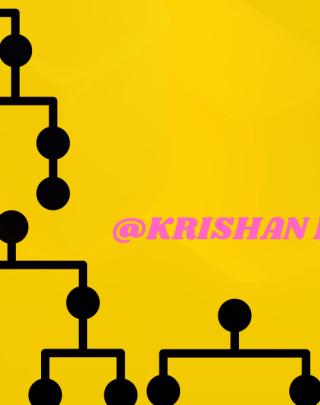


Data Structure & Algorithm

Time Complexity & Space Complexity



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DSA

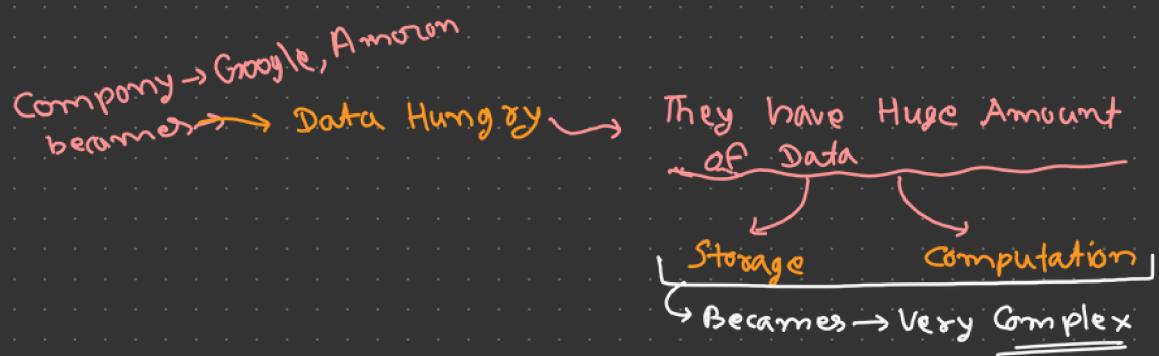
Data structure & Algorithm

Data Structure :- Data Structure is like organizing and storing the data so that we can use it efficiently.

- think of it as a method that helps a computer arrange and manage information, making it easy to work with.
- It's all about structuring data in a way that makes sense for solving problems on the computer.



- ① Storage of the data
- ② Computation of the data



Q Is every data important to collect.?

→ For ex,

I'm Building IRCTC website



[we need to collect data from
customer in many form
like]

- How much the click time.
- No. of features that they have interested in.
- How much the interaction time.
- How much the transaction time.

Apple We need different Data for the different Use case.

Now a Days Company collect all the Data which is related to the customer they actually storing their each single information.

Data Structure

↳ Structuring the Data

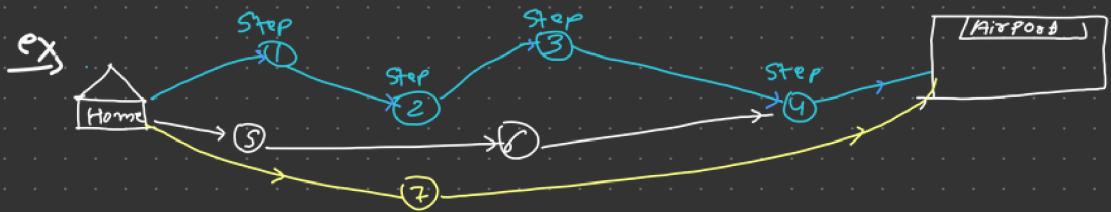
so that

Efficiently

► Storage Data

► Computation Data

Algorithm :- let's suppose i have a problem. then the logical steps that I follow to solve those problems will be called as algorithm.



Prob. → To Reach the airport.

1 problem → There are multiple algorithm or solution to solve that specific Problem.

