

# BirthTimeSeries

## Part A decomposition

```
library(forecast)
```

```
## Warning: package 'forecast' was built under R version 3.4.4
```

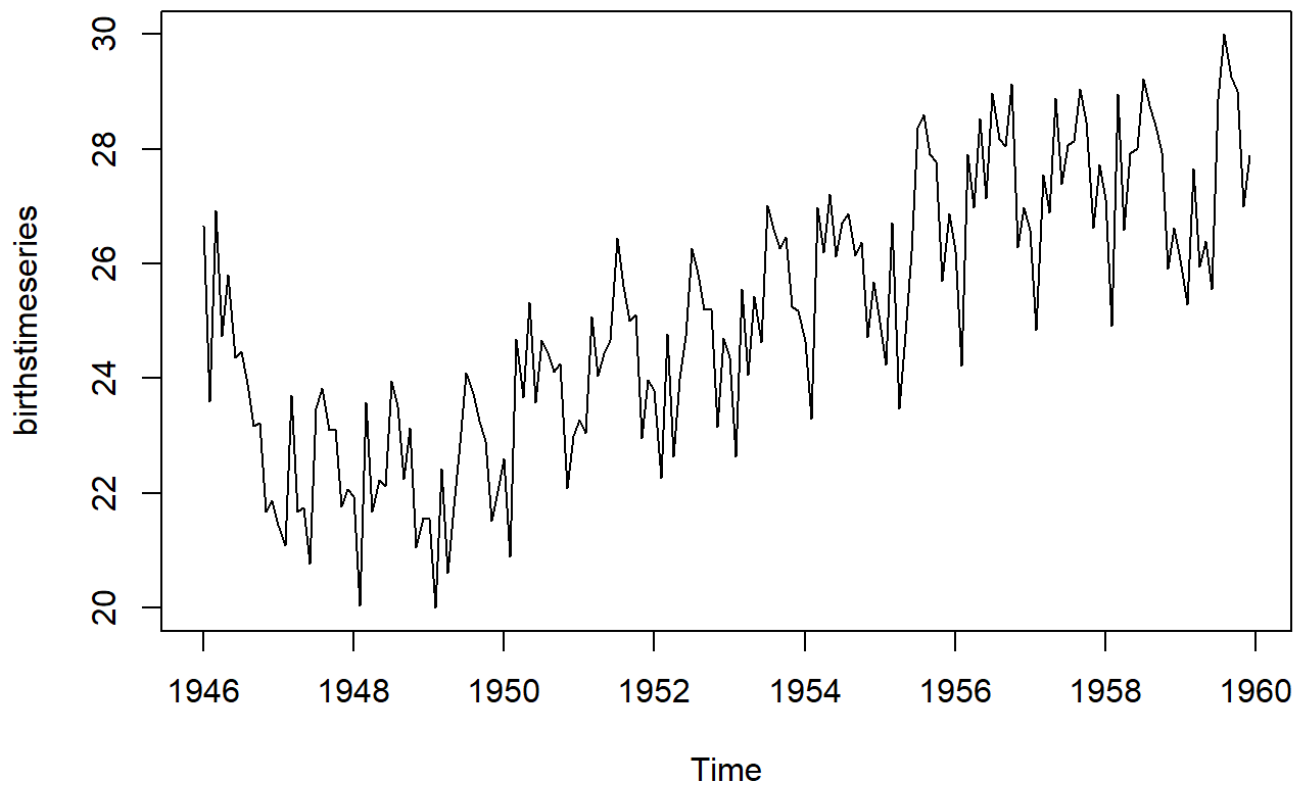
```
births <- scan("http://robjhyndman.com/tsdldata/data/nybirths.dat")
birthstimeseries <- ts(births, frequency=12, start=c(1946,1))
birthstimeseries
```

```
##           Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep      Oct
## 1946 26.663 23.598 26.931 24.740 25.806 24.364 24.477 23.901 23.175 23.227
## 1947 21.439 21.089 23.709 21.669 21.752 20.761 23.479 23.824 23.105 23.110
## 1948 21.937 20.035 23.590 21.672 22.222 22.123 23.950 23.504 22.238 23.142
## 1949 21.548 20.000 22.424 20.615 21.761 22.874 24.104 23.748 23.262 22.907
## 1950 22.604 20.894 24.677 23.673 25.320 23.583 24.671 24.454 24.122 24.252
## 1951 23.287 23.049 25.076 24.037 24.430 24.667 26.451 25.618 25.014 25.110
## 1952 23.798 22.270 24.775 22.646 23.988 24.737 26.276 25.816 25.210 25.199
## 1953 24.364 22.644 25.565 24.062 25.431 24.635 27.009 26.606 26.268 26.462
## 1954 24.657 23.304 26.982 26.199 27.210 26.122 26.706 26.878 26.152 26.379
## 1955 24.990 24.239 26.721 23.475 24.767 26.219 28.361 28.599 27.914 27.784
## 1956 26.217 24.218 27.914 26.975 28.527 27.139 28.982 28.169 28.056 29.136
## 1957 26.589 24.848 27.543 26.896 28.878 27.390 28.065 28.141 29.048 28.484
## 1958 27.132 24.924 28.963 26.589 27.931 28.009 29.229 28.759 28.405 27.945
## 1959 26.076 25.286 27.660 25.951 26.398 25.565 28.865 30.000 29.261 29.012
##           Nov      Dec
## 1946 21.672 21.870
## 1947 21.759 22.073
## 1948 21.059 21.573
## 1949 21.519 22.025
## 1950 22.084 22.991
## 1951 22.964 23.981
## 1952 23.162 24.707
## 1953 25.246 25.180
## 1954 24.712 25.688
## 1955 25.693 26.881
## 1956 26.291 26.987
## 1957 26.634 27.735
## 1958 25.912 26.619
## 1959 26.992 27.897
```

