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TIME AND WORK :-

1, Core idea :

$$\text{Work} = \text{Efficiency} \times \cancel{\text{Time}}$$

2, Basic Golden Rule :

i) If A can do a work in X days
then A's 1 day work = $\frac{1}{X}$
(This is Most ~~✓~~).

Example : A can do a work in 10 days
so A's 1 day work = $\frac{1}{10}$.

Problems (Basic problems to solve) :

2) Person A can complete a piece of work in 10 days
Person B can complete a same piece of work in
15 days. How long will it take for both of them
working together to complete the work?

Method 1 (Fraction but little bit complicated).

$$A = 10 \text{ days} \text{ then } A = \frac{1}{10}$$

$$B = 15 \text{ days} \text{ then } B = \frac{1}{15}$$

They work together :

$$A+B = \frac{1}{10} + \frac{1}{15} \text{ (Take LCM then)}$$

$$A+B = \frac{3+2}{30} = \frac{5}{30} = \frac{1}{6}$$

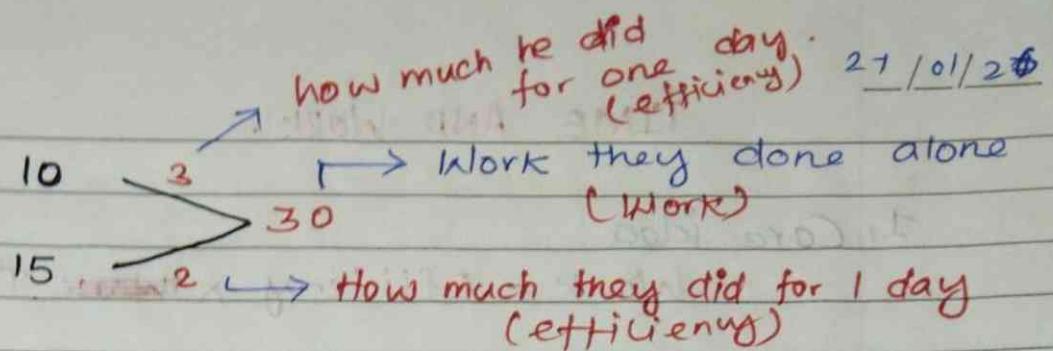
Ans : 6 days.

Method 2 (concept wise more easy).

$$\text{Work} = \text{Efficiency} \times \text{Time}.$$

$$A = 10 \text{ days}, B = 15 \text{ days}$$

(They given time so we need to find
out the efficiency and work).



- * Ippo A Vanthu oru Velaya mudika 10 days
Aguthu, avan oru nalaiku 3 unit work mudikan
Total avan complete pannathu 30 unit work.
- * Ippo Inga paaru avanga & perum seruthu
Mudikora $3+2 = 5$ unit of Work. per day.

$$= \frac{5}{20} = 6 \text{ ans} = 6 \text{ days}$$

Ippo \rightarrow work = time \times efficiency then
Time = work / efficiency

Q) A person A can complete a piece of work in 20 days, person B can complete a same piece of work in 30 days. How long will it take for both of them working together?

$$A = 20 \quad B = 30$$

$20 - 3$ (efficiency) \rightarrow Work they done (units).

$30 - 2$ \rightarrow Work they done per day.

$$\text{Time} = \text{Work} / \text{efficiency}$$

$$= 60 / 3+2 \Rightarrow 60/5 = 12.$$

Ans: 12 days.

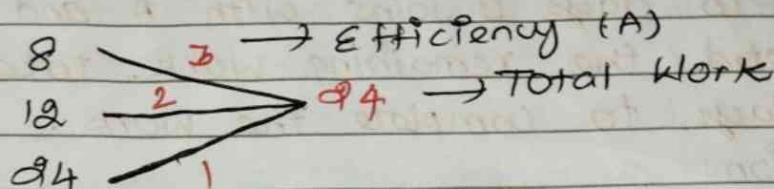
3- person A can complete a piece of work in 8 days, person B can complete a piece of work in 12 days, person C can complete a work in 8 days. How long they take to complete it

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working together to complete the work?

