

27/01/26.

TIME AND WORK.

1, Core idea:

$$\text{Work} = \text{Efficiency} \times \text{Time}$$

2, Basic Golden Rule:

i) If A can do a work in X days
then A's 1 day work = $\frac{1}{X}$
(This is Most \otimes).

Example: A can do a work in 10 days
so A's 1 day work = $\frac{1}{10}$.

Problems (Basic problems to solve):

1, Person A can complete a piece of work in 10 days
person B can complete a same piece of work in 15 days.
How long will it take for both of them working together to complete the work?

Method 1 (Fraction but little bit complicated).

A = 10 days then $A = \frac{1}{10}$

B = 15 days then $B = \frac{1}{15}$.

They work together:

$$A+B = \frac{1}{10} + \frac{1}{15} \text{ (Take LCM then)}$$

$$A+B = \frac{3+2}{30} = \frac{5}{30} = \frac{1}{6} = 6$$

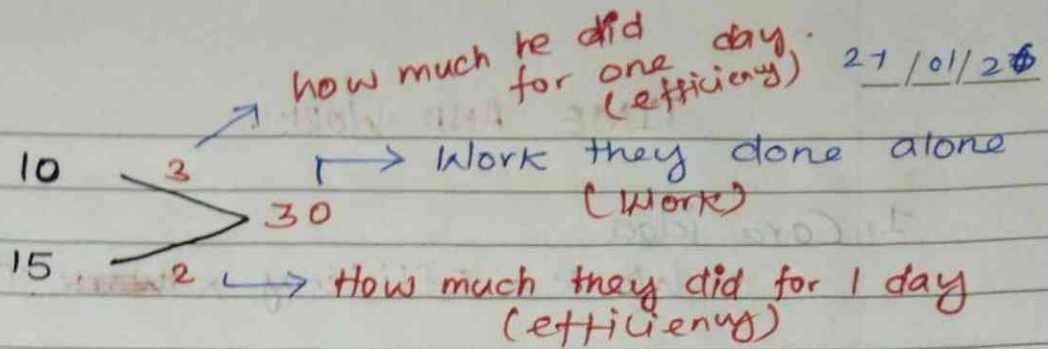
Ans: 6 days.

Method 2 (concept wise more easy).

$$\text{Work} = \text{Efficiency} \times \text{Time}.$$

A = 10 days B = 15 days

(They given time so we need to find out the efficiency and work).



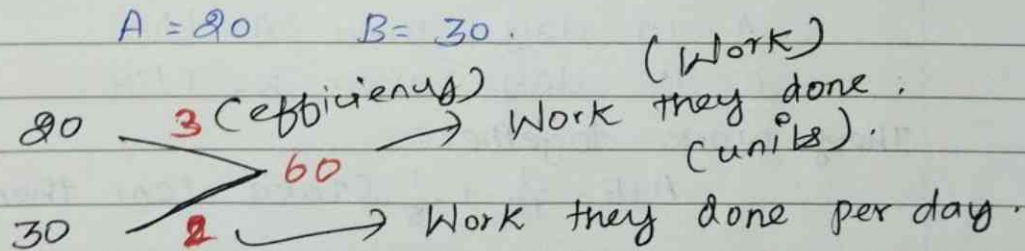
*) Ippo A Vanthu oru Velaya mudika 10 days aguthu, avan oru nalaiku 3 unit work mudipadu. Total avan complete pannathu 30 unit work.

*) Ippo Inga paaru avanga 2 perum seranthu Mudikora $3+2 = 5$ unit of Work. per day.

$$= \frac{30}{5} = 6 \text{ ans} = 6 \text{ days}$$

Ippo \rightarrow Work = time \times efficiency then
Time = Work / efficiency

Q) A person A can complete a piece of work in 20 days, person B can complete a same piece of work in 30 days. How long will it take for both of them working together?



Time = Work / efficiency.

$$= 60 / 3+2 \Rightarrow 60 / 5 = 12.$$

Ans: 12 days.

