



**BITS Pilani**  
Pilani Campus

# Blockchain Technology (BITS F452)

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# *Proof of Work*

# Remaining Problems

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How to pick a random node?

How to avoid a free-for-all due to rewards?

How to prevent the Sybil attack?

Are of these problems are related and have same solution :  
**Proof of Work**

# Proof of Work



To approximate selecting a random node  
select node in proportion to a resource that no one can monopolize (we hope)

- In proportion to computing power : Proof-of-Work
- In proportion to ownership: Proof-of-stake

**Idea:** allow nodes to compete with each other using their computing power that implies the nodes automatically being picked in that proportion

# Equivalent views of POW

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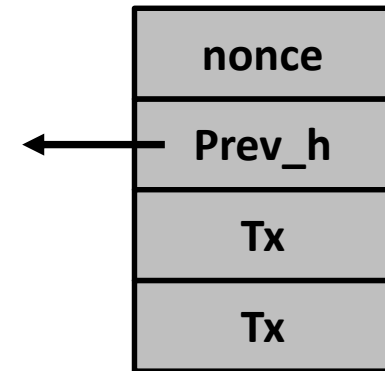


1. Select nodes in proportion to computing power
2. Let nodes compete for right to create blocks
3. Make it moderately hard to create new identities  
protection against Sybil attack

# Hash Puzzles

To create block, find nonce (a random value) such that

$$H(\text{nonce} \parallel \text{prev\_hash} \parallel \text{tx} \parallel \text{tx} \parallel \dots \parallel \text{tx}) < \text{target}$$



Output space of hash



**If hash function is secure:  
Only way to succeed is to try enough nonces until  
you get lucky**

# POW property 1: difficult to compute

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As of Feb 2022 the bitcoin difficulty is  **$26.69 \times 10^{12}$**  hashes

It requires approximately  **$2.7 \times 10^{15}$**  hashes to create one BITCOIN

Only some nodes bother to compete - minors

# POW property 2: parameterizable cost



Nodes automatically re-calculate the target every two weeks

Goal average time between blocks = 10 minutes

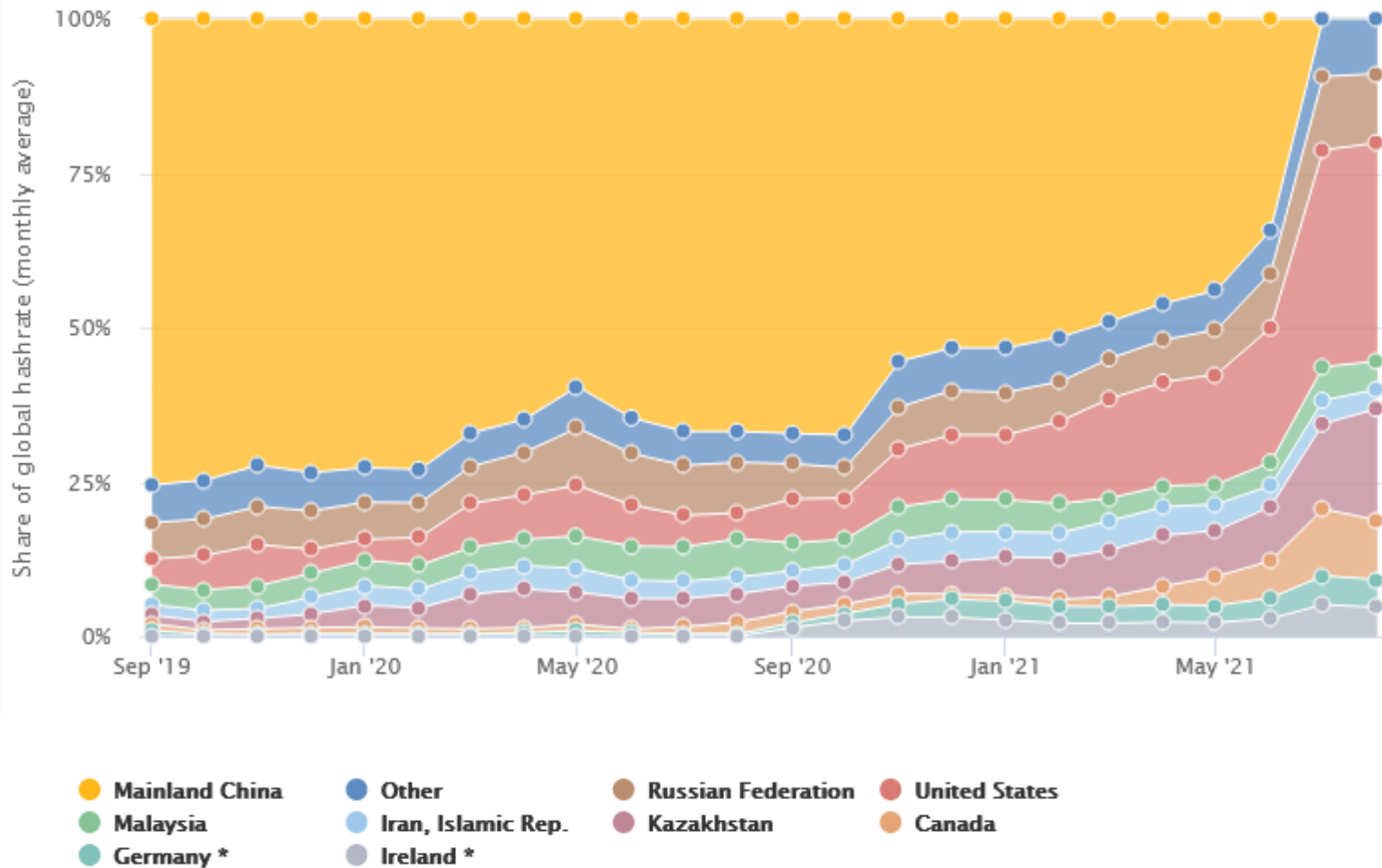
Each 2016-block interval is known as a ***difficulty epoch***. At the beginning of every epoch the Bitcoin network recalculates the Current Target.