Solution:

$$A = 8 \text{ days} \quad B = 12 \text{ days} \quad C = 24 \text{ days}$$



$$\text{Time} = \text{Work} / \text{Efficiency}$$

$$\text{Time} = 24 / (3+2+1) = 24/6 = 4$$

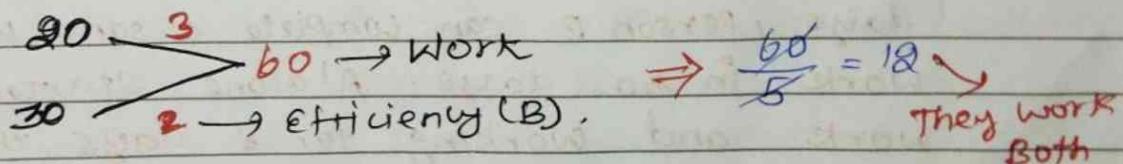
Ans: 4 days.

PART-II PERSON LEFT AFTER SOME DAYS:

Question 2: Person A can complete a piece of work in 20 days. Person B can complete a same piece of work in 30 days? They both started the work together. After 4 days 'A' left the job and remaining work done by B alone. How long will it take to complete the remaining work? Total number of days to complete the work?

Solution:

$$A = 20 \text{ days} \quad B = 30 \text{ days}$$



*) After 4 days A left the job (means they work 4 days together).

$$A = 3 \text{ units} \quad B = 2 \text{ units} \quad 4 \times 5 = 20$$

$$60 - 20 = 40 \text{ Remaining.}$$

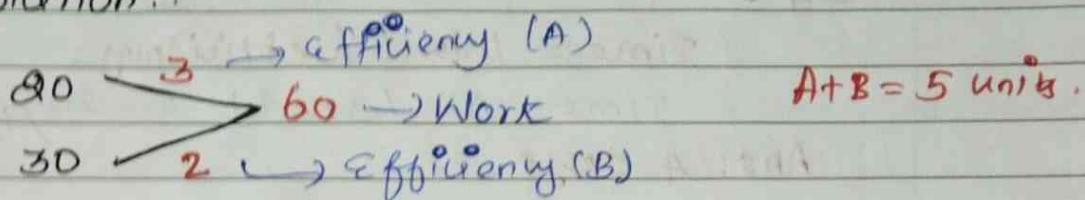
Remaining work done in 20 days,

$$do \times 2 = 40 \rightarrow \begin{matrix} \text{remaining} \\ \text{work} \\ (\text{pending}) \end{matrix}$$

\checkmark B efficiency days to complete remaining work

Q) person A can complete a piece of work in 80 days, person B can complete a piece of work in 30 days. A alone started the work, after 10 days B joins with A and together completed the remaining work. Total number of days to complete the work.

Solution:-



A' Alone started the work 10 days.

$$10 \times 3 = 30 \quad 60 - 30 = 30 \text{ (remaining)}$$

A) Ippo into the remaining 30 units of work is did by the A and B.

$$= \frac{30}{5} = 6 \text{ days.}$$

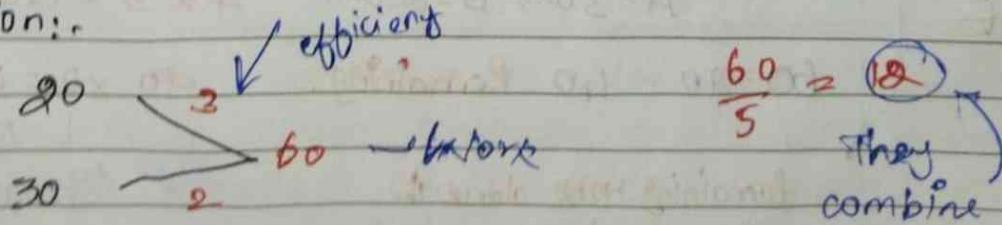
A' alone work for 10 days then the both complete the remaining work in 6 days.

$$10 + 6 = 16 \text{ days.}$$

Ans: 16 days.

3, person A can complete a piece of work in 80 days, person B can complete a same piece of work in 30 days. A' alone started the work and working for 8 days, then left B complete the remaining work by working alone. Find the days to complete by B.

Solution:-



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A' started to working alone for 8 days.

$$\rightarrow 3 \times 8 = 24 \Rightarrow 60 - 24$$

A's unit \downarrow 8 days 36 remaining

(A left and B Working alone)

* $36/2 = 18$ days.

