

## QUICK SORT - Steps:

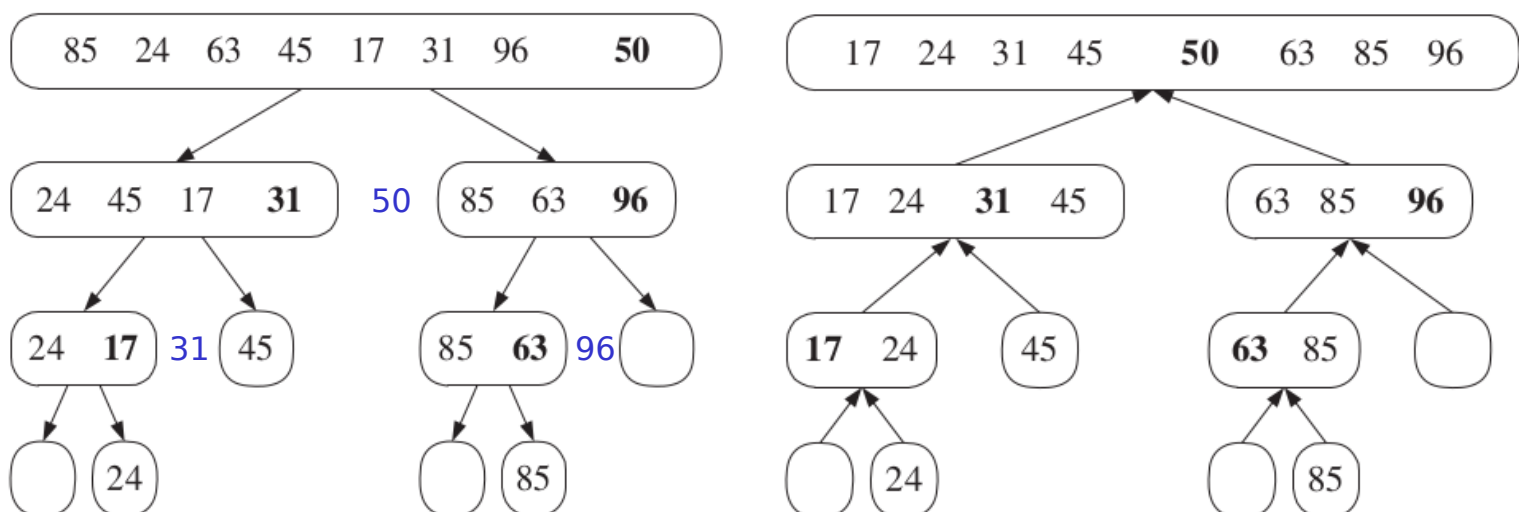
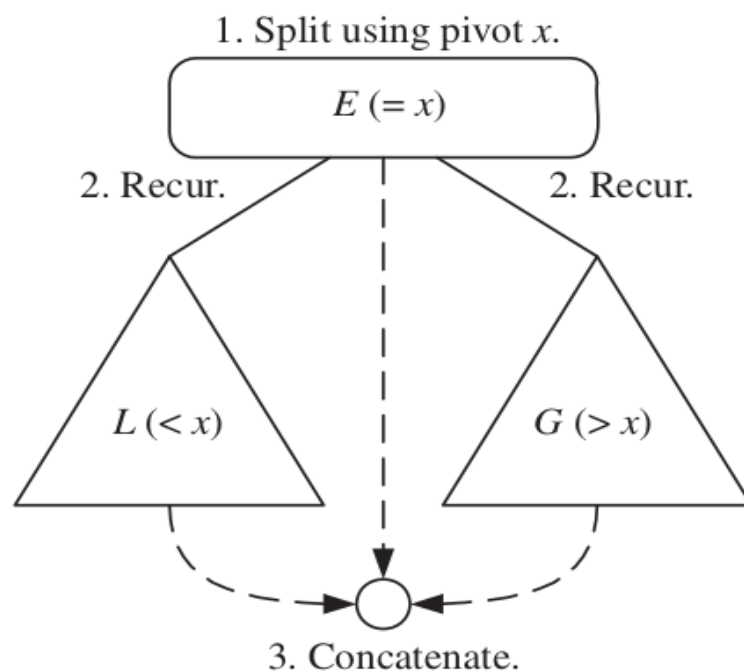
1. **Divide:** If  $S$  has at least two elements (nothing needs to be done if  $S$  has zero or one element), select a specific element  $x$  from  $S$ , which is called the **pivot**. As is common practice, choose the pivot  $x$  to be the last element in  $S$ . Remove all the elements from  $S$  and put them into three sequences:

