

# **Elective in Robotics**

## **Modeling and Control of Multi-Rotor UAVs**

Marilena Vendittelli

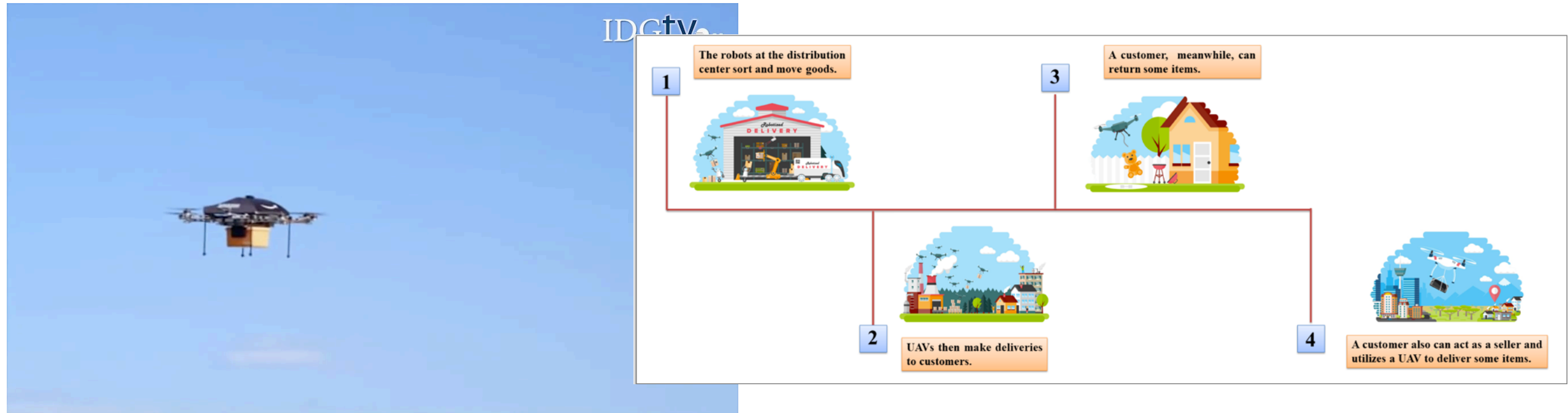
**2020**  
**Final projects**



**SAPIENZA**  
UNIVERSITÀ DI ROMA

- 7 projects + possible additional ones proposed and **well motivated** by students
- work **must** be carried out in groups of **3-4 students**
- programming in C/C++ or Matlab required
- projects must be chosen by **November 30**
  - **written report** with selected results + pdf, software, videos, **presentation** (all in a shared Drive folder)
- 20 min presentation of the obtained results
- **NOTE:** projects are alternative to individual presentation of a scientific paper
  - **presentation assignment:** a list of papers will be provided in the e-learning environment

# Project I: External wrench estimation



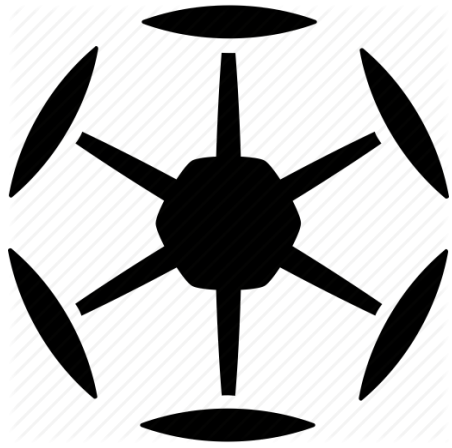
- estimate the external wrench generated by an unknown load placed on an unknown point on the quadrotor frame
- simulation environment at your choice

