

5 Arithmetic Progression

Q → What is AP?

Ans. → whose common difference is same.

$a \rightarrow$ first term

$n \rightarrow$ number of terms

n^{th} term $\rightarrow a_n$

$d \rightarrow$ common difference

$l \rightarrow$ last term

Sum of n terms $\rightarrow S_n$

* $a_n = a + (n-1)d$

n^{th} term

* $S_n = \frac{n}{2} [2a + (n-1)d]$

Sum of n terms

* $S_n = \frac{n}{2} (a + l)$

$$a_1 = S_1$$

$$a_2 = S_2 - S_1$$

$$a_3 = S_3 - S_2$$

* $a_n = S_n - S_{n-1}$

A.P.:-

$$\begin{array}{ccccccccc} a & a+d & a+2d & a+3d & a+4d & a+5d & & & \\ \uparrow & \uparrow & \uparrow & \uparrow & \uparrow & \uparrow & & & \\ a_1 & a_2 & a_3 & a_4 & a_5 & a_6 & \dots & & \end{array}$$

$$d = a_2 - a_1$$

$$d = a_3 - a_2$$

$$d = a_4 - a_3$$

6th term $\rightarrow a_6$

7th term $\rightarrow a_7$

n^{th} term $\rightarrow a_n$

Sum of 3 terms = S_3

Sum of 5 terms = S_5

Sum of n terms = S_n

odd :-

3 terms

$a-d$, a , $a+d$

5 terms

$a-2d$, $a-d$, a , $a+d$, $a+2d$

7 terms

$a-3d$, $a-2d$, $a-d$, a , $a+d$, $a+2d$, $a+3d$

even :-

4 terms

$$\underbrace{a-3d} \quad \underbrace{a-d} \quad \underbrace{a+d} \quad \underbrace{a+3d}$$

6 terms

$$\underbrace{a-5d} \quad \underbrace{a-3d} \quad \underbrace{a-d} \quad \underbrace{a+d} \quad \underbrace{a+3d} \quad \underbrace{a+5d}$$