- $L$ , storing the elements in  $S$  less than  $x$
- $E$ , storing the elements in  $S$  equal to  $x$
- $G$ , storing the elements in  $S$  greater than  $x$ .

(If the elements of  $S$  are all distinct,  $E$  holds just one element—the pivot.)

2. **Recur:** Recursively sort sequences  $L$  and  $G$ .

3. **Conquer:** Put the elements back into  $S$  in order by first inserting the elements of  $L$ , then those of  $E$ , and finally those of  $G$ .



{85 24 63 45 50 31 96 17}

{85 24 63 45 17 31 50 96}

L={} E={17} G={85 24 63 45 50 31 96}

L={85 24 63 45 31 50} E={96} G={}

```
partition (arr[], low, high)
{
    pivot = arr[high];
    i = (low - 1)
    for (j = low; j < high; j++)
    {
        // If current element is smaller than the pivot
        if (arr[j] < pivot)
        {
            i++; // increment index of smaller element
            swap arr[i] and arr[j]
        }
    }
    swap arr[i+1] and arr[high])
    return (i + 1)
}
```

Initial: 85 24 63 45 17 31 96 50  
low = 0, high = 7

Pivot: arr[7] = 50

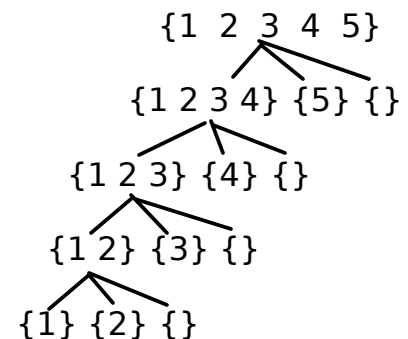
i = 3  
j = 6

85 24 63 45 17 31 96 50  
24 85 63 45 17 31 96 50  
24 45 63 85 17 31 96 50  
24 45 17 85 63 31 96 50  
24 45 17 31 63 85 96 50  
24 45 17 31 50 85 96 63

24 45 17 31 | 50 | 85 96 63

```
/* low --> Starting index, high --> Ending index */
quickSort(arr[], low, high)
{
    if (low < high) // i.e. if arr[] is of length >= 2
    {
        pi = partition(arr, low, high);
        /* pi is partitioning index, i.e. index of pivot */

        quickSort(arr, low, pi - 1); // Before pi, i.e. L
        quickSort(arr, pi + 1, high); // After pi, i.e. G
    }
}
```



Worst case time complexity:

(n-1) levels, and  
O(n) operations at each level  
(counted over all partition functions)  
= O(n<sup>2</sup>)

```
partition (arr[], low, high)
{
    pivot = arr[high];
    i = low
    for (j = low; j < high; j++)
    {
        // If current element is smaller than the pivot
        if (arr[j] < pivot)
        {
            swap arr[i] and arr[j]
            i++; // increment index of smaller element
        }
    }
    swap arr[i] and arr[high])
    return (i)
}
```

Best case time complexity:

O(log(n)) levels, and  
O(n) operations at each level  
(counted over all partition functions)  
= O(n log(n))

Average case time complexity:  
O(n log(n))