## bibliography

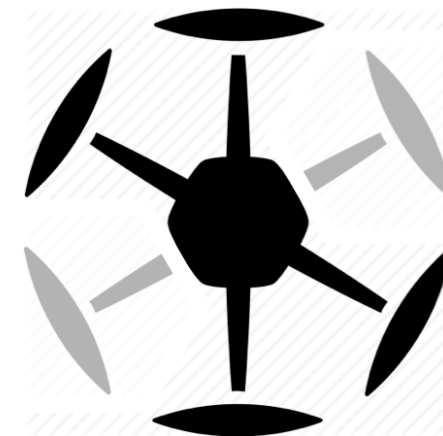
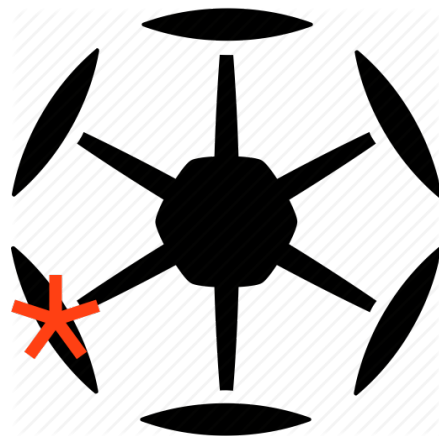
- Tomić, Teodor and Lutz, Philipp and Schmid, Korbinian and Mathers, Andrew and Haddadin, Sami, “Simultaneous Contact and Aerodynamic Force Estimation (s-CAFE) for Aerial Robots,” International Journal of Robotics Research (IJRR), 2019 [[PDF](#)]

# Project 2: Fault-isolation for multi-rotor UAVs

supervised by Prof. A. Cristofaro



- consider a system with  $n \geq 2$  pairs of rotors
- assume that one rotor fails
- design observers and compute residuals to isolate the fault
- extend the technique to handle simultaneous faults

