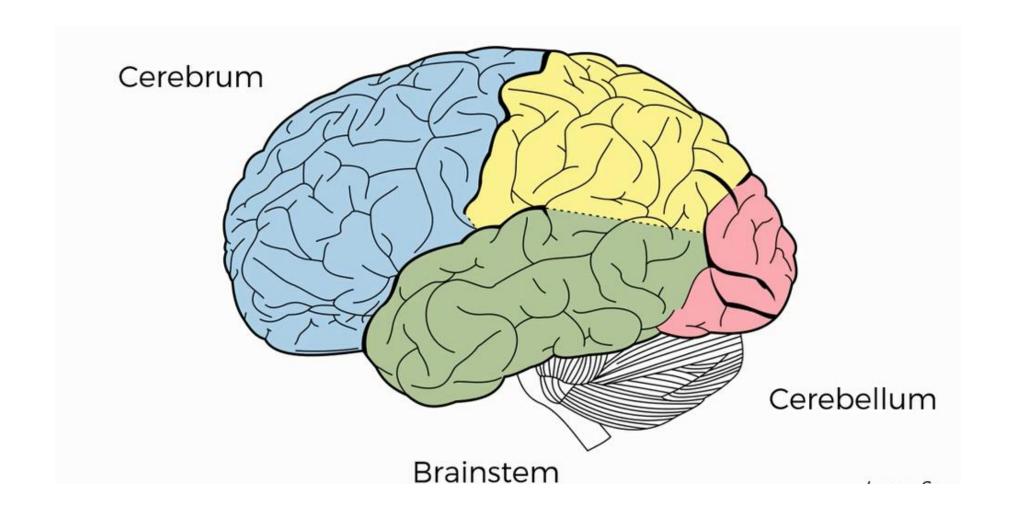
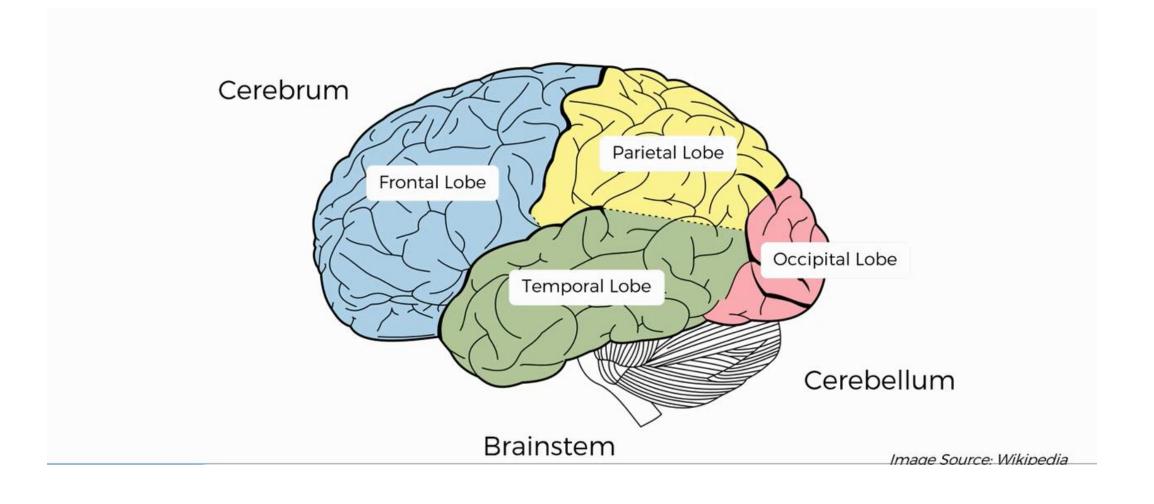
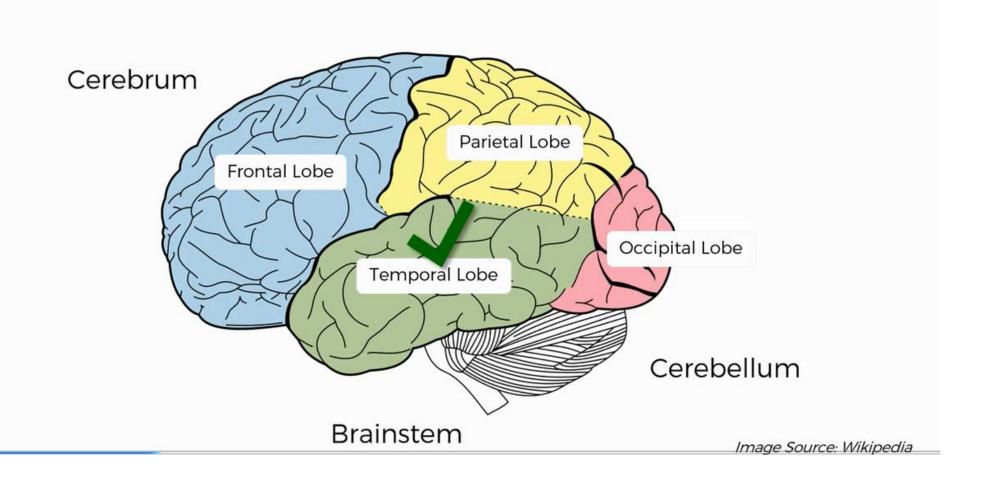
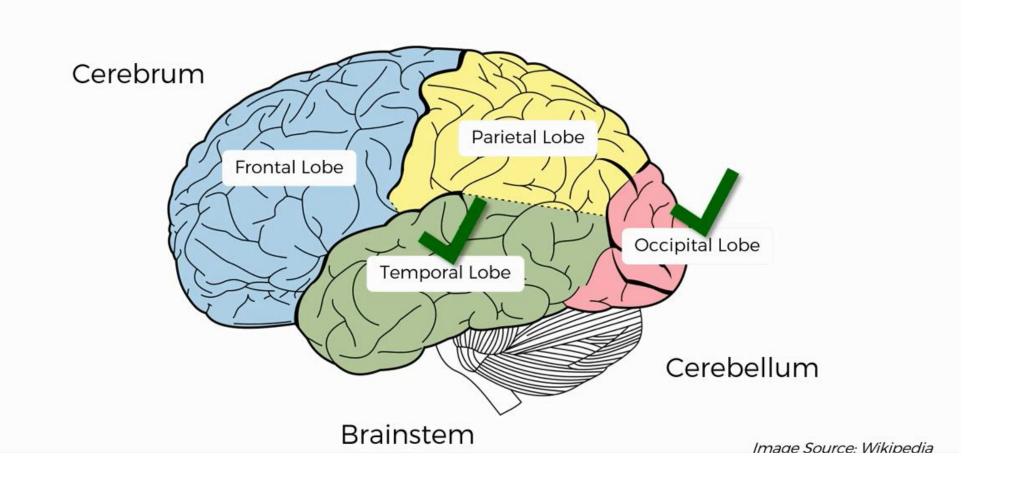
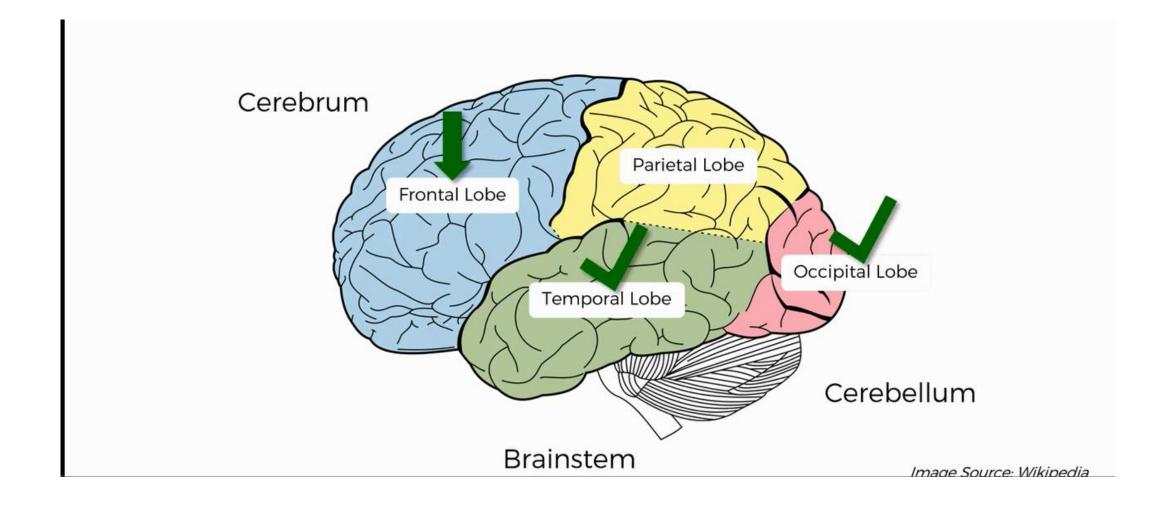
## Recurrent Neural Network