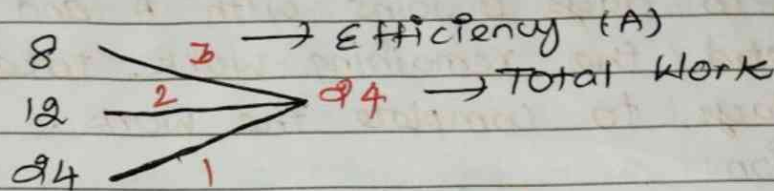
3- person A can complete a piece of work in 8 days, person B can complete a piece of work in 12 days, person C can complete a work in 24 days. How long they take to complete it

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Working together to complete the Work?

Solution:

A = 8 days B = 12 days C = 24 days



Time = Work / efficiency.

$$\text{Time} = 24 / (3 + 2 + 1) = 24 / 6 = 4.$$

Ans: 4 days.

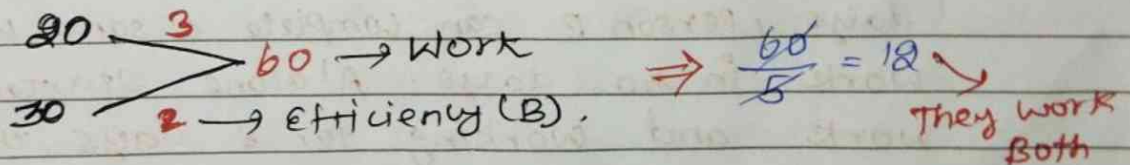
PART-II

PERSON LEFT AFTER SOME DAYS!

Question 1: Person A can complete a piece of work in 20 days. Person B can complete a same piece of work in 30 days? They Both started the work together After 4 days 'A' left the job and remaining work done by B alone. How long will it take to complete the remaining work? total number of days to complete the work?

Solution:

A = 20 days B = 30 days



$$\Rightarrow \frac{60}{5} = 12 \rightarrow \text{They work Both}$$

*) After 4 days A left the job (means they work 4 days together).

A = 3 unit B = 2 unit $4 \times 5 = 20$

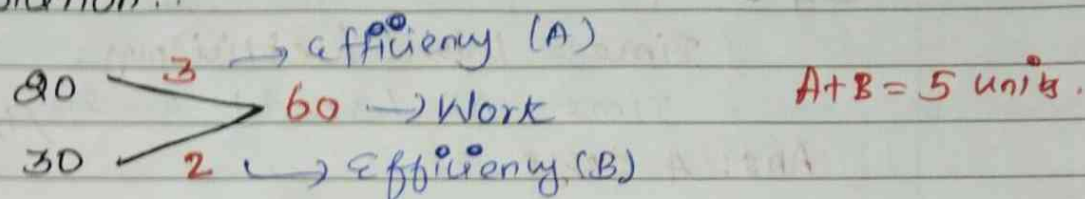
$60 - 20 = 40$ Remaining.

$40 \times 2 = 40 \rightarrow$ remaining work (pending).
B efficiency
days to complete remaining work

remaining work done in 20 days,

2) person A can complete a piece of work in 20 days, person B can complete a piece of work in 30 days, A alone started the work, after 10 days B joins with A and together completed the remaining work. Total number of days to complete the work.

Solution:



A alone started the work 10 days.

$$10 \times 3 = 30 \quad 60 - 30 = 30 \text{ (remaining)}$$

4) Tppo into the remaining 30 units of work is did by the A and B.