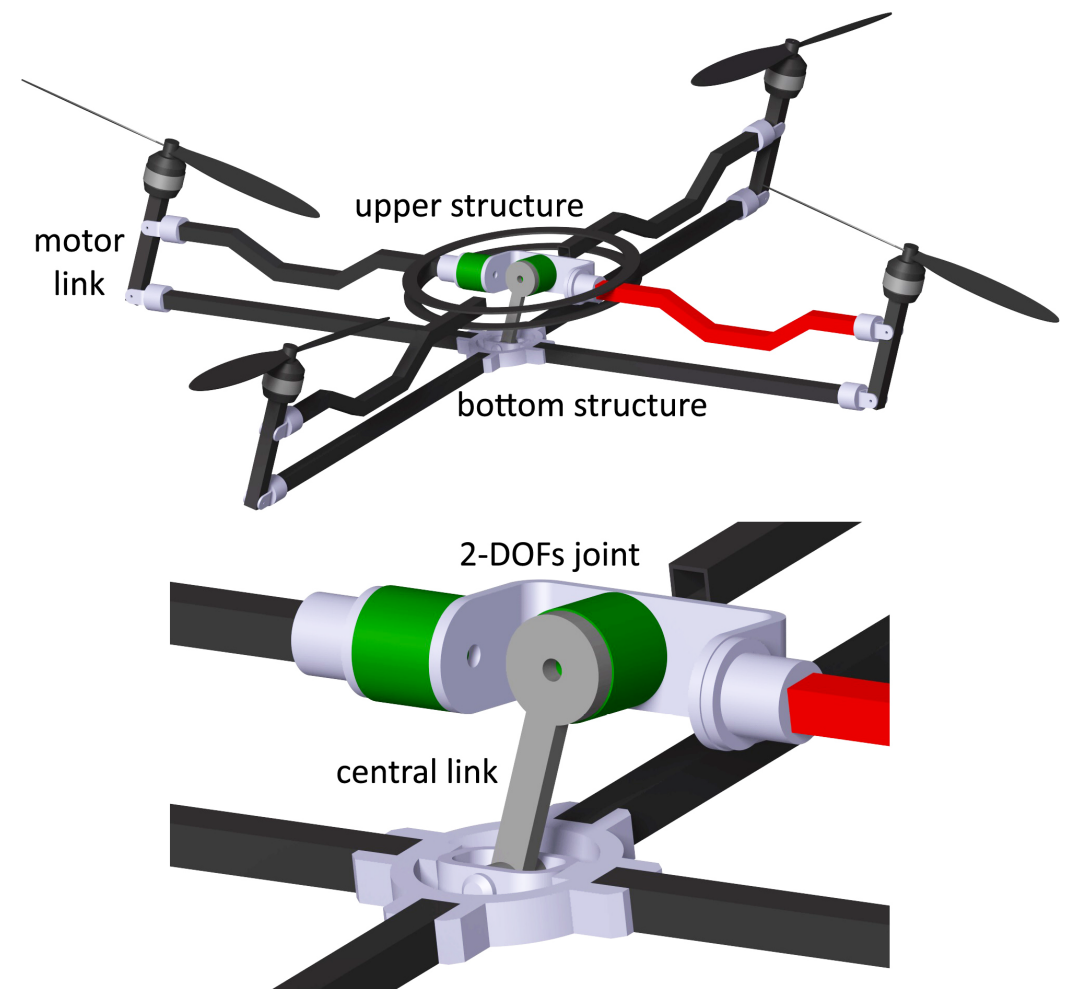


## bibliography

- J. Chen, R.J. Patton and H.-Y. Zhang, Design of unknown input observers and robust fault detection filters, Int. J. of Control, 1996
- L. Imbrenda et al., On non-linear unknown input observers - applied to lateral vehicle velocity estimation on banked roads, Int. J. of Control, 2007
- Z. Cen et al., Robust fault diagnosis for quadrotor UAVs using adaptive Thau observer, J. Intelligent & Robotic Systems, 2014

# Project 3: Simulation model and control of a fully actuated quadrotor

- Matlab implementation of the simulation model and control of a fully actuated quadrotor with a 2-DOFs tilting mechanism

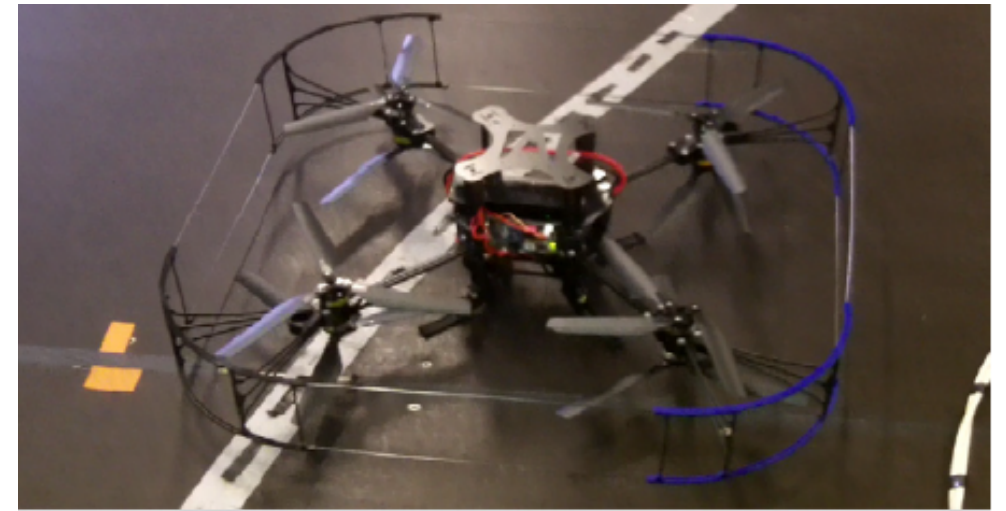


## bibliography

- Marcin Odelga, Paolo Stegagno and Heinrich H. Bühlhoff, A Fully Actuated Quadrotor UAV with a Propeller Tilting Mechanism: Modeling and Control, 2016 IEEE International Conference on Advanced Intelligent Mechatronics (AIM) Banff, Alberta, Canada, July 12–15, 2016

