

$$\begin{aligned} \dot{x}_1' &= -\frac{R}{L}x_1 - \frac{1}{L}x_2 + f \\ \dot{x}_2' &= \frac{1}{C}x_1 + 0 \cdot x_2 + 0.4 \end{aligned}$$

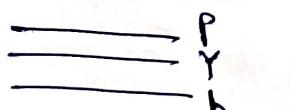
$$\begin{bmatrix} \frac{dx_1}{dt} \\ \frac{dx_2}{dt} \end{bmatrix} = \begin{bmatrix} -\frac{R}{L} & -\frac{1}{L} \\ \frac{1}{C} & 0 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} \cdot v_0(t)$$

## Power System I Syllabus

→ Introduction, P.U system, Distribution system, transmission line, parameters ( $R, L, C$ ), Performance of lines, Sag, Tension, Corona, Simulator load flow studies, PF dependent improvements, cables.

Distribution system: Feeder, Distributor, Service main, Ring main system, Radial system.

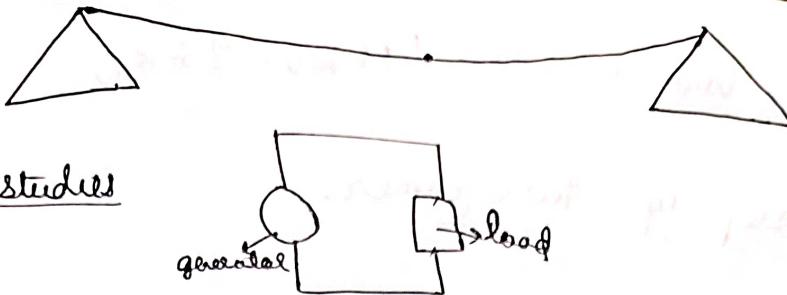
Performance of lines → short line, Medium line, long line



Neutral

Zero Current

Sag



\* Load flow studies

\* P.F Improvement :-

→ Installed capacity

Central sector - 98,795

State Sector - 1,04,918

Private Sector → 2,06,627.

Total - 4,10,339 (MW)

Non-Fossil fuel :-

Hydro - 46,850.

Liquid, Solar & Other RE → 120,900.

Nuclear - 6,780.

Total Generation (Billion units) - (B)  
12,23,135.

1 unit = 1 kWh.

fossil fuel

Coal - 203775 MW

Lignite - 6620 MW

Gas - 24,824 MW

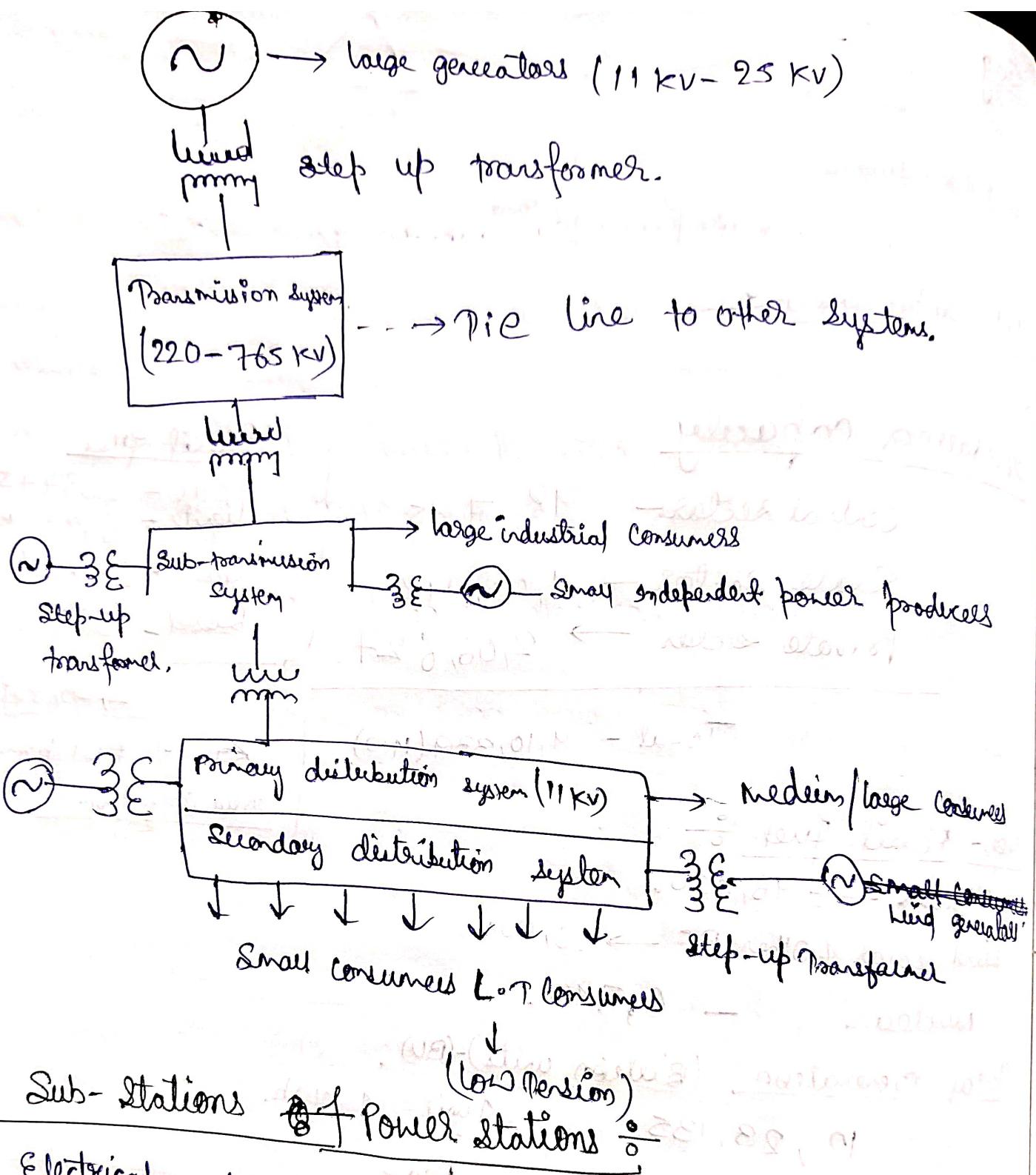
Diesel - 589. MW

2,35,809 MW

57.5% total power of

India comes from fossil fuels

Required	Availability	Surplus/Deficit	Peak		Surplus/Deficit
			Peak demand	Peak supply	
11,33,192	11,23,139	-6053 (-0.5%)	2,15,838	2,07,731	-8657 (-4%)



Electrical network comprises the following regions:

- ① Generating stations
- ② Transmission System
- ③ Distribution System
- ④ Load and points.

In all these regions, the power flow of electrical energy takes place through Electrical sub-stations. An electrical

Sub-stations is an assemblage of electrical components including bus bars, switchgears, power transformers, auxiliaries, etc. The sub-station are located in generating stations, transmission and distribution system and in consumers premises. Generally an electric substation consists of a number of incoming and outgoing circuits connected to common busbar system.