\downarrow remaining work to done.

** Hence the remaining work 18 days to complete

- 4) person A can complete a piece of work in 8 days, person B can complete a work in 12 days and person C can complete a work in 24 days. All of them working together. After 2 days A left the job. In how many days the remaining work to be done.

$$\begin{array}{r} 8 \\ 12 \\ 24 \end{array} \begin{array}{l} \xrightarrow{3} \text{efficiency (A)} \\ \cancel{\xrightarrow{2}} \quad \xrightarrow{24} \text{Work} \\ \cancel{\xrightarrow{1}} \quad \xrightarrow{1} \text{efficiency (B).} \end{array} \frac{24}{6} = 4.$$

All working together (2 days) = $2 \times \frac{1}{12} = \frac{1}{6}$ $24 - \frac{1}{6} = \frac{13}{6}$.

Remaining Work = $18/3 = 6$

The remaining work done in 6 days.

- 5) person A complete in 8 days, person B can complete a piece of work 12 days, person C complete 24 days. A alone started the work after 2 days B and c joins with the A. Find total?

$$\begin{array}{r} 8 \\ 12 \\ 24 \end{array} \begin{array}{l} \xrightarrow{3} \\ \cancel{\xrightarrow{2}} \quad \xrightarrow{24} \\ \cancel{\xrightarrow{1}} \end{array} \begin{array}{l} A \text{ Alone} \\ 2 \times 3 = 6 \\ 24 - 6 = 18 \end{array} \frac{18}{6} = 3$$

Total number of days = $3 + 2 = 5$ days.

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CISTREN SUMS:-

- 1) A cistren has 3 pipes A,B,C. Pipe A can fill a tank in 5 hours, pipe B can fill a tank in 6 hours. Pipe C can empty a filled tank in 3 hours. How long will it take if all the three pipes are opened together to fill the tank?

$$\begin{array}{r} A = 5 \quad 6 \\ B = 6 \quad 5 \quad \cancel{30} \\ C = 3 \quad 10 \end{array} \quad A+B-C = 5+6-10 = \frac{30}{1} = 30 \text{ hrs.}$$

$$\frac{\text{Total work}}{EA+EB-EC} = \frac{30}{1} = 1 \quad \text{Because it empty the tank.}$$

- 2) A cistren can be filled by a pipe A in 20 hours. It can empty by B in 30 hours. If both opened together how long will it take to fill the tank?

$$\begin{array}{r} 20 \quad 3 \quad 60 \\ 30 \quad 2 \quad \cancel{60} \end{array} \quad \frac{W}{EA-EB} = \frac{60}{3-2} = \frac{60}{1} = 60 \text{ hrs.}$$

- 3) A cistren can be filled by a pipe A in 20 hours, while it can empty by pipe B in 30 hours. If pipe A opened first, after 10 hours pipe B also opened. Find the total time taken to fill the whole tank?

$$\begin{array}{r} 20 \quad 3 \quad 60 \\ 30 \quad 2 \quad \cancel{60} \end{array} \quad A \text{ is } 10 \text{ hours} = 10 \times 3 = 30$$

$$\text{Remaining} = 60 - 30 = 30.$$

Now Both A and B pipes are opened.

$$\frac{30}{3-2} = \frac{30}{1} = 30 \text{ hrs.}$$

$$\text{Then total} = 10 \text{ hrs} + 30 \text{ hrs} = 40 \text{ hrs.}$$

- 4) A cistren has 3 pipes A,B,C. Pipe A can fill tank in 5 hours, pipe B in 6 hours, C empty a tank in 3 hours. Pipe A and B opened for 2 hours. After that C also opened. Find total time taken.

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$$\begin{array}{r} 5 \\ 6 \\ \hline 6 \\ 5 \\ \hline 30 \\ 10 \\ \hline \end{array}$$

A = 6 litres per hour

B = 5 litres per hour

C = 10 litres per hour

A and B for two hours = $6+5=11$ for 2 hours

$$2 \times 11 = 22$$

Balance = $30 - 22 = 8$ litr., C also opened

$$\Rightarrow \frac{8}{6+5-10} = \frac{8}{1} = 8 \text{ hours.}$$

Total time taken = $2 + 8 = 10$ hrs.

