## q32

## April 19, 2020

```
[]: import numpy as np
     import matplotlib.pyplot as plt
[]: def h(t,a,b,c,d):
         return a*np.exp(b*t) + c*np.exp(d*t)
[]: def momentum_update(x0, A, eta, gamma, num_iters=200):
        X = [x0*1.0]
         x = x0*1.0
         g = 0.0
         for t in range(num_iters):
             g = (1-gamma)*g + gamma*(2*A*x)
             x = x - eta*g
     #
               print(x)
             X.append(x*1.0)
         return X
[]: a = 1.270711
     b = -0.036617
     c = -0.207107
     d = -0.213388
     x0 = 1.0
     A = 1.0
     eta = 1/64
     gamma = 1/4
     num_iters = 200
     def h(t):
         return a*np.exp(b*t) + c*np.exp(d*t)
     t = np.arange(0,200,0.01)
     H = h(t)
     X = momentum_update(x0, A, eta, gamma, num_iters)
     plt.plot(t,H,label=r'continuous estimate of $x_t$')
     plt.plot(X, label=r'True $x_t$')
     plt.xlabel("t")
     plt.ylabel(r'x_t')
```

```
plt.title(r'$x_0 = {}, a = {}, \eta = 1/{}, \gamma = 1/{}$'.format(x0,A,64, 4))
plt.legend()
plt.savefig("./q32_1.png")
plt.show()

[]: a = 1.270711
b = -0.036617
c = -0.207107
d = -0.213388
```

```
x0 = 1.0
A = 1.0
eta = 1/64
gamma = 1/8
num_iters = 200
def h(t):
                               return (1/16)*(np.exp(-t/16))*(t+16)
t = np.arange(0,200,0.01)
H = h(t)
X = momentum_update(x0, A, eta, gamma, num_iters)
plt.plot(t,H,label=r'continuous estimate of $x_t$')
plt.plot(X, label=r'True $x_t$')
plt.xlabel("t")
plt.ylabel(r'x_t')
plt.title(r'$x_0 = {}, a = {}, \beta = 1/{}, \gamma =
plt.legend()
plt.savefig("./q32_2.png")
plt.show()
```

```
[]: a = 1.270711
     b = -0.036617
     c = -0.207107
     d = -0.213388
     x0 = 1.0
     A = 1.0
     eta = 1/64
     gamma = 1/16
     num_iters = 200
     def h(t):
         return np.exp(-t/32)*(np.sin(t/32) + np.cos(t/32))
     t = np.arange(0,200,0.01)
     H = h(t)
     X = momentum_update(x0, A, eta, gamma, num_iters)
     plt.plot(t,H,label=r'continuous estimate of $x t$')
     plt.plot(X, label=r'True $x_t$')
     plt.xlabel("t")
```

```
plt.ylabel(r'x_t')
plt.title(r'$x_0 = {}, a = {}, \eta = 1/{}, \gamma = 1/{}$'.format(x0,A,64, 16))
plt.legend()
plt.savefig("./q32_3.png")
plt.show()
```

```
[]: a = 1.270711
    b = -0.036617
     c = -0.207107
     d = -0.213388
     x0 = 1.0
     A = 901
     eta = 1/64
     gamma = 1/16
     num_iters = 200
     def h(t):
         return (1/30)*np.exp(-t/16)*(np.sin(15*t/8) + 30*np.cos(15*t/8))
     t = np.arange(0,200,0.01)
     H = h(t)
     X = momentum_update(x0, A, eta, gamma, num_iters)
     plt.plot(t,H,label=r'continuous estimate of $x_t$')
     plt.plot(X, label=r'True $x_t$')
     plt.xlabel("t")
     plt.ylabel(r'x_t')
     plt.title(r'$x_0 = {}), a = {}), eta = 1/{}, gamma = 1/{}$'.format(x0,A,64,8))
     plt.legend()
     plt.savefig("./q32_4.png")
     plt.show()
```