Each ckt has certain electrical components such as ckt breakers isolator, earthing switches, CT, PT etc. These components are connected in a different sequence such that a ckt can be switched off during normal operation by manual command, and also automatically during abnormal condition such as short ckt. Electrical energy is generally generated today in large hydrothermal and nuclear power stations. But the power stations are located far away from the load centre. Hence, large and long transmission network are used to carry the power from these power stations. To substation in the load center several electrical equipments are used for proper transmission and distribution of the generated power. The transmission system of an area is popularly known as a grid. Different grids are interconnected through tie lines to form a regional grid. Several regional grids are interconnected to form a national grid. Each grid operates independently through power can be exchanged b/w grids also.

During the third 5-year plan - 1950-1955 - first  
transmission growth took place very rapidly. A significant development in this phase was the emergence of an interstate grid system.

1956-1960 - second  
1961-1966 - third

Five year Plan.

The country was divided into 5 regions each with a regional electricity board to promote integrated operation of constituent power system.

Northern region :- Delhi, Haryana, H.P., Punjab, U.P., U.K., Raj, Ladakh, J&K.

Northeastern region :- Tripura, Mizoram, Meghalaya, Assam, Nagaland, Manipur.

Eastern region :- Bihar, Jharkhand, Orissa, Sikkim, W.B.

Western region :- Chhattisgarh, Gujarat, G.O.R., M.P., Maharashtra.

Southern region :- A.P., Telangana, Karnataka, Kerala, Tamil Nadu, Pondicherry.

## # Power Unit System (P.U)

Per unit value of any quantity = Actual Value of any quantity in volt / Base value of that quantity in that unit.

Impedance, voltage, current.

Base KVA, Base Voltage.

Let  $V_{base}$  and  $KVA_{base}$  be base voltage and base KVA respectively then,

$$V_{p.u} = \frac{\text{Actual}}{V_{base}}$$

$$I_{base} = \frac{KVA_{base} \times 1000}{V_{base}}$$

$$= \frac{MVA_{base} \times 10^6}{V_{base}}$$

$$I_{pu} = \frac{I_{actual}}{I_{base}} = \frac{I_{actual} \times V_{base}}{MVA_{base} \times 10^6}$$

Base impedance,  $Z_{base} = \frac{V_{base}}{I_{base}} = \frac{V_{base} \times V_{base}}{MVA_{base} \times 10^6} = \frac{V_{base}^2}{MVA_{base} \times 10^6} = \frac{(KV_{base})^2}{MVA_{base} \times 10^6}$

$$Z_{base} = \frac{(KV_{base})^2 \times 10^6}{MVA_{base} \times 10^6}$$

$$Z_{pu} = \frac{Z_{actual}}{Z_{base}} = \frac{Z_{actual} \times MVA_{base}}{(KV_{base})^2}$$

$$Z_{pu} = \frac{Z_{actual}}{Z_{base}} = \frac{R + jX}{Z_{base}} = \frac{R}{Z_{base}} + \frac{jX}{Z_{base}}$$

$$= R_{pu} + jX_{pu}$$

Change of Base

→ It is sometimes necessary to convert pu quantities from one base to another. Let the base kVA and base voltage of system 1 are  $kVA_{base1}$  and  $KV_{base1}$  respectively and that of system 2 are  $kVA_{base2}$  and  $KV_{base2}$ .

Impedance :

$$Z_{pu1} = \frac{Z_{actual}}{Z_{base1}} = \frac{Z_{actual} \times (KV_{base1})^2}{MVA_{base1} \times (KV_{base1})^2}$$

$$Z_{actual} = Z_{pu1} \times \frac{(KV_{base1})^2}{MVA_{base1}}$$

$$Z_{pu2} = \frac{Z_{actual}}{Z_{base2}} = \frac{(Z_{actual})(MVA_{base2})}{(KV_{base2})^2}$$

$$Z_{actual} = \frac{Z_{pu2} \cdot (KV_{base2})^2}{(MVA_{base2})}$$

$$\frac{Z_{pu2} \cdot (KV_{base2})^2}{(MVA_{base2})} = \frac{Z_{pu1} \cdot (KV_{base1})^2}{(MVA_{base1})}$$

$$Z_{pu2} = \left( \frac{KV_{base1}}{KV_{base2}} \right)^2 \times \left( \frac{MVA_{base2}}{MVA_{base1}} \right) \times Z_{pu1}$$

Q)

$$[I_{pu2} = (?) I_{pu1}] \rightarrow \text{solve your self.}$$

Sol<sup>(n)</sup>

$$\frac{I_{pu1}}{I_{pu2}} = \left[ \frac{MVA_2 \text{ base}}{MVA_1 \text{ base}} \right] \times \left[ \frac{V_{base1}}{V_{base2}} \right]$$

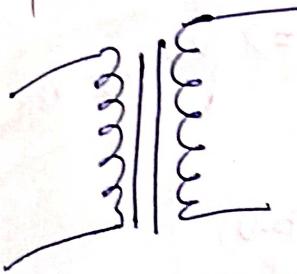
$$I_{pu2} = \left[ \frac{V_{base2}}{V_{base1}} \right] \times \left[ \frac{MVA_1 \text{ base}}{MVA \text{ base}_2} \right] \times I_{pu1}$$

### P. V dependence of a phase transformer

Let  $I_1, V_1$  be base current and voltage  $V_2$  in the primary side of the transformer and  $V_2, I_2$  be the base voltage & current on the secondary side of the transformer.

Let  $N_1, N_2$  are no. of turns on primary and secondary side.  
of the transformer.

$Z_s$  and  $Z_p$  are the total impedances of transformer of secondary & primary sides.



$$V_2 = V_1 \left( \frac{N_2}{N_1} \right)$$

→ Base impedance in primary side,  $Z_1 = \frac{V_1}{I_1}$   
" " secondary side,  $Z_2 = \frac{V_2}{I_2}$ .

$$Z_p(\text{pu}) = \frac{Z_p}{Z_1}$$

$$Z_s(\text{p.u}) = \frac{Z_s}{Z_2}$$

$$V_2 = V_1 \left( \frac{N_2}{N_1} \right)$$

$$Z_s = Z_p \left( \frac{N_2}{N_1} \right)^2$$

$$Z_s = Z_p \left( \frac{N_2}{N_1} \right)^2$$

$$Z_s(\text{p.u}) = \frac{Z_p \left( \frac{N_2}{N_1} \right)^2}{V_2 / I_2}$$

$$Z_s(\text{p.u}) = \frac{Z_p \left( \frac{N_2}{N_1} \right)^2}{\frac{V_1 \left( \frac{N_2}{N_1} \right)^2}{Z_1}}$$