5) A cistern has 3 pipes A, B, C, A fill 5 hours, B fill in 6 hours, C empty in 3 hours. Pipe A opened first, after 3 hours pipe B also opened after 1 hour pipe C also opened. Total time taken to fill the tank?

$$\begin{array}{r} 5 \\ 6 \\ \hline 6 \\ 5 \\ \hline 30 \\ 10 \\ \hline \end{array}$$

i) A opened first 3 hrs

$$3 \times 6 = 18 \quad \text{Bal} = 30 - 18 = 12$$

ii) A and B both 1 hour

$$1 \times 11 = 11 \quad \text{Bal} = 12 - 11 = 1$$

iii) All three opened :-

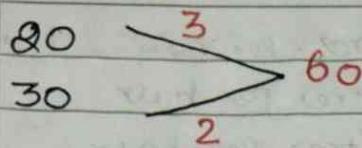
$$\frac{1}{6+5-10} = \frac{1}{1} = 1$$

$$\text{Total time} = 3+1+1 = 5 \text{ hrs}$$

ALTERNATE DAYS:

1) person A can complete a piece of work in 20 days. person B can complete a same piece of work in 30 days. A started the work then they work on alternate days. How long it will take to complete the work, if they work on alternate days?

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They work on alternate days.

ABABAB

↓↓↓
3 2 3 2

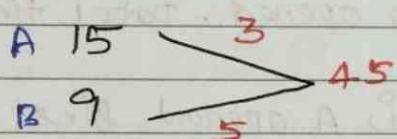
$$= \frac{60}{5} = 12 \text{ cycle.} \quad 12 \text{ cycle} = 60 \text{ units}$$

1 cycle = 2 days.

$$12 \text{ cycle} = 12 \times 2 = 24 \text{ days.}$$

ANS: 24 days.

Q, person A can complete a piece of work in 15 days, person B can complete a same piece of work in 9 days. Starting on 'A' they worked on Alternate days. How long will it take to complete the work?



④ Hint for LCM

$$\begin{array}{r} 15 : 9 \\ 5 : 3 \end{array}$$

$$\text{F} = A : B = 3 : 5 \quad (\text{small comes first})$$

They worked on Alternate

A B A B A
↓ ↓ ↓ ↓ ↓
3 5 3 5 3

1 cycle = 8 units

5 cycle = 40 units.

1 cycle = 2 days.

5 cycle = 10 days to complete complete 40.

(Bal = 5 units. A start)

