Lecture 6-1

Introducing data visualization in Python: Matplotlib

Week 6 Monday

Miles Chen, PhD

Adapted from Python for Data Science by Jake VanderPlas

References:

https://matplotlib.org/stable/api/pyplot_summary.html

https://matplotlib.org/stable/api/_as_gen/matplotlib.pyplot.html#module-matplotlib.pyplot

Always: import matplotlib.pyplot as plt

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Always: import matplotlib.pyplot as plt

```
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
```

Creating a simple plot.

First, we create arrays of the values to plot.

We create an array of 500 values from 0 to pi.

```
In [2]: x = np.linspace(0, np.pi * 2, 500)
```

We then calculate the y values we wish to plot. In this case, we'll keep it simple and calculate sin of x (in radians).

```
In [3]: y = np.sin(x)
```

Line Plot

To create a plot, you can call plt.plot(x, y). To have it appear, you call plt.show(). plt.show() is much like calling print(). In Jupyter, if you do not call plt.show(), the plot will still often appear, but it is generally considered good practice to call plt.show().

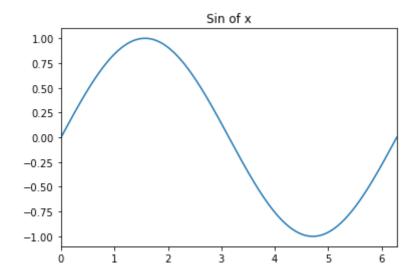
Prior to calling plt.show(), you can call optionally other functions which will modify the plot, such as adding a title or changing the axis limits.

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Prior to calling plt.show(), you can call optionally other functions which will modify the plot, such as adding a title or changing the axis limits.

```
In [4]:
    plt.plot(x, y)
    plt.title("Sin of x") # optional
    plt.xlim(0,2 * np.pi) # optional
    plt.show()
```

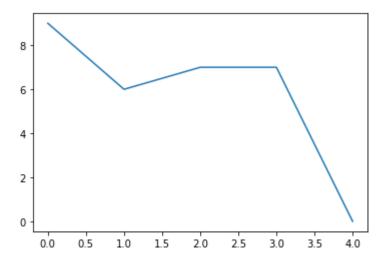


The default behavior of plt.plot() is to plot the points and connect them with lines.

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```
In [5]:
    x = np.arange(0, 5, 1)
    print(x)
    y = np.random.randint(0, 10, 5)
    print(y)
    plt.plot(x, y)
    plt.show()
```

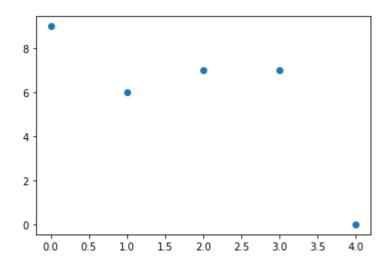
[0 1 2 3 4] [9 6 7 7 0]



Scatterplot

If you do not want the points to be connected with a line, you can ask for a scatterplot.

```
In [6]:
   plt.scatter(x,y)
   plt.show()
```



Multiple functions or sequences on the same graph

Repeated calls to plt.plot() will add lines to the same plot.

Multiple functions or sequences on the same graph

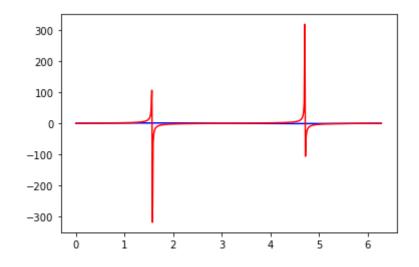
Repeated calls to plt.plot() will add lines to the same plot.

Multiple functions or sequences on the same graph

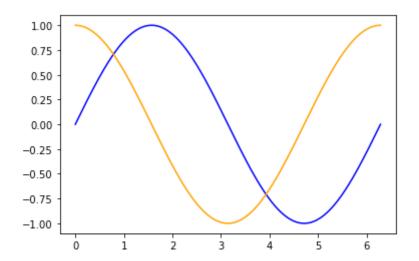
Repeated calls to plt.plot() will add lines to the same plot.

