

Pre class Assignment - 24

01. $f(x) = x^3 - 3x^2 - x + 3$ for $x \geq 0$.

$$f'(x) = 3x^2 - 6x - 1$$

for gradient descent part.

Starting at $x=0$.

$$\begin{aligned} 1 > x_1 &= x_0 - \gamma f'(x_0) \\ 2 > x_2 &= x_1 - \gamma f'(x_1) \\ 3 > x_3 &= x_2 - \gamma f'(x_2) \end{aligned}$$

Now lets fail the approximation by using $\gamma=5$

$$x_4 = x_3 - 5 f'(x_3)$$

$$x_5 = x_4 - 5 f'(x_4)$$

$$x_6 = x_5 - 5 \cdot f'(x_5)$$

$x_3 \cong$ value after 3 rounds of GD.

Q2. $f(x) = x^4 - x^3 - x^2 + 1$

at $x = -1$

$\gamma = 1/100.$

- 1) after several iterations observe the value of x to which it seems to be getting closer.
- 2) for the graph, we can use online plotting tools or software to visualize the function $f(x)$ on the interval $(-1, 2)$.
- 3) If there is an issue on the first part such as not converging to an unexpected value, it could be due to variety of reasons including poor choice of learning rate.