**ts** is a timeseries function that will convert data to time series.

Frequency 12 means data will be represented on a monthly basis and start defines the starting date (in this case from january 1946)

```
plot(birthstimeseries)
```



Plotting values on Y axis. Time is represented on X axis.

```
birthstimeseriescomponents <- decompose(birthstimeseries)
```

To estimate the trend, seasonal and irregular components of this time series.

The estimated values of the seasonal, trend and irregular components are now stored in variables.

```
birthstimeseriescomponents$seasonal
```

##		Jan	Feb	Mar	Apr	May	Jun
## 1946	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1947	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1948	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1949	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1950	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1951	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1952	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1953	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1954	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1955	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1956	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1957	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1958	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
## 1959	-0.6771947	-2.0829607	0.8625232	-0.8016787	0.2516514	-0.1532556	
##		Jul	Aug	Sep	Oct	Nov	Dec
## 1946	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1947	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1948	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1949	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1950	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1951	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1952	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1953	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1954	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1955	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1956	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1957	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1958	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	
## 1959	1.4560457	1.1645938	0.6916162	0.7752444	-1.1097652	-0.3768197	

get the estimated values of the seasonal component

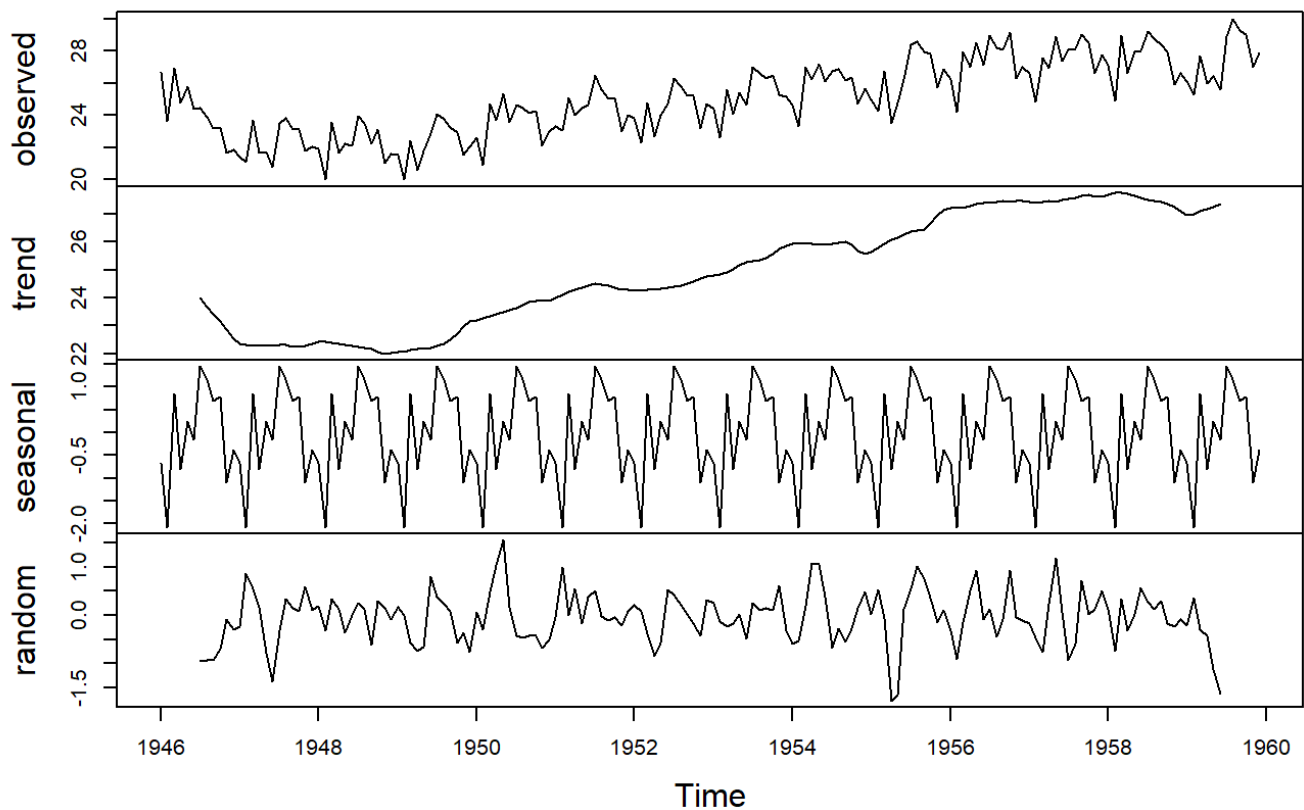
```
birthstimeseriescomponents$trend
```