$$= 30 / 5 = 6 \text{ days.}$$

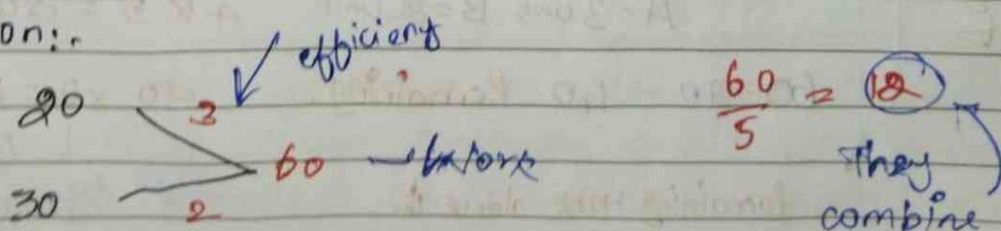
A alone work for 10 days then the both complete the remaining work in 6 days.

$$10 + 6 = 16 \text{ days.}$$

Ans: 16 days.

3, person A can complete a piece of work in 20 days, person B can complete a same piece of work in 30 days. A alone started the work and working for 8 days, then left B complete the remaining work by working alone. Find the days to complete by B.

Solution:-



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A' started to working alone for 8 days.

$$\rightarrow 3 \times 8 = 24$$

A's unit \uparrow 8 days

$$\Rightarrow 60 - 24$$

36 remaining

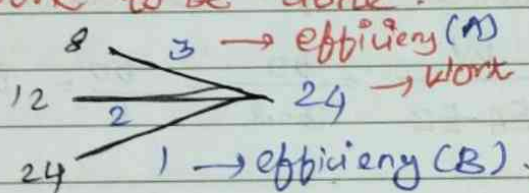
(A' left and B Working alone)

$$\star) 36/2 = 18 \text{ days.}$$

\rightarrow remaining work to done.

\star) Hence the remaining work 18 days to complete

- 4) person A can complete a piece of work in 8 days, person B can complete a work in 12 days and person C can complete a work in 24 days. All of them working together. After 2 days A left the job. In how many days the remaining work to be done.



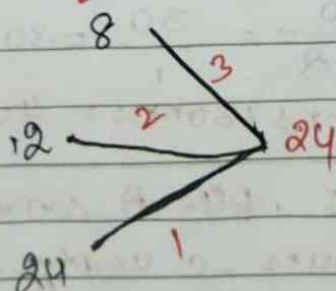
$$\frac{24}{6} = 4$$

All working together (2 days) = $2 \times 4 = 8$ $24 - 8 = 16$

Remaining Work = $16/3 = 6$

The remaining work done in 6 days.

- 5) person A complete in 8 days, person B can complete a piece of work 12 days, person C complete 24 days. A alone started the work after 2 days B and C joins with the A. Find total?



A Alone

$$2 \times 3 = 6$$

$$24 - 6 = 18$$

B and C join

$$\frac{18}{6} = 3$$

Total number of days = $3 + 2 = 5$ days.

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CISTERN SUMS:

- 1) A cistern has 3 pipes A, B, C. pipe A can fill a tank in 5 hours, pipe B can fill a tank in 6 hours. Pipe C can empty a filled tank in 3 hours. How long will it take if all the three pipes are opened together to fill the tank?

$$\begin{array}{rcl} A & 5 & 6 \\ B & 6 & 5 \\ C & 3 & 10 \end{array} \rightarrow 30$$

$$\begin{array}{l} A+B-C \\ 5+6-3 \\ 1 \end{array}$$

$$\frac{30}{1} = 30 \text{ hrs.}$$

$$\frac{\text{Total work}}{EA+EB-EC} = \frac{30}{1} = 30$$

Because it empty the tank.

- 2) A cistern can be filled by a pipe A in 20 hours it can empty by B in 30 hours, if both opened together how long will it take to fill the tank?

$$\begin{array}{rcl} 20 & 3 & 60 \\ 30 & 2 & \end{array} \rightarrow 60$$

$$\frac{W}{EA-EB} = \frac{60}{3-2} = \frac{60}{1} = 60 \text{ hrs.}$$

- 3) A cistern can be filled by A pipe A in 20 hours, while it can empty by pipe B in 30 hours, If pipe A opened first, after 10 hours pipe B also opened, Find the total time taken to fill the whole tank?