If if you put a fixed amount of H/W for mining the rate at which you find the block depends upon the total computer power available with others

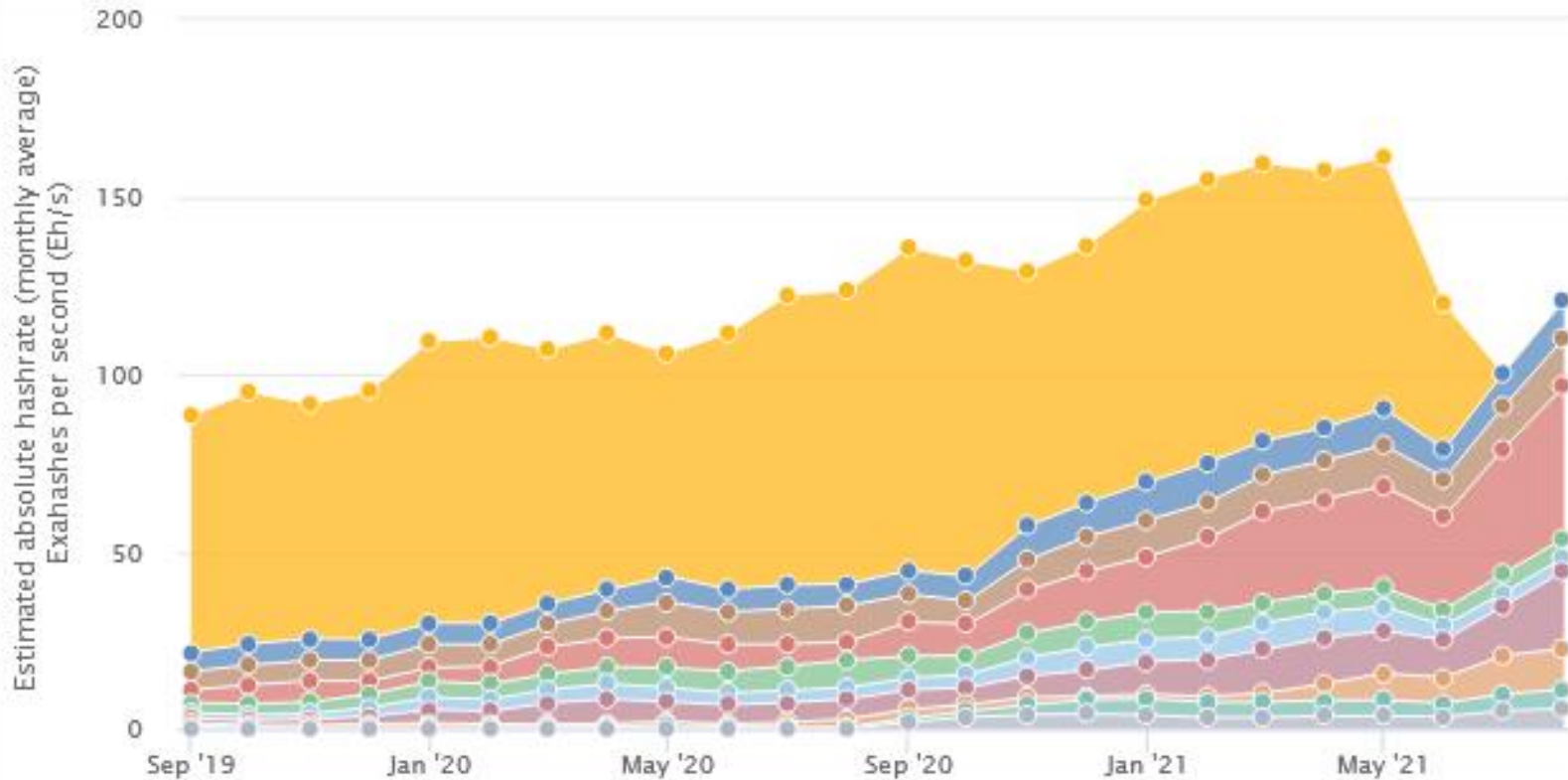
Prob (Alice wins the next block) = fraction of global hash power she controls