##	Jan	Feb	Mar	Apr	May	Jun	Jul
## 1946	NA	NA	NA	NA	NA	NA	23.98433
## 1947	22.35350	22.30871	22.30258	22.29479	22.29354	22.30562	22.33483
## 1948	22.43038	22.43667	22.38721	22.35242	22.32458	22.27458	22.23754
## 1949	22.06375	22.08033	22.13317	22.16604	22.17542	22.21342	22.27625
## 1950	23.21663	23.26967	23.33492	23.42679	23.50638	23.57017	23.63888
## 1951	24.00083	24.12350	24.20917	24.28208	24.35450	24.43242	24.49496
## 1952	24.27204	24.27300	24.28942	24.30129	24.31325	24.35175	24.40558
## 1953	24.78646	24.84992	24.92692	25.02362	25.16308	25.26963	25.30154
## 1954	25.92446	25.92317	25.92967	25.92137	25.89567	25.89458	25.92963
## 1955	25.64612	25.78679	25.93192	26.06388	26.16329	26.25388	26.35471
## 1956	27.21104	27.21900	27.20700	27.26925	27.35050	27.37983	27.39975
## 1957	27.44221	27.40283	27.44300	27.45717	27.44429	27.48975	27.54354
## 1958	27.68642	27.76067	27.75963	27.71037	27.65783	27.58125	27.49075
## 1959	26.96858	27.00512	27.09250	27.17263	27.26208	27.36033	NA
##	Aug	Sep	Oct	Nov	Dec		
## 1946	23.66213	23.42333	23.16112	22.86425	22.54521		
## 1947	22.31167	22.26279	22.25796	22.27767	22.35400		
## 1948	22.21988	22.16983	22.07721	22.01396	22.02604		
## 1949	22.35750	22.48862	22.70992	22.98563	23.16346		
## 1950	23.75713	23.86354	23.89533	23.87342	23.88150		
## 1951	24.48379	24.43879	24.36829	24.29192	24.27642		
## 1952	24.44475	24.49325	24.58517	24.70429	24.76017		
## 1953	25.34125	25.42779	25.57588	25.73904	25.87513		
## 1954	25.98246	26.01054	25.88617	25.67087	25.57312		
## 1955	26.40496	26.45379	26.64933	26.95183	27.14683		
## 1956	27.44150	27.45229	27.43354	27.44488	27.46996		
## 1957	27.56933	27.63167	27.67804	27.62579	27.61212		
## 1958	27.46183	27.42262	27.34175	27.25129	27.08558		
## 1959	NA	NA	NA	NA	NA		

get the estimated values of the trend component

```
plot(birthstimeseriescomponents)
```

## Decomposition of additive time series



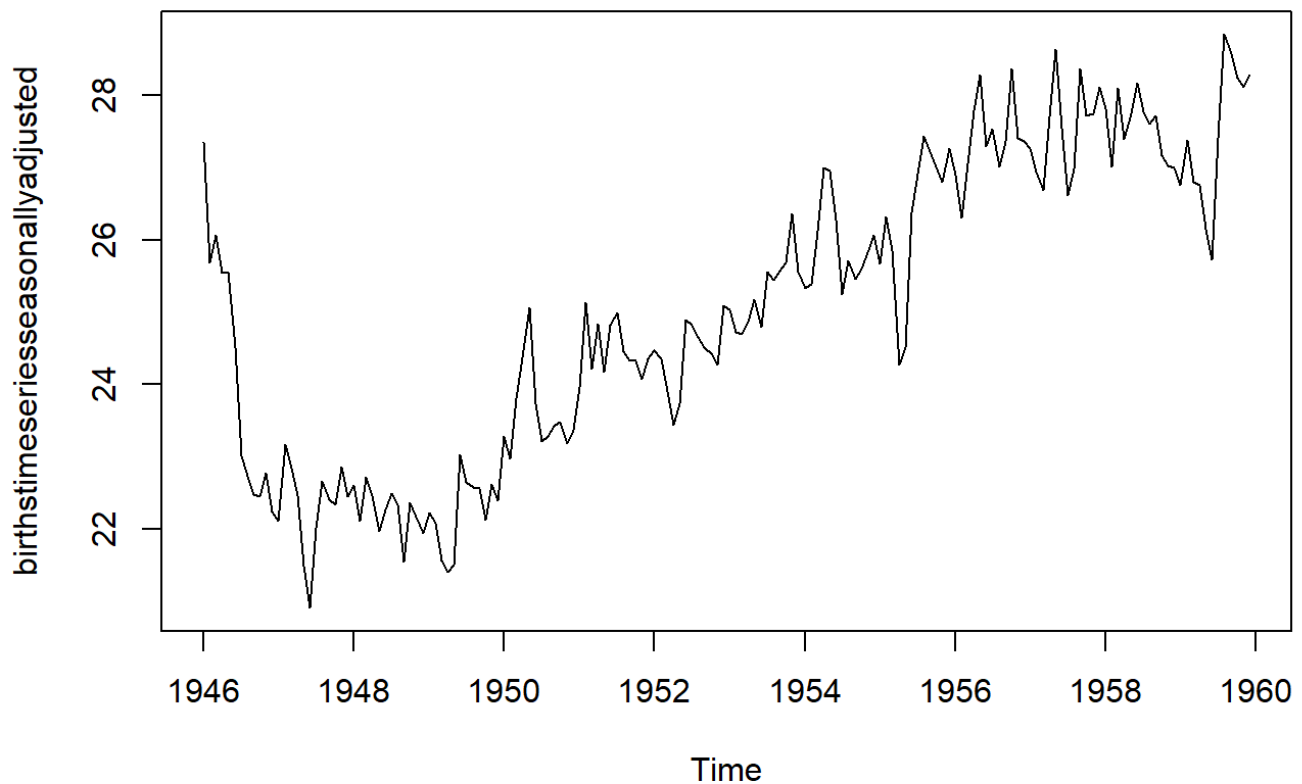
First graph is between Observed value and Time

Second graph is between Trend and Time. Trend defines the kind of trend the value is forming over a time period

Third graph is between Seasonal and time. Seasonal component

Fourth graph is irregular component

```
birthstimeseriesseasonallyadjusted <- birthstimeseries - birthstimeseriescomponents
$seasonal
plot(birthstimeseriesseasonallyadjusted)
```



Seasonal time series that can be described using an additive model

Seasonal variation has been removed from the seasonally adjusted time series.