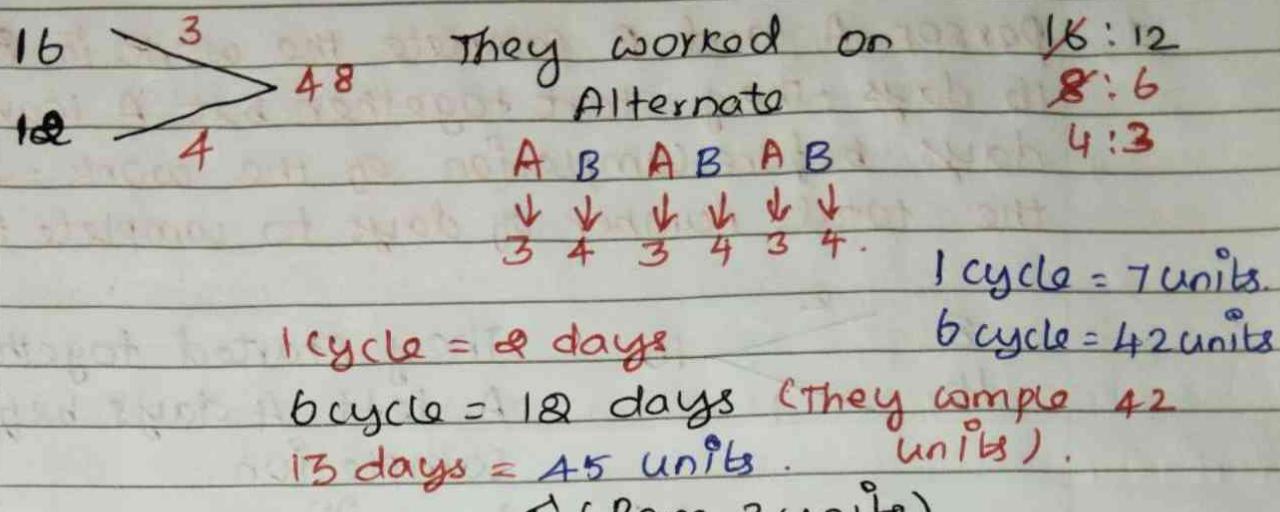
Rem ~

11 days = 43 units. rem = 2 units

B effi = 5 units

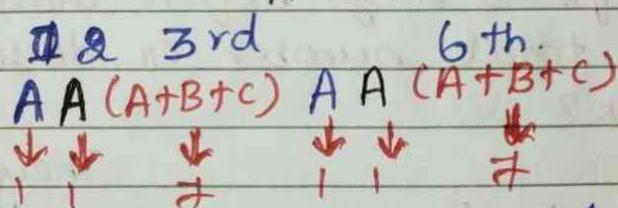
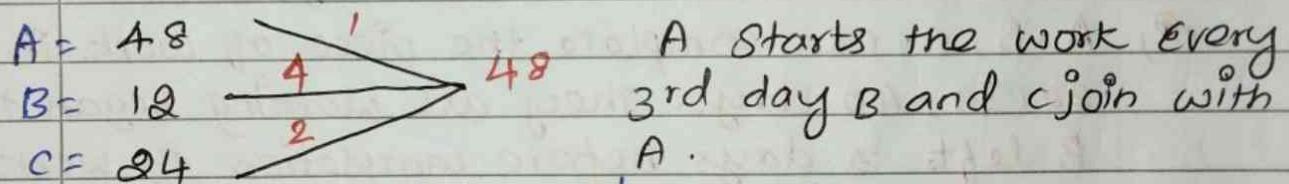
ANS = $11 \frac{2}{5}$ → efficiency of B.

Q, person A can complete a piece of work in 16 days. person B can complete a same piece of work in 12 days. Starting on 'A' they worked on Alternate days. How long will it take to complete the work?



ANS: 13 $\frac{3}{4}$.

- 20) A, B, C can complete a piece of work in 48, 18, 24 days. A starts the work every 3rd day B and C join with 'A'. Find the total number of days to complete the work?



1 cycle = 9 days.

1 cycle = 9 units.
5 cycles = 45 units

5 cycles = 15 days. (Rem 3 units).

16 day A complete - 1 unit $\left\{ \begin{array}{l} 47 \text{ units complete} \\ (\text{Rem 1 unit}) \end{array} \right.$
17 day A complete - 1 unit

ANS: $17 \frac{1}{7}$ days.

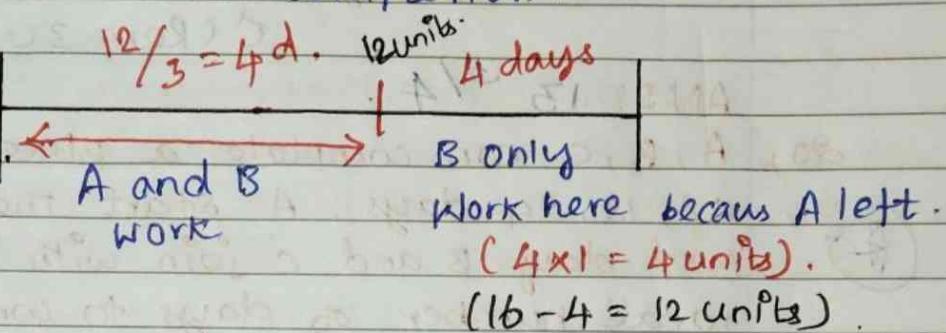
PERSON LEAVING BEFORE
COMPLETION OF WORK.

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- 1, Person A and B complete the work in 8 and 16 days. They start together but A leaves 4 days before completion of the work. Find the total number of days to complete the work?

$$\begin{array}{r} 8 \\ 16 \\ \hline 1 \end{array}$$

They started together but A left 4 days before completion.