```
In [7]:     x = np.linspace(0, np.pi * 2, 500)
     y = np.sin(x)
     z = np.tan(x)
     w = np.cos(x)

In [8]:     plt.plot(x, y, 'blue')
     plt.plot(x, z, 'red')
     plt.show() # the scale of the two functions make this graph undesirable
```



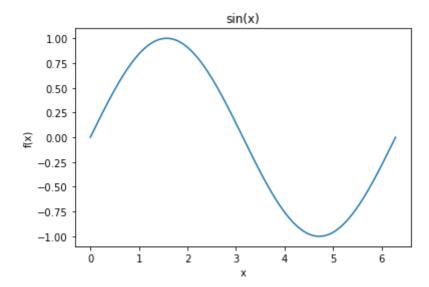
```
In [9]:
    plt.plot(x, y, 'blue')
    plt.plot(x, w, 'orange')
    plt.show()
```



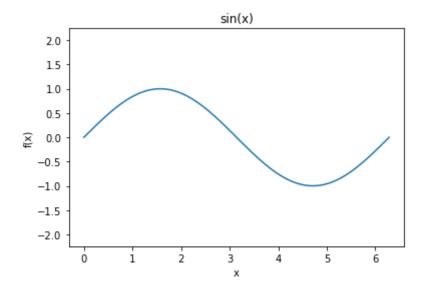
changing labels and axis limits

changing labels and axis limits

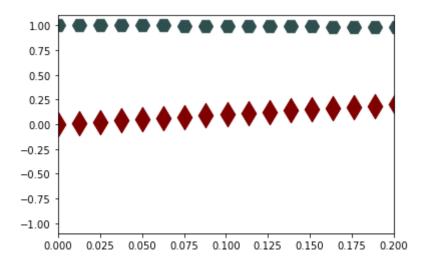
```
In [10]:
    plt.plot(x, y)
    plt.title('sin(x)')
    plt.xlabel('x')
    plt.ylabel('f(x)')
    plt.show()
```



```
In [11]:
    plt.plot(x, y)
    plt.title('sin(x)')
    plt.xlabel('x')
    plt.ylabel('f(x)')
    plt.xlim(0, 2 * np.pi)
    plt.axis('equal') # aspect ratio # investigate Later
    plt.show()
```



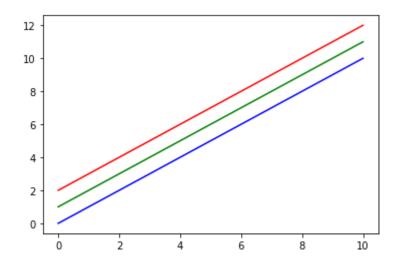
```
In [12]:
    plt.scatter(x, y, s = 300, marker = 'd', color = 'maroon')
    plt.scatter(x, w, s = 200, marker = 'H', color = 'darkslategrey')
    plt.xlim([0, .2])
    plt.show()
```



Plot options: colors

Plot options: colors

```
In [13]:
# colors
x = np.linspace(0, 10, 1000)
plt.plot(x, x, color = 'b')
plt.plot(x, x+1, color = 'g')
plt.plot(x, x+2, color = 'r')
plt.show()
```



List of colors and single character shortcuts

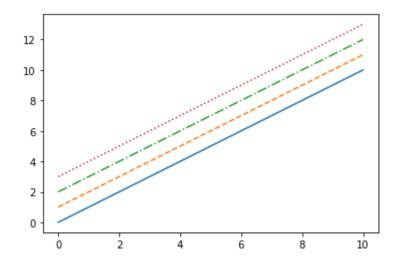
character	color		
'b'	blue		
'g'	green		
'r'	red		
'c'	cyan		
'm'	magenta		
'y'	yellow		
'k'	black		
'W'	white		

List of Named Colors: https://matplotlib.org/examples/color/named_colors.html

Plot options: line type

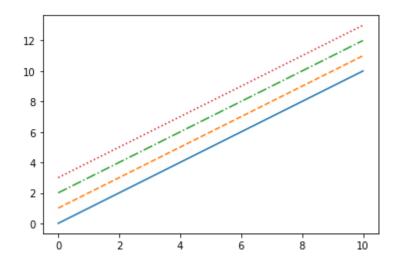
Plot options: line type

```
In [14]:
# line style
x = np.linspace(0, 10, 1000)
plt.plot(x, x , linestyle = '-') # solid
plt.plot(x, x+1, linestyle = '--') # dashed
plt.plot(x, x+2, linestyle = '--') # dash dot
plt.plot(x, x+3, linestyle = ':') # dotted
plt.show()
# default behavior uses different colors for multiple lines
```



Plot options: line type

```
In [14]:
# line style
x = np.linspace(0, 10, 1000)
plt.plot(x, x , linestyle = '-') # solid
plt.plot(x, x+1, linestyle = '--') # dashed
plt.plot(x, x+2, linestyle = '--') # dash dot
plt.plot(x, x+3, linestyle = ':') # dotted
plt.show()
# default behavior uses different colors for multiple lines
```

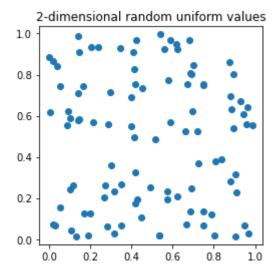


https://matplotlib.org/examples/lines_bars_and_markers/line_styles_reference.html

Plot options: figure size, axis, title

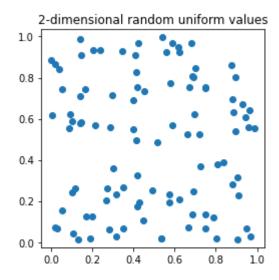
Plot options: figure size, axis, title

