

A Project Report

submitted by

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THESIS CERTIFICATE

This is to certify that the thesis entitled , submitted by **D Akshay Rangasai**, to the Indian Institute of Technology, Madras, for the award of the degree of **Master of Technology**, is a bona fide record of the research work carried out by him under my supervision. The contents of this thesis, in full or in parts, have not been submitted to any other Institute or University for the award of any degree or diploma.

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I want to thank myself for this completely pointless endeavour and my parents for paining me constantly about this. This is in the end, quite depressing.

ABSTRACT

Most materials have two regimes of operation when it comes to the relationship between stress and strain of the material, namely linear and non-linear. While phenomenon and material characterization in the linear regime of operation is pretty well understood, the non-linear regime is not as well understood. This is an intriguing part of the problem as materials that undergo plastic deformation and fatigue loading operate under this non-linear regime, and characterization of these properties help in various manufacturing processes.

This study aims to statistically model and extract relevant parameters to measure non-linearity and its effects on a material by the use of ultrasonic waves, which provide a high strain rate, but very low strain, which is ideal to test the material without changing any of its properties at the current state. We first characterize parameters through harmonics generation and then proceed to non-linear wave mixing, a technique which gives us spatial specificity in our measurements.

The forward model was first built by creating a Finite Difference Time Domain (FDTD) solution to a set of differential equations that represent two dimensional non-linear wave propagation in an isotropic solid medium in a euclidean coordinate system. Wave mixing was simulated using a transverse and a longitudinal wave mixing in collinear path, with a phased array simulated as the transducer. Sensitivity analysis was performed for this solution and this formed the basis of our inverse model that helped predict material parameters.

The inverse model for the forward model was first built using linear regression and the results were compared with a statistical learning technique. We used Gaussian Process modelling to model the predictive model, which we further used to build the inverse model. To evaluate the model, noise was added to the measurements at various Signal to Noise Ratio (SNR) and the error percentage was measured. This model proved to be sufficient for the inverse model. From this, we could effectively estimate model parameters from wave mixing measurements.

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CHAPTER 1

Introduction

The subject of the present work deals with the propagation, non-linear mixing effects of high-frequency shear and longitudinal waves which help us characterize material properties. This section is a brief introduction containing the background, outline and applications of the presented work.

1.1 Background

The stress-strain curve for most ductile materials starts in a linear relationship and moves into a non-linear relationship with a few invariants that define the said relationship. Determining these constants is of great use to characterize the material and predict its behaviour under various conditions and also optimize processes with respect to these constants. While the physical relationship between the linear constants and their estimation has been studied to a great extent, the non-linear constants are more difficult to estimate. Our work aims to estimate these non-linear constants through statistical estimation techniques.

1.1.1 The stress-strain curve

The significant points from fig 1.1.1 are as follows:

