

## CSE 310 Assignment #2

(Max. Points: 30)

**Due on: Wednesday, Sep. 20, 2017, 11:59pm Arizona time**

### General Instructions:

- This is an individual assignment, please do not collaborate. If there's programming part, make sure that you write every line of your own code. Using code written by someone else will be considered a violation of the academic integrity and will result in a report sent to the Dean's office.
- For all written exercises: **your answer should be clearly typed or written and must be saved in .pdf or .jpg format. Note: unreadable answer receives no credits!**
- All assignments must be submitted through the link posted on Blackboard, we do NOT accept any hand-in submissions or submissions sent through emails!
- Submission link will be closed automatically once the due date/time is past and **no late assignment will be accepted.**
- You will be allowed 3 times to submit the assignment before the due date/time, but we will only grade your last submission.

### Objectives

- Asymptotic notation.
- InsertionSort, MergeSort, QuickSort, recurrence, etc.
- Be familiar with OpenMP

### Questions

1. [1 pt each, total 3 pts] For each of the following pairs of functions  $f(n)$  and  $g(n)$ , determine only one of  $f(n) = O(g(n))$ ,  $f(n) = \Omega(g(n))$ , or  $f(n) = \Theta(g(n))$ . Note: if  $f(n) = \Theta(g(n))$ , then do not choose  $f(n) = O(g(n))$  or  $f(n) = \Omega(g(n))$ .

1)  $f(n) = 72n^2\sqrt{n} + 87n\sqrt{n} + 3n^3$ ,  $g(n) = 15n^2\sqrt{n} + 3n\sqrt{n}$

2)  $f(n) = 9n^5$ ,  $g(n) = (26n^4 + 4n^3)/3$

3)  $f(n) = \log_4(n^8)$ ,  $g(n) = \log_4(n^5)$

2. [2 pts] Suppose that the running time of an algorithm  $A$  is  $1300n^2$ , and the running time of an algorithm  $B$  is  $50n^4$ . What is the largest value of  $n$  (a positive integer) for which the running time of the algorithm  $A$  is larger than that of  $B$ ?

3. [4 pts] Suppose that  $T(n) = 3$  for  $n = 1$ , and for all  $n \geq 2$ ,  $T(n) = T(n-1) + 2n - 3$ . Solve this recurrence exactly by drawing a ***recursion tree***. (You will need to give an exact explicit solution for  $T$ ).

4. [3 pts each, total 9 pts] Use the master method to give tight asymptotic bounds ( $\theta$  bound) for the following recurrences. (Specify,  $a$ ,  $b$ ,  $f(n)$ , and  $\varepsilon$  value when they apply.)

1)  $T(n) = 16T(n/4) + n$

2)  $T(n) = 8T(n/2) + n^3$

3)  $T(n) = 4T(n/8) + n^2$

5. [4 pts] Illustrate the operation of MAX-HEAPIFY( $A$ , 2) on the array  $A = \{ 15, 5, 2, 26, 11, 13, 8, 6, 9, 12, 3, 7 \}$  by re-drawing the tree for every swap.

1) [3 pts] For the program in the file *parfor.cc* vary the value of the variable  $n$  and the number of threads specified in the `num threads` clause. How are the iterations distributed among threads? Be sure to try out fewer iterations than threads, and more iterations than threads, etc. Write your observation.

3) [2 pts] For the program in the file *reduction.cc* explore the run time of the reduction clause by varying the number of threads in the num threads clause Write your observation.