$$\begin{array}{rcl} 20 & 3 & 60 \\ 30 & 2 & \end{array} \rightarrow 60$$

$$A's 10 \text{ hours} = 10 \times 3 = 30$$

$$\text{Remaining} = 60 - 30 = 30$$

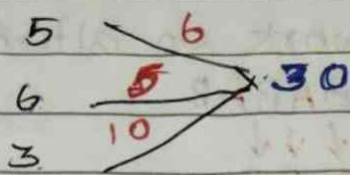
Now Both A and B pipes are opened.

$$\frac{30}{3-2} = \frac{30}{1} = 30 \text{ hrs.}$$

$$\text{Then total} = 10 \text{ hrs} + 30 \text{ hrs} = 40 \text{ hrs.}$$

- 4) A cistern has 3 pipes A, B, C. pipe A can fill tank in 5 hours, pipe B in 6 hours, C empty a tank 3 hours. pipe A and B opened for 2 hours, after that C also opened. Find total time taken

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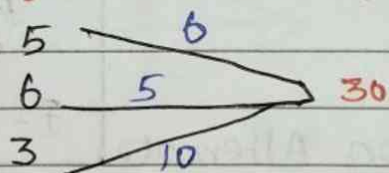
A = 6 litres per hour
B = 5 litres per hour
C = 10 litres per hour

A and B for two hours = $6 + 5 = 11$ for 2 hours
 $2 \times 11 = 22$

Balance = $30 - 22 = 8$ litre, C also opened
 $= \frac{8}{6+5+10} = \frac{8}{1} = 8$ ~~litres~~ hours.

Total time taken = $2 + 8 = 10$ hrs.

5) A cistern has 3 pipes A, B, C, A fill 5 hours, B fill in 6 hours, C empty in 3 hours. pipe A opened first, after 3 hours pipe B also opened after 1 hour pipe C also opened. Total time taken to fill the tank?



i) A opened first 3 hrs

$$3 \times 6 = 18 \quad \text{Bal} = 30 - 18 = 12$$

ii) A and B both 1 hour

$$1 \times 11 = 11 \quad \text{Bal} = 12 - 11 = 1$$

iii) All three opened:

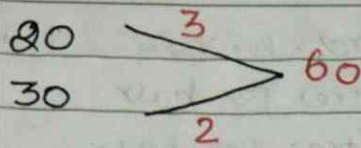
$$\frac{1}{6+5+10} = \frac{1}{1} = 1$$

$$\text{Total time} = 3 + 1 + 1 = 5 \text{ hrs}$$

ALTERNATE DAYS:

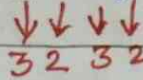
1) person A can complete a piece of work in 20 days. person B can complete a same piece of work in 30 days. A started the work then they work on Alternate days, How long it will take to complete the work, if they work on Alternate days?

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They work on alternate days.

ABABAB



1 cycle = 5 units

12 cycle = 60 units

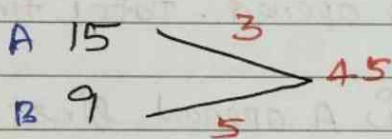
$$= \frac{60}{5} = 12 \text{ cycle.}$$

1 cycle = 2 days.

12 cycle = $12 \times 2 = 24$ days.

Ans: 24 days.

2, person A can complete a piece of work in 15 days, person B can complete a same piece of work in 9 days. Starting on 'A' they worked on Alternate days. How long will it take to complete the work?



⊗ Hint for LCM

$$15:9$$

$$5:3$$

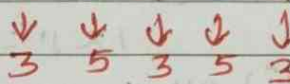
$$E = A:B$$

$$3:5$$

(small comes first)

They worked on Alternate

A B A B A



1 cycle = 8 units

5 cycle = 40 units.

1 cycle = 2 days.