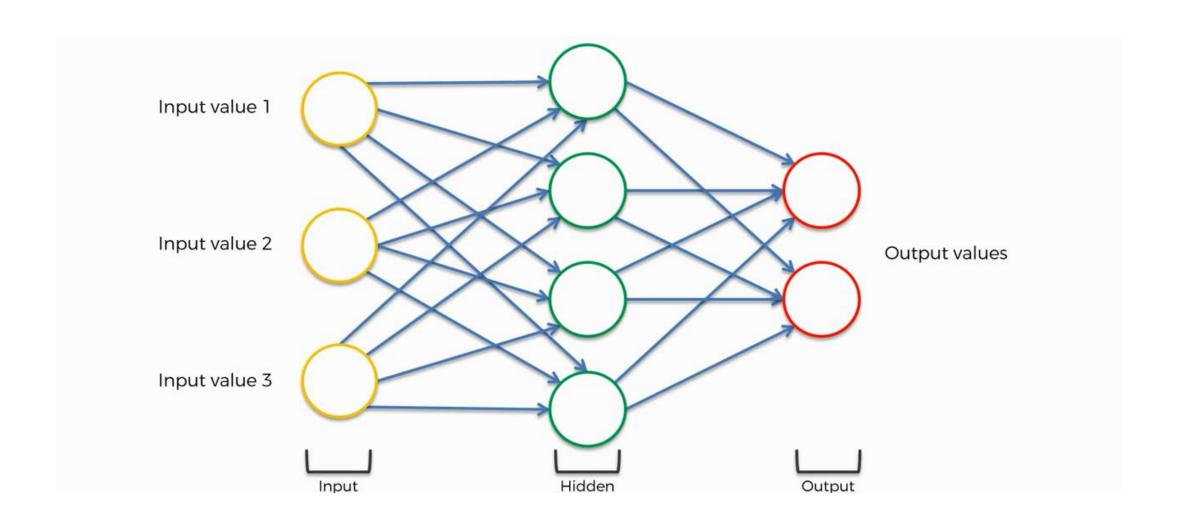


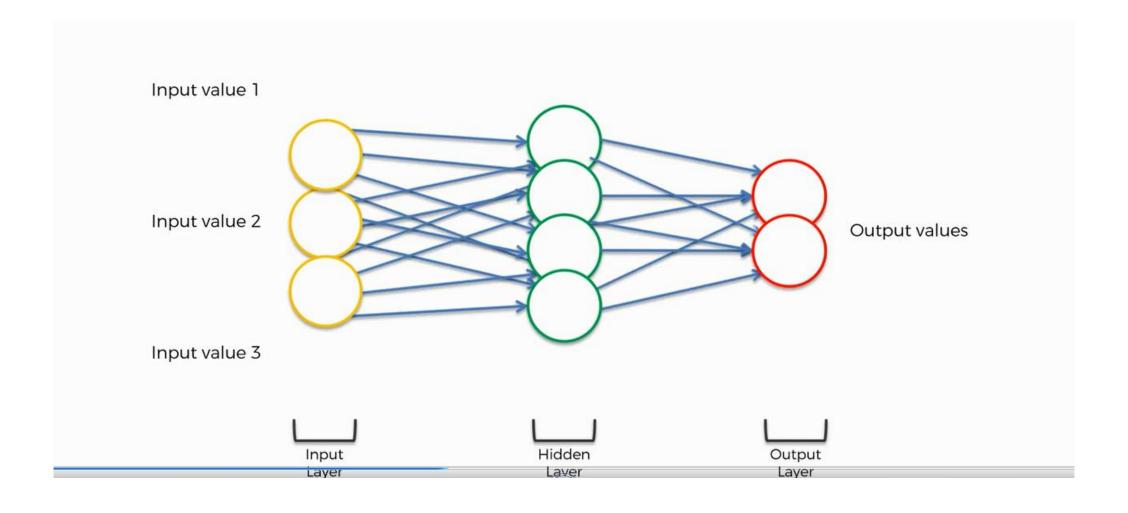


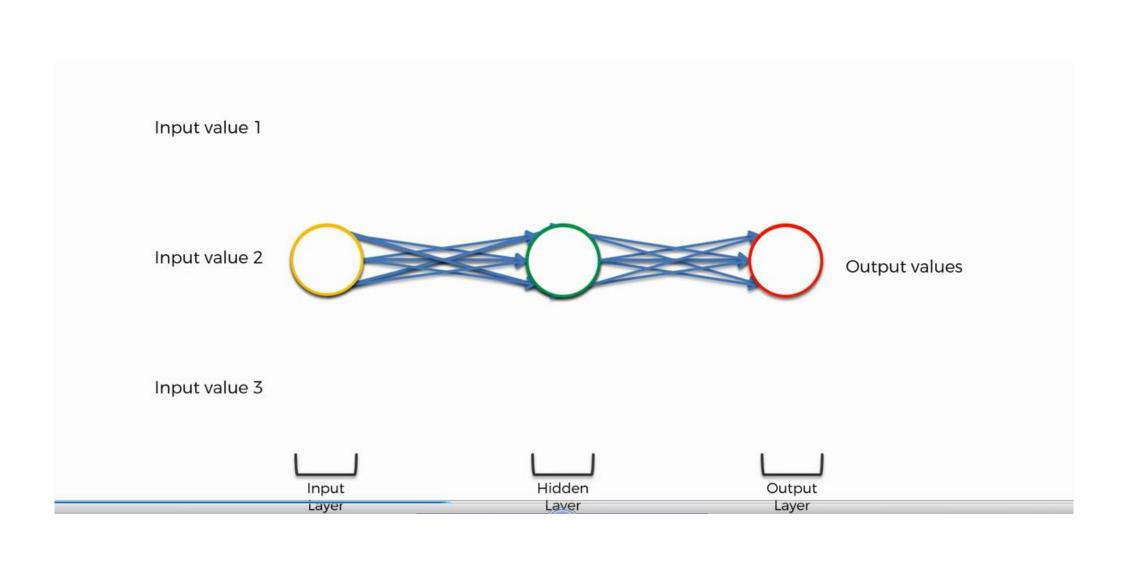


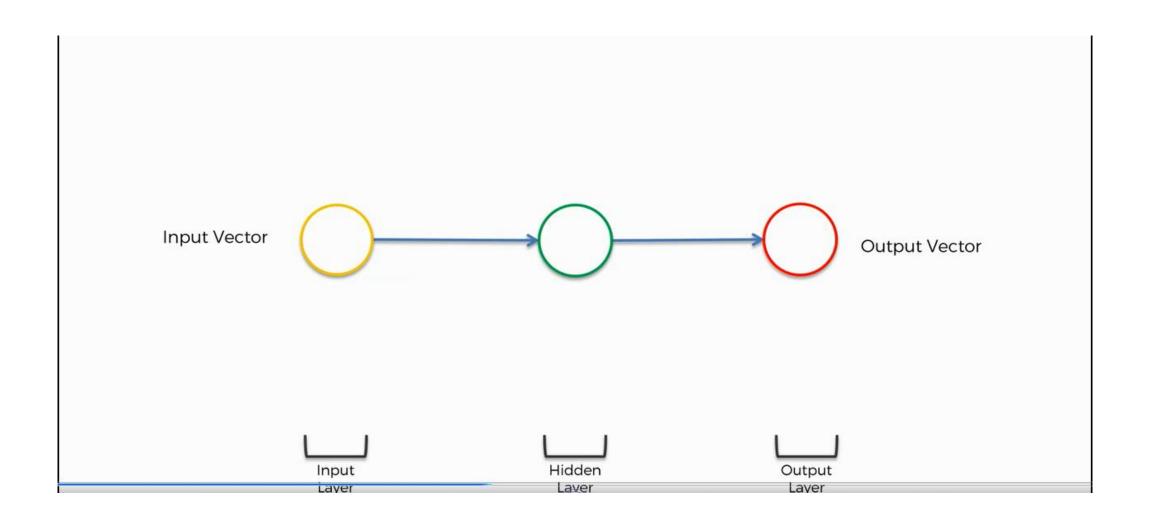


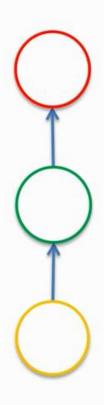


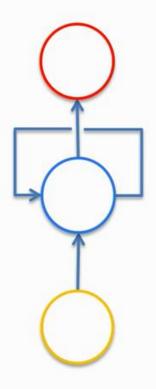


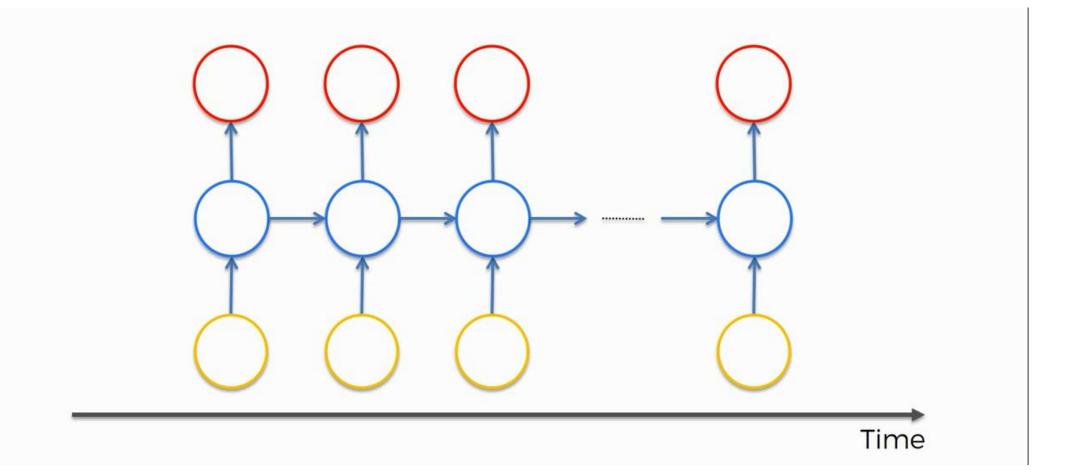


