

# K Nearest Neighbor



# Instance Based Learning

- Also known as “Lazy Learning”
- Store the given training data and don’t learn any model
- During query time, retrieve a set of “similar” instances from the training data and use them to classify/predict the new instance
- Essentially construct only local approximations to the target function
- There is no global model learnt to perform well across all instances



# K-NN (K-Nearest Neighbours)

- One of the most basic forms of instance learning
- K-NN Algorithm for Classification
- Training method:
  - Save the training examples
- At prediction time:
  - Find the  $k$  training examples  $(x_1, y_1), \dots, (x_k, y_k)$  that are closest to the test example  $x$
  - Predict the most frequent class among those  $y_i$ 's.

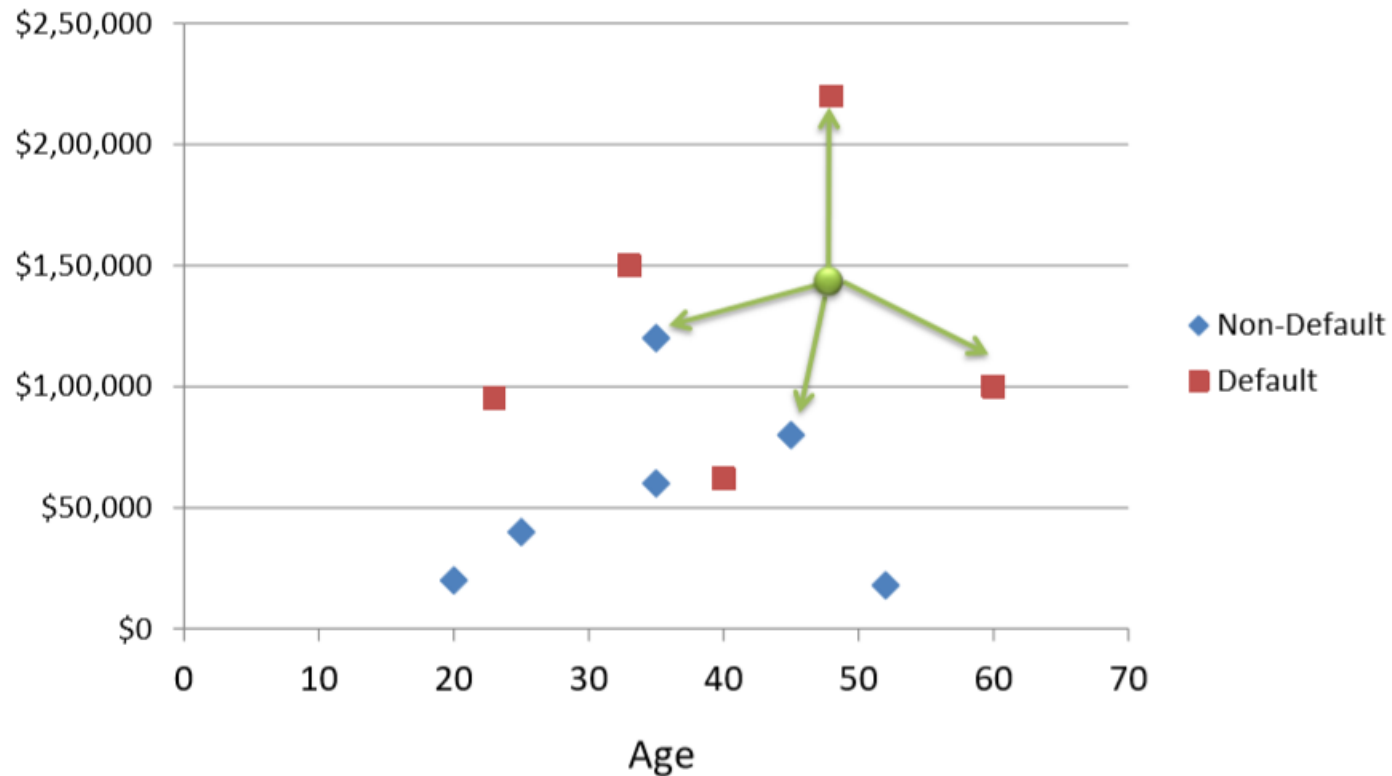


# K-NN - Classification

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# K-NN - Classification





# K-NN – Classification (Contd..)

Age	Loan	Default	Distance
25	\$40,000	N	102000
35	\$60,000	N	82000
45	\$80,000	N	62000
20	\$20,000	N	122000
35	\$120,000	N	22000
52	\$18,000	N	124000
23	\$95,000	Y	47000
40	\$62,000	Y	80000
60	\$100,000	Y	42000
48	\$220,000	Y	78000
33	\$150,000	Y	8000
<b>48</b>	<b>\$142,000</b>	<b>?</b>	