The seasonally adjusted time series now just contains the trend component and an irregular component.

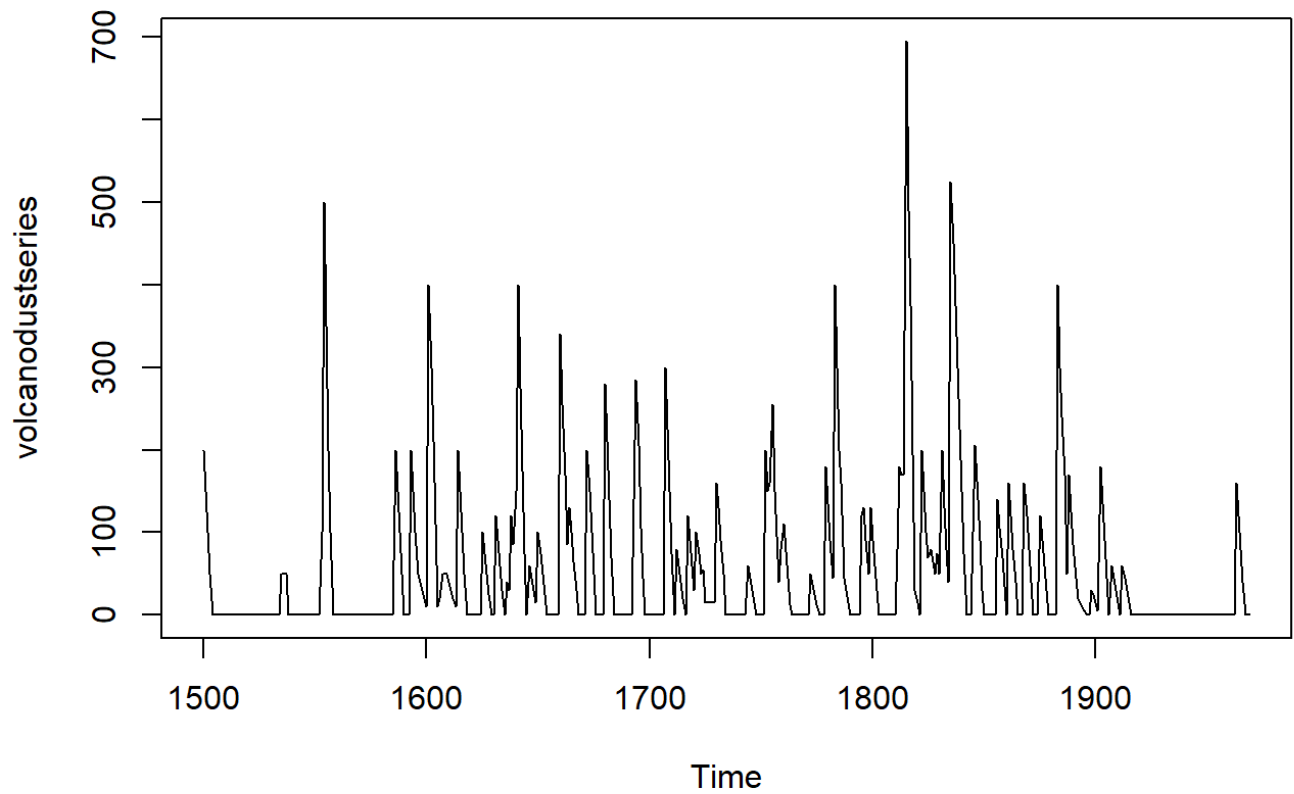
## Part B Using Arima

```
volcanodust <- scan("http://robjhyndman.com/tsdldata/annual/dvi.dat", skip=1)

volcanodustseries <- ts(volcanodust, start=c(1500))
class(volcanodustseries)
```

```
## [1] "ts"
```