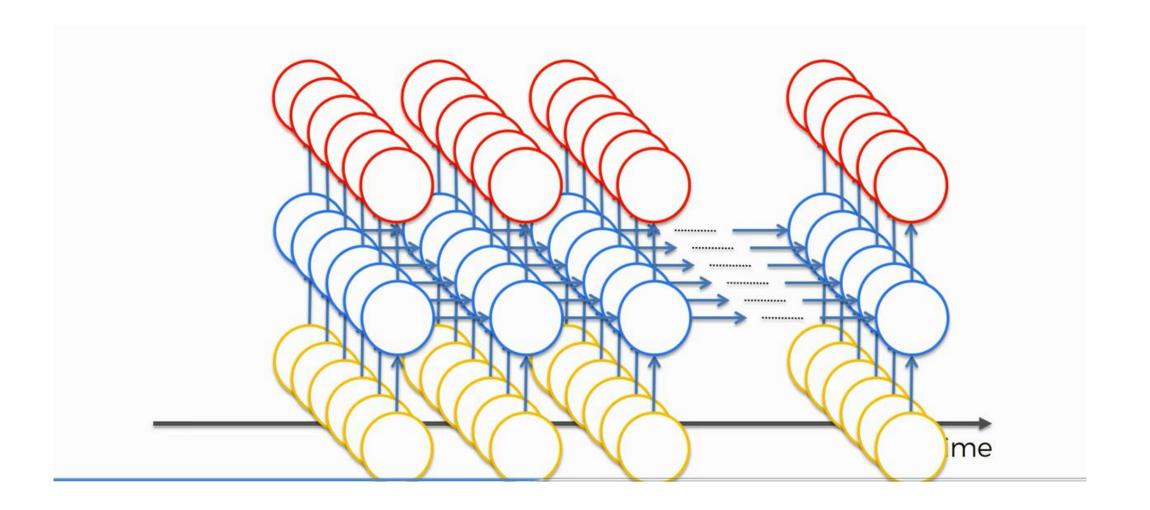


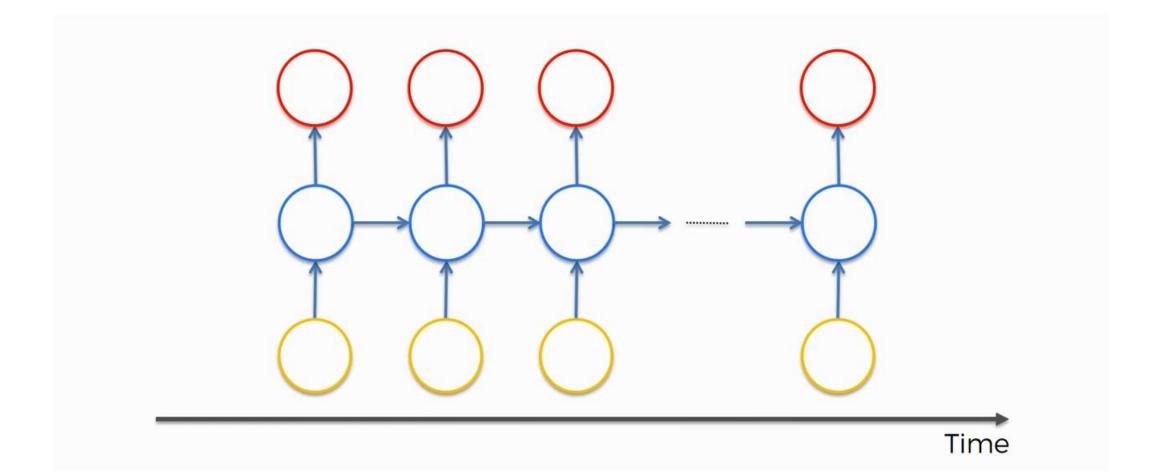








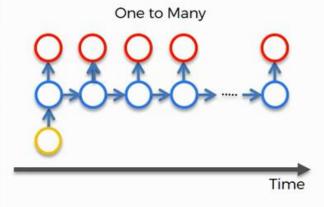


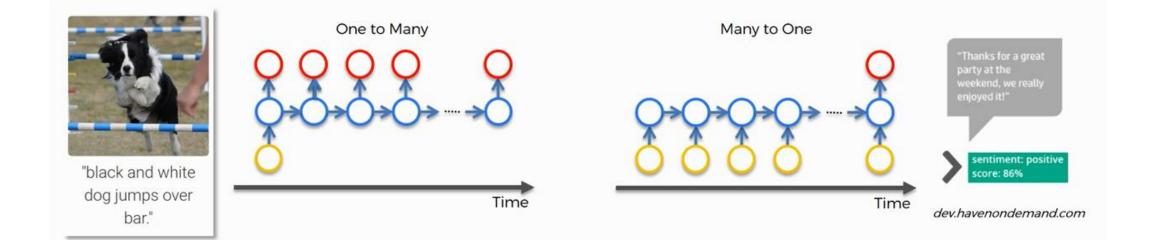




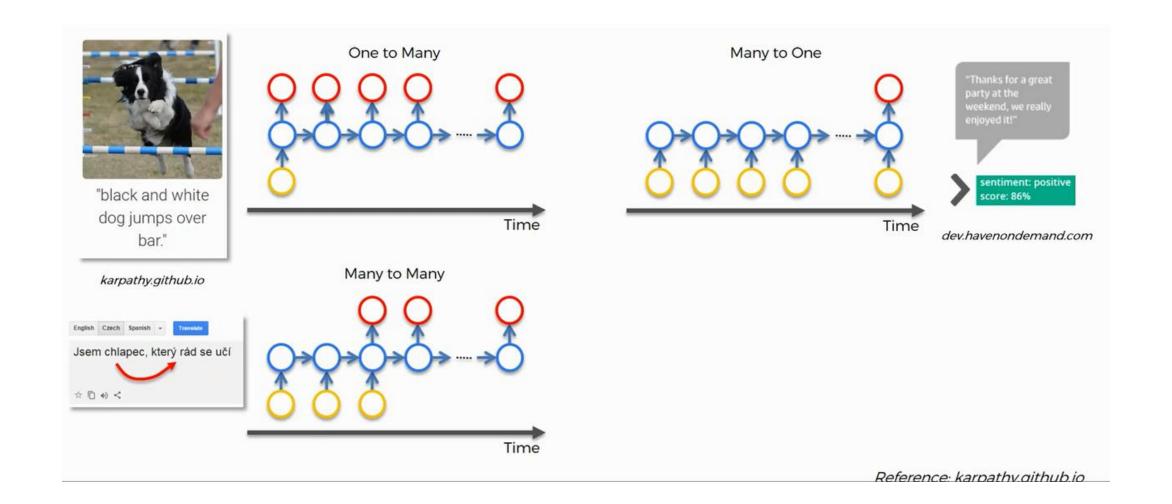
"black and white dog jumps over bar."