P.U quantities in 3-phase system :-

(i) Star connected circuit

$$V_L = \sqrt{3} V_p \quad I_L = I_p$$

$$V_{LB} = \sqrt{3} V_{pb} \quad I_{LB} = I_{pb}$$

$$V_{L\text{p.u}} = \frac{V_L}{V_{LB}} = \frac{\sqrt{3} V_p}{\sqrt{3} V_{pb}} = \frac{V_p}{V_{pb}} = V_p(\text{p.u})$$

$$\Rightarrow V_L(\text{p.u}) = V_p(\text{p.u})$$

$$\Rightarrow I_L(\text{p.u}) = I_p(\text{p.u})$$

\* In  $\Delta$  connected circuit :

$$V_L = V_p, Z_L = \sqrt{3} Z_p.$$

$$V_{LB} = V_{pb}, Z_{LB} = \sqrt{3} Z_{pb}.$$

$$V_L(p.v) = \frac{V_L}{V_b} = \frac{V_p}{V_{pb}} = V_p(p.v) \Rightarrow V_p(p.v) = V_L(p.v)$$

$$Z_L(p.v) = \frac{Z_L}{Z_{LB}} = \frac{\sqrt{3} Z_p}{\sqrt{3} Z_{pb}} = Z_L(p.v)$$

\* In star connected circuit :

$$3\text{-phase Volt-amp} |, S = \sqrt{3} V_L I_L.$$

$$\text{Base Volt-amperes} |, S_b = \sqrt{3} V_{LB} I_{LB}$$

$$S(p.v) = \frac{S}{S_b} = \frac{\sqrt{3} V_L I_L}{\sqrt{3} V_{LB} I_{LB}} = \frac{V_L(p.v) \cdot I_L(p.v)}{V_{LB} I_{LB}}$$

$S \rightarrow S$  (Apparent power).

Power  $\rightarrow P$  (Real power / Active power).

Q (Reactive Power)

\* In  $\Delta$  circuit :

$$Z_{pov}(\Delta) = \frac{Z_{\text{actual}}}{Z_{\text{base}}} = \frac{Z_\Delta \times 1/\beta (\text{MVA base})}{(Kv_{\text{base}})^2} \quad (1)$$

\* In  $\gamma$ -circuit :

$$Z_{pov}(\gamma) = \frac{Z_{\text{actual}}}{Z_{\text{base}}} = \frac{Z_\gamma \times 1/\beta (\text{MVA base})}{(Kv_{\text{base}}/\sqrt{3})^2} \quad (2)$$

$$Z_Y = \frac{1}{3} Z_\Delta$$

gm Δ ckt

$$Z_{P.U \Delta} = \frac{Z_{actual}}{Z_{base}} = \frac{Z_\Delta \cdot \frac{1}{3} (MVA_{base})}{KV_{base}^2} \quad \text{--- (1)}$$

gm Y ckt

$$Z_{P.U Y} = \frac{Z_{actual}}{Z_{base}} = \frac{Z_Y \cdot \frac{1}{3} (MVA_{base})}{\left( \frac{KV_{base}}{\sqrt{3}} \right)^2} = \frac{Z_Y (MVA_{base})}{KV_{base}^2}$$

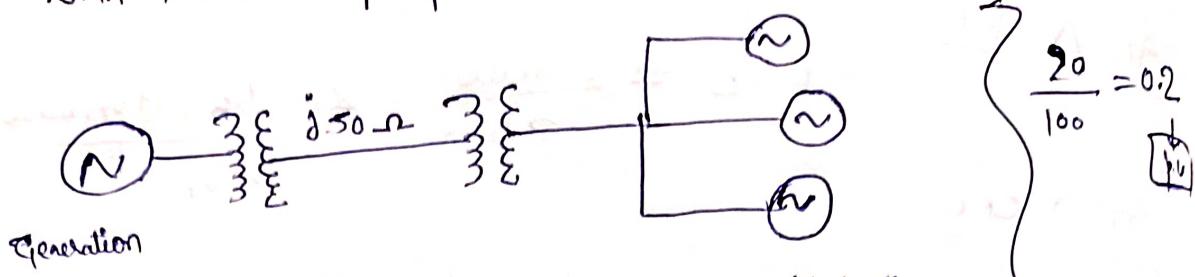
$$= \frac{1/3 Z_\Delta MVA_{base}}{KV_{base}^2} = Z_{P.U \Delta}$$

$$Z_{P.U Y} = Z_{P.U \Delta}$$

### Advantages of P.U representation :-

- ① Voltage, impedance, losses etc vary considerably with the variation of physical size, terminal voltage, power rating of the apparatus while the P.U parameter are independent of these quantities for a wide range of the same type of apparatus.
- ② The P.U quantities in 3-Φ system are same for Y or Δ connection so it reduces the confusion.
- ③ P.U impedances are same referred to either side of single Φ transformer.
- ④ The P.U impedances referred to either side of a 3-Φ transformer is same regardless of Y-Y, Δ-Δ, Y-Δ, Δ-Y connection

③ The computational effort in power system ~~is~~ is very much reduced with the use of per unit quantities.



Generator  $\rightarrow 100 \text{ MVA}, 33 \text{ kV, 3 phase}$

$$X_d'' = 15\%$$

Motors rated input  $\rightarrow 30 \text{ MVA}, 20 \text{ MVA, } 50 \text{ MVA, at } 30 \text{ kV}$

$$\text{With } X_d'' = 20\%$$

3-phase transformers  $\rightarrow 110 \text{ MVA, } 32 \text{ kV } \Delta / 110 \text{ kV } Y$  with

$$X_d'' = 8\%$$

$$\text{Line, } X_d = 50 \Omega$$

Selecting the generator rating as the base quantity in the generator ckt. Determine the base quantities in other part of the system and evaluate the corresponding per unit value.

Ans Selecting 100 MVA, 33 KV as base values in the generator ckt.

The base voltage in the transmission line will be.

$$33 \times \frac{110}{32} = 118.43 \text{ kV}$$

In the Motor circuit, the base voltage will be  $= \frac{113.43 \times 32}{110} = 32 \text{ kV}$

$$X_g'' = 15\% = 0.15 \text{ p.u.}$$

Transmission Transformer reactance at 100 MVA base and 33 KV base

$$X_T = X_{T_2} = \frac{8}{100} \times \left( \frac{32}{33} \right) \times \left( \frac{100}{110} \right) \rightarrow \left\{ \begin{array}{l} Z_T = 2 \text{ p.u.} \\ X_T = 2 \text{ p.u.} \end{array} \right.$$

$$= 0.06838 \text{ p.u.}$$

### Transmission Line :-

Base MVA is 100 & Base voltage is 113.43 kV.

Base impedance,  $Z_{base} = \frac{(4V_{base}/\sqrt{3})^2}{1/3 (\text{MVA}_{base})} \text{ k}\Omega$ .

$$X_{p.u} = \frac{X_{line}}{Z_{base}} = \frac{50 \times 100}{(113.43)^2} = 0.3888 \text{ p.u.}$$

### In Motors :-

Base MVA is 100, Base voltage is 33 kV.

$$Z_{M1}(\text{p.u.}) = (0.20) \times \left(\frac{100}{30}\right) \left(\frac{30}{33}\right)^2 = 0.5509 \text{ p.u.}$$

$$Z_{M2}(\text{p.u.}) = (0.20) \times \left(\frac{100}{20}\right) \left(\frac{20}{33}\right)^2 =$$

$$Z_{M3}(\text{p.u.}) = (0.20) \times \left(\frac{100}{50}\right) \left(\frac{50}{33}\right)^2 =$$

### Inductance of a conductor due to internal flux :-

~~with~~ ~~current~~ ~~a conductor is~~ carrying a ~~conductor~~ conductor of infinite length ~~at infinity~~.  
Let us assume that the ~~other~~ conductor is at infinity.