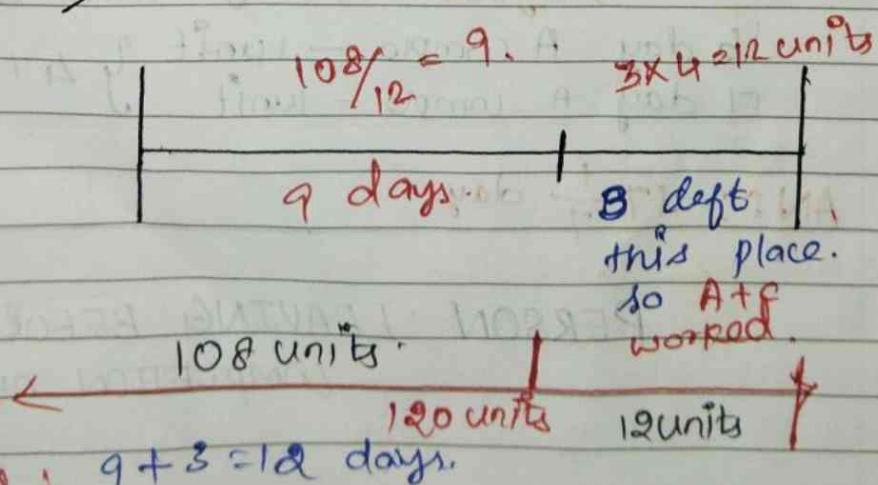


$$\text{Total} = 4 + 4 = 8 \text{ days.}$$

- 2, A, B, C can complete the piece of work in 24, 30, 40 days. They all working began together. B left 3 days before completion of work. Find the total number of days to complete the work?

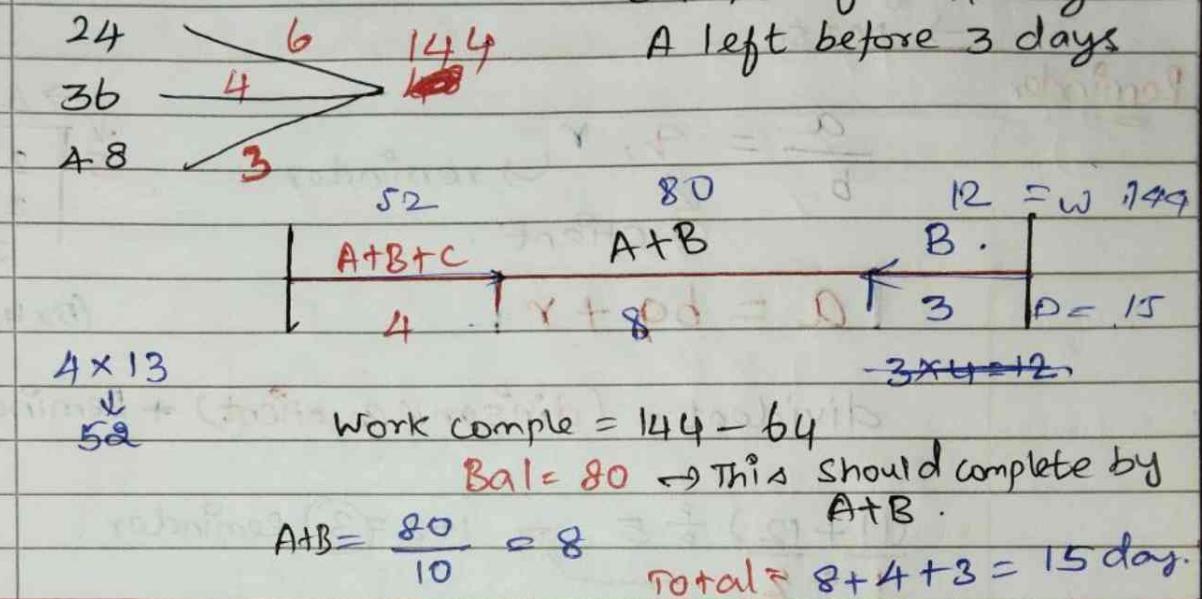
$$\begin{array}{r} 24 \\ 30 \\ 40 \\ \hline 4 \end{array}$$

They all started together. B only left before 3 days.



$$\text{ANS: } 9 + 3 = 12 \text{ days.}$$

3) A, B, C can complete the piece of work in 24, 36, 48 days. C left 4 days before start of the work. A left 3 days before completion of the work. Find the total number of days to complete the work?



4) A, B and C can complete a piece of work in 24, 30, 20 days. A leaves 6 days and B leaves 3 days before completion of the work. Find the total number of days to complete the work?