- Distribution of Bitcoin mining by country



# BTCOIN Global Hashrate



- |                  |                      |                      |                 |
|------------------|----------------------|----------------------|-----------------|
| ● Mainland China | ● Other              | ● Russian Federation | ● United States |
| ● Malaysia       | ● Iran, Islamic Rep. | ● Kazakhstan         | ● Canada        |
| ● Germany *      | ● Ireland *          |                      |                 |

# Key Security Assumptions

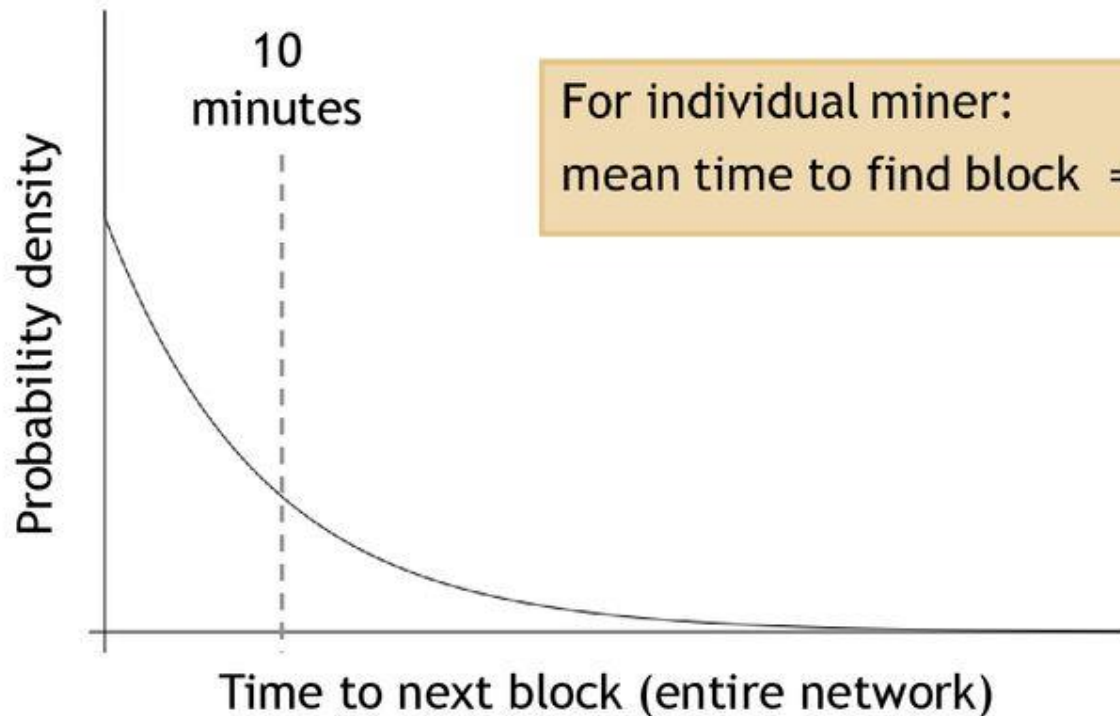
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Attacks infeasible if majority of minors  
weighted by hash power follow the protocol

This will ensure a more than 50% chance  
that the next node is proposed by a honest  
node

# Solving hash puzzles is probabilistic



For individual miner:

$$\text{mean time to find block} = \frac{10 \text{ minutes}}{\text{fraction of hash power}}$$

## PoW property 3: trivial to verify

Nonce must be published as part of block

Other miners simply verify that

$H(\text{nonce} \ \text{prev\_hash} \ \text{tx} \ \dots \ \text{tx}) < \text{target}$

Advantage?

No centralized verifier needed! Any node or miner can verify that the block was correctly mined

# Mining economics

$$\text{If mining reward (block reward + Tx fees)} > \text{mining cost (hardware + electricity cost)} \rightarrow \text{Profit}$$

## Complications:

- Fixed (hardware) vs. variable (electricity) costs
- Reward depends on rate at which miners propose blocks (ratio of their hash rate to the global hash rate)
- Cost in dollars, but reward in BTC  $\rightarrow$  profit depends on exchange rate

Recap

Identities

Block chain & consensus

Transactions

Hash puzzles & mining

P2P network

# Bitcoin has three types of consensus

- Value
- State
- Rules



# Bitcoin is bootstrapped