↳ We Pick the best solution so that → get speed



How do we choose the best algorithm

↳ To choose the best algorithm we deploy a technique called as "Time Complexity". to get the best algorithm

"Time Complexity"

Prob: Can i say A₁ is better than A₂, while

A₁ taking t_1 Second $\{t_1 < t_2\}$

A₂ taking t_2 Second

(A) Yes
(B) No
(C) it Depends

Why Time taken by a algorithm is depends upon

- ① Logic
- ② Programming language
- ③ Operating System that we are using

Note: Just measuring the absolute time is not good enough
only measuring time will not give us the best result.

Means,

Comparing algorithm

Based on execution time

↳ is not only the right way.

► If a algorithm good in python then it also good in C++, Java, HTML

So choose which algorithm is best we apply and go with → Time complexity Technique.

Time Complexity :-

When i choose algorithm it should be independent of operating system/ Programming Langauge /processor.

Algorithm → Logic



Defination

What is time complexity?

Number of operation = input Size



Q. def printName(n):
 print('Hello Mp') } if $n = 0, 1, 2, 3$
 How many time
 print('Hello Mp') execute.

Sol.

n	/ No. of execution
if $n=0$	/ 1
if $n=1$	/ 1
if $n=2$	/ 1

Here, No. of operation is independent of n .

So, the

$$T(1) = O(1) \quad \{ \text{constant} \}$$

Q.2

def printName(n):
 Nested loop { for i in range(n):
 for j in range(n):
 print("Hello world").

Sol. $n=1 \rightarrow$ How many time Hello world $\Rightarrow 1$
 printed

$$\begin{aligned} \text{if } n=2 &\Rightarrow 4 = 2^2 \\ n=3 &\Rightarrow 9 = 3^2 \\ n=4 &\Rightarrow 16 = 4^2 \end{aligned}$$

No. of operation $\propto n^2$

$$\underline{\underline{T(c) = O(n^2)}} \\ \text{time complexity}$$

Q.3 ~~def~~ printName(n):

i=1

while (i < n):

i = i * 2

print ("Hello World")

What is the $T(c)$ = Time complexity

Ans

$T(c) = \text{No. of operation} = \text{input Size}$

to

How many time
Hello world printed.

Note → Here No. of operation < input size

When $i \geq n \Rightarrow$ loop Break

Let's

$n=5$, then No. of operation \rightarrow 1st $\rightarrow i=1$

2nd $\rightarrow i=2 \Rightarrow$ 3 times

3rd $\rightarrow i=4$

$n=10$, then No. of operation \rightarrow

1st $\rightarrow i=1$
2nd $\rightarrow i=2$
3rd $\rightarrow i=4$
4th $\rightarrow i=8$

5th $\rightarrow i=16$ (Not accepted)

```

def printName(n):
    i=1
    while (i < n):
        i = i * 2
        print ("Hello World")

```

| When $i \geq n$ / loop → Exit OR
Break

→ No. of operation & input Size = $T(c)$

↳ No. of operation $\leq n$ (Here)

(How many time while loop will execute)

So $T(c) \neq O(n)$

Right way to finding time complexity

Loop Run

$$1^{\text{st}} \rightarrow i = 1 = 2^0 = 2^{1-1}$$

$$2^{\text{nd}} \rightarrow i = 2 = 2^1 = 2^{2-1}$$

$$3^{\text{rd}} \rightarrow i = 4 = 2^2 = 2^{3-1}$$

$$4^{\text{th}} \rightarrow i = 16 = 2^3 = 2^{4-1}$$

Let Loop Runs for the K times then

$$K = i = 2^{k-1}$$

Next $(K+1)^{\text{th}} = i = 2^K$

And loop Breaks the i values becomes

$$i \geq n$$

When loop Brake ,

$$j \geq n$$

{ i Becomes $\rightarrow 2^k$

$$2^k \geq n$$

$$2^k \approx n$$

what is
12

\rightarrow No. of time loop Run \Rightarrow No. of operation

$$2^k \approx n$$

$$\log_2 2^k \approx \log n$$

$$k = \log n \rightarrow \text{Input size}$$

No. of operation

$$T(c) = O(\log n)$$



Q.4

```
def PrintName(n):
    for i in range(n):
        j = 1
        while (j < n):
            j = j * 2
            print("Hello")
```