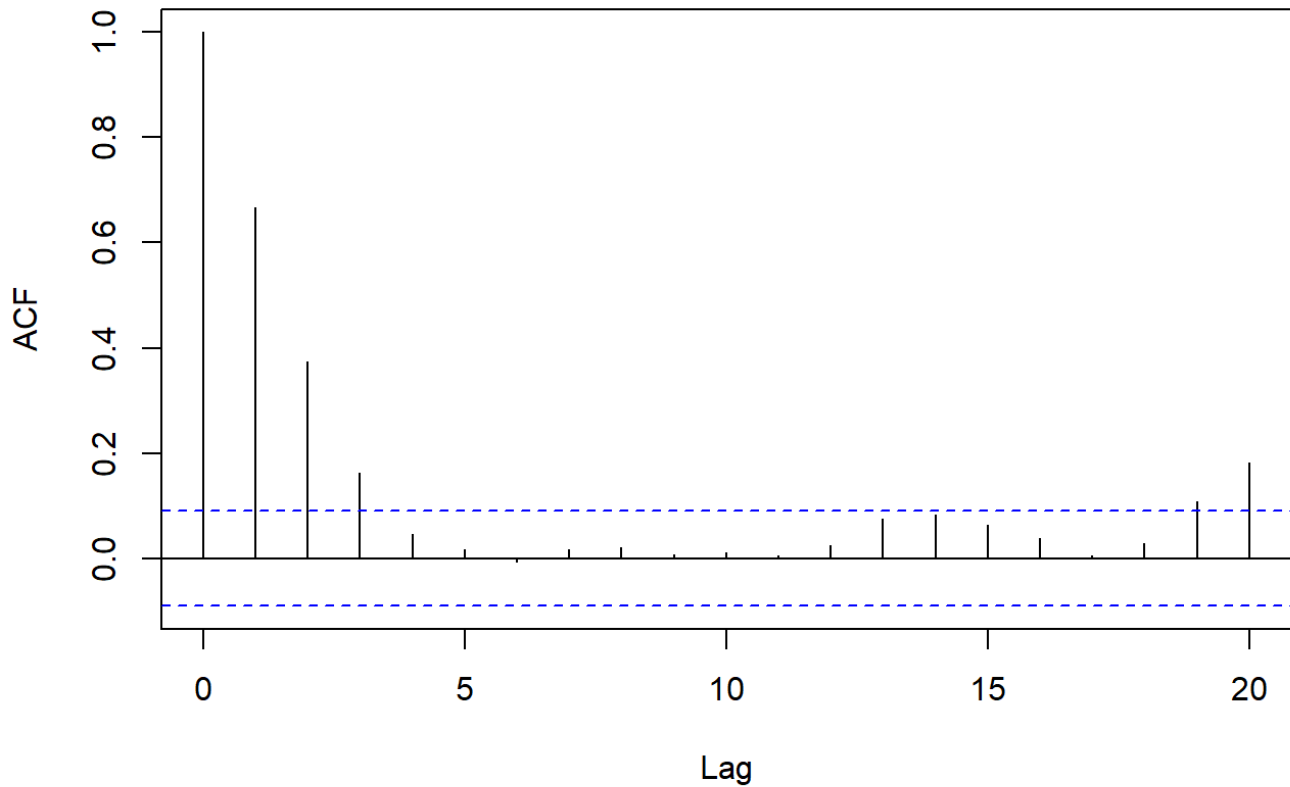
```
plot.ts(volcanodustseries)
```



From the time plot, it appears that the random fluctuations in the time series are roughly constant in size over time, so an additive model is probably appropriate for describing this time series.

```
acf(volcanodustseries, lag.max=20)
```

## Series volcanodustseries



```
acf(volcanodustseries, lag.max=20, plot=FALSE)
```

```
##
## Autocorrelations of series 'volcanodustseries', by lag
##
##      0      1      2      3      4      5      6      7      8      9
## 1.000 0.666 0.374 0.162 0.046 0.017 -0.007 0.016 0.021 0.006
##    10    11    12    13    14    15    16    17    18    19
## 0.010 0.004 0.024 0.075 0.082 0.064 0.039 0.005 0.028 0.108
##    20
## 0.182
```

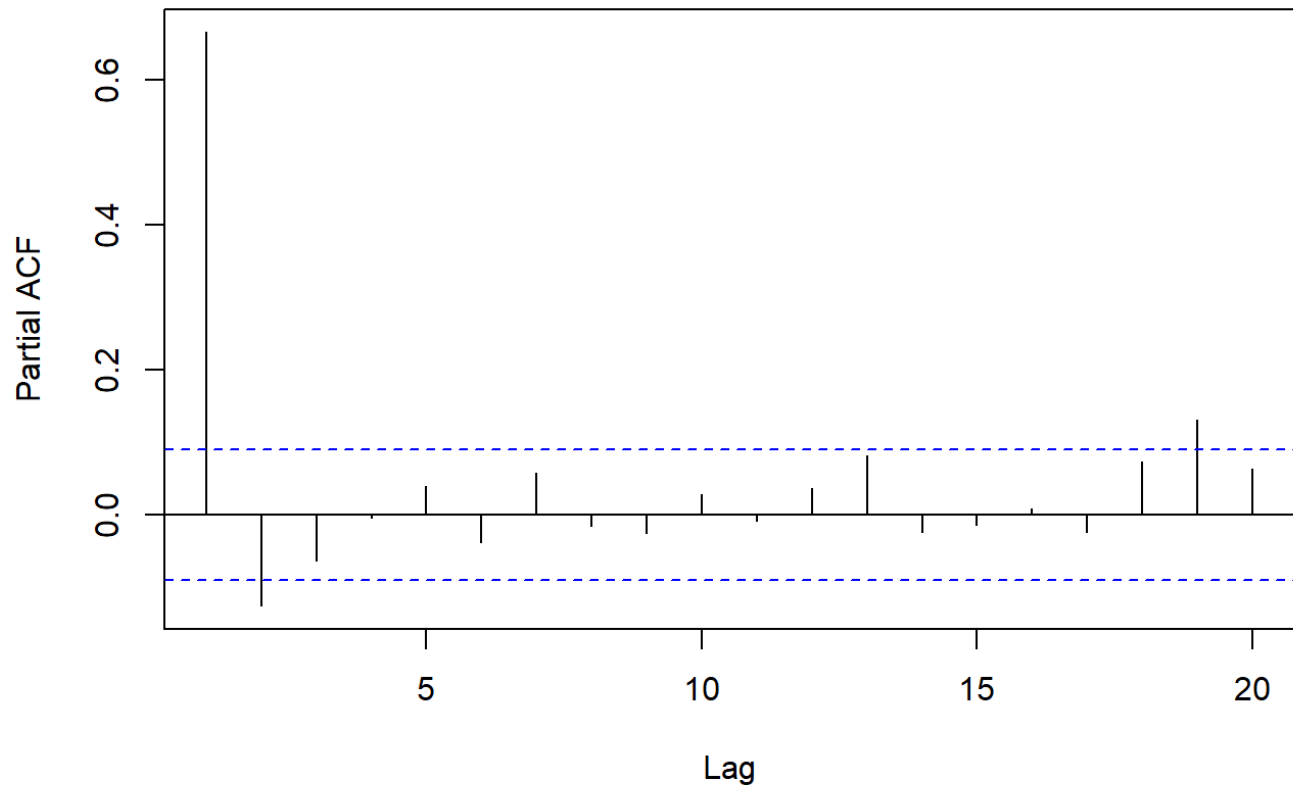
Autocorrelations for lags 1, 2 and 3 exceed the significance bounds, and that the autocorrelations tail off to zero after lag 3.