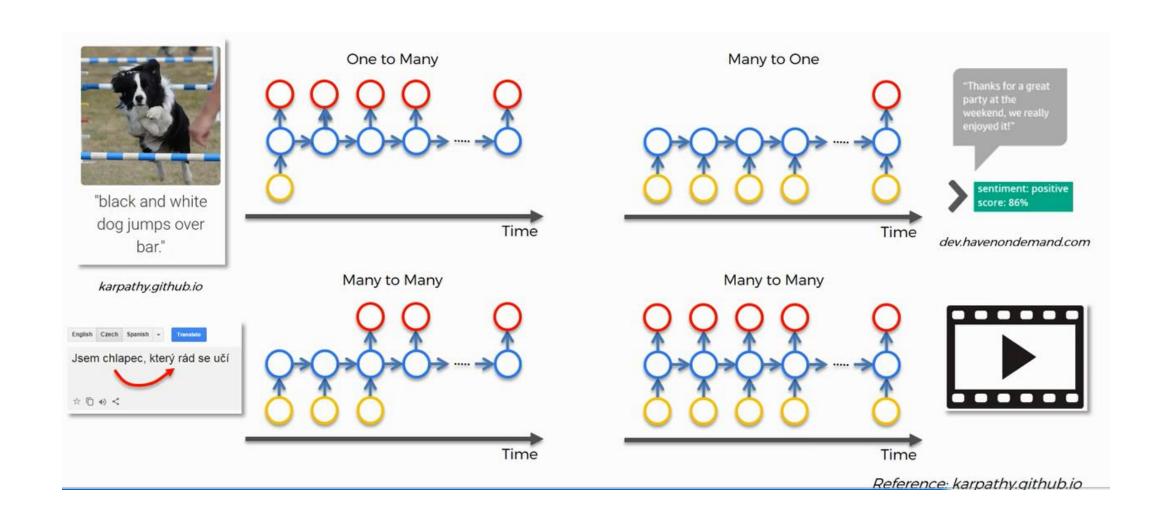
karpathy.github.io



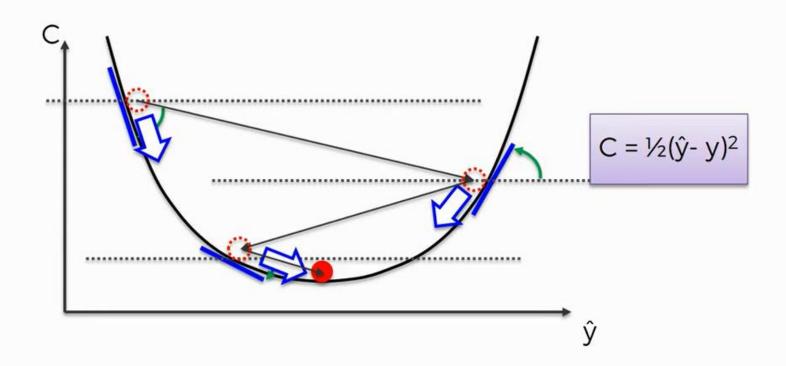


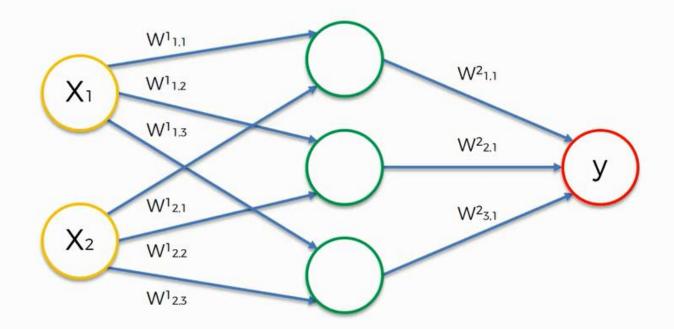
karpathy.github.io

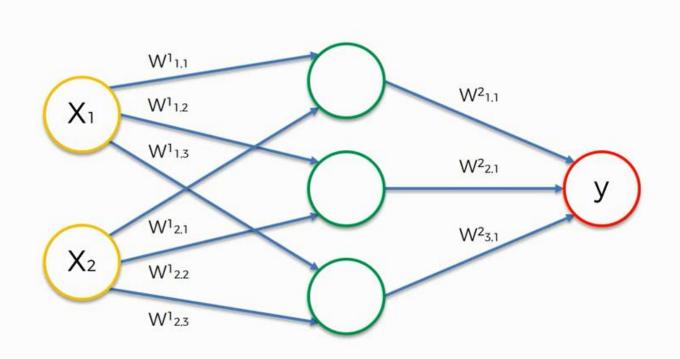


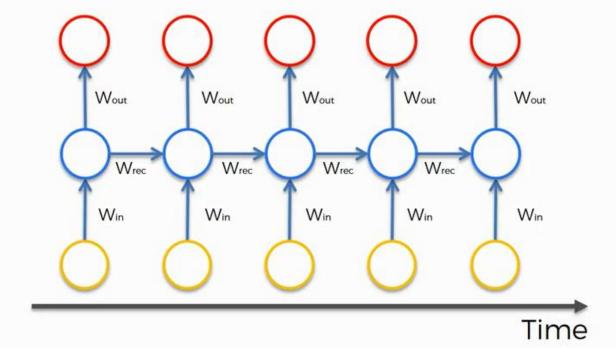


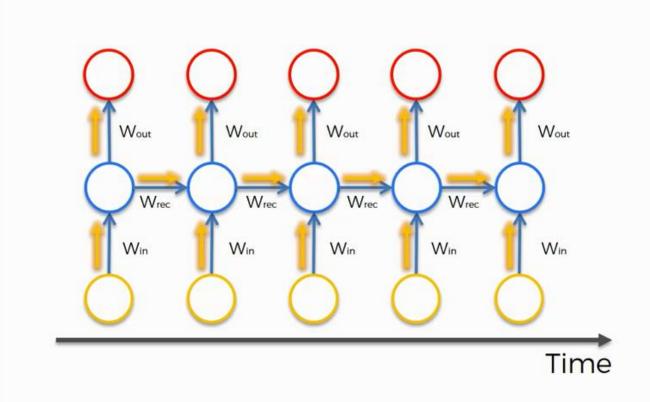
## Vanishing Gradient

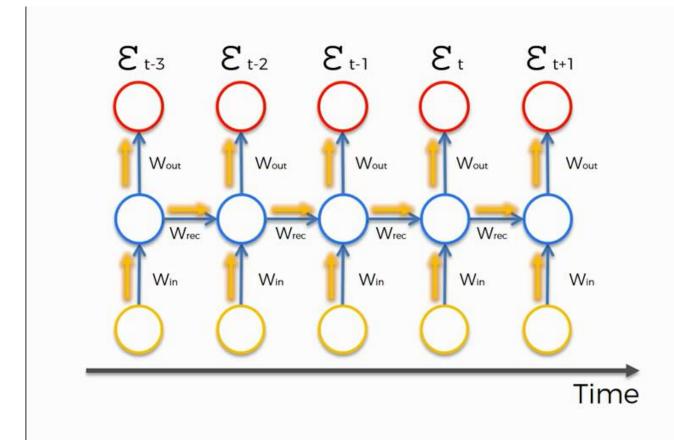


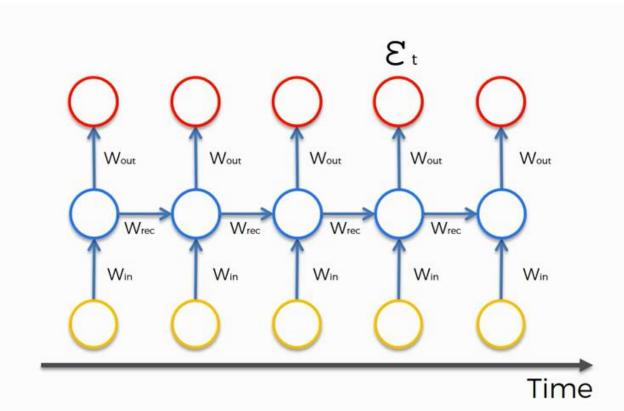


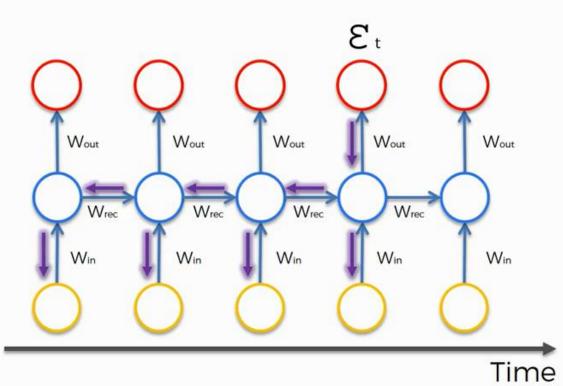


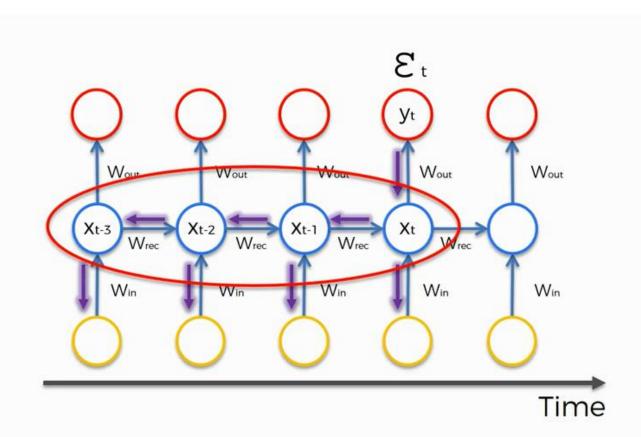


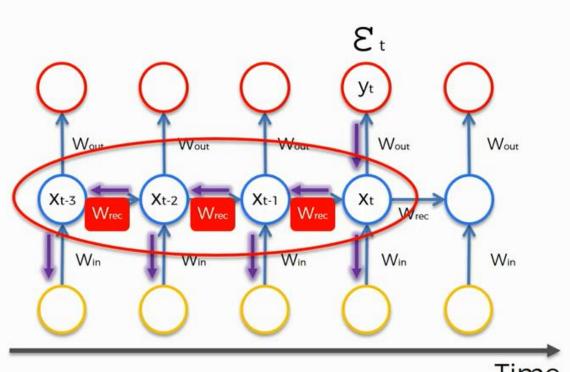










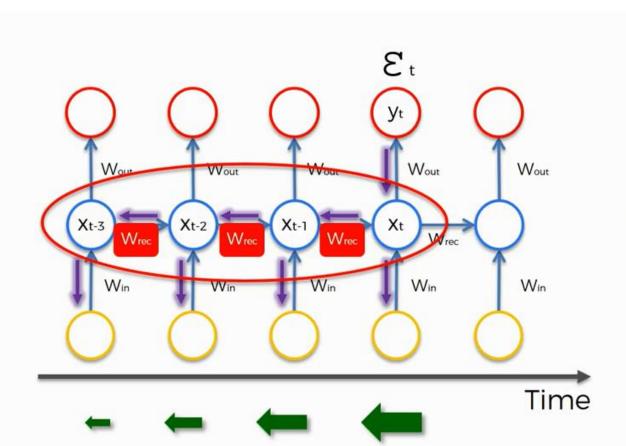


$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \le t \le T} \frac{\partial \mathcal{E}_t}{\partial \theta} \tag{3}$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \le k \le t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \tag{4}$$

$$\frac{\partial \mathbf{x}_{t}}{\partial \mathbf{x}_{k}} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_{i}}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^{T} diag(\sigma'(\mathbf{x}_{i-1})) \quad (5)$$

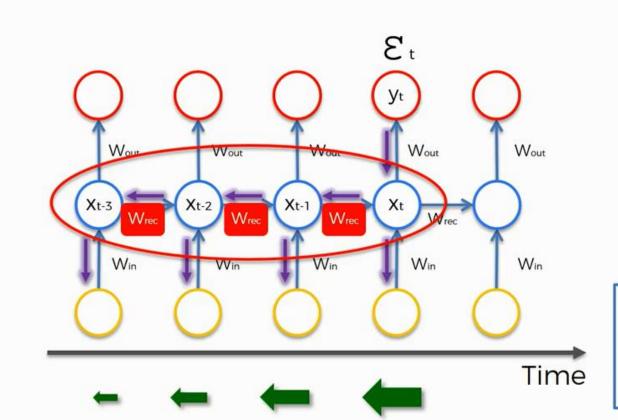
Time



$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \le t \le T} \frac{\partial \mathcal{E}_t}{\partial \theta} \tag{3}$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \le k \le t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \tag{4}$$

$$\frac{\partial \mathbf{x}_{t}}{\partial \mathbf{x}_{k}} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_{i}}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^{T} diag(\sigma'(\mathbf{x}_{i-1}))$$
(5)