Conductor's radius -  $r$ .

Magnetic field intensity at a distance ' $r$ ' from centre is  $Hx$ .

$$\text{Current density } J_{density} = \frac{I}{\pi r^2}$$

According to Ampere's law which states that MMF around any closed path equals the current enclosed in the path

$$\oint H_z ds = I_a, \quad \text{MMF} = N \cdot I$$

$$I_x = J_{density} \times \text{Area} = \frac{1}{\pi r^2} \times \pi r^2 = \frac{I}{r^2}$$

$$H_a \cdot (2\pi x \cdot 1) = 2m = \frac{2\pi^2}{x^2}$$

$$H_a = \frac{2\pi^2}{x^2} \cdot \frac{1}{2\pi x} = \frac{\pi x}{2\pi x^2} A \cdot I / M.$$

flux density inside the conductor at a distance  $x$ :

$$B_a = M H_a = M_0 M_r H_a = M_0 H_a. \quad [\text{Here, } M_r = 1]$$

→ flux enclosed in element of thickness  $dx$  per meter length of the conductor.

$$d\phi = B_a (dx \cdot 1) = \text{flux density} \times \text{Area}.$$

$$d\phi = \frac{M_0 \chi I}{2\pi x^2} \cdot dx \text{ Weber.}$$

This flux ( $d\phi$ ) consists of a fraction of tens.

$$N_a = \frac{m}{x^2} \quad \left[ \frac{I_m}{I} = \frac{\pi x^2}{\pi x^2} \right]$$

Hence, flux linkage per unit meter length of conductor:

$$d\lambda = N_a \cdot d\phi = \frac{x^2}{x^2} \left[ \frac{M_0 \chi I}{2\pi x} \right] \text{ wb - T}$$

Integration, we get the total internal flux linkage.

$$\begin{aligned} \lambda &= \int_0^x d\lambda = \int_0^x \frac{M_0 I}{2\pi x^4} x^3 dx = \frac{M_0 I}{2\pi x^4} \left[ \frac{x^4}{4} \right]_0^x \\ &= \frac{M_0 I}{2\pi x^4} \left( \frac{x^4}{4} \right) = \frac{M_0 I}{8\pi} \text{ wb - T.} \end{aligned}$$

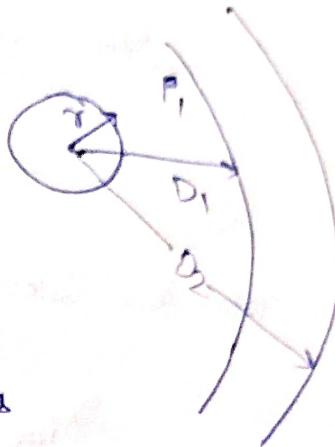
$$\lambda_{int} = \frac{M_0 I}{8\pi} \text{ wb - T/M.}$$

$L_{int}$  = Inductance of Conductor due to internal flux

~~external flux.~~ flux.

$$= \frac{\mu_0 I_{int}}{I} = \frac{\mu_0}{8\pi} = \frac{4\pi \times 10^{-7}}{8\pi} = \frac{10^{-7}}{2} \text{ H/M.}$$

Inductance of a conductor due to flux between two points external to the conductor.



Electric field intensity at a distance 'x' from the centre of conductor is

$$H_x = \frac{I}{2\pi x} = \frac{I}{2\pi x} \text{ A-T/m.}$$

→ Flux density in the element of thickness 'dn' is

$$B_x = \mu_0 H_x = \mu_0 \frac{I}{2\pi x} = \mu_0 \frac{I}{2\pi x} \text{ wb/m}^2 \quad (\mu_0 = 1)$$

Flux enclosed in element of thickness 'dn' per meter length is

$$d\phi = B_x \cdot (dx \cdot 1) = \mu_0 \cdot \frac{I dx}{2\pi x} \text{ wb.}$$

Electric field intensity at a distance 'x' from the flux links with total current 'I', flux linkage.

$$d\lambda = N_A d\phi = 1 \cdot \mu_0 \frac{I dx}{2\pi x} \quad \text{wb-turns/meter.}$$

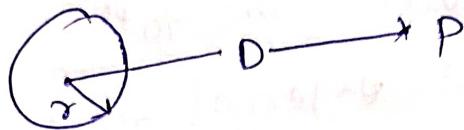
Here flux linkage b/w  $\Phi_1$  and  $\Phi_2$  is

$$\lambda_{12} = \int_{D_1}^{D_2} d\lambda = \int_{D_1}^{D_2} \frac{\mu_0 I}{2\pi} \left(\frac{1}{x}\right) dx.$$

$$= \frac{\mu_0 I}{2\pi} \ln \left( \frac{D_2}{D_1} \right) \text{ wb-T/M.}$$

The inductance of the conductor contributed by the flux included b/w points P<sub>1</sub> & P<sub>2</sub> is then,

$$L_{12} = \frac{\gamma_{12}}{I} = 2 \times 10^{-7} \ln\left(\frac{D_2}{D_1}\right) \text{ H/m.}$$



Total flux linkage upto a point P (a distance 'D' from centre),

$$\gamma_{int} = \frac{10^{-7}}{2} \text{ Vs.}$$

$$\gamma_{ext} = \left[ 2 \times 10^{-7} \ln(D_s) \right] \text{ Vs.}$$

Total flux linkages due to current I (upto a distance D from center),

$$\gamma = \gamma_{int} + \gamma_{ext} = \left[ \frac{10^{-7}}{2} + 2 \times 10^{-7} \ln\left(\frac{D}{r}\right) \right] \text{ Vs.}$$

$$= 2 \times 10^{-7} I \left[ \frac{1}{4} + \ln(D_s) \right].$$

$$= 2 \times 10^{-7} I \left[ -6 e^{-1/4} + \ln(D_s) \right].$$

$$= 2 \times 10^{-7} I \ln\left(\frac{D}{2e^{1/4}}\right) = 2 \times 10^{-7} I \ln\left(\frac{D}{\gamma'}\right).$$

$\rightarrow \gamma'$  can be regarded as the radius of fictitious conductor with no internal inductance but the same total inductance as the actual conductor.