The autocorrelations for lags 1, 2, 3 are positive, and decrease in magnitude with increasing lag.

```
pacf(volcanodustseries, lag.max=20)
```



## Series volcanodustseries



```
pacf(volcanodustseries, lag.max=20, plot=FALSE)
```

```
##
## Partial autocorrelations of series 'volcanodustseries', by lag
##
##      1      2      3      4      5      6      7      8      9     10
## 0.666 -0.126 -0.064 -0.005  0.040 -0.039  0.058 -0.016 -0.025  0.028
##     11     12     13     14     15     16     17     18     19     20
## -0.008  0.036  0.082 -0.025 -0.014  0.008 -0.025  0.073  0.131  0.063
```

Partial autocorrelation at lag 1 is positive and exceeds the significance bounds (0.666), while the partial autocorrelation at lag 2 is negative and also exceeds the significance bounds (-0.126). The partial autocorrelations tail off to zero after lag 2.

```
volcanodustseriesarima <- arima(volcanodustseries, order=c(2,0,0))
volcanodustseriesarima
```

```
##
## Call:
## arima(x = volcanodustseries, order = c(2, 0, 0))
##
## Coefficients:
##          ar1      ar2  intercept
##      0.7533 -0.1268   57.5274
## s.e.  0.0457   0.0458    8.5958
##
## sigma^2 estimated as 4870:  log likelihood = -2662.54,  aic = 5333.09
```

ARIMA model for the time series of volcanic dust veil index may be an ARIMA(2,0,0) model. To fit an ARIMA(2,0,0) model to this time series