5 cycle = 10 days to complete 40

(B) = 5 units. A start)

11 days = 43 units. rem = 2 units

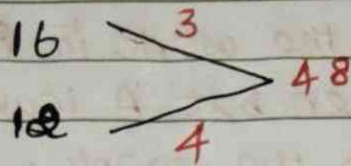
Rem

B effi = 5 units

Ans = 11 $\frac{2}{5}$ → Efficiency of B.

3, person A can complete a piece of work in 16 days. person B can complete a same piece of work in 12 days, starting on 'A' they worked on Alternate days. How long will it take to complete the work?

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They worked on Alternate

16:12
8:6
4:3

A B A B A B
↓ ↓ ↓ ↓ ↓ ↓
3 4 3 4 3 4

1 cycle = 7 units
6 cycle = 42 units

1 cycle = 2 days

6 cycle = 12 days (They complete 42 units)

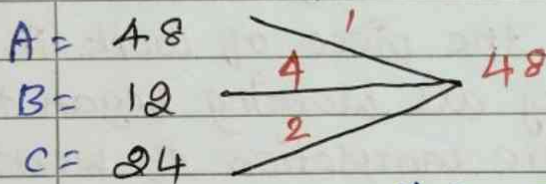
13 days = 45 units

↑ (Rem 3 units)

ANS: $13 \frac{3}{4}$



20, A, B, C can complete a piece of work in 48, 12, 24 days. A start the work Every 3rd day B and C join with 'A'. Find the total number of days to complete the work?



A Starts the work Every 3rd day B and C join with A.

1st 3rd 6th
A A (A+B+C) A A (A+B+C)
↓ ↓ ↓ ↓ ↓ ↓
1 1 4 1 1 4

1 cycle = 9 units
5 cycle = 45 units

1 cycle = 3 days

5 cycles = 15 days (Rem 3 units)

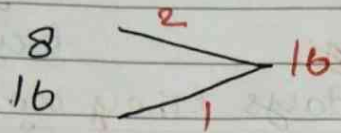
16 day A complete - 1 unit } 47 units complete
17 day A complete - 1 unit } (Rem 1 unit)

ANS: $17 \frac{1}{7}$ days

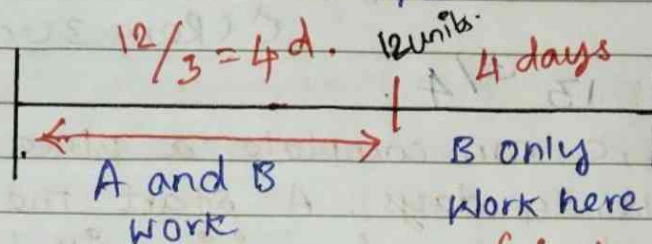
PERSON LEAVING BEFORE COMPLETION OF WORK

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- 1, Person A and B complete the work in 8 and 16 days. They start together but A leaves 4 days before completion of the work. Find the total number of days to complete the work?



They started together but A left 4 days before completion.

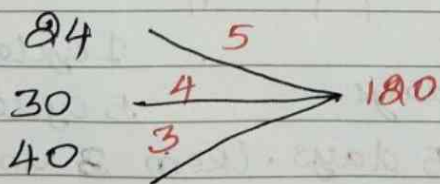


$$(4 \times 1 = 4 \text{ units})$$

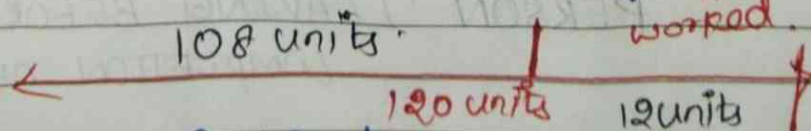
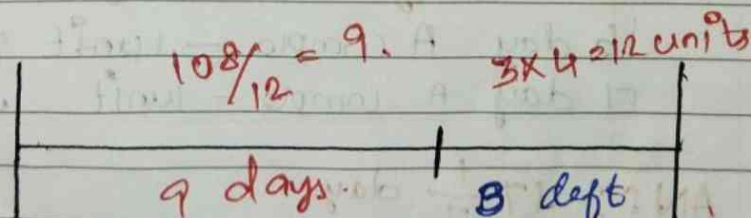
$$(16 - 4 = 12 \text{ units})$$

$$\text{Total} = 4 + 4 = 8 \text{ days.}$$

- 2, A, B, C can complete the piece of work in 24, 30, 40 days. They all working began together. B left 3 days before completion of work. Find the total number of days to complete the work?

