

Question (1) a

$$h = \theta^T(x) + \theta_0$$

$$h(x) = \theta_0 + \theta_1 x$$

to find θ_0 & θ_1

$$\arg \min_{\theta} \sum_{i=1}^m (y^{(i)} - (\theta_0 + \theta_1 x^{(i)}))^2$$

Taking partial derivatives.

$$\theta_0 = \frac{\sum_{i=1}^m y^{(i)} - \theta_1 x^{(i)}}{m} \quad \text{--- (a)}$$

$$\theta_1 = \frac{\sum_{i=1}^m x^{(i)} (y^{(i)} - \theta_0)}{\sum_{i=1}^m (x^{(i)})^2} \quad \text{--- (b)}$$

i	x	y
1	-2	2
2	2	4
3	3	8
4	5	11
5	4	17

$m=5$

$$\theta_0 = (2 + 2\theta_1 + 4 - 2\theta_1 + 8 - 3\theta_1 + 11 - 5\theta_1 + 17 - 4\theta_1) / 5$$

$$\theta_0 = (42 - 12\theta_1) / 5$$

$$5\theta_0 + 12\theta_1 = 42 \quad \text{--- (c)}$$

Putting (x^i, y^i) in (b)

$$\theta_1 = \frac{-2(2 - \theta_0) + 2(4 - \theta_0) + 3(8 - \theta_0) + 5(11 - \theta_0) + 4(17 - \theta_0)}{4 + 4 + 9 + 25 + 16}$$

$$4 + 4 + 9 + 25 + 16$$

$$1200 + 580 = 151 \quad \text{--- ②}$$

$$500 + 120 = 42 \quad \text{--- ①}$$

$$\textcircled{1} \times 12/5$$

→

$$1200 + \frac{1440}{5} = 1008 \quad \text{--- ③}$$

$$1200 + 580 = 151$$

$$- 29.20 = -50.2$$

$$(1000) - 1000 = 0, = 1.72$$

$$Q_0 = 51.29$$

$$y = 51.29 + 1.72x$$

$$Q_0 = 151 - 58 \times 1.72$$

$$12$$

$$= 4.27$$

$$3.6825$$

$$6.41 \times 16.157$$