Euclidean Distance

$$D = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$



# K-NN – Classification (Contd ..)

Age	Loan	Default	Distance
0.125	0.11	N	0.7652
0.375	0.21	N	0.5200
0.625	0.31	N	0.3160
0	0.01	N	0.9245
0.375	0.50	N	0.3428
0.8	0.00	N	0.6220
0.075	0.38	Y	0.6669
0.5	0.22	Y	0.4437
1	0.41	Y	0.3650
0.7	1.00	Y	0.3861
0.325	0.65	Y	0.3771
0.7	0.61	?	

Standardized Variable

$$X_s = \frac{X - \text{Min}}{\text{Max} - \text{Min}}$$



# K-NN - Regression

Age	Loan	House Price Index	Distance
25	\$40,000	135	102000
35	\$60,000	256	82000
45	\$80,000	231	62000
20	\$20,000	267	122000
35	\$120,000	139	22000
52	\$18,000	150	124000
23	\$95,000	127	47000
40	\$62,000	216	80000
60	\$100,000	139	42000
48	\$220,000	250	78000
33	\$150,000	264	8000
<b>48</b>	<b>\$142,000</b>	<b>?</b>	

$$D = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$





# K-NN Regression (Contd..)

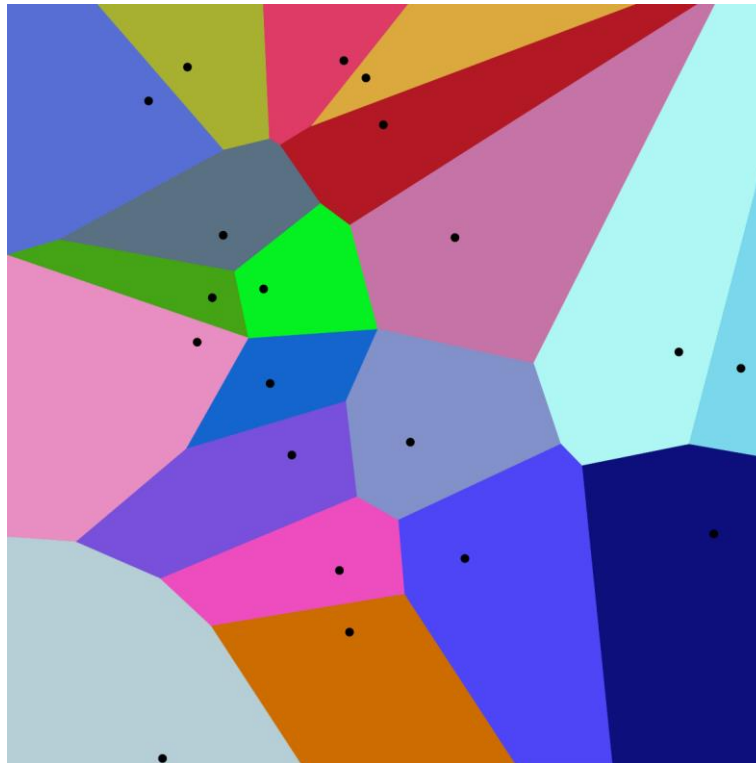
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$$X_s = \frac{X - Min}{Max - Min}$$



# K-NN Decision Boundaries

- Voronoi Diagrams





# How to determine a good value of “K”

- Usually tuned using a validation set
- Start with  $k=1$  and test the error rate on validation set
- Repeat with  $k=k+2$
- Choose the value of  $k$  which has minimum error rate on validation set
- Note: Odd values of  $k$  chosen to avoid ties



# Improving K-NN

- Weighting examples from the neighborhood
- Measuring “closeness”
- Finding “close” examples in a large training set quickly

# Reference

