

LinearSearch(int[] A, int n, int key)

```
pos = -1
for i = 0 to (n-1)
    if (A[i] == key)
    {
        pos = i
        break
    }
if pos == -1
    print "Not found!"
else
    print "Found!"
return pos
```

A = { 1, 7, 4, 3, 9, 6, 2 }

key = 5 ---> Not found - failed!

key = 4 ---> Found, at index 2!

Worst case time complexity: $O(n)$

Best case time complexity: $O(1)$

A = { 1, 3, 4, 6, 8, 9, 11 }
key = 4

Comparison 1: key < 6

A' = { 1, 3, 4 }
key = 4

Comparison 2: key > 3

A'' = { 4 }
key = 4

Comparison 3: key == 4

A = { 1, 3, 4, 6, 8, 9, 11 }
key = 8

Comparison 1: key > 6

A' = { 8, 9, 11 }
key = 8

Comparison 2: key < 9

A'' = { 8 }
key = 8

Comparison 3: key == 8

Algorithm BinarySearch(A, k, low, high):

Input: An ordered array, A, storing n items, whose keys are accessed with method `key(i)` and whose elements are accessed with method `elem(i)`; a search key k ; and integers `low` and `high`

Output: An element of A with key k and index between `low` and `high`, if such an element exists, and otherwise the special element *null*

if low > high **then**

return null

else

 mid $\leftarrow \lfloor (\text{low} + \text{high}) / 2 \rfloor$

if $k = \text{key}(\text{mid})$ **then**

return elem(mid)

else if $k < \text{key}(\text{mid})$ **then**

return BinarySearch(A, k, low, mid - 1)

else

return BinarySearch(A, k, mid + 1, high)

A = { 1, 3, 4, 6, 8, 9, 11 }
key = 2

Comparison 1: key < 6

A' = { 1, 3, 4 }
key = 2

Comparison 2: key < 3

A'' = { 1 }
key = 2

Comparison 3: key > 1

A''' = { }
Return "Not found"

Worst case time complexity: $O(\log n)$

BinarySearch(A, key, low, high)

if (low > high) // if A is an empty array
 return (-1) // "Not found"

mid <- $\lfloor (low + high) / 2 \rfloor$

if key == A[mid]
 return mid

else if key < A[mid]
 BinarySearch(A, key, low, mid-1)

else if key > A[mid]
 BinarySearch(A, key, mid+1, high)

low = 6
high = 7
mid = $(6+7)/2 = 6$

key < A[6] =>
low = 6, high = 5

key > A[6] =>
low = 7, high = 7

A = { 1, 3, 4, 6, 8, 9, 11 }
key = 2

low = 0
high = 7
mid = $\lfloor (0+7)/2 \rfloor = 3$

Comparison 1: key < A[3] = 6

low = 0
high = mid-1 = 3-1 = 2
mid = $\lfloor (0+2)/2 \rfloor = 1$

Comparison 2: key < A[1] = 3

low = 0
high = mid-1 = 1-1 = 0
mid = $\lfloor (0+0)/2 \rfloor = 0$

Comparison 3: key > A[0] = 1

low = 0
high = mid-1 = 0-1 = -1

Since (low > high) => "Not found"

A = { 1, 3, 4, 6, 8, 9, 11 }
key = 8

low = 0
high = 7
mid = $\lfloor (0+7)/2 \rfloor = 3$

Comparison 1: key > A[3] = 6

low = mid+1 = 3+1 = 4
high = 7
mid = $\lfloor (4+7)/2 \rfloor = 5$

Comparison 2: key < A[5] = 9

low = 4
high = mid-1 = 5-1 = 4
mid = $\lfloor (4+4)/2 \rfloor = 4$

Comparison 3: key == A[4] = 8

Return (mid) => "Found at index 4"