# Project 4: Local controllability and actuators failure

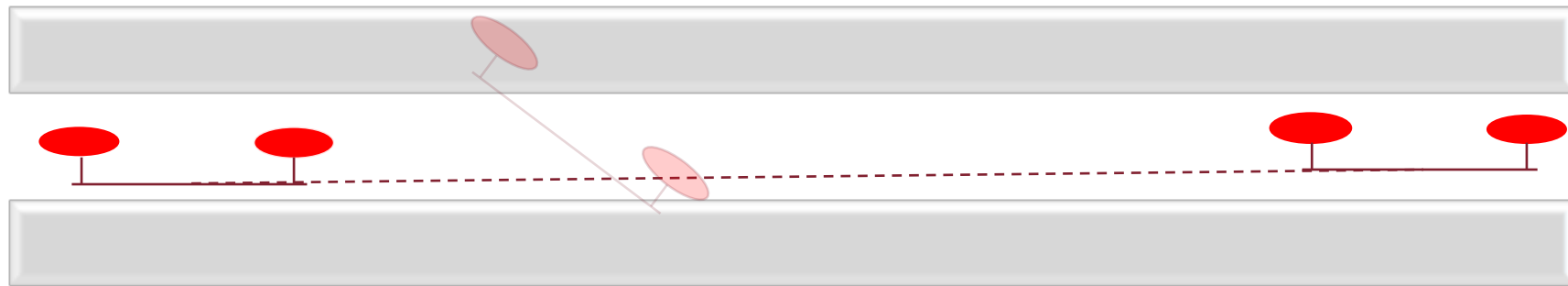
- Matlab implementation of the simulation model of an octorotor
- analysis of the effect of actuators failures on local controllability



## bibliography

- Majd Saied, Hassan Shraim, Benjamin Lussier, Isabelle Fantoni, Clovis Francis, Local controllability and attitude stabilization of multirotor UAVs: Validation on a coaxial octorotor, Robotics and Autonomous Systems 91 (2017) 128–138

# Project 5: Local controllability and motion planning



consider the problem sketched in the figure

- a geometric, collision-free, path is not dynamically feasible for a quadrotor
- is it always possible to find dynamically feasible approximating paths arbitrarily close to the original geometric one?

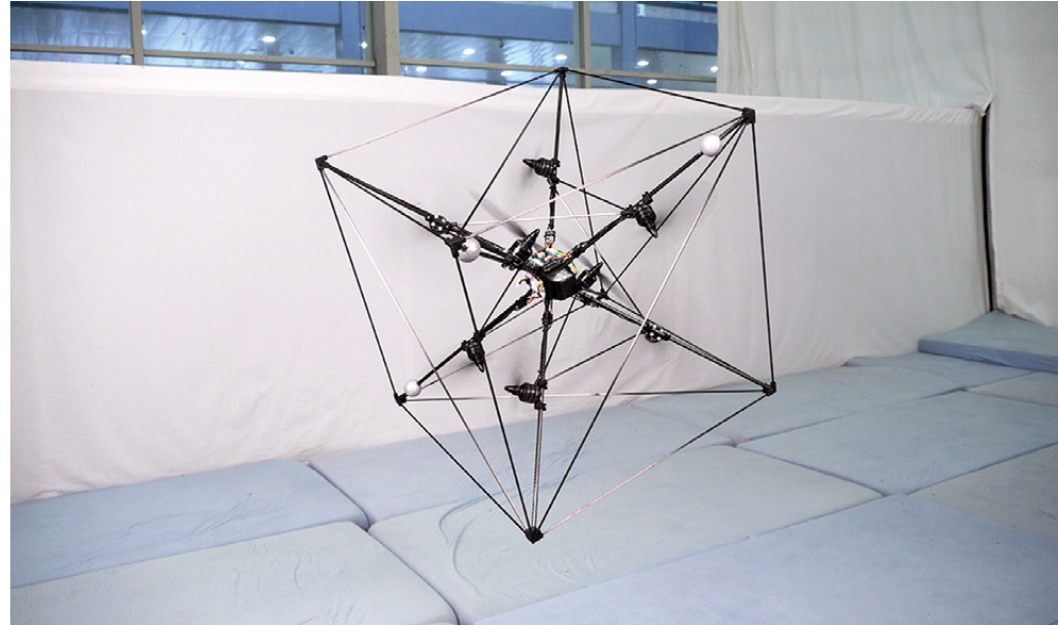
find the theoretical conditions allowing or preventing the adoption of the two-steps planning paradigm based on a preliminary geometric path planning followed by its approximation by a feasible one; provide simulations to illustrate your proof (simulation environment at your choice)

