

Artificial Intelligence Lab - 9

Aim : Implementation of uncertain methods – Dempster Shafer Theory

Algorithm :

1. Start
2. Each piece of evidence is represented by a separate belief function
3. Combination rules are then used to successively fuse all these belief
4. functions in order to obtain a belief function representing all available evidence.
5. Specifically, the combination (called the joint mass) is calculated from the two sets of masses m_1 and m_2 in the following manner:

- $m_{1,2}(\emptyset) = 0$
- $m_{1,2}(A) = (m_1 \oplus m_2)(A) = (1/1-K) \sum_{B \cap C = A \neq \emptyset} m_1(B) m_2(C)$

where,

- $K = \sum_{B \cap C = \emptyset} m_1(B) m_2(C)$

K is a measure of the amount of conflict between the two mass sets.

6. In python Mass-Function has the built-in combination rules.
7. Stop

Code :

```
from numpy import *
def DempsterRule(m1, m2):
    ## extract the frame of discernment
    sets=set(m1.keys()).union(set(m2.keys()))
    result=dict.fromkeys(sets,0)
    ## Combination process
    for i in m1.keys():
        for j in m2.keys():
            if set(str(i)).intersection(set(str(j))) == set(str(i)):
                result[i]+=m1[i]*m2[j]
            elif set(str(i)).intersection(set(str(j))) == set(str(j)):
                result[j]+=m1[i]*m2[j]
    ## normalize the results
    f= sum(list(result.values()))
    for i in result.keys():
        result[i] /=f
    return result
m1 = {'a':0.4, 'b':0.2, 'ab':0.1, 'abc':0.3}
m2 = {'b':0.5, 'c':0.2, 'ac':0.3, 'a':0.0}
print(DempsterRule(m1, m2))
```

Output :

```
{'b': 0.5263157894736842, 'ab': 0.0, 'ac': 0.15789473684210523, 'abc': 0.0, 'c': 0.10526315789473682, 'a': 0.21052631578947364}
```

```
Process exited with code: 0
```

Result :

Hence, the Implementation of Dempster Shafer Theory is done successfully.

Artificial Intelligence Lab

Lab-9

Aim : Implementation of uncertain methods
(Dempster Shafer Theory)

Problem Formulation:

To solve inference problem representing uncertain method to obtain a belief function.

Using the mass function which has built-in combination rules obtain the Dempster rule of combination.

Initial State

$$m_1 = \{ 'a': 0.4, 'b': 0.2, 'ab': 0.1, 'abc': 0.3 \}$$

$$m_2 = \{ 'b': 0.5, 'c': 0.2, 'ac': 0.3, 'a': 0.0 \}$$

Final State

$$\{ 'ac': 0.157894,$$

$$'c': 0.105263,$$

$$'b': 0.5263157,$$

$$'ab': 0.0, 'abc': 0.0,$$

$$'a': 0.21052631 \}$$

Problem Solving

The combination is calculated from the two sets of masses m_1 & m_2 in the following manner:

$$\bullet m_{1,2}(\emptyset) = 0$$

$$\bullet m_{1,2}(A) = (m_1 \oplus m_2)(A) = \frac{1}{1-K} \sum_{B \cap C = A \neq \emptyset} m_1(B) m_2(C)$$

where, $K = \sum_{B \cap C = \emptyset} m_1(B) m_2(C)$

Combination of m_1 & m_2 ,

$$\{ 'b' \}: 0.5, \{ 'a' \}: 0.2499, \{ 'c', 'a' \}: 0.1499, \{ 'c' \}: 0.09999 \}$$