```
In [15]:
    np.random.seed(1)
    x = np.random.random(100)
    y = np.random.random(100)
    plt.figure(figsize = (4,4)) # define the properties of the figure first
    plt.scatter(x,y) # then add content
    plt.axis('equal') # alter properties
    plt.title('2-dimensional random uniform values')
    plt.show()
```



Plot options: figure size, axis, title

```
In [15]:
    np.random.seed(1)
    x = np.random.random(100)
    y = np.random.random(100)
    plt.figure(figsize = (4,4)) # define the properties of the figure first
    plt.scatter(x,y) # then add content
    plt.axis('equal') # alter properties
    plt.title('2-dimensional random uniform values')
    plt.show()
```



documentation for figure() https://matplotlib.org/api/_as_gen/matplotlib.pyplot.figure.html

adding point size and color options to a scatter plot

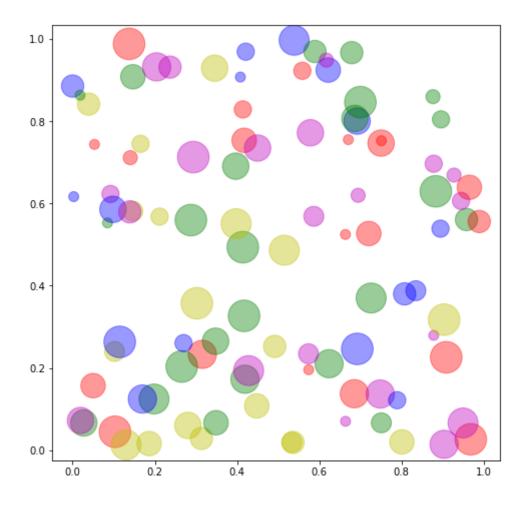
adding point size and color options to a scatter plot

```
In [16]:
           z = 100 * np.random.randint(1,11,100) # use for size
           w = np.random.randint(0,5,100) # use for color
           print(z)
           print(w)
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```

adding point size and color options to a scatter plot

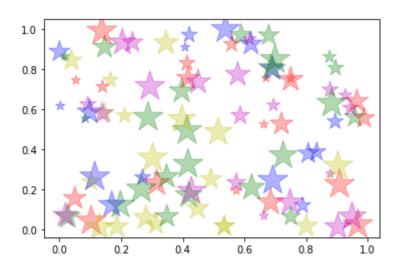
```
In [16]:
           z = 100 * np.random.randint(1,11,100) # use for size
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           print(z)
           print(w)
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In [17]:
           colors = np.array(['r','b','g','m','y'])
           c = colors[w]
           print(c)
            ['g' 'r' 'b' 'y' 'g' 'm' 'y' 'y' 'g' 'b' 'g' 'r' 'm' 'm' 'g' 'r' 'r' 'r'
             'b' 'm' 'm' 'm' 'b' 'm' 'm' 'm' 'b' 'm']
```

```
In [18]:
# we can map the property size (s) to a variable z
# we can map the color (c) to a variable c
plt.figure(figsize = (8,8))
plt.scatter(x, y, s = z, c = c, alpha = 0.4) # alpha modifies transparency
plt.axis('equal')
plt.show()
```



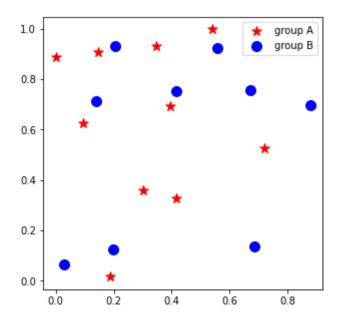
```
In [19]:
```

```
# you can change the point markers
plt.scatter(x, y, s = z, c = c, marker = "*", alpha = 0.3)
# But you can't map the markers to a variable
plt.show()
```



character	description
11	point marker
1.1	pixel marker
'o'	circle marker
'V'	triangle_down marker
١٨١	triangle_up marker
'<'	triangle_left marker
'>'	triangle_right marker
'1'	tri_down marker
'2'	tri_up marker
'3'	tri_left marker
'4'	tri_right marker
's'	square marker
'p'	pentagon marker
1*1	star marker
'h'	hexagon1 marker
'H'	hexagon2 marker
'+'	plus marker
'X'	x marker
'D'	diamond marker
'd'	thin_diamond marker