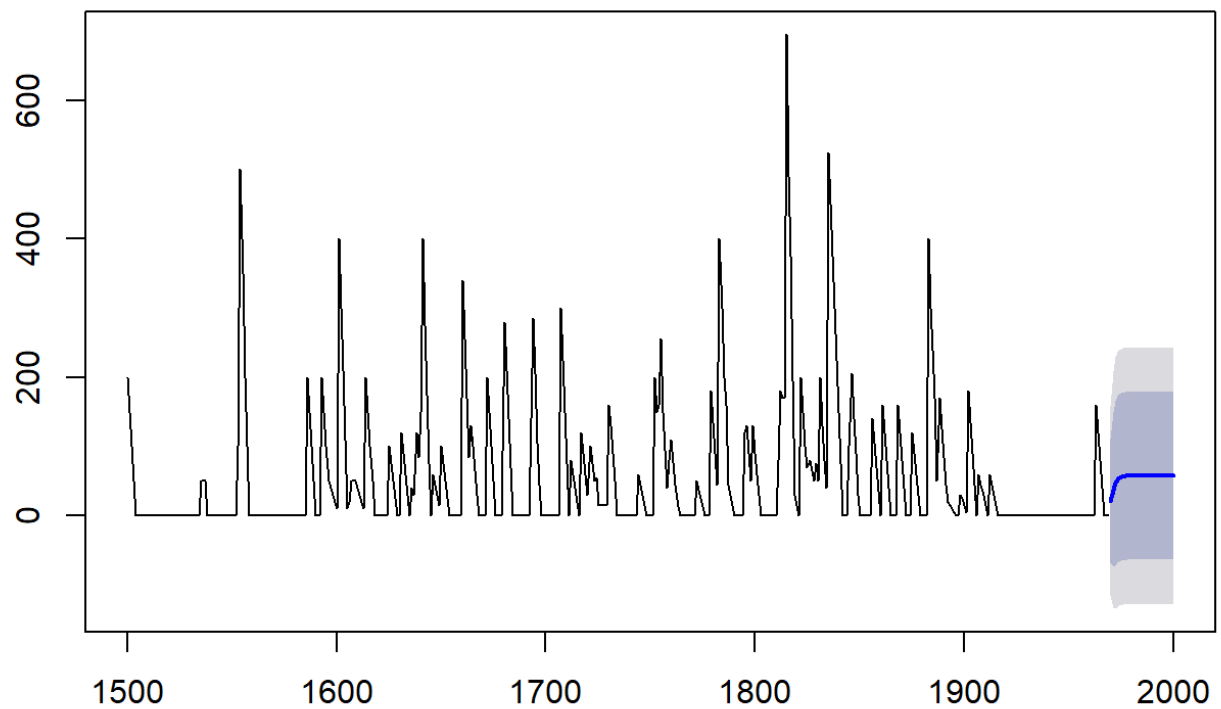
```
volcanodustseriesforecasts <- forecast(volcanodustseriesarima, h=31)
volcanodustseriesforecasts
```

```
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## 1970      21.48131 -67.94860 110.9112 -115.2899 158.2526
## 1971      37.66419 -74.30305 149.6314 -133.5749 208.9033
## 1972      47.13261 -71.57070 165.8359 -134.4084 228.6737
## 1973      52.21432 -68.35951 172.7881 -132.1874 236.6161
## 1974      54.84241 -66.22681 175.9116 -130.3170 240.0018
## 1975      56.17814 -65.01872 177.3750 -129.1765 241.5327
## 1976      56.85128 -64.37798 178.0805 -128.5529 242.2554
## 1977      57.18907 -64.04834 178.4265 -128.2276 242.6057
## 1978      57.35822 -63.88124 178.5977 -128.0615 242.7780
## 1979      57.44283 -63.79714 178.6828 -127.9777 242.8634
## 1980      57.48513 -63.75497 178.7252 -127.9356 242.9059
## 1981      57.50627 -63.73386 178.7464 -127.9145 242.9271
## 1982      57.51684 -63.72330 178.7570 -127.9040 242.9376
## 1983      57.52212 -63.71802 178.7623 -127.8987 242.9429
## 1984      57.52476 -63.71538 178.7649 -127.8960 242.9456
## 1985      57.52607 -63.71407 178.7662 -127.8947 242.9469
## 1986      57.52673 -63.71341 178.7669 -127.8941 242.9475
## 1987      57.52706 -63.71308 178.7672 -127.8937 242.9479
## 1988      57.52723 -63.71291 178.7674 -127.8936 242.9480
## 1989      57.52731 -63.71283 178.7674 -127.8935 242.9481
## 1990      57.52735 -63.71279 178.7675 -127.8934 242.9481
## 1991      57.52737 -63.71277 178.7675 -127.8934 242.9482
## 1992      57.52738 -63.71276 178.7675 -127.8934 242.9482
## 1993      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1994      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1995      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1996      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1997      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1998      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 1999      57.52739 -63.71275 178.7675 -127.8934 242.9482
## 2000      57.52739 -63.71275 178.7675 -127.8934 242.9482
```

forecast() model to predict future values of the volcanic dust veil index.  
The original data includes the years 1500-1969.  
To make predictions for the years 1970-2000 (31 more years)

```
plot(forecast(volcanodustseriesforecasts))
```

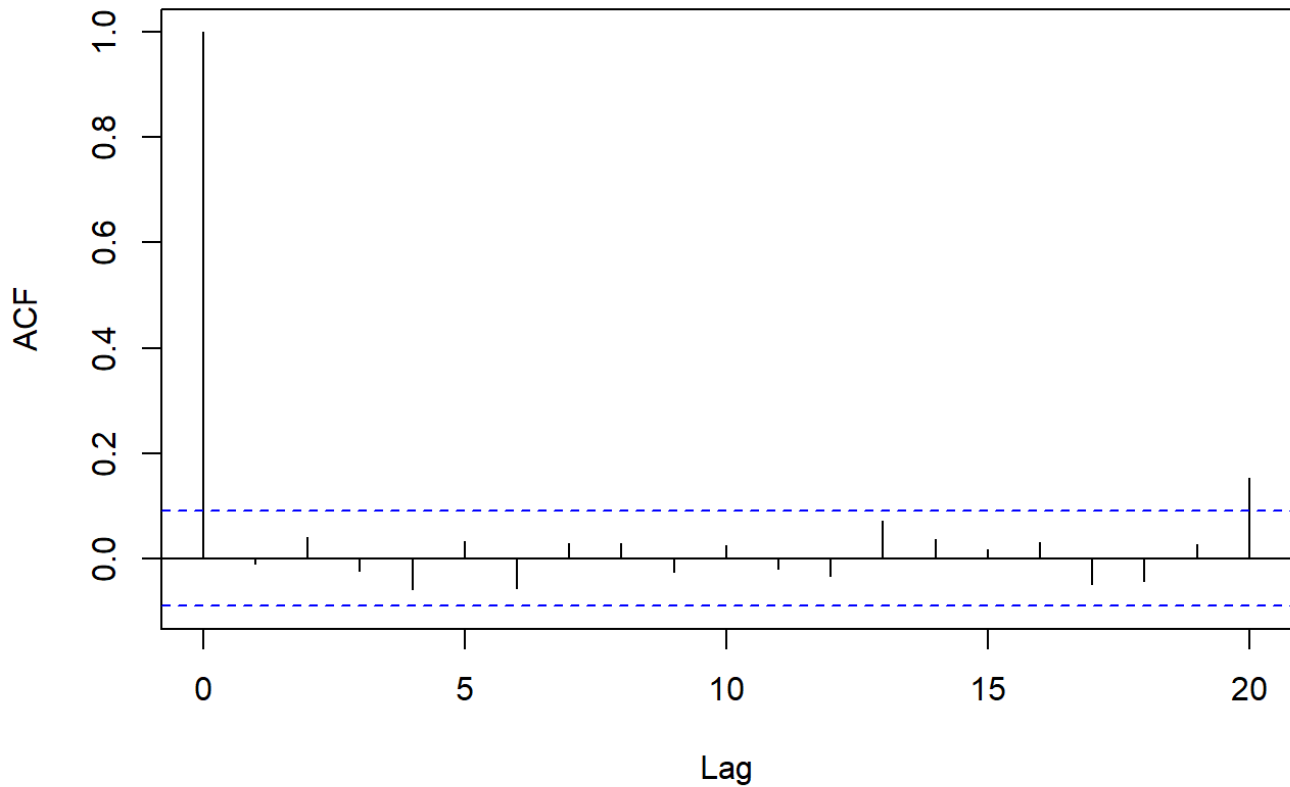
### Forecasts from ARIMA(2,0,0) with non-zero mean