Inductance of a 1-phase 2-wire system

$$\bar{I}_1 + \bar{I}_2 =$$

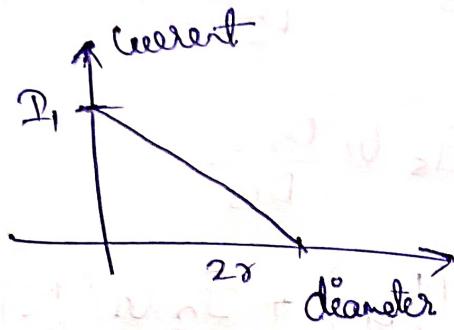
$\frac{\pi_1}{1, \gamma}$



2-wire system

$\frac{2, \gamma, I_2}{\gamma}$

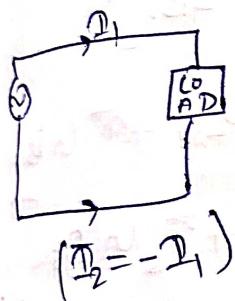
Flux leakage of conductor 1,



$$\lambda_1 = 2 \times 10^7 \times G \frac{D}{\gamma} \times I_1$$

$$L_1 = \frac{\lambda_1}{I_1} = 2 \times 10^7 G D / \gamma, \text{ H/M}$$

flux linkage of conductor 2,  $\lambda_2 = 2 \times 10^7 \bar{I}_2 \ln \frac{D}{\gamma}$



$$\lambda_2 = 2 \times 10^7 \ln D / \gamma, \text{ H/M.}$$

$$L = 4 \times 10^7 \ln D / \gamma, \text{ H/M.}$$

Flux linkage of conductor 1,  $\lambda_1 = I_1 \times 2 \times 10^7 \ln D / \gamma$

$$= 2 \times 10^7 \bar{I}_1 \left[ \ln \frac{D}{\gamma} \cdot \frac{D_0}{D} \right]$$

$I_1, \gamma$



$I_2, \gamma$



$$= 2 \times 10^7 \left[ \bar{I}_1 \left( \ln \frac{D_0}{D} \right) + \bar{I}_2 \left( \ln \frac{D_0}{\gamma} \right) \right]$$



$$= 2 \times 10^7 \left[ \bar{I}_1 \ln \frac{D_0}{\gamma} + (-\bar{I}_2) \ln \frac{D}{D_0} \right]$$

Flux

linkage of conductor 1,  $\lambda_1 = 2 \times 10^7 \left[ \bar{I}_1 \ln \left( \frac{D_0}{\gamma} \right) + \bar{I}_2 \ln \left( \frac{D_0}{D} \right) \right]$

self  
linkage

mutual  
linkage

$$\bar{I}_1 + \bar{I}_2 + \bar{I}_3 + \bar{I}_4 + \bar{I}_5 = 0.$$

$$\begin{aligned} \gamma_1 &= 2 \times 10^{-7} I_1 \ln \frac{D_{10}}{D_1} + 2 \times 10^{-7} \bar{I}_2 \ln \frac{D_{10}}{D_{12}} \\ &\quad + 2 \times 10^{-7} \bar{I}_3 \ln \frac{D_{300}}{D_3} + 2 \times 10^{-7} \bar{I}_4 \ln \frac{D_{100}}{D_{14}} \\ &\quad + 2 \times 10^{-7} \bar{I}_5 \ln \frac{D_{500}}{D_{15}} \end{aligned}$$

$$\begin{aligned} \gamma_1 &= 2 \times 10^{-7} \left[ I_1 \ln \left( \frac{1}{D_{11}} \right) + \bar{I}_2 \ln \left( \frac{1}{D_{12}} \right) + \bar{I}_3 \ln \left( \frac{1}{D_{13}} \right) \right. \\ &\quad \left. + \bar{I}_4 \ln \left( \frac{1}{D_{14}} \right) + \bar{I}_5 \ln \left( \frac{1}{D_{15}} \right) \right]. \end{aligned}$$

$$+ 2 \times 10^{-7} \left[ I_1 \ln D_{10} + \bar{I}_2 \ln (D_{200}) + \bar{I}_3 \ln D_{300} \right. \\ \left. + \bar{I}_4 \ln D_{100} + \bar{I}_5 \ln (D_{500}) \right].$$

$$\bar{I}_1 + \bar{I}_2 + \bar{I}_3 + \bar{I}_4 + \bar{I}_5 = 0$$

$$\bar{I}_5 = -(\bar{I}_1 + \bar{I}_2 + \bar{I}_3 + \bar{I}_4)$$

$$2 \times 10^{-7} \left[ I_1 \ln (D_{10}) + \bar{I}_2 \ln (D_{200}) + \bar{I}_3 \ln (D_{300}) + \bar{I}_4 \ln (D_{100}) - (\bar{I}_1 + \bar{I}_2 + \bar{I}_3 + \bar{I}_4) \ln \left( \frac{1}{D_{15}} \right) \right]$$

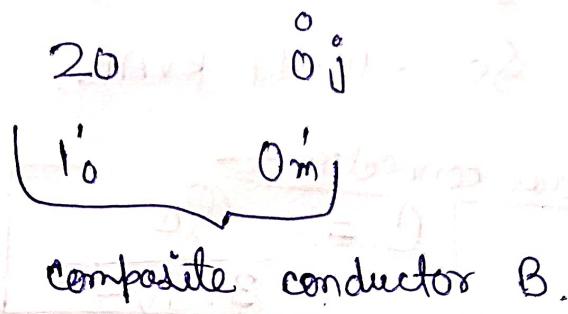
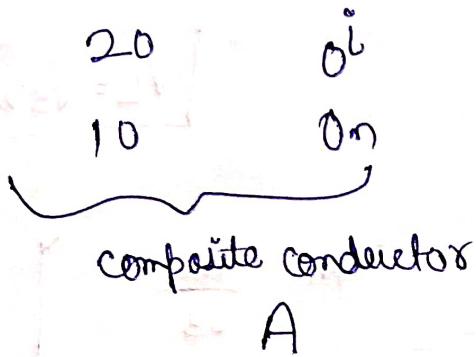
$$= 2 \times 10^{-7} \left[ I_1 \ln \left( \frac{D_{10}}{D_{500}} \right) + \bar{I}_2 \ln \left( \frac{D_{200}}{D_{500}} \right) + \dots + \bar{I}_4 \ln \left( \frac{D_{100}}{D_{500}} \right) \right].$$

$$\begin{aligned} &= 2 \times 10^{-7} \left[ \bar{I}_1 \ln \left( \frac{1}{D_{11}} \right) + \bar{I}_2 \ln \left( \frac{1}{D_{12}} \right) + \bar{I}_3 \ln \left( \frac{1}{D_{13}} \right) + \bar{I}_4 \ln \left( \frac{1}{D_{14}} \right) + \bar{I}_5 \ln \left( \frac{1}{D_{15}} \right) \right] \\ &\quad + \left[ 2 \times 10^{-7} \left[ I_1 \ln (D_{10}) + \bar{I}_2 \ln (D_{200}) + \bar{I}_3 \ln (D_{300}) + \bar{I}_4 \ln (D_{100}) + \bar{I}_5 \ln (D_{500}) \right] \right]. \end{aligned}$$

$$\lambda_1 = 2 \times 10^{-7} \left[ \bar{I}_1 \ln\left(\frac{1}{D_{11}}\right) + \bar{I}_2 \ln\left(\frac{1}{D_{12}}\right) + \bar{I}_3 \ln\left(\frac{1}{D_{13}}\right) + \bar{I}_4 \ln\left(\frac{1}{D_{14}}\right) + \bar{I}_5 \ln\left(\frac{1}{D_{15}}\right) \right]$$

## Inductance of Composite conductor lines

A carries current  $\bar{I}$  & B carries current  $-\bar{I}$ .



$$\lambda_1 = 2 \times 10^{-7} \left( \frac{\bar{I}}{n} \right) \left[ \ln\left(\frac{1}{D_{11}}\right) + \ln\left(\frac{1}{D_{12}}\right) + \dots + \ln\left(\frac{1}{D_{1n}}\right) \right]$$

$$= 2 \times 10^{-7} \left( \frac{\bar{I}}{M'} \right) \left[ \ln\left(\frac{1}{D_{11'}}\right) + \ln\left(\frac{1}{D_{12'}}\right) + \dots + \ln\left(\frac{1}{D_{1M'}}\right) \right].$$

$$\frac{1}{n} \ln\left(\frac{1}{A}\right) = \log\left(\frac{1}{A}\right)^{1/n}$$

$$\lambda_1 = 2 \times 10^{-7} \bar{I} \left[ \left( \ln\left(\frac{1}{D_{11}}\right)^{1/n} + \left( \ln\left(\frac{1}{D_{12}}\right)^{1/n} + \dots + \left( \ln\left(\frac{1}{D_{1n}}\right)^{1/n} \right) \right] \right]$$

$$= 2 \times 10^{-7} \bar{I} \left[ \left( \ln\left(\frac{1}{D_{11}}\right)^{1/M'} + \left( \ln\left(\frac{1}{D_{12}}\right)^{1/M'} + \dots + \left( \ln\left(\frac{1}{D_{1M'}}\right)^{1/M'} \right) \right] \right]$$

$$= 2 \times 10^{-7} \bar{I} \left[ \ln\left(\frac{1}{(D_{11} + D_{12} + \dots + D_{1n})^{1/n}}\right) \right] - 2 \times 10^{-7} \left[ \ln\left(\frac{1}{D_{11} \times D_{12} \times \dots \times D_{1n}}\right)^{1/M'} \right]$$

$$= 2 \times 10^{-7} \bar{I} \left[ \ln\left(\frac{1}{(D_{11} \times D_{12} \times \dots \times D_{1n})^{1/M'}}\right) \right] + 2 \times 10^{-7} \left[ \ln\left(\frac{1}{D_{11} \times D_{12} \times \dots \times D_{1n}}\right)^{1/M'} \right]$$

$$\lambda_i = 2 \times 10^7 \left[ \ln \left( \frac{D_{i1} \cdot D_{i2} \cdots D_{in}}{(D_{i1} + D_{i2} + \cdots + D_{in})^M} \right)^{1/M} \right]$$

$$V_b - T / M$$

Lab

$$\cos \phi = 0.8 \Rightarrow \phi = 36.87^\circ \quad S = 12 \text{ kVA}$$

$$P = S \cos \phi = 16.62 \text{ kW}$$

$$Q = S \sin \phi = 12.47 \text{ kVA}$$

$$Q_c = -12.47 \text{ kVAR}$$

for star connection:

$$C = \frac{Q_c}{3 \sqrt{3} V^2}$$

$$V_L = \sqrt{3} V_{ph}$$

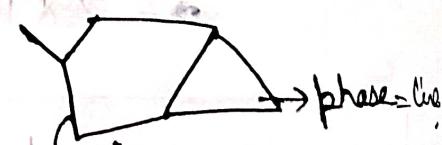
$$V_{ph} = \frac{400}{\sqrt{3}}$$



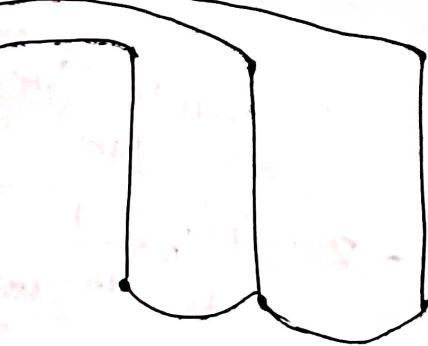
$$C = \frac{12.47 \times 1000}{3 \times 2\pi \times 50 \times \left(\frac{400}{\sqrt{3}}\right)^2} = 248 \text{ fF}$$

for  $\Delta$  connection:

$$C = \frac{12.470}{3 \times 2\pi \times 50 \times 400 \times 400} = 82.7 \text{ fF}$$

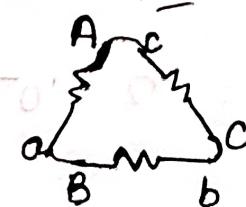
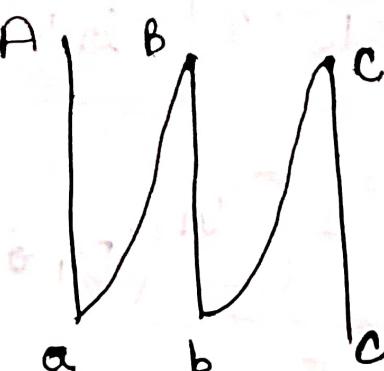


star



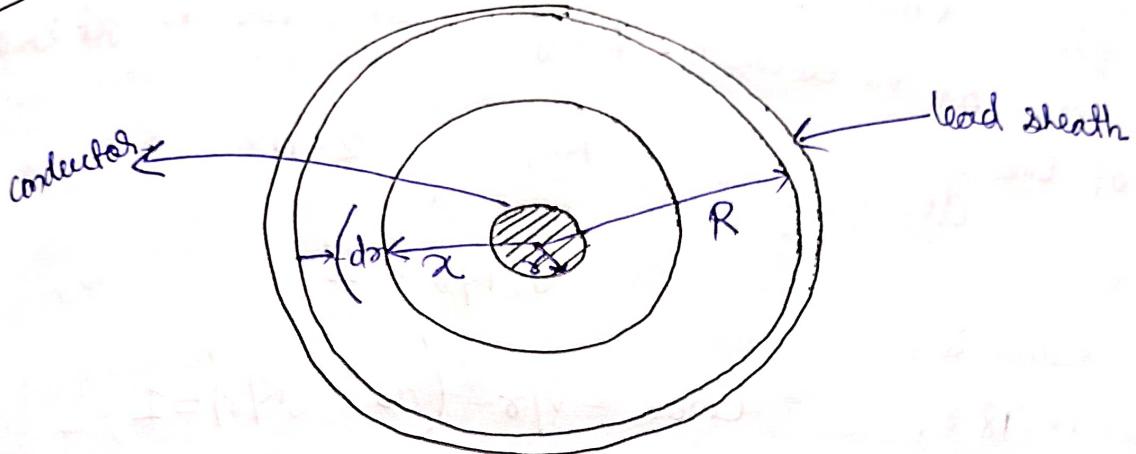
star

delta



cable :-

electrical characteristics of cables :-



r: conductor radius.

R: outside Radius of Insulation or inside radius of Sheath.