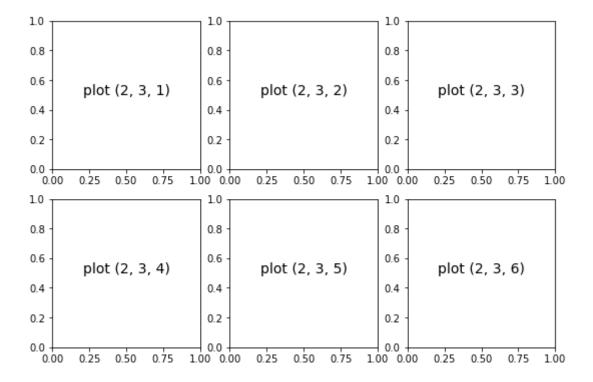
```
In [20]:
# You can call 'scatter' multiple times to plot different groups, each with its own label
# then call plt.legend() to add a legend with the appropriate labels
plt.figure(figsize = (5,5))
plt.scatter(x[0:10] , y[0:10] , s = 100, c = 'red' , marker = "*", label = 'group A')
plt.scatter(x[11:20], y[11:20], s = 100, c = 'blue', marker = "o", label = 'group B')
plt.legend()
plt.show()
```



Complex layouts with subplots

Complex layouts with subplots

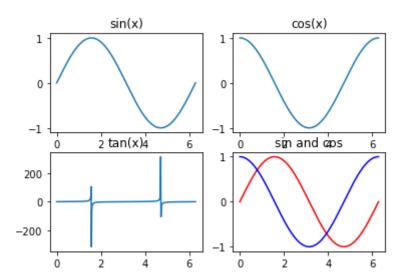
```
In [21]:
# Subplots
plt.figure(figsize = (9,6))
for i in range(1, 7):
    plt.subplot(2, 3, i) # two rows of subplots, three columns of plots, work in plot i
    plt.text(0.5, 0.5, 'plot ' + str((2, 3, i)), fontsize = 14, ha='center')
    # plt.text adds text, first two will be the xy position, the character string
```



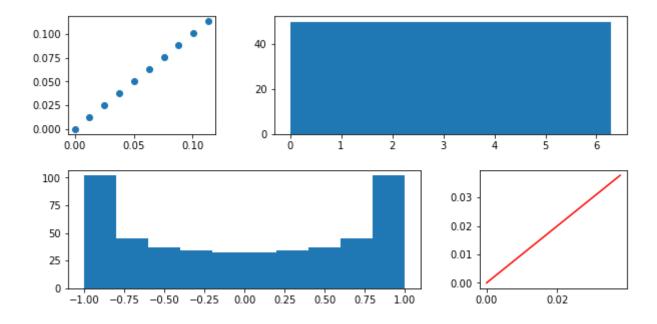
Subplots example

Subplots example

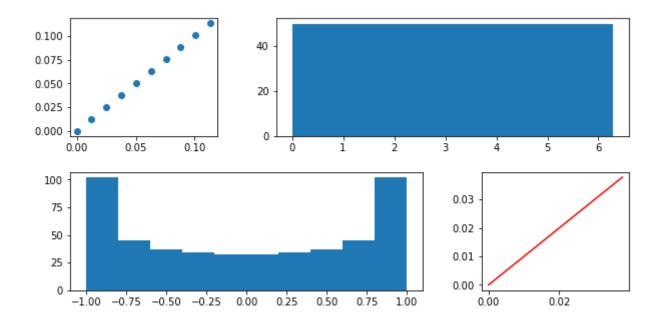
```
In [22]:
            x = np.linspace(0, np.pi * 2, 500)
            y = np.sin(x)
            z = np.tan(x)
            w = np.cos(x)
            plt.subplot(2,2,1) # number of rows, number of columns, which plot you want to draw
            plt.plot(x, y)
            plt.title("sin(x)")
            plt.subplot(2,2,2) # subplot 2 will be upper right
            plt.plot(x, w)
            plt.title("cos(x)")
            plt.subplot(2,2,3) # subplot 3 will be lower left
            plt.plot(x, z)
            plt.title("tan(x)")
            plt.subplot(2,2,4)
            plt.plot(x,y, 'red')
            plt.plot(x,w, 'blue')
            plt.title("sin and cos")
            plt.show()
```



```
In [23]:
    plt.figure(figsize = (10,5))
    # More Complicated Grids
    grid = plt.GridSpec(2, 3, wspace=0.4, hspace=0.3)
    plt.subplot(grid[0, 0]) # gridspec uses 0 based indexing
    plt.scatter(x[0:10], y[0:10])
    plt.subplot(grid[0, 1:3]) # top row, columns 1:3
    plt.hist(x)
    plt.subplot(grid[1, :2])
    plt.hist(y)
    plt.subplot(grid[1, 2])
    plt.plot(x[0:4], y[0:4], c = 'r')
    plt.show()
```



```
In [23]:
    plt.figure(figsize = (10,5))
        # More Complicated Grids
        grid = plt.GridSpec(2, 3, wspace=0.4, hspace=0.3)
        plt.subplot(grid[0, 0]) # gridspec uses 0 based indexing
        plt.scatter(x[0:10], y[0:10])
        plt.subplot(grid[0, 1:3]) # top row, columns 1:3
        plt.hist(x)
        plt.subplot(grid[1, :2])
        plt.hist(y)
        plt.subplot(grid[1, 2])
        plt.plot(x[0:4], y[0:4], c = 'r')
        plt.show()
```



subplot documentation: https://matplotlib.org/api/_as_gen/matplotlib.pyplot.subplot.html? highlight=subplot#matplotlib.pyplot.subplot