The model has predicted negative values for the volcanic dust veil index, but this variable can only have positive values

```
acf(volcanodustseriesforecasts$residuals, lag.max=20)
```

## Series volcanodustseriesforecasts\$residuals



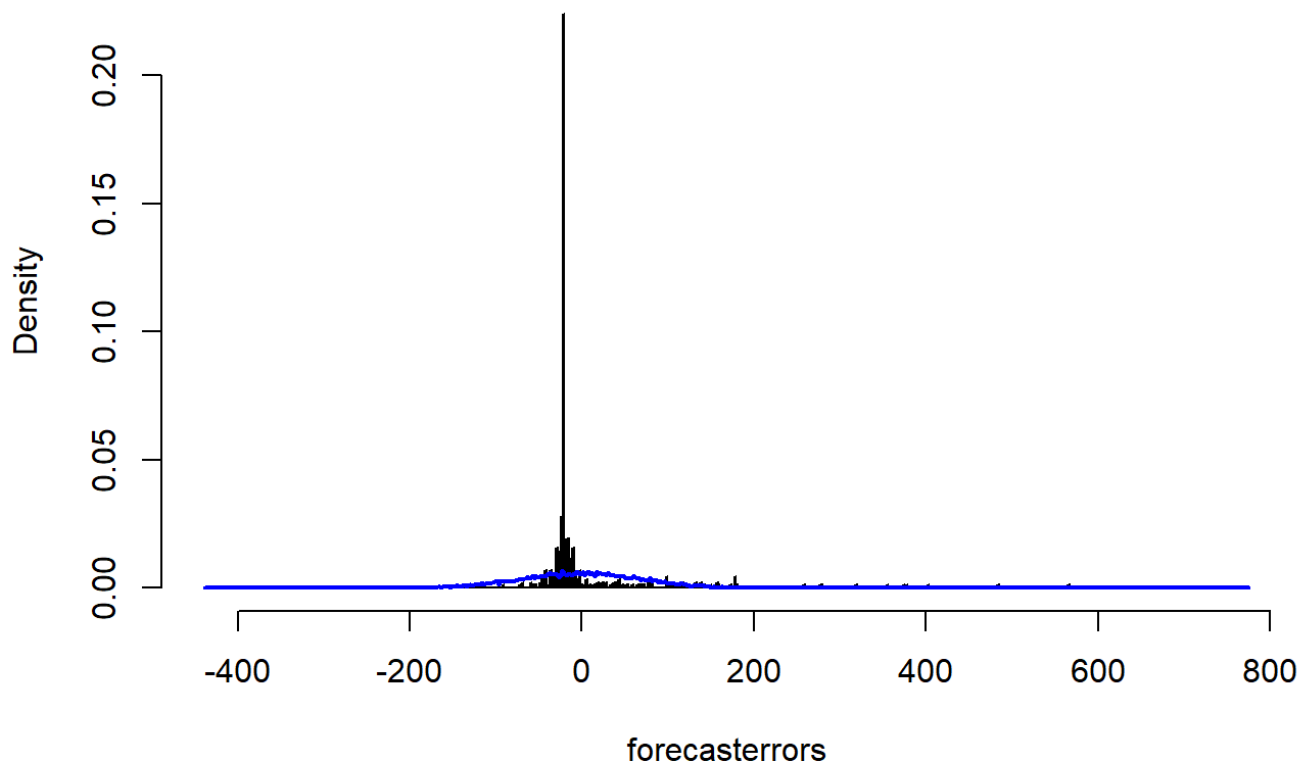
```
Box.test(volcanodustseriesforecasts$residuals, lag=20, type="Ljung-Box")
```

```
##  
## Box-Ljung test  
##  
## data: volcanodustseriesforecasts$residuals  
## X-squared = 24.364, df = 20, p-value = 0.2268
```

Correlogram shows that the sample autocorrelation at lag 20 exceeds the significance bounds.

```
plotForecastErrors(volcanodustseriesforecasts$residuals)
```

## Histogram of forecast errors



```
mean(volcanodustseriesforecasts$residuals)
```

```
## [1] -0.2205417
```

Time plot of forecast errors shows that the forecast errors seem to have roughly constant variance over time. However, the time series of forecast errors seems to have a negative mean, rather than a zero mean. We can confirm this by calculating the mean forecast error, which turns out to be about -0.22: