

# EE450 Discussion #7



- Multiplexing



# Statistical TDM Parameters

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- $I$  = Number of Input Sources
- $R$  = Data rate of each source (bps)
- $\alpha$  (Alpha) = mean fraction of time each source is transmitting
- $M$  = Effective capacity of multiplexed line
- $K = M / (I \times R)$  = Ratio of multiplexed line capacity to total input rate
- $\lambda$  (lambda) =  $\alpha \times I \times R$  = Average Arrival time
- $T_s = 1 / M$  = Service time in seconds



# $\rho$ : Line Utilization

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- $\rho$  = Fraction of total link capacity being used
- Many different forms to express line utilization
  - $\rho = \lambda T_s$
  - $\rho = (a \times I \times R) / M$
  - $\rho = a / K$
  - $\rho = \lambda / M$



## Sample Problem #5

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- Ten 9600 bps lines are multiplexed using TDM. Ignoring overhead bits what is the total capacity required for Synchronous TDM?
  - Simple:  $10 \times 9600 = 96 \text{ kbps (96,000)}$



# Sample Problem #6

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- Ten 9600 bps lines are multiplexed using TDM.  
Assuming that we limit line utilization to 0.8 and each line is busy 50 % of the time. What is the capacity required for Statistical TDM?
- What do we know?
  - Line utilization –  $\rho = .8$
  - Fraction of time transmitting -  $\alpha = .5$
  - R Data Rate of each input source = 9600 bps
  - I number of Input Sources = 10



# Continued

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- The Equation:
- $\rho = a \times I \times R \times /M$ 
  - Where M is the capacity of the multiplexed line
- Rearrange for M
  - $M = a \times I \times R / \rho$
- Plug in the given parameters
  - $M = 0.5 \times 10 \times 9600 / 0.8$
  - $M = 60 \text{ kbps}$



# Sample Problem #7

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- Calculate the capacity of a Multiplexed carrier?
  - 24 voice channels multiplexed
  - 8000 samples per second
    - Each frame lasts  $1/8000 = 125 \mu \text{ sec}$
  - Uses 8 bit encoding per sample
  - Capacity
    - $24 \times 8000 \text{ samples/second} \times 8 \text{ bits/sample}$
    - 1,536,000 bits/second
  - T-1 Adds an extra bit per frame (for synchronization) which makes it 1.544 Mbps



# Sample Problem #8

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- What is the percent overhead on a T-1 Carrier?
  - T-1 Carrier bandwidth of 1.544 Mbps
    - Every 192 bits one more bit is added for framing.
  - What is the overhead?





# Continued

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- Overhead in a T-1 Line
  - Every frame consists of 193 bits
  - $24 \times 8 = 192$  bits
  - $193 - 192 = 1$  overhead bit
  - $1/193 = .5\%$