

MID SEM REGULAR

Q1.

SET A

Correct order should be:--

$3\log(\log(n))$, $5\log(n^2) + 3$, $(4n)^{0.5}$, $2^{\log(8n)}$, $13n(\log(n))^3$, $4n(\log(n))^4$, $2n^3 + 9n + 7$, $5n^{11} + 2$, $33^{(n+3)}$, n^3 , $1001n^{(n/2)}\log(n)$

SET B

Correct order should be:--

$7\log(\log(n))$, $6\log(n^3) + 2$, $(3n)^{0.25}$, $17n(\log(n))^2$, $5n(\log(n))^3$, $4^{\log(4n)}$, $3n^5 + 7n + 4$, $8n^{13} + 3$, $22^{(n-2)}$, n^2 , $909n^{(n/3)}\log(n)$

SET C:

correct ans should be:--

$5\log(\log n)$, $7\log(n^5) + 9$, $(2n)^{.75}$, $19n(\log(n))^4$, $3n(\log(n))^5$, $8^{\log(2n)}$, $9n^7 + 5n + 3$, $4n^{17} + 6$, $66^{(n-6)}$, n^6 , $404 n^{(n/4)} \log(n)$.

Example solution for SET C – Q1.. Similar for other sets as well.

First of all follow this order :

Constant < Logarithmic < Poly Logarithmic < Polynomial < Exponential < $n!$ or n^n .

There are several methods to solve this. One such simple method is by looking at the terms and trying to identify the order according to the rule specified above

$5\log(\log n)$, $7\log(n^5) + 9$ purely logarithmic so should be placed at the beginning.

Then comes $(2n)^{.75} < 19n(\log(n))^4$ because the term $19n(\log(n))^4$ contains n^1 which is definitely greater than $n^{0.75}$ in $(2n)^{.75}$. After that $19n(\log(n))^4 < 3n(\log(n))^5$ as both are same type of terms just the difference in power.

$8^{\log(2n)} = (2n)^{(\log 8 \text{ with base } 2)} = (2n)^3$ which is greater than the previous term. similarly, $9n^7 + 5n + 3$ then $4n^{17} + 6$ comes in order. $66^{(n-6)}$ is the exponential term just like we use to have 2^n that's why it is at 2nd highest place. Last one is $404 n^{(n/4)} \log(n) \sim O(n^n)$ which is of highest order.

And hence the ordering comes out to be:

$5\log(\log n)$, $7\log(n^5) + 9$, $(2n)^{.75}$, $19n(\log(n))^4$, $3n(\log(n))^5$, $8^{\log(2n)}$, $9n^7 + 5n + 3$, $4n^{17} + 6$, $66^{(n-6)}$, n^6 , $404 n^{(n/4)} \log(n)$.

MID SEM MAKE UP

Q1.

SET A

Correct order:

$2n^{\log(3)/\log(n)}$, $4\log(\log n)$, $71\log(n^2)+9$, $5n(\log n)^5$, $3n^3+8n+6$, $(\pi n)^{4.5}$, $(512)^{\log(8n)}$, $6n^{13}+5$, $44^{(n+4)}n^3$, $1729n^{(n/2)}\log(n)$.

SET B

correct order:

$3\pi n^{\log(4)/\log(n)}$, $9\log(\log n)$, $8\log(n^3)+55$, $6n(\log n)^4$, $3n^5+7n+4$, $64^{(\log 4n)}$, $(3n)^{6.25}$, $8n^{11}+3$, $33^{(n-3)}n^2$, $202n^{(n/3)}\log(n)$.

SET C

Correct order:

$4n^{\log(5)/\log(n)}$, $\pi\log(\log n)$, $7\log(n^5)+91$, $3n(\log n)^5$, $(128)^{\log(2n)}$, $9n^7+5n+1$, $(2n)^{7.75}$, $6n^{17}+4$, $77^{(n-7)}n^6$, $505n^{(n/4)}\log(n)$.

Solution for SET C Q1.. Similar for other sets as well.

First of all follow this order :

Constant < Logarithmic < Poly Logarithmic < Polynomial < Exponential < n! or n^n .

$4n^{\log(5)/\log(n)}=20(\text{constant})$ should be placed at the beginning. among logarithmic functions the order suffice $\pi\log(\log n)$, $7\log(n^5)+9$.

Among $3n(\log n)^5$, $(128)^{\log(2n)}=(2n)^7$ which is greater than $3n(\log n)^5$. Similarly u can have $9n^7+5n+1$, $(2n)^{7.75}$, $6n^{17}+4$ as the order of terms. $77^{(n-7)}n^6$ = exponential term which has higher time complexity in comparison to polynomial. Lastly, $505n^{(n/4)}\log(n)$. Cuz it has the term n^n which is again more than exponential so the given order follows as :

$4n^{\log(5)/\log(n)}$, $\pi\log(\log n)$, $7\log(n^5)+91$, $3n(\log n)^5$, $(128)^{\log(2n)}$, $9n^7+5n+1$, $(2n)^{7.75}$, $6n^{17}+4$, $77^{(n-7)}n^6$, $505n^{(n/4)}\log(n)$.