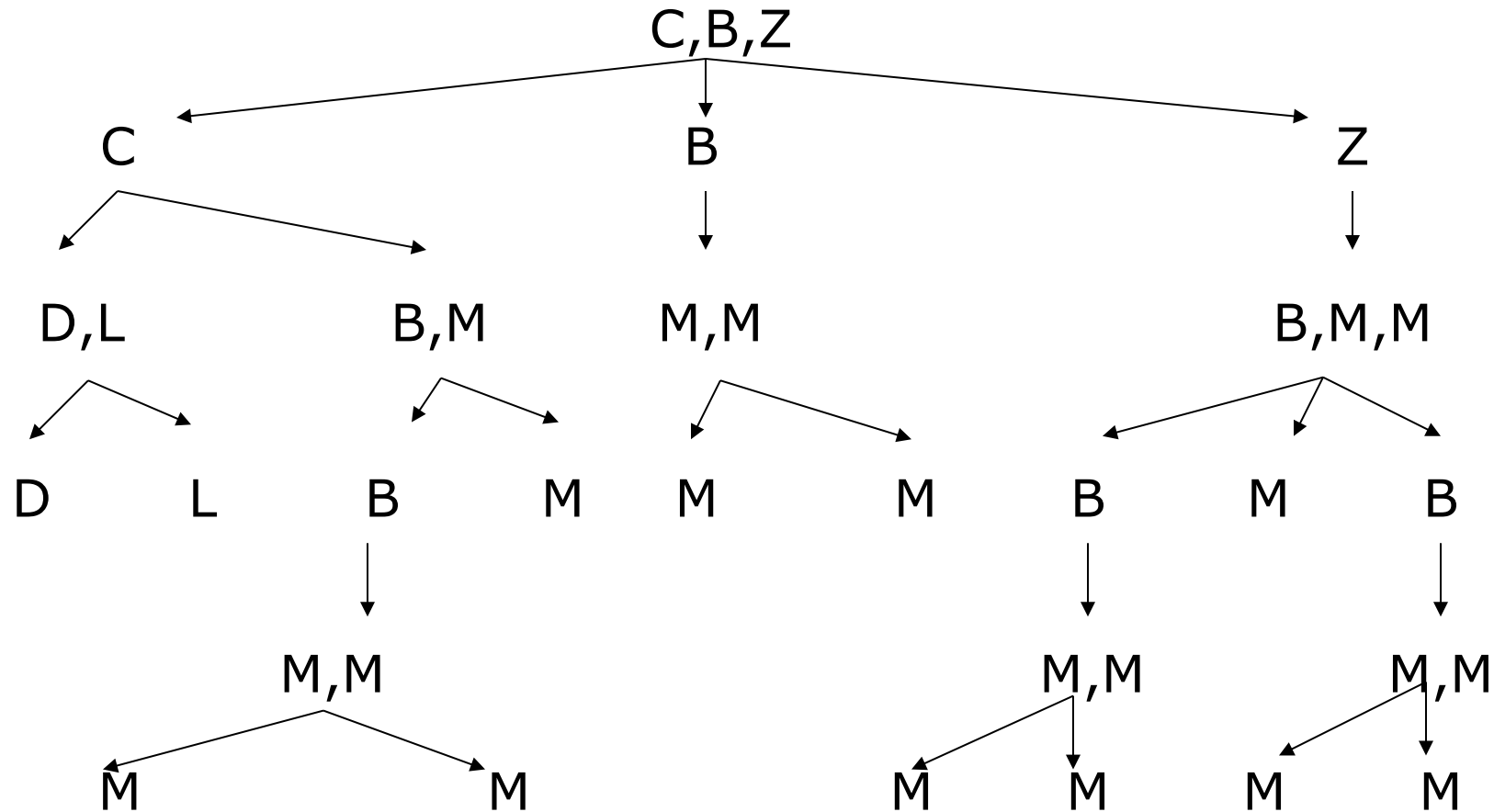
**Redundant paths** can lead to inefficiencies because the control strategy might attempt to explore all of them; worse it might do work that is wasted ultimately in **exploring paths that do not terminate!**

One way to avoid the exploration of these redundant paths is to recognize that the initial database can be **decomposed** or **split** into separate components that can be processed independently.

