

β -value = upper bound.



Roll No.

(B.Tech./MTech./Ph.D.) Name:

Problem: Consider the problem of maximizing the function $f(x) = x^2, 0 \leq x \leq 31$.

Simulated annealing

Given initial temperature, $T = 1000$

A solution is represented with a 5-bit string.

The initial State (or solution) is 10011 ($x = 19$ and $f(x) = 361$).

A neighbouring state is obtained just by flipping a bit randomly.

Candidate state 1: 11011 ($x = 27$ and $f(x) = 729$)

Compute $\Delta E = 361 - 729 = -368$

$\Delta E \leq 0$ accept the state

Candidate state 2: 01011 ($x = 11$ and $f(x) = 121$)

Compute $\Delta E = 729 - 121 = 608$

Compute the acceptance probability with $T = 1000$

$$\exp\left(\frac{-\Delta E}{T}\right) = \exp\left(\frac{-608}{1000}\right) = 0.544$$

Try computing the acceptance probability with $T = 100$

$$\exp\left(\frac{-\Delta E}{T}\right) = \exp\left(\frac{-608}{100}\right) = 0.002$$

Genetic algorithm

Initial Population

String no.	Initial popln.	X value	f(x)	Selec. Prob.	Selection
1	01101	13	169	0.144	1
2	11000	24	576	0.492	2
3	01000	8	64	0.054	0
4	10011	19	361	0.308	1

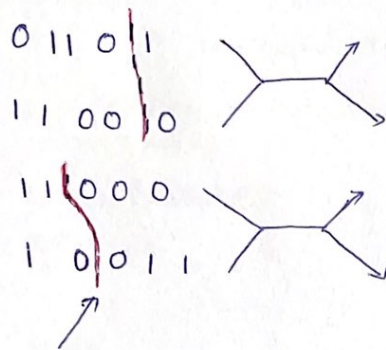
String 1
Selected
once
twice
not
selected
Selected
once

Given: Mating pool : 2-1, 4-3

Cross over site: 44 2 2

Selected
population

New population



01100 → 12
11001 → 25
11011 → 27
10000 → 16

Cross over
site

Roll No.

(B.Tech./MTech./Ph.D.) Name:

1. Consider the candy examples as discussed in the class. Show the calculations for the first iteration of EM. [5 marks]

Learning of parameter θ

E-Step

$$\hat{N}(\text{Bag} = 1) = \sum_{j=1}^N P(\text{Bag} = 1 | \text{flavor}_j, \text{wrapper}_j, \text{hole}_j)$$

M-step

$$\theta_1 = \frac{\hat{N}(\text{Bag} = 1)}{N}$$

* solution is available in the book.

2. Consider a single Boolean random variable Y (the 'classification'). Let the prior probability $P(Y = \text{true})$ be π . Let's try to find π , given a training set $D = (y_1, \dots, y_N)$ with N independent samples of Y . Furthermore, suppose p of the N are positive and n of the N are negative. [5 marks]

(a) Write down an expression for the likelihood of D (i.e. the probability of seeing this particular sequence of examples, given a fixed value of π) in terms of π , p and n .

(b) By differentiating the log likelihood L , find the value of π that maximizes the likelihood.

$$P(Y = \text{true}) = \pi$$

$$P(Y = \text{false}) = (1 - \pi)$$

$p = \#$ positive samples

$n = \#$ negative samples

Probability of data is $\pi^p (1 - \pi)^n$

$$\text{Log likelihood} = L = p \log \pi + n \log (1 - \pi)$$

Setting the derivative to 0.

$$\frac{\partial L}{\partial \pi} = \frac{p}{\pi} - \frac{n}{1 - \pi} = 0$$

so, ML value is $\pi = p / (p + n)$ which is the

proportion of positive examples in the data.