## bibliography

- Majd Saied, Hassan Shraim, Benjamin Lussier, Isabelle Fantoni, Clovis Francis, Local controllability and attitude stabilization of multirotor UAVs: Validation on a coaxial oct rotor, Robotics and Autonomous Systems 91 (2017) 128–138



# Project 6: CoppeliaSim model of a fully actuated OM multirotor aerial vehicle



- implement the simulation model with basic position and attitude control of an omnidirectional multirotor aerial vehicle at your choice, from the catalog provided in the bibliographic reference below
- simulation environment: CoppeliaSim

## **bibliography**

- Mahmoud Hamandi, Federico Usai, Quentin Sablé, Nicolas Staub, Marco Tognon, Antonio Franchi, Survey on Aerial Multirotor Design: a Taxonomy Based on Input Allocation, <https://hal.archives-ouvertes.fr/hal-02433405>



# Project 7: Complementary filter for state estimation

$${}^I a_{\text{IMU}} = R a_{\text{IMU}} \simeq \hat{R} a_{\text{IMU}} \simeq -g \hat{R} \vec{z}_I - g \hat{R} D \hat{R}^T v$$

$$\dot{\hat{R}} = \hat{R}(\Omega_{\text{IMU}} - \hat{b})_{\times} - \alpha_{\times}$$

$$\dot{\hat{b}} = k_b \alpha$$

$$\alpha_{\times} = \left( \frac{k_a}{g^2} ((\hat{R}^T \vec{z}_I) \times \bar{a}_{\text{IMU}}) + \frac{k_m}{|\mathbf{I}_m|^2} ((\hat{R}^T \mathbf{I}_m) \times m_{\text{IMU}}) \right)_{\times} + \dots$$

↓

$$v = -\frac{1}{g} (\hat{R} D \hat{R}^T)^{-1} ({}^I a_{\text{IMU}} + g \hat{R} \vec{z}_I)$$

$$\dot{\hat{v}} = -g(\hat{R} \vec{z}_I + \hat{R} D \hat{R}^T \hat{v}) - k_w(\hat{v} - v)$$

- implementation of the complementary filter in (I) for the CoppeliaSim quadrotor model provided in the e-learning environment
- possibly include the improved dynamic model provided in (II)
- simulation environment at your choice

## bibliography

- (I) R. Mahony, T. Hamel and J. M. Pflimlin, "Nonlinear Complementary Filters on the Special Orthogonal Group," in IEEE Transactions on Automatic Control, vol. 53, no. 5, pp. 1203-1218, June 2008. doi: 10.1109/TAC.2008.923738
- (II) R. C. Leishman, J. C. Macdonald Jr., R. W. Beard, and, T. W. Mc Lain, Quadrotors and Accelerometers - State Estimation with an Improved Dynamic Model, IEEE Control Systems Magazine, DOI: 10.1109/MCS.2013.2287362