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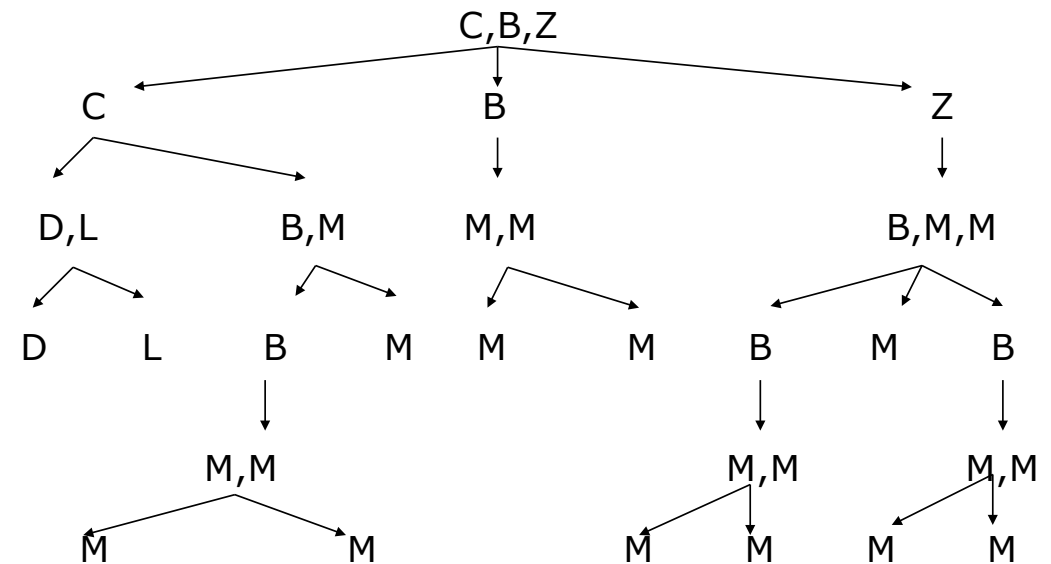