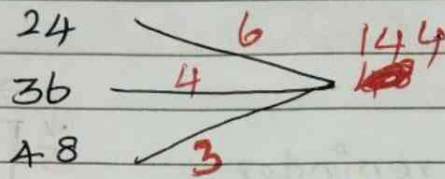


They all started together. B only left before 3 days.

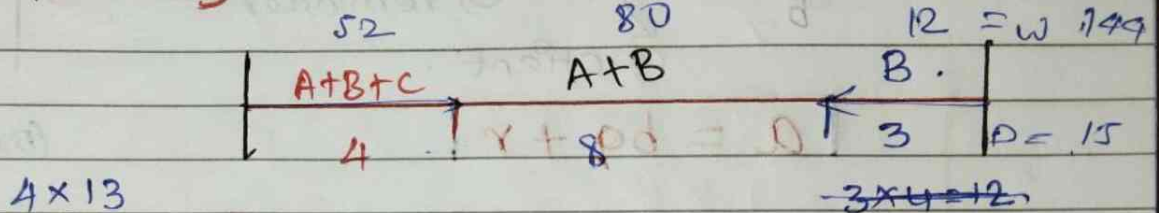


$$\text{Ans: } 9 + 3 = 12 \text{ days.}$$

- 3) A, B, C can complete the piece of work in 24, 36, 48 days. C left 4 days of start of the work. A left 3 days before completion of the work. Find the total number of days to complete the work?



C left after 4 days
A left before 3 days



$$4 \times 13 = 52$$

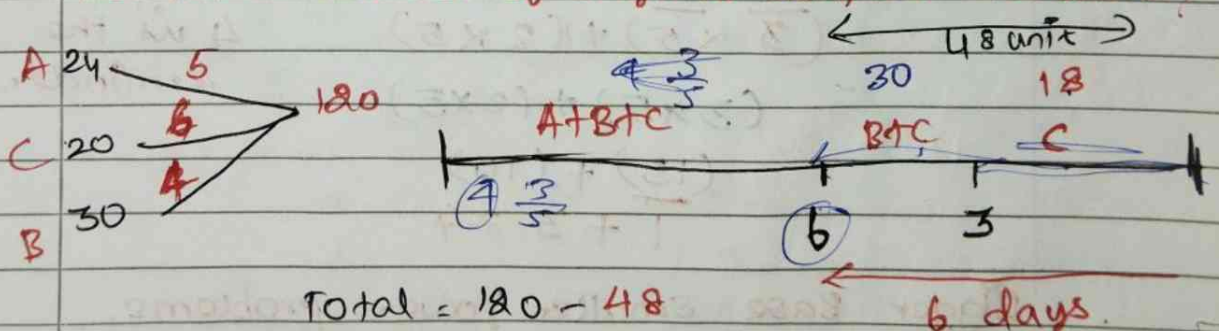
$$\text{Work comple} = 144 - 64$$

Bal = 80 \rightarrow This should complete by A+B.

$$A+B = \frac{80}{10} = 8$$

$$\text{Total} = 8 + 4 + 3 = 15 \text{ day.}$$

- 4) A, B and C can complete a piece of work in 24, 30, 20 days. A leaves 6 days and B leaves 3 days before completion of the work. Find the total number of days to complete the work?



$$\text{Total} = 120 - 48$$

$$= 72$$

$$A+B+C = \frac{72}{15} = \frac{12}{5} = \frac{2}{5}$$

$$(4), 60$$

$$\text{ANS} = 10 \frac{3}{5}$$