V: Potential difference between conductor and sheath.

q: charge on conductor surface.

D: Electric flux density.  $D = q/2\pi x$

E: Electric field, or electric stress or dielectric stress.

$\epsilon$ : Permittivity ( $\epsilon = \epsilon_0 \cdot \epsilon_r$ ).  $E = D/\epsilon = q/2\pi x \epsilon$

$\epsilon_r$ : Relative permittivity of material.

$$V = \int_r^R E \cdot dr = \left[ \frac{q}{2\pi \epsilon} \right] \left[ \ln(R/r) \right]$$

$$E = \frac{q}{2\pi \epsilon r^2} = \frac{V}{r \cdot \ln(R/r)}$$

Dielectric strength: Maximum voltage that dielectric can withstand before it breakdown.

Tension stress: It is the amount of voltage across the insulation material divided by the thickness of the insulation.

$$E_{\max} = E \text{ at } x=\sigma = V/(2 \ln R/\sigma)$$

$$E_{\min} = E \text{ at } x=R = V/(R \cdot \ln R/\sigma)$$

For a given  $V$  and  $R$ , there is conductor radius that gives the minimum stress at the conductor surface. In order to get smallest value of  $E_{\max}$ :

$$\frac{dE_{\max}}{d\sigma} = 0 \quad R/\sigma = e = 2.718$$

$\uparrow$   
 $\ln R/\sigma = 1$

Insulation thickness is:

$$R - \sigma = 1.718 \sigma. \quad E_{\max} = V/\sigma \quad (\text{as } \ln(R/\sigma) = 1)$$

where  $\sigma$  is the optimum value of conductor radius that satisfies  $R/\sigma = 2.718$ .

**Ex**) A single core conductor cable of 5 km length has a conductor diameter of 2cm and an inside diameter of sheath 5cm. The cable is used at 24.9 KV and 50 Hz. Calculate the following.

a) Maximum & Minimum Value of electrical stress

b) Optimum value of conductor radius that results in smallest value of maximum stress.

$$\text{Soln} \quad a) E_{\max} = \frac{V}{\sigma \ln R/\sigma} = \frac{24.9 \times 10^3}{1 \times 10^{-2} \ln 2.5} = \frac{24.9 \times 10^3 \times 10^2}{0.91} = 2736 \text{ V/m}$$

or  $27.36 \text{ KV/cm}$

$$E_{\min} = \frac{24.9 \times 10^3}{2.5 \times 10^{-2} \ln 2.5} = \frac{24.9 \times 10^5}{0.91} = 10.94 \times 10^5 \text{ V/m}$$

or  $10.94 \text{ KV/cm}$

$$b) \sigma = \frac{R}{2.718} = \frac{2.5 \text{ cm}}{2.718} = 0.919 \text{ cm.}$$

\* The inductance of filament is

$$L_i = \frac{\lambda_i}{(I/\eta)} = 2 \times 10^{-7} \frac{\ln((D_{i1}, D_{i2}, \dots, D_{in})^{1/m})}{(D_{i1}, D_{i2}, \dots, D_{in})^{1/m}}$$

the average inductance of the filament of the composite conductor A is  $L_{avg} = \frac{L_1 + L_2 + \dots + L_n}{n}$ .

Since conductor A is composite of n filaments electrically is parallel, its inductance is

$$L_A = \frac{L_{avg}}{n} = \frac{L_1 + L_2 + \dots + L_n}{n^2}$$

$$L_A = \frac{2 \times 10^{-7}}{n} \left[ \frac{\ln \left( \frac{(D_{11} \cdot D_{12} \cdot \dots \cdot D_{1n}) (D_{21} \cdot D_{22} \cdot D_{23} \dots D_{2n}) (D_{n1} \cdot D_{n2} \dots D_{nn})}{(D_{11} \cdot D_{12} \cdot \dots \cdot D_{1n}) (D_{21} \cdot D_{22} \cdot \dots \cdot D_{2n}) \dots (D_{n1} \cdot D_{n2} \cdot D_{nn})} \right)^{1/m}}{n^2} \right] \quad (A)$$

$$= \frac{2 \times 10^{-7}}{n} \ln \left( \frac{D_M}{D_{SA}} \right) H/M.$$

- The numerator of argument of the logarithmic in Eq (A) is the  $M^{th}$  root of the  $M^n$  term which is the product of all possible mutual distances from the  $n^{th}$  filament of conductor A to  $M^{th}$  filament of conductor B.
- It is called mutual geometric mean distance between conductors A and B. If it is written as  $D_M$ .
- Similarly denominator of the argument of logarithm in eqn A. is the  $n^{th}$  root of the  $n^2$  term. This is also called self GMD or GMR ( $D_{SA}$ ).

$$L_B = 2 \times 10^{-7} \ln \left( \frac{D_M}{D_{BB}} \right),$$

Inductance of 3-phase, single circuit line :-

$$\bar{I}_1 + \bar{I}_2 + \bar{I}_3 = 0, \quad D_{11} = D_{22} = D_{33} = \gamma'.$$

$$\gamma_1 = 2 \times 10^{-7} \left[ \bar{I}_1 \ln \left( \frac{1}{\gamma'} \right) + \bar{I}_2 \ln \left( \frac{1}{D_{12}} \right) + \bar{I}_3 \ln \left( \frac{1}{D_{13}} \right) \right]$$

$$\gamma_2 = 2 \times 10^{-7} \left[ \bar{I}_2 \ln \left( \frac{1}{\gamma'} \right) + \bar{I}_1 \ln \left( \frac{1}{D_{21}} \right) + \bar{I}_3 \ln \left( \frac{1}{D_{23}} \right) \right]$$

$$\gamma_3 = 2 \times 10^{-7} \left[ \bar{I}_3 \ln \left( \frac{1}{\gamma'} \right) + \bar{I}_1 \ln \left( \frac{1}{D_{31}} \right) + \bar{I}_2 \ln \left( \frac{1}{D_{32}} \right) \right]$$

Inductance of conductor '1' is

$$L_1 = \frac{\gamma_1}{\bar{I}_1} = 2 \times 10^{-7} \left[ \ln \left( \frac{1}{\gamma'} \right) + \frac{\bar{I}_2}{\bar{I}_1} \ln \left( \frac{1}{D_{12}} \right) + \frac{\bar{I}_3}{\bar{I}_1} \ln \left( \frac{1}{D_{13}} \right) \right]$$

$$L_2 = \frac{\gamma_2}{\bar{I}_2} = 2 \times 10^{-7} \left[ \ln \left( \frac{1}{\gamma'} \right) + \frac{\bar{I}_1}{\bar{I}_2} \ln \left( \frac{1}{D_{21}} \right) + \frac{\bar{I}_3}{\bar{I}_2} \ln \left( \frac{1}{D_{23}} \right) \right]$$

$$\text{let } I_1 = I \angle 0^\circ, \quad I_2 = I \angle -120^\circ, \quad I_3 = I \angle 120^\circ.$$