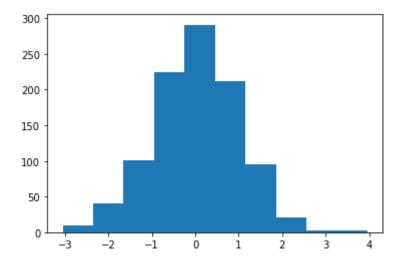
Histograms

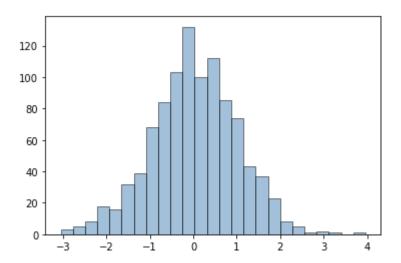
Histograms

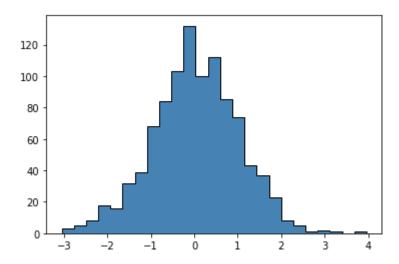
```
In [24]: # more histograms

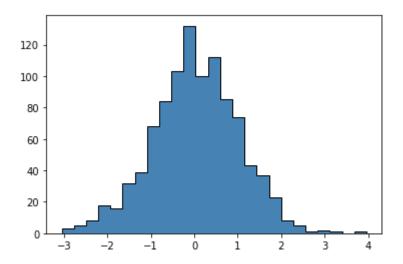
data = np.random.randn(1000)

plt.hist(data)
plt.show()
```







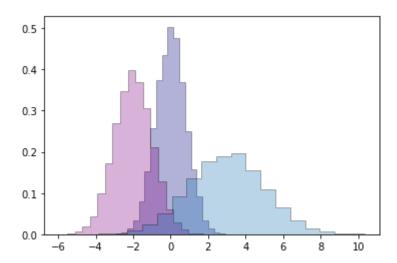


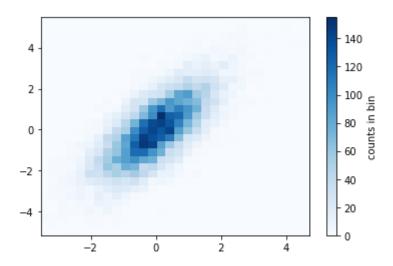
hist documentation: https://matplotlib.org/api/_as_gen/matplotlib.pyplot.hist.html? highlight=hist#matplotlib.pyplot.hist

```
In [27]:
    x1 = np.random.normal(0, 0.8, 10000)
    x2 = np.random.normal(-2, 1, 10000)
    x3 = np.random.normal(3, 2, 10000)

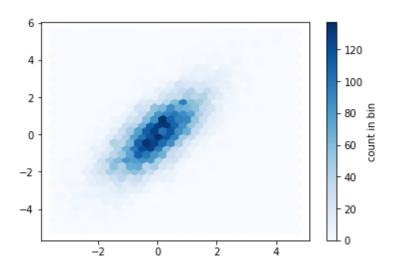
# set up a dictionary with arguments
    kwargs = dict(histtype='stepfilled', alpha=0.3, density=True, bins=20, edgecolor = 'black')

# use the same arguments for all of the histograms without the need to copy and paste
    plt.hist(x1, **kwargs, color = 'navy')
    plt.hist(x2, **kwargs, color = "purple")
    plt.hist(x3, **kwargs)
    plt.show()
```





```
In [29]:
    plt.hexbin(x, y, gridsize=30, cmap='Blues')
    cb = plt.colorbar(label='count in bin')
```



two dimensional functions

two dimensional functions

two dimensional functions

```
In [30]:
           x = np.array([0,1,2,3])
           y = np.array([-1,0,1, 2])
           print(x)
           print(y)
           X, Y = np.meshgrid(x,y) # sees x has length 3, y has length 4, so the result is a 4 x 3 grid
           [0 1 2 3]
           [-1 \ 0 \ 1 \ 2]
In [31]:
           def f(x, y):
              return x * y
           X, Y = np.meshgrid(x,y)
           Z = f(X, Y)
           print(Z)
           [[ 0 -1 -2 -3]
            [0 0 0 0]
            [ 0 1 2 3]
             [0 2 4 6]]
```

