

Input: { 1, 4, 7, 5, 2, 3 }

Output: { 1, 2, 3, 4, 5, 7 }

Inversions:

(4, 2)

(4, 3)

(7, 5)

(7, 2)

(7, 3)

(5, 2)

(5, 3)

Insertion Sort --

Initial : 1 4 7 5 2 3

Pass 1: 1 4 | 7 5 2 3 4 > 1

Pass 2: 1 4 7 | 5 2 3 7 > 4

Pass 3: 1 4 5 7 | 2 3 5 < 7, 5 > 4

Pass 4: 1 2 4 5 7 | 3 2 < 7, 2 < 5, 2 < 4, 2 > 1

Pass 5: 1 2 3 4 5 7 3 < 7, 3 < 5, 3 < 4, 3 > 2

Pass 4: j=3, j=2, j=1, j=0

Elements at indices (j+1) to (i-1) to be shifted

1 4 5 7 2 3

1 4 5 \_ 7 3 tmp <- 2

1 4 \_ 5 7 3 tmp <- 2

1 \_ 4 5 7 3 tmp <- 2

1 2 4 5 7 3

InsertionSort( int[] A, int n )

Input: An array A containing  $n \geq 1$  integers

Output: The sorted version of the array A

for i = 1 to (n-1)

{

j <- i - 1 { 4, 1, ... }

while A[i] < A[j]

j <- j - 1

if j < 0

break

tmp <- A[i]

// shift all elements > A[i] by 1 position

k = i - 1

while k >= j+1

{

A[k+1] <- A[k]

k <- k - 1

}

// insert A[i] in position (j+1)

A[j+1] <- tmp

}

return A

Worst case complexity =  $O(n^2)$

Best case complexity =  $O(n)$

Input: { 7, 5, 4, 3, 2, 1 }

Output: { 1, 2, 3, 4, 5, 7 }

Insertion Sort --

Initial : 7 5 4 3 2 1

Pass 1: 5 7 | 4 3 2 1 5 < 7

Pass 2: 4 5 7 | 3 2 1 4 < 7, 4 < 5

Pass 3: 3 4 5 7 | 2 1 3 < 7, 3 < 5, 3 < 4

Pass 4: 2 3 4 5 7 | 1

Pass 5: 1 2 3 4 5 7

InsertionSortOptimized( int[] A, int n )

Input: An array A containing  $n \geq 1$  integers

Output: The sorted version of the array A

for i = 1 to (n-1)

{

inversions = 0

for j = 0 to (n-1)

if A[j] > A[j+1]

inversions <- inversions + 1

if inversions == 0:

break

j <- i - 1

while A[i] < A[j]

j <- j - 1

if j < 0

break

tmp <- A[i]

// shift all elements > A[i] by 1 position

k = i - 1

while k >= j+1

{

A[k+1] <- A[k]

k <- k - 1

}

// insert A[i] in position (j+1)

A[j+1] <- tmp

}

return A

Worst case complexity =  $O(n^2)$

Best case complexity =  $O(n)$