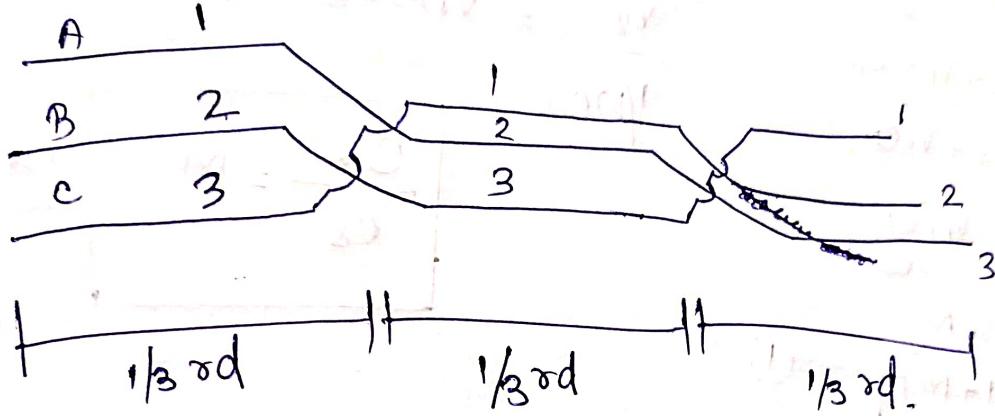
$$L_1 = 2 \times 10^{-7} \left[ \ln \left( \frac{1}{\gamma'} \right) + \left( \dots \right) \right]$$

Due to unsymmetrical spacing

Phase inductance is  $\gamma_0$  equal & due to mutual inductance they contain imaginary term  $j \gamma_0 D_{12}$ .

Asymmetrical spacing which makes the gives complex values of phase inductances study of power system difficult. However

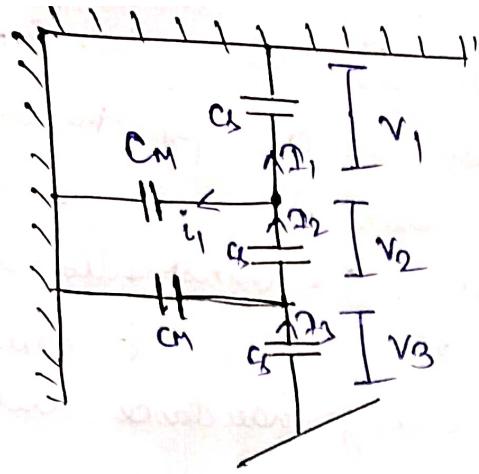
one way to regain symmetry in good measure and obtain a balanced model by exchanging the position of conductor at regular interval along the line such that each conductor occupy the adjacent position. Such an exchange of conductor is called transposition. The transposition usually carried out at switching station to have the same average inductance over the transposition cycle.



### [Lab - 2]

A 3- $\phi$ , 50 Hz, 33 $\sqrt{3}$  kV distribution system used to supply industrial load. Each of the conductor is suspended by an insulator string having three identical porcelain insulator. The self capacitance and the mutual capacitance of the insulator is 1 μF and 0.1 μF respectively.

- a) Calculate voltage across each conductor.
- b) Calculate string efficiency and verify the result in simulink
- c) if a wire guard wire is used to improve the string efficiency. Then calculate the guard wire to pin capacitance such that string efficiency becomes 100%.



Active Power once lost can not be compensated; we deal with reactive power.

$$V_3 > V_2 > V_1$$

$$I_3 > I_2 > I_1$$

$$I_2 = I_1 + i_1$$

$$\frac{V_2}{1/\mu C_s} = V_1 \mu C_s + V_1 \mu C_m$$

$$\boxed{\frac{C_m}{C_s} = M}$$

$$\frac{C_m = 0.1 \mu F}{1 \mu F} = M$$

$$M = 1/10 = 0.1$$

$$V_2/\mu C_s = V_1/\mu C_s + V_1/\mu C_m$$

$$V_2 C_s = V_1 C_s + V_1 C_m$$

$$V_2 = V_1 + V_1 \left( \frac{C_m}{C_s} \right)$$

$$V_2 = V_1 + V_1 M$$

$$\boxed{V_2 = V_1 (1+M)} \quad \textcircled{1}$$

$$I_3 = I_2 + i_2 \Rightarrow \frac{V_3}{\mu C_s} = V_2/\mu C_s + (V_1 + V_2)/\mu C_m$$

$$\Rightarrow \boxed{V_3 = V_2 + (V_1 + V_2) M} \quad \textcircled{2}$$

Put  $V_2$  from  $\textcircled{1}$

$$\cancel{V_3 = V_1 (1+M) + V_1 M + V_2 M}$$

$$\cancel{V_3 = V_1 (1+2M) + V_2 M} \quad \textcircled{3}$$

$$\cancel{V_3 = V_1 (1+2M) + V_1 (1+M)}$$

$$\cancel{V_3 = V_1 (2+3M)}$$

$$\boxed{V_1 + V_2 + V_3 = V_{ph}}$$

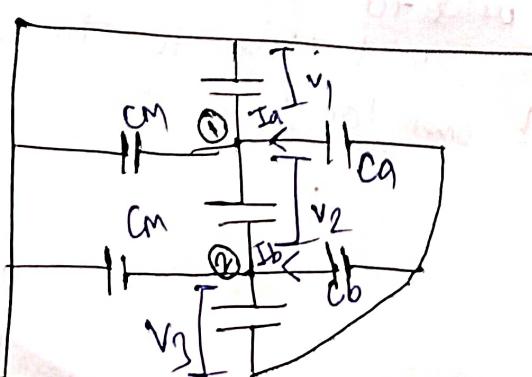
$$V_3 = V_1 (1+M) + (V_1 (1+M) + V_2) M$$

$$V_3 = V_1 + V_1 M + V_1 M + V_1 M^2 + V_2 M$$

$$V_3 = V_1 M^2 + 3V_1 M + V_1$$

$$V_3 = V_1 (M^2 + 3M + 1)$$

$$\eta = \frac{V_1 + V_2 + V_3}{m \times V_3} \quad m: \text{no of insulators}$$



$$V_1 = V_2 = V_3$$

$$I_1 = I_2 = I_3$$

St-1

$$I_a = i,$$

$$(V_2 + V_3) \text{ } \square C_a = V_1 \text{ } \square C_m$$

$$2V_1 C_a = V_1 C_m$$

St-2

$$I_b = i_2$$

$$C_a = C_m/2 \rightarrow \text{for point 1}$$

$$V_3 \text{ } \square C_b = (V_1 + V_2) \text{ } \square C_m ; V_1 + V_2 = 2V_1$$

$$C_b = 2 \text{ cm}, \rightarrow \text{for point 2.}$$

$$\text{When } V_1 = V_2 = V_3 \Rightarrow I_1 = I_2 = I_3$$

$$C_p = \frac{P C_m}{n - P}$$

→ no of insulators

$$C_1 = \frac{1 \cdot \text{cm}}{3-1} = \text{cm}/2$$

$$C_2 = \frac{2 \cdot \text{cm}}{3-2} = 2 \text{ cm},$$