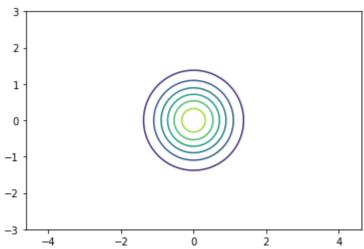
```
In [32]:
    x = np.linspace(-3, 3, 101)
    y = np.linspace(-3, 3, 101)
    X, Y = np.meshgrid(x, y)

def g (x, y):
    return np.exp(-(x**2)) * np.exp(-(y**2)) # product of 2 normal distributions

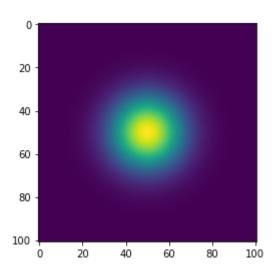
Z = g(X, Y)
```

Out[33]: (101, 101)

```
In [32]:
            x = np.linspace(-3, 3, 101)
            y = np.linspace(-3, 3, 101)
            X, Y = np.meshgrid(x, y)
            def g (x, y):
                return np.exp(-(x**2)) * np.exp(-(y**2)) # product of 2 normal distributions
            Z = g(X, Y)
In [33]:
            Z.shape
Out[33]:
            (101, 101)
In [34]:
            plt.contour(X, Y, Z)
            plt.axis('equal')
            plt.show()
```



```
In [35]: plt.imshow(Z)
    plt.show()
```



```
In [36]:
    ts = pd.Series(np.random.randn(1000),
        index=pd.date_range('1/1/2000', periods=1000))
```

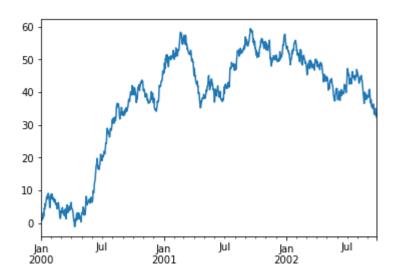
```
In [36]:
          ts = pd.Series(np.random.randn(1000),
             index=pd.date_range('1/1/2000', periods=1000))
In [37]:
          ts
           2000-01-01
Out[37]:
                         1.161351
           2000-01-02
                        -0.399784
           2000-01-03
                        0.688814
           2000-01-04
                        -0.253723
           2000-01-05
                        -0.136547
           2002-09-22
                        -0.068322
           2002-09-23
                        0.453897
           2002-09-24
                        -2.010975
           2002-09-25 0.871980
           2002-09-26
                        -1,478780
           Freq: D, Length: 1000, dtype: float64
```

```
In [36]:
           ts = pd.Series(np.random.randn(1000),
             index=pd.date_range('1/1/2000', periods=1000))
In [37]:
           ts
           2000-01-01
Out[37]:
                         1.161351
           2000-01-02
                        -0.399784
           2000-01-03
                        0.688814
           2000-01-04
                        -0.253723
           2000-01-05
                        -0.136547
           2002-09-22
                        -0.068322
           2002-09-23
                       0.453897
           2002-09-24
                        -2.010975
           2002-09-25 0.871980
           2002-09-26
                        -1.478780
           Freq: D, Length: 1000, dtype: float64
In [38]:
           ts = ts.cumsum()
```

```
In [39]:
Out[39]:
           2000-01-01
                          1.161351
           2000-01-02
                          0.761566
           2000-01-03
                          1.450381
           2000-01-04
                          1.196657
           2000-01-05
                          1.060111
           2002-09-22
                         34.602416
           2002-09-23
                         35.056313
           2002-09-24
                         33.045338
           2002-09-25
                         33.917318
           2002-09-26
                         32.438537
           Freq: D, Length: 1000, dtype: float64
```

In [40]: ts.plot()

Out[40]: <AxesSubplot:>



DataFrames in Pandas support basic visualizations directly.

https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.plot.html

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Example 1:

A data frame with several columns of time-series data

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https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.plot.html

Example 1:

A data frame with several columns of time-series data

```
In [41]:
    df = pd.DataFrame(np.random.randn(1000, 4), index = ts.index, columns = list('ABCD'))
```

DataFrames in Pandas support basic visualizations directly.

https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.plot.html

Example 1:

A data frame with several columns of time-series data

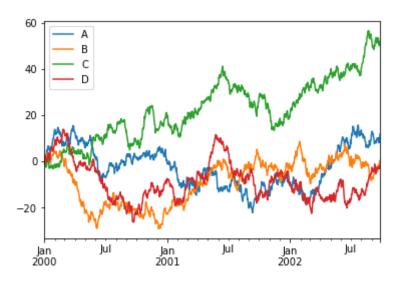
```
In [41]:
                df = pd.DataFrame(np.random.randn(1000, 4), index = ts.index, columns = list('ABCD'))
In [42]:
                df = df.cumsum()
                df
                                                      C
Out[42]:
               2000-01-01
                                     -0.455540
                                                         -1.028464
                            1.228413
                                               -0.532579
               2000-01-02
                            2.621425
                                      0.000538
                                               -0.742925
                                                          1.427698
                            2.170190
               2000-01-03
                                     -1.408664
                                               -1.085901
                                                          2.218128
               2000-01-04
                            1.959056 -1.738246
                                               -0.956508
                                                          2.225535
                                               -0.550996
               2000-01-05
                            1.871284
                                     -0.332684
                                                          0.869890
               2002-09-22
                            8.019642
                                     -1.526915
                                               51.653375
                                                         -3.242759
               2002-09-23
                            8.525085 -2.704152
                                               50.186367 -2.390122
               2002-09-24
                            8.122309
                                     -0.464831
                                               50.595956
                                                         -2.749689
               2002-09-25
                           10.585510
                                      0.196054
                                               51.958605
                                                        -1.728218
               2002-09-26 11.858522
                                     0.356034
                                               49.999471 -3.080693
```

 $1000 \text{ rows} \times 4 \text{ columns}$

Calling plot on the data frame will produce a plot with a line for each column with a legend

Calling plot on the data frame will produce a plot with a line for each column with a legend

In [43]:
 plt.figure()
 df.plot()



You can also call plot on a single series and specify kind = "bar" to create a bar plot

You can also call plot on a single series and specify kind = "bar" to create a bar plot

```
In [44]: df.iloc[5]

Out[44]: A    2.575327
    B    1.572246
    C    -2.606275
    D    0.626440
    Name: 2000-01-06 00:00:00, dtype: float64
```

You can also call plot on a single series and specify kind = "bar" to create a bar plot

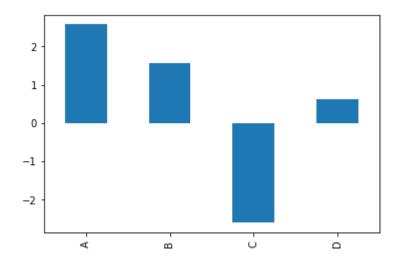
```
In [44]: df.iloc[5]
```

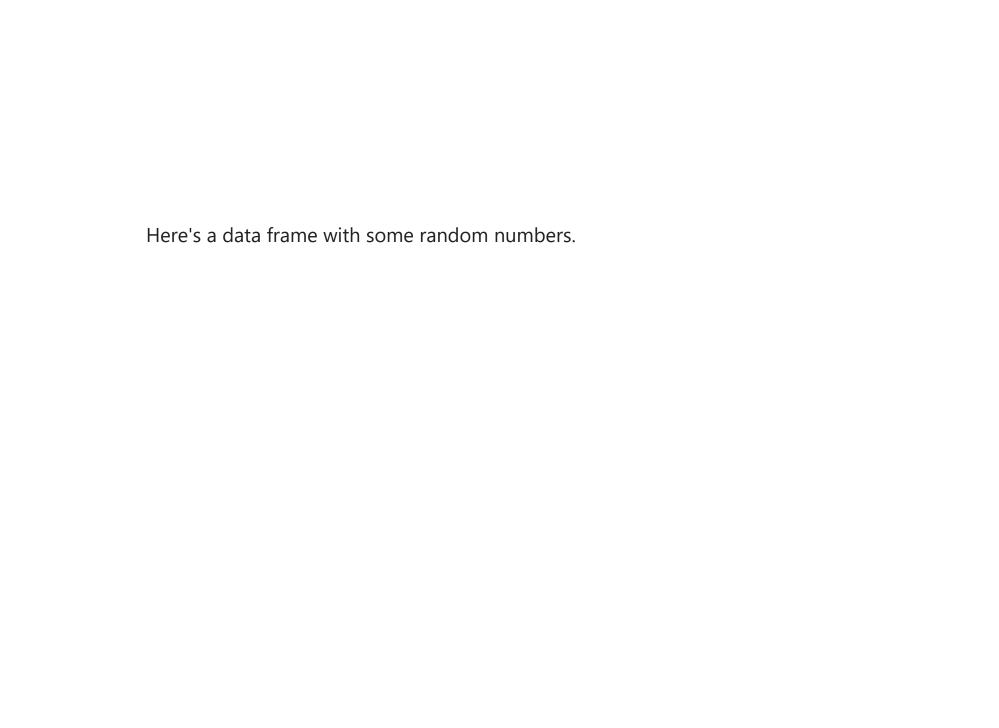
Out[44]: A 2.575327 B 1.572246 C -2.606275 D 0.626440

Name: 2000-01-06 00:00:00, dtype: float64

```
In [45]:
    df.iloc[5].plot(kind = "bar")
```

Out[45]: <AxesSubplot:>





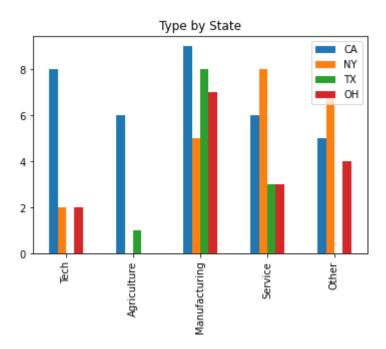
Here's a data frame with some random numbers.