$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \le t \le T} \frac{\partial \mathcal{E}_t}{\partial \theta} \tag{3}$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \le k \le t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \tag{4}$$

$$\frac{\partial \mathbf{x}_{t}}{\partial \mathbf{x}_{k}} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_{i}}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^{T} diag(\sigma'(\mathbf{x}_{i-1})) \tag{5}$$

W<sub>rec</sub> ~ small  $\implies$ 



Vanishing

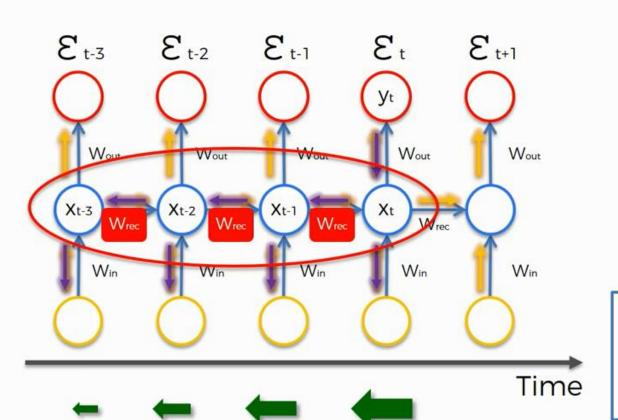


W<sub>rec</sub> ~ large  $\implies$  Exploding

## Solutions:

- 1. Exploding Gradient
  - Truncated Backpropagation
  - Penalties
  - Gradient Clipping
- 2. Vanishing Gradient
  - Weight Initialization
  - Echo State Networks
  - Long Short-Term Memory Networks (LSTMs)





$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \le t \le T} \frac{\partial \mathcal{E}_t}{\partial \theta} \tag{3}$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \le k \le t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \tag{4}$$

$$\frac{\partial \mathbf{x}_{t}}{\partial \mathbf{x}_{k}} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_{i}}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^{T} diag(\sigma'(\mathbf{x}_{i-1})) \quad (5)$$

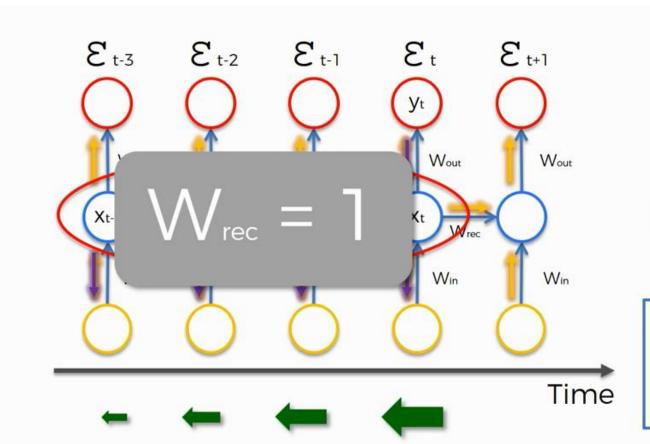
W<sub>rec</sub> < 1 ⇒



Vanishing



W<sub>rec</sub> > 1 **⇒** Exploding



$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \le t \le T} \frac{\partial \mathcal{E}_t}{\partial \theta} \tag{3}$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \le k \le t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \tag{4}$$

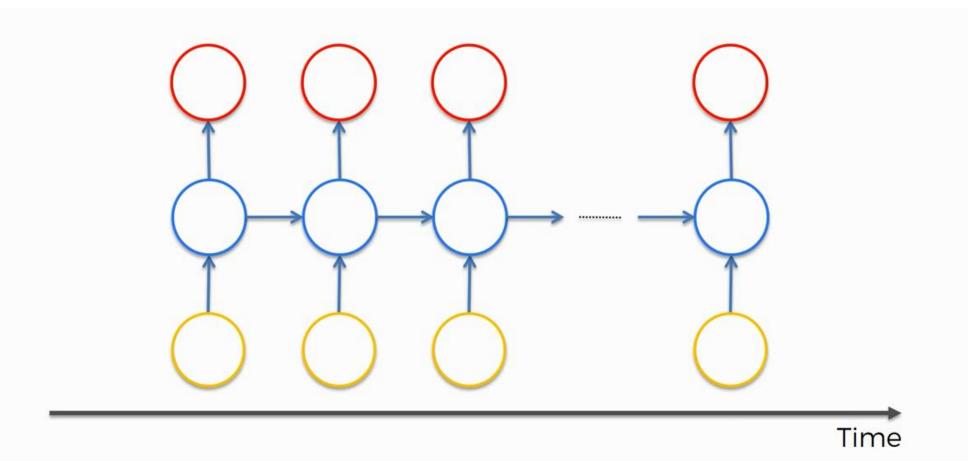
$$\frac{\partial \mathbf{x}_{t}}{\partial \mathbf{x}_{k}} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_{i}}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^{T} diag(\sigma'(\mathbf{x}_{i-1}))$$
(5)

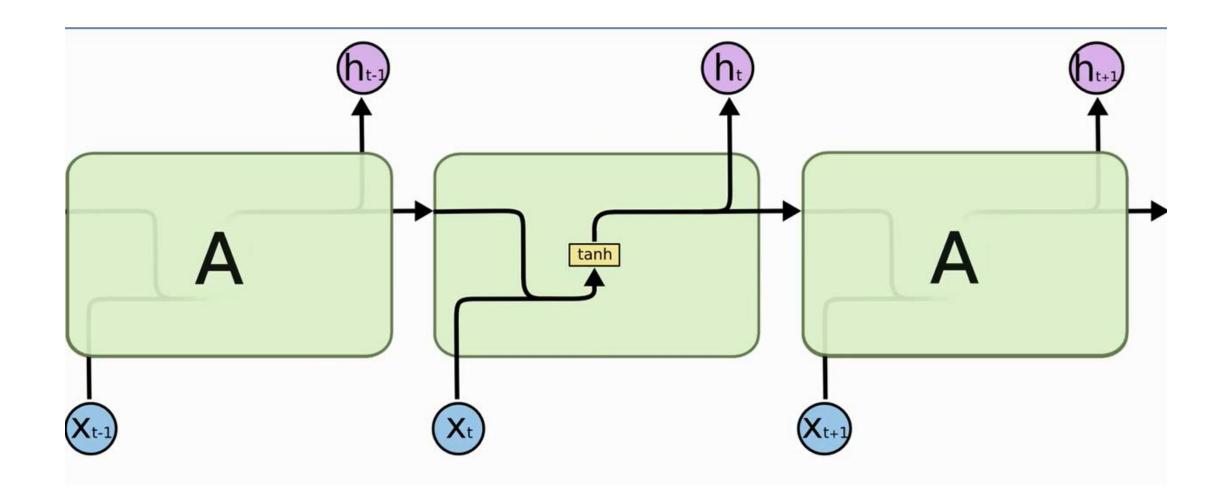
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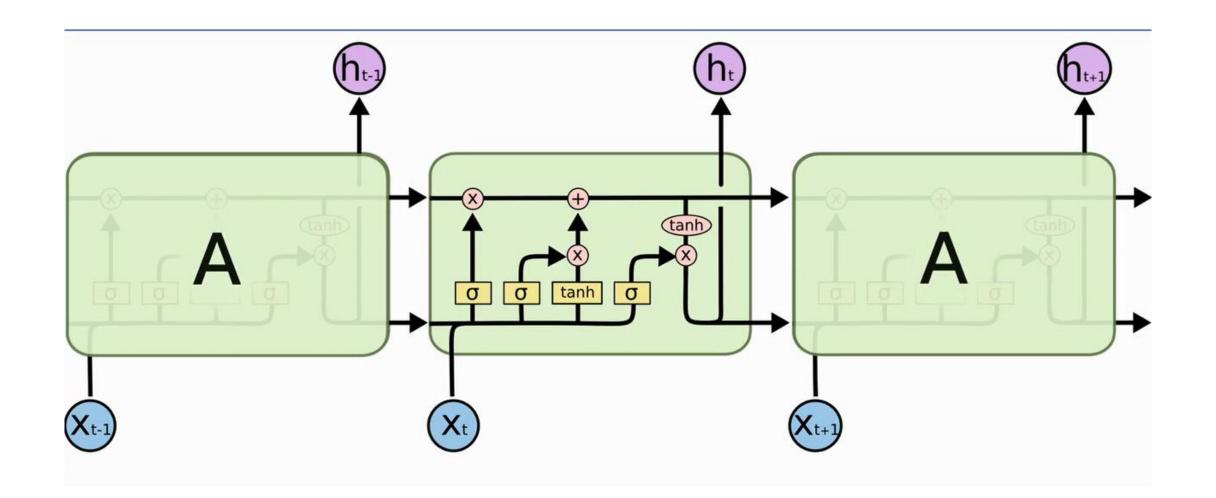