# Decomposable Production System



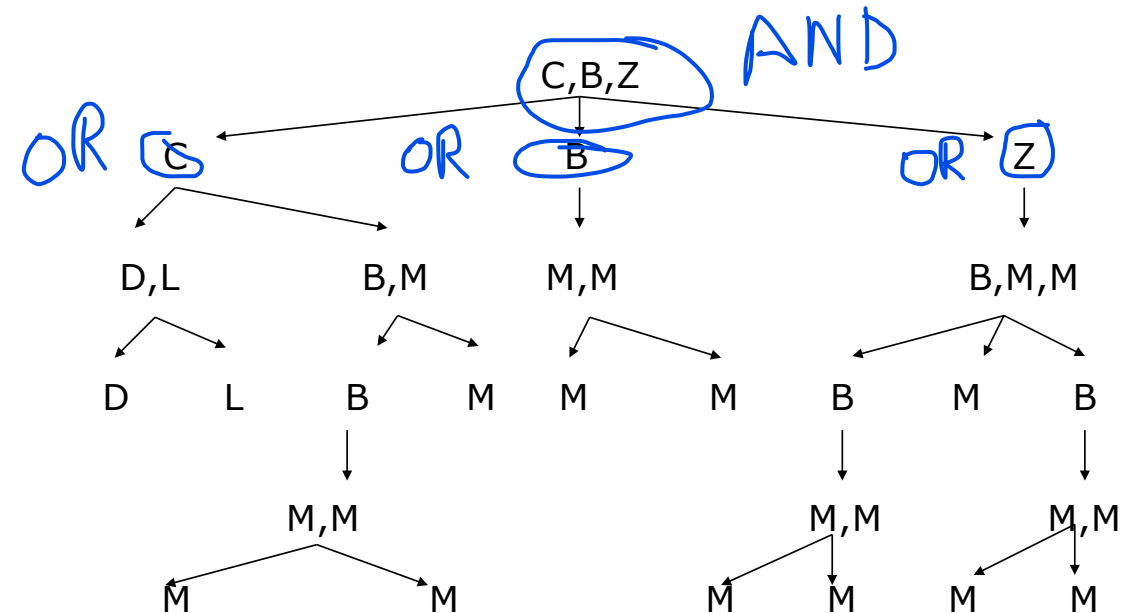
# AND-OR Graph

Nodes labeled by component databases have sets of successor nodes each labeled by one of the components. These nodes are called **AND nodes** because in order to process the compound database to termination **all of the component database must be processed** to termination.



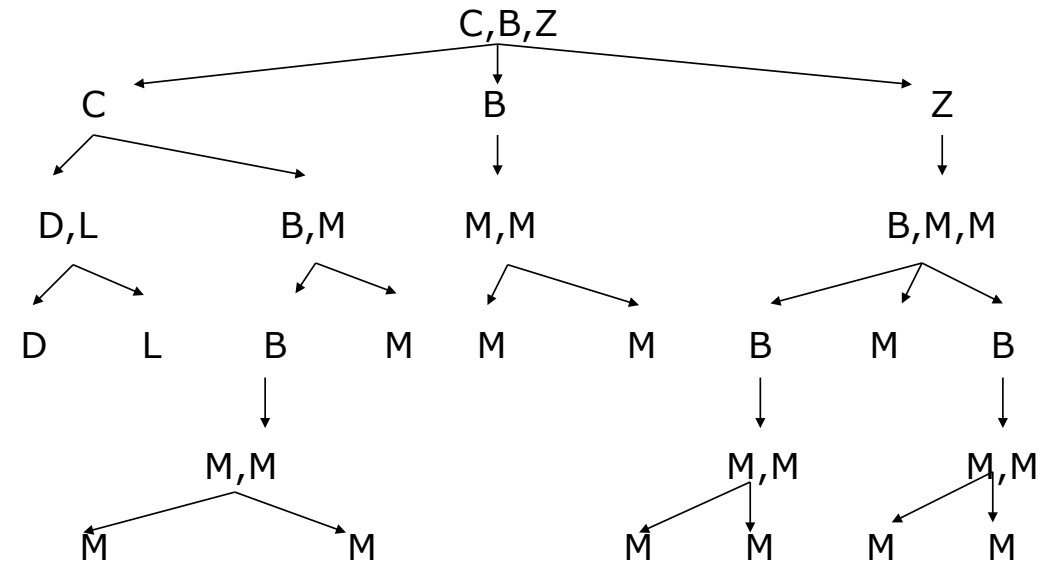
# AND-OR Graph

Successor nodes labeled by the result of rule application are called **OR nodes** because in order to process a component database to termination, the database resulting from **just one** of the rule application **must be processed to termination**.

