

## Gradient descent

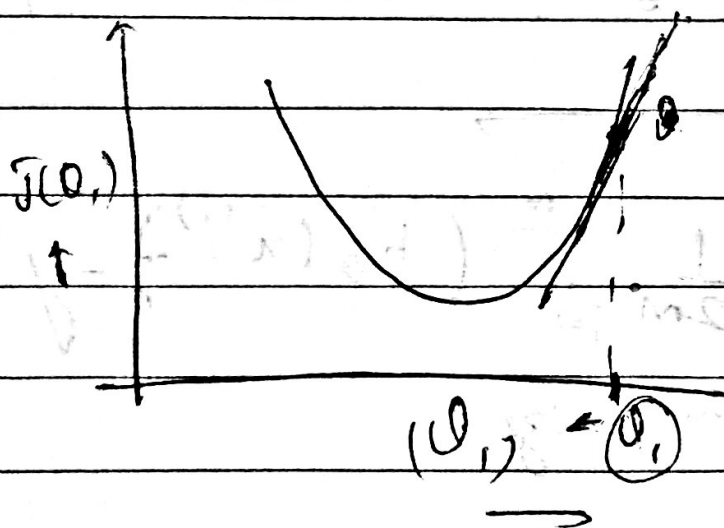
$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

learning rate (tiny steps downhill)

$$j = 0 \text{ to } j = 1$$

Simultaneously update  $\theta_0$  &  $\theta_1$

$\alpha \rightarrow$  determines how far your steps



$$J(\theta_1) = c$$

$$\theta_1 = \theta_1 - \alpha \frac{d}{d\theta_1} J(\theta_1)$$

$\geq \theta'$  derivative = slope

$$\therefore \theta_1 = \theta_1 - \alpha (\text{value})$$

therefore,  $\theta_1$  will move towards left.

$\rightarrow$  If  $\alpha$  is too small, it will take tiny steps

$\rightarrow$  If  $\alpha$  is too large, it may overshoot.

## Gradient descent algorithm.

$$\theta_j = \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) \quad (\text{until convergence})$$

for  $j=1$  &  $j=0$  simultaneously

## Linear Regression Model.

$$h_\theta(x) = \theta_0 + \theta_1 x \quad (\text{hypothesis})$$

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

squared error cost function.

$$\frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) = \frac{\partial}{\partial \theta_0} \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

$$= \frac{\partial}{\partial \theta_0} \frac{1}{2m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})^2$$

Gradient  
descent  
algo

$$\theta_{0,j} = 0 : \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\theta_{1,j} = 1 : \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

'Batch' gradient descent.

~~Optimal~~

$$2 = 0_0 + 0_1(4)$$

$$40_1 + 0_0 = 2$$

$$20_1 + 0_0 = 1$$

$$20_1 = 1$$

$$0_1 = 0.5$$

$$h(6) = 0_0 + 0_1 x$$
$$= -1 + 2(6)$$

$$= 11$$

Test of Hessian

$$2 + 6 \leq 10$$

$$\begin{bmatrix} 1 & 0 & 3 \\ 2 & 1 & 5 \\ 3 & 1 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 6 \\ 2 \end{bmatrix} = \begin{bmatrix} 4 \\ 18 \end{bmatrix}$$

$$2 \times 8 = 16$$

House

2104

1416

1534

852

3 company hypotheses

$$h_1(x) = -40 + 0.25x$$

$$h_2(x) = 200 + 0.1x$$

$$h_3(x) = -150 + 0.4x$$

18 hypotheses

$$\begin{bmatrix} 1 & 2104 \\ 1 & 1416 \\ 1 & 1534 \\ 1 & 852 \end{bmatrix} \quad \begin{bmatrix} -40 & 200 & -150 \\ 0.25 & 0.1 & 0.4 \end{bmatrix}$$

★ Matrix multiplication is not commutative.

$$A \times B \neq B \times A.$$

★ Associative law

$$A \times (B \times C) = (A \times B) \times C.$$

Matrix is associative.

★ for identity matrix,

$$A \cdot I = I \cdot A = A$$