Out[46]: CA NY TX OH Agriculture 8 2 0 2 Agriculture 6 0 1 0 Manufacturing 9 5 8 7 Service 6 8 3 3

Other

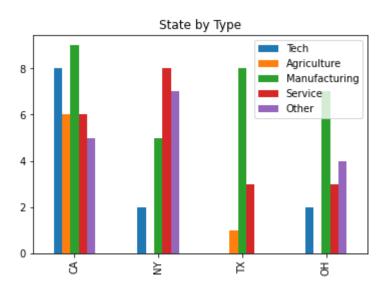
```
In [47]:
    df2.plot.bar()
    plt.title("Type by State")
```

Out[47]: Text(0.5, 1.0, 'Type by State')



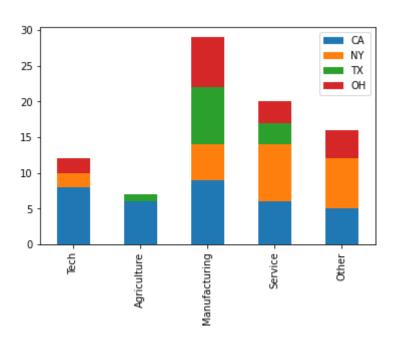
```
In [48]:
    df2.T.plot.bar()
    plt.title("State by Type")
```

Out[48]: Text(0.5, 1.0, 'State by Type')



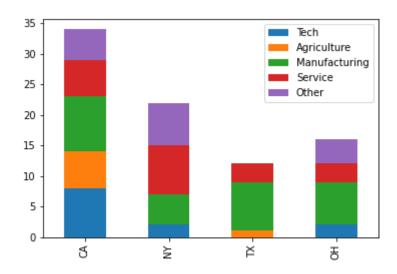
In [49]: df2.plot.bar(stacked=True)

Out[49]: <AxesSubplot:>



In [50]: df2.T.plot.bar(stacked=True)

Out[50]: <AxesSubplot:>



A data frame consisting of random die rolls.

Column 'one' shows the sum after one roll. (min is 1, max is 6, dist is uniform)

Column 'two' shows the sum after two rolls. (min is 2, max is 12, dist is triangular)

A data frame consisting of random die rolls.

Column 'one' shows the sum after one roll. (min is 1, max is 6, dist is uniform)

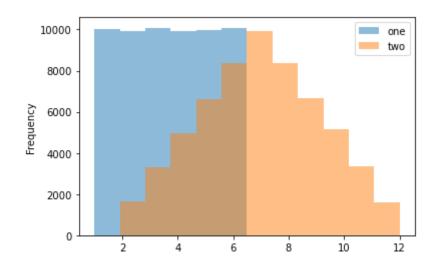
Column 'two' shows the sum after two rolls. (min is 2, max is 12, dist is triangular)

```
In [51]:

df = pd.DataFrame(np.random.randint(1, 7, 60000), columns = ['one'])

df['two'] = df['one'] + np.random.randint(1, 7, 60000)

ax = df.plot.hist(bins=12, alpha=0.5)
```



Column 'three' shows the sum after three rolls. (min is 3, max is 18)

And so on... as we add more dice rolls, we see the central limit theorem start to take effect.

Column 'three' shows the sum after three rolls. (min is 3, max is 18)

And so on... as we add more dice rolls, we see the central limit theorem start to take effect.

```
In [52]:

df['three'] = df['two'] + np.random.randint(1, 7, 60000)

df['four'] = df['three'] + np.random.randint(1, 7, 60000)

df['five'] = df['four'] + np.random.randint(1, 7, 60000)
```

Column 'three' shows the sum after three rolls. (min is 3, max is 18)

And so on... as we add more dice rolls, we see the central limit theorem start to take effect.

```
In [52]:
    df['three'] = df['two'] + np.random.randint(1, 7, 60000)
    df['four'] = df['three'] + np.random.randint(1, 7, 60000)
    df['five'] = df['four'] + np.random.randint(1, 7, 60000)
In [53]:

df.plot.hist(bins = 30, alpha = 0.5)
```

Out[53]: <AxesSubplot:ylabel='Frequency'>