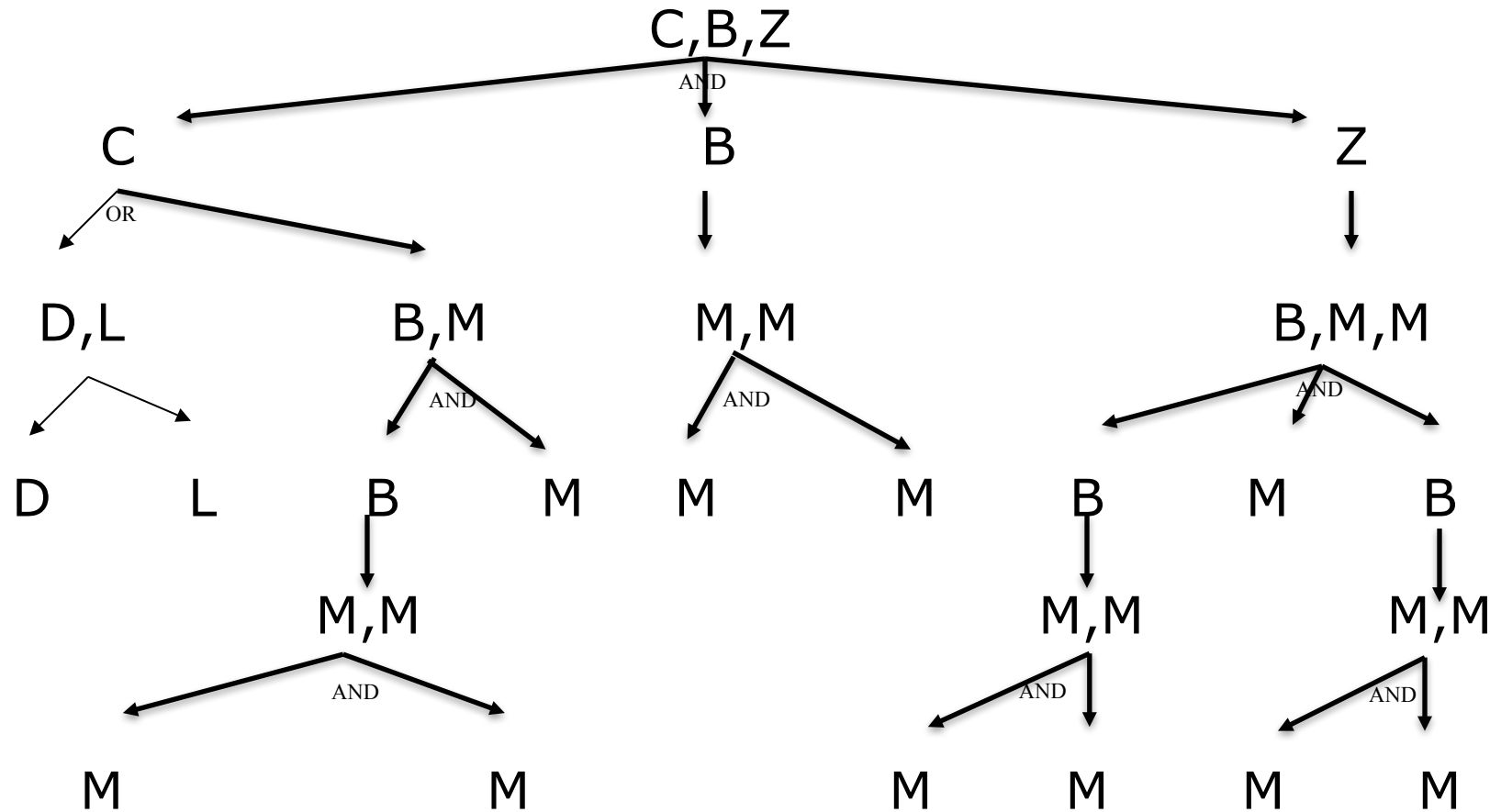


# AND-OR Graph

Structures called **AND-OR graphs** are useful for depicting the activity of production systems under the control regime of decomposable production systems.



# Decomposable Production System



# Decomposable Production System

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- The notion of Decomposable Production System encompasses a technique often called **Problem Reduction** in AI.
- Problem Reduction idea usually **involves replacing a problem goal by a set of subgoals** such that if the subgoals are solved, the main goal is also solved.
- Explaining problems in terms of decomposable production systems **allows us to be indefinite** about whether we are **decomposing problem goals or problem states**.

# Knowledge of the Problem Domain

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- ❑ Efficient AI systems **require knowledge of the problem domain**. This knowledge can be subdivided into three broad categories
  - **Declarative Knowledge**
    - ❑ Knowledge about a problem that is represented in the global database. Declarative knowledge includes specific facts!
  - **Procedural Knowledge**
    - ❑ Knowledge about a problem that is represented in the rules! General information that allows us to manipulate the declarative knowledge.
  - **Control Knowledge**
    - ❑ Includes knowledge about a variety of processes, strategies and structures used to coordinate the entire problem-solving process.