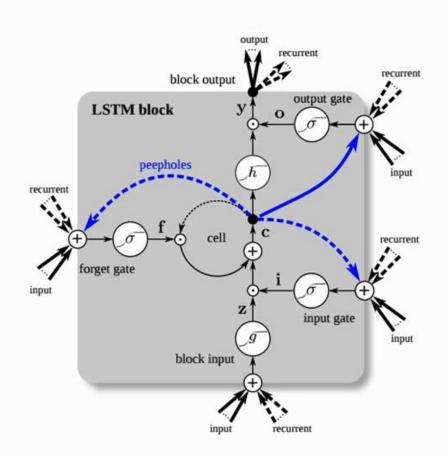
Vanishing

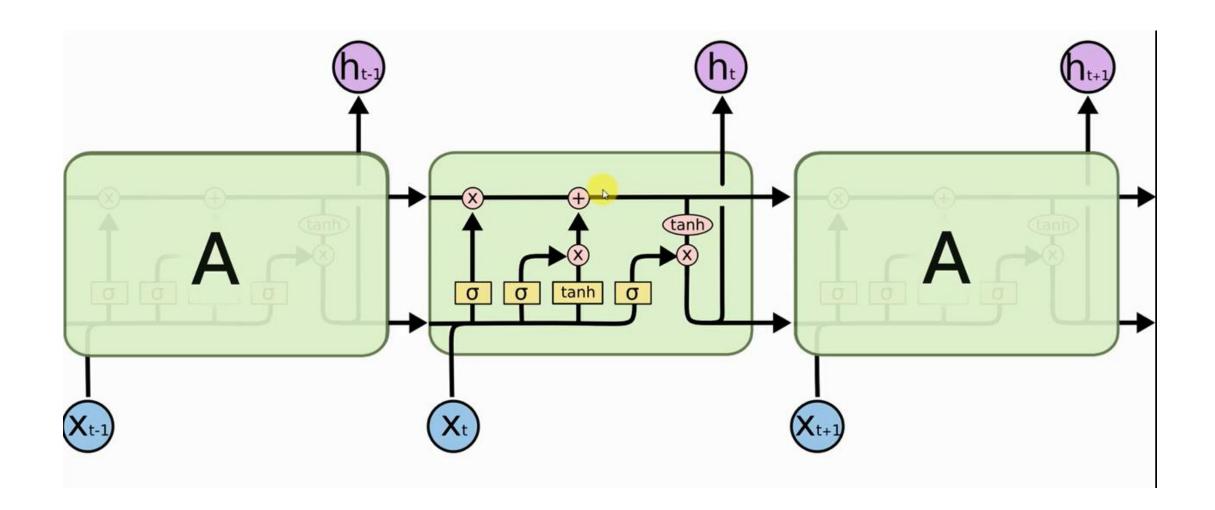


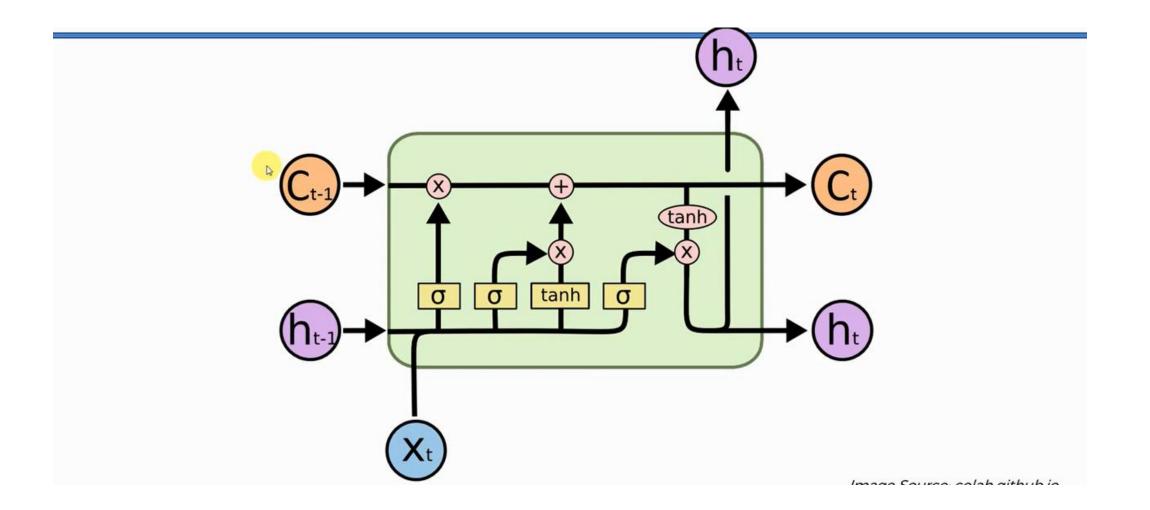


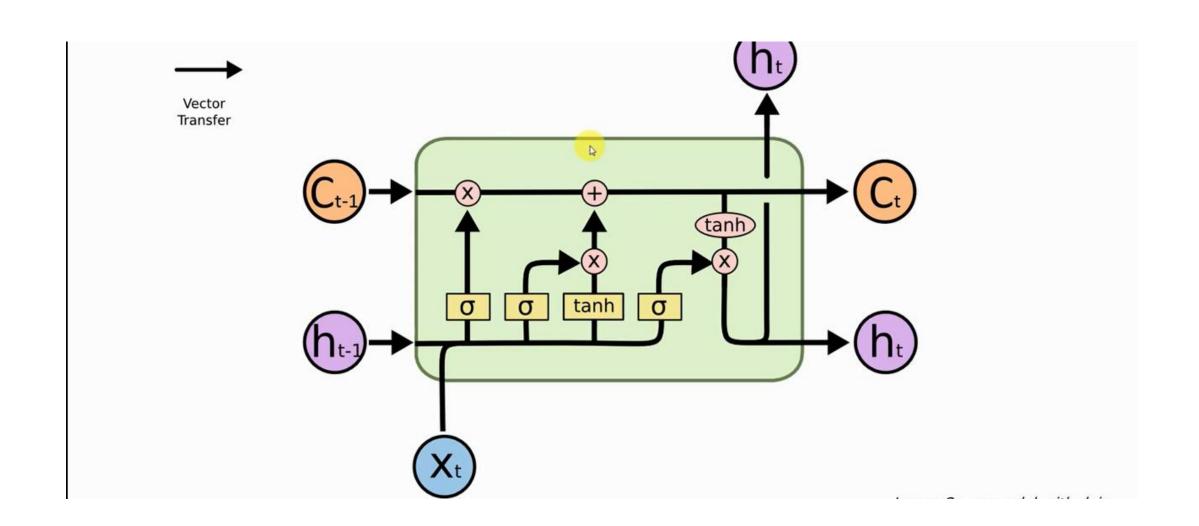


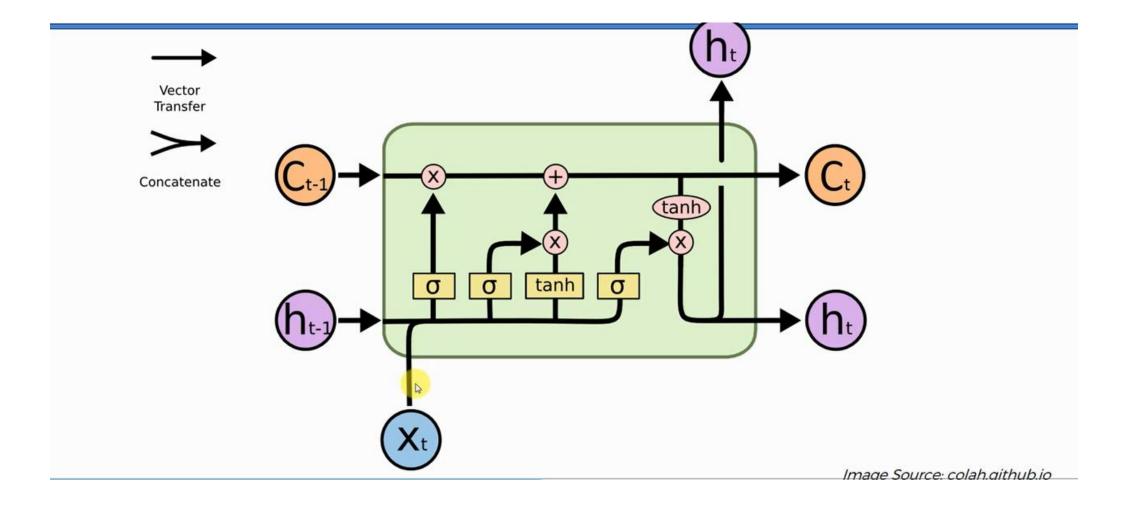


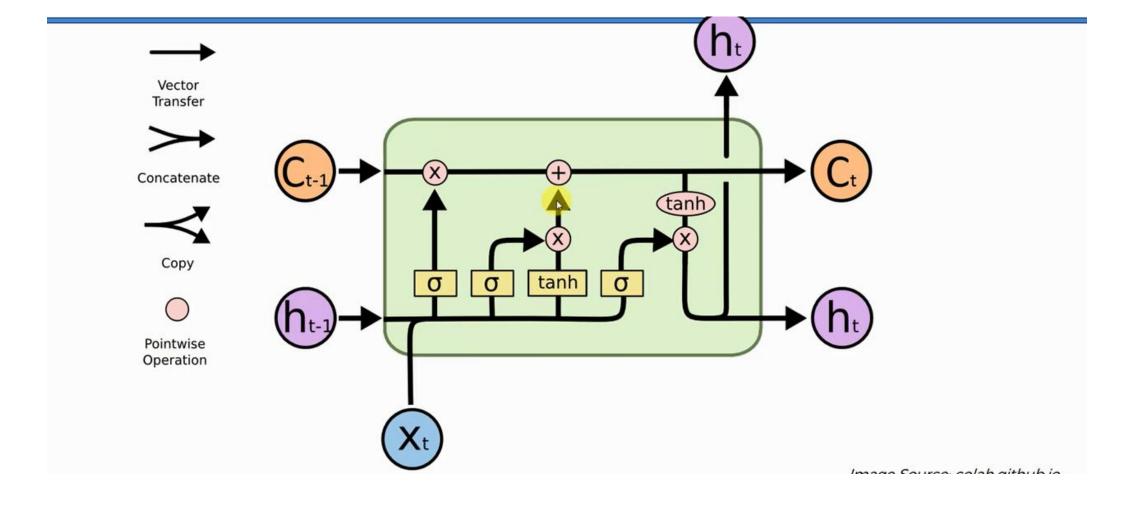




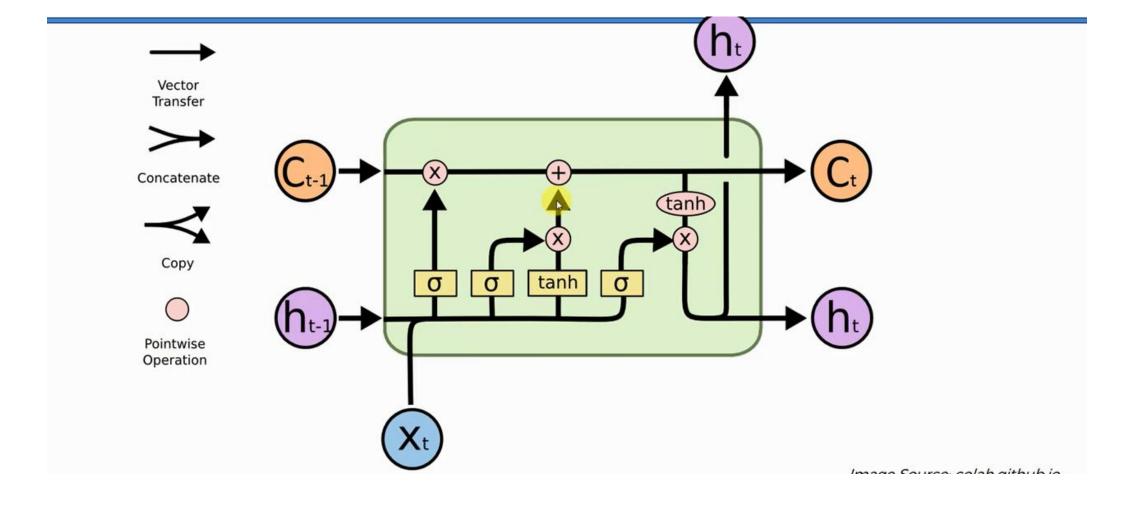




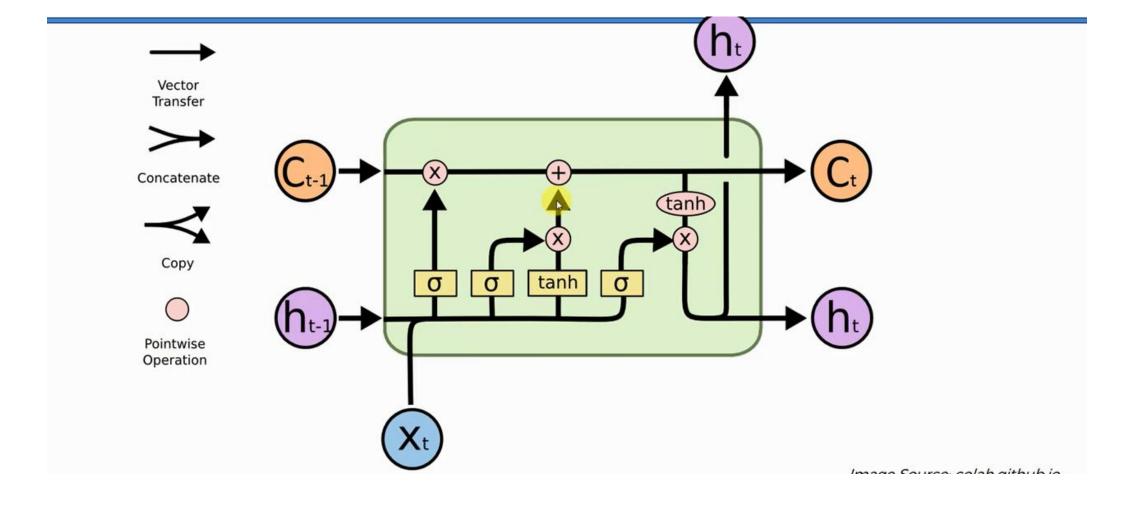