What is the $T(c) = ?$

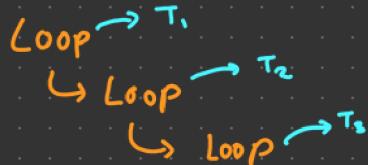
Ans →

```
def PrintName(n):
    T(c) → O(n) ← for i in range(n):
                j = 1
                while (j < n):
                    j = j * 2
                    print("Hello")
```

For this the $T(c) = O(n \log n)$ ✓

Rule

* if we have nested loop like, then time complexity,



$$T(c) = T_1 \times T_2 \times T_3$$

* if we have loop like, then time complexity,

$$\text{Loop 1} \rightarrow T_1$$

$$\text{Loop 2} \rightarrow T_2$$

$$\text{Loop 3} \rightarrow T_3$$



$$T(c) = \text{Max}(T_1, T_2, T_3)$$

Q.5

```

def printName(n):
    for i in range(n):
        for j in range(n):
            print("Hello")
            break
  
```

↳ Break → Break the for loop, as we know their are 2 Loop. 1st loop runs → n times
2nd loop runs → 1 time {Because of Break}

$$\text{So } T(c) = n \times 1$$

$$T(c) = O(n)$$

Q.6

```
def PrintName(n):
    i = s = 1
    while (s < n)
        i += 1
        s += i
    Print ("Hello")
```

Time complexity
⇒ ??

Ans →

```
def PrintName(n):
    i = s = 1
    while (s < n)
        i += 1
        s += i
    Print ("Hello")
```

$T(i) = \text{No. of opera.} \times \text{Input Size}$

\downarrow

No. of time while loops runs

\downarrow

Let $i = 12$ ← finding the relation

\downarrow

n

$$① \quad i=1, \quad s=1$$

$$② \quad i=2, \quad s=1+2$$

$$③ \quad i=3, \quad s=1+2+3$$

$$④ \quad i=4, \quad s=1+2+3+4$$

K times ↓

$$⑤ \quad i=K, \quad s=1+2+3+4+5+\dots+K$$

$$S_K = \frac{K(K+1)}{2}$$

$$S_{K+1} = \frac{(K+1)(K+2)}{2} \rightarrow \text{then loop Break}$$

$$\left\{ \frac{n(n+1)}{2} \right\}$$

$$\therefore S_{k+1} \approx n$$

$$\frac{(k+1)(k+2)}{2} \approx n$$

$$(k+1)(k+2) < n$$

$$k^2 + 2k + k + 2 < n$$

$$k^2 + \underbrace{3k+2}_{\leftarrow \text{Ignore}} < n$$

$$k^2 < n$$

$k < \sqrt{n} \rightarrow \text{Input size}$

No. of
operations

$$T(c) = O(\sqrt{n})$$



Types of time complexity

- ▶ Best case
- ▶ Average case
- ▶ Worst case

Let's understand the best case, Average case and worst case using a small example. ↴

Suppose you have to find Rahul in the class.



Best case → if you find Rahul in first try that will be my Best case.

Worst case → if you find Rahul at the last try that will be our worst case.

When we have dealing with computer
we have to prepare for the
worst case

Because when we prepare for the worst we already
cover for the Best or Average Case.



$T(i)$ \Rightarrow Worst case time complexity.
OR

also called \rightarrow Big O

* Space Complexity *

The extra space that you need to solve the problem respect to the input size.

Ex) I have a list = [1, 2, 3, 4, 5], Please reverse list?

Ans) list = [1, 2, 3, $\xleftarrow{9}$, 4, 5]

New list = [5, 4, 3, 2, 1]

for reversing I am take new list that it the extra space that I used to solving the problem statement.

Now more people aware about time complexity not for the space complexity.

In any algorithm
if we are using space to solving problem

that will be in Space complexity problem.

↓
Called → Constant Space complexity
OR

Inplace algorithm

These types of algorithm is really good algorithm.