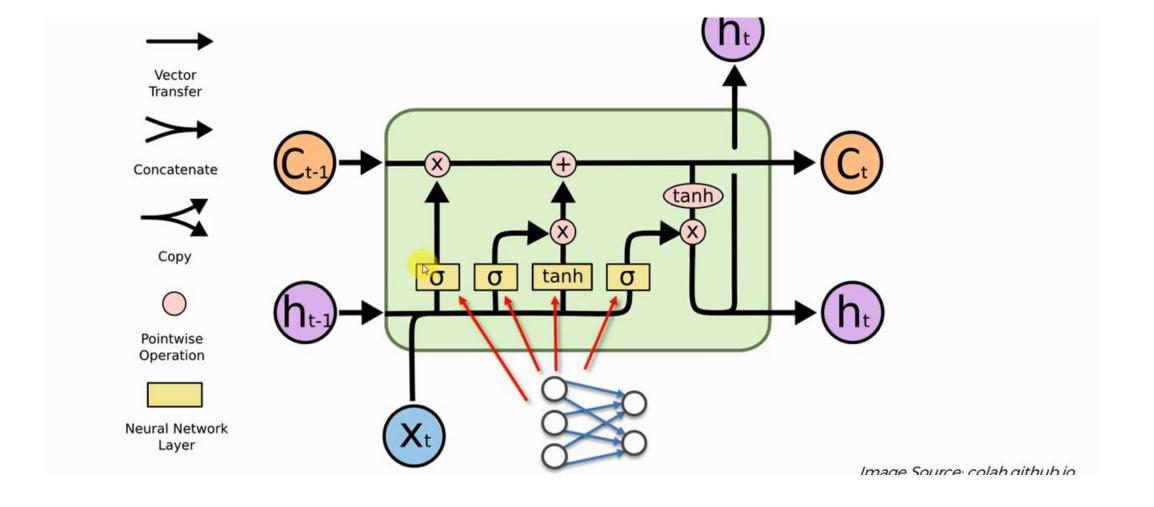


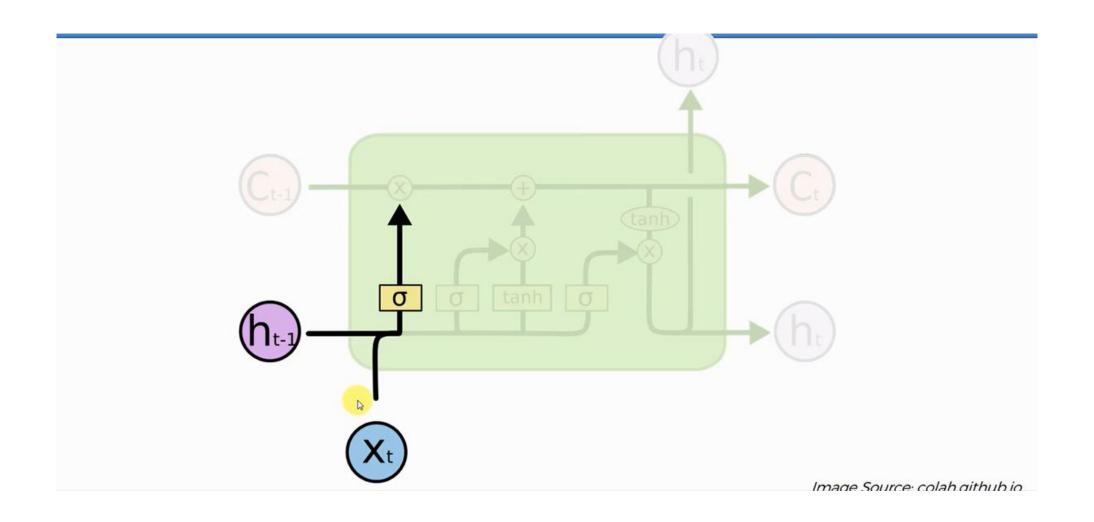


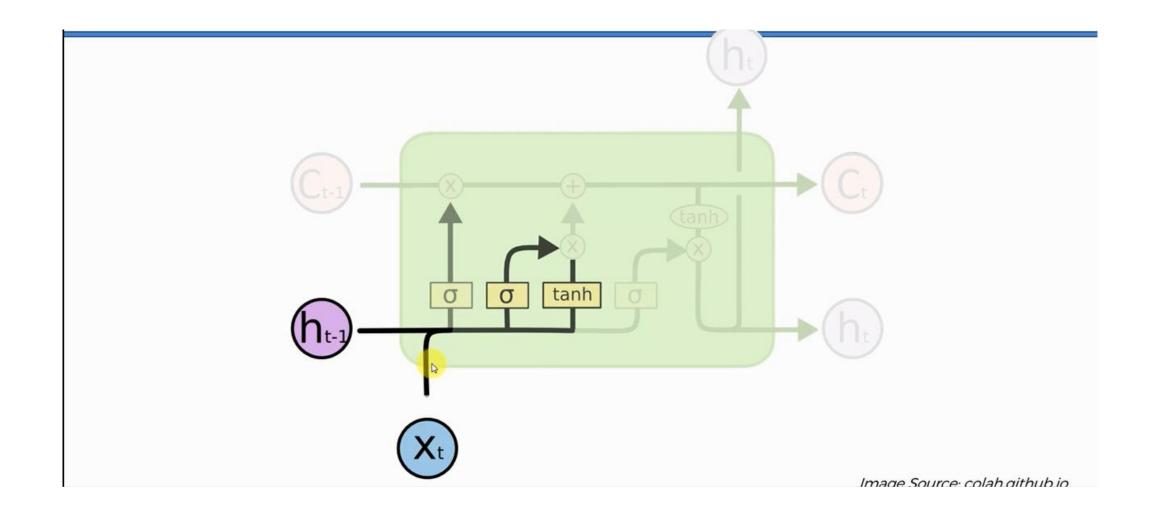


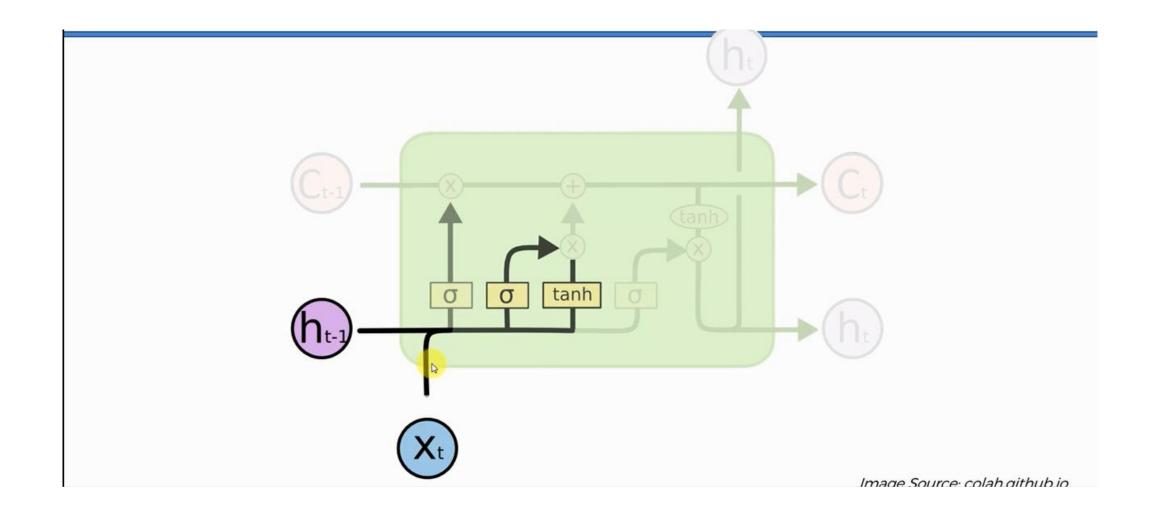


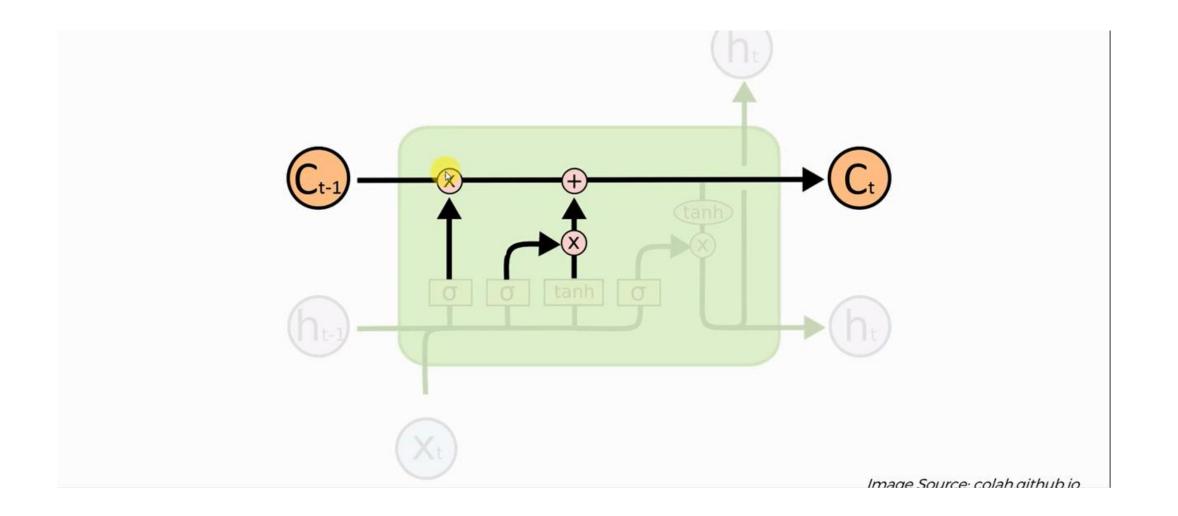


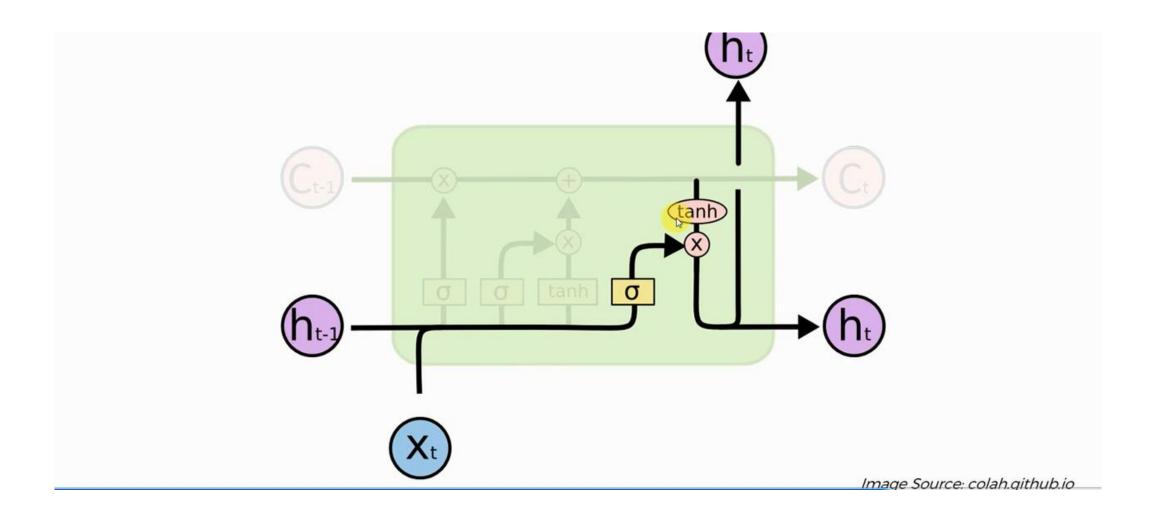


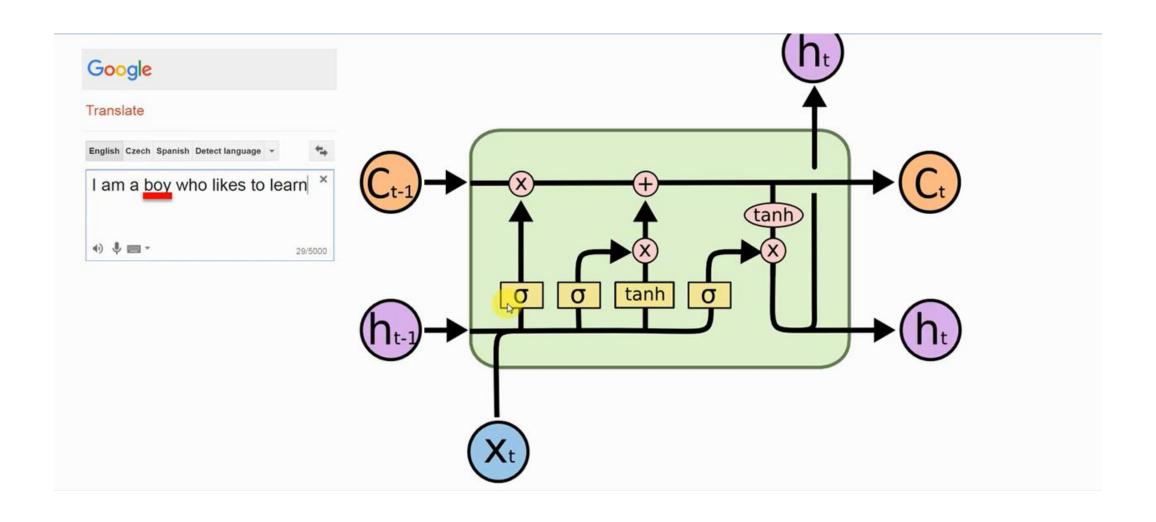










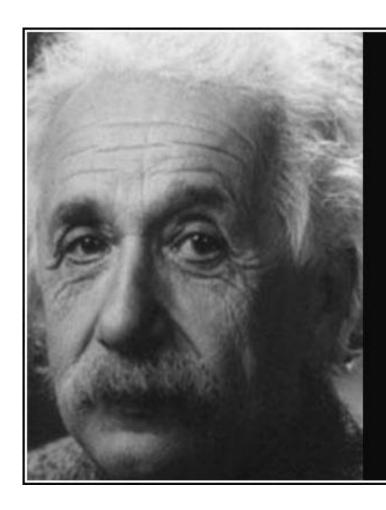


## Summary

## Recurrent Neural Networks



Artificial Neural Networks	Used for Regression & Classification
Convolutional Neural Networks	Used for Computer Vision
Recurrent Neural Networks	Used for Time Series Analysis



A person who never made a mistake never tried anything new.

— Albert Einstein —

AZ QUOTES

## Thank You!!!