1. A - Proportional Limit
2. B - Elastic Limit
3. y - Yield Point
4. u - Ultimate Tensile Strength
5. f - Fracture point

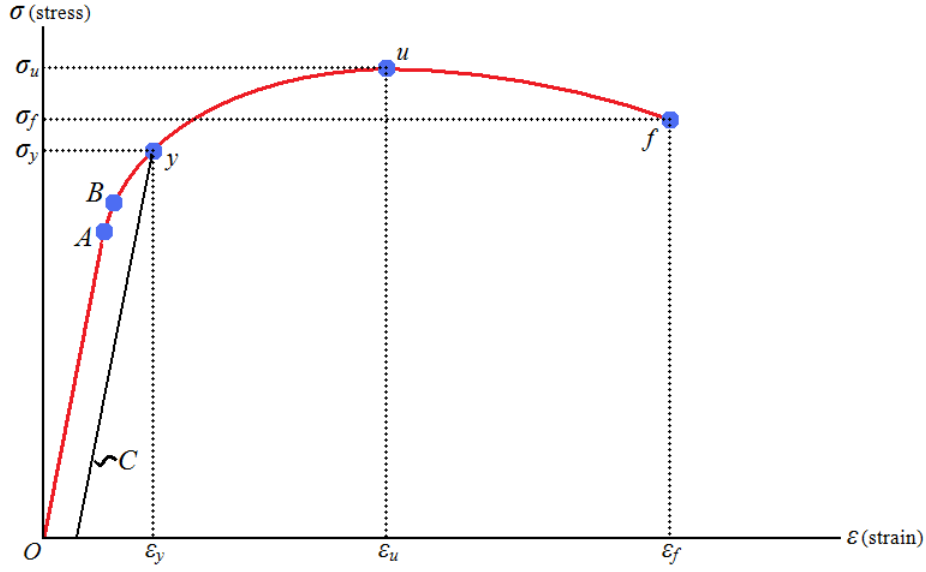


Figure 1.1: The Stress Strain Curve for a Ductile Material

1.1.2 Non-Destructive Testing

There are multiple methods of figuring out the elastic constants of a material, most significant of them being destructive methods, where the material is stressed to its Ultimate Tensile Strength and then, a curve is fit to get the second order constants of the material. This results in the material specimen being destroyed and deemed useless. This method is good for laboratory conditions, but not in a real-world scenario.

To account for this, we employ a method of Non-Destructive testing using ultrasonics. Ultrasonic waves have the characteristic of extremely high strain rates, but the magnitude of strain itself is minimal, and the changes to material properties are thus negligible. These high strain rates result in interesting phenomenon occurring, which in turn helps us estimate parameters of the material, without any physical damage to the specimen.

1.1.3 Wave Propagation and Mixing

One of the main concepts that are used in this study are that of wave propagation in solid media and mixing of waves in linear and non-linear zones. To solve the differential equations involved, we use FDTD simulations. We employed multiple solvers to evaluate the equations and multiple approaches to solve the problem. This will be discussed in detail in upcoming chapters.

1.1.4 Statistical Inversion and Learning

The forward model is inverted by using purely statistical techniques. We employ various techniques from Support Vector Machines (SVM), Gaussian Mixture Models (GMMs), and Gaussian Processes. The mathematics and results will be discussed in detail in the coming chapters.

1.2 Outline of the Report

This report is organized into 6 chapters.

1. The current chapter gives a basic introduction to the project and explains very briefly what we hope to achieve and techniques we've employed with a little bit of background information.
2. Chapter 2 deals with Literature Review and what we worked on and the subsequent results of the same with reasons as to what method we finally adopted and why with a discussion about the same.
3. Chapter 3 describes the construction of the FDTD model for the forward problem and the collinear wave mixing approach that is taken by us and describes the problem and solution in detail.
4. Chapter 4 explores the sensitivity analysis of our constructed forward model with respect to various parameters of interest and and exploratory analysis of the inverse model.
5. Chapter 5 validates the inverse model and also describes the pitfalls of the model. We make the model more real world friendly and check its performance.
6. Chapter 6 summarizes our work and has a section on how this project can be pursued along with suggestions for experimental validation.

1.3 Applications of present work

The present work has wide range of uses from aircraft industry to the shipping industry. A manufacturing specific application of this current technique will be in the estimation of material parameters in forming process and cold working processes where materials undergo plastic deformation.

This technique will help us understand material deformation better and give us a physical insight into what the constants mean and at the same time help improve existing processes and diagnose issues in current processes.

CHAPTER 2

Future Work

CHAPTER 3

Appendix

3.1 Solver Code

```
1 import numpy as np
2 import scipy as sp
3 import defaults as df
4 from math import sin, pi, cos
5 from matplotlib.pyplot import imshow, plot, show, draw, pause, clim,
    ↪ figure
6 import sys
7 from constants import *
8 #from matplotlib import figure
9 class Solver:
10
11     Simulation = None
12     Location = None
13     Width = None
14     #Create a Movie Variable to calculate number of movies and plots
    ↪ , to bring them up when necessary. add arguments to put it
    ↪ in grid, instead of what's happening here. This is
    ↪ hardcoded waste.
15     def putMovie(self, pauseTime):
16         data = np.reshape(self.Simulation.Grid[:, :, 0, 1], (self.
            ↪ Simulation.ElementSpan[0], self.Simulation.ElementSpan
            ↪ [1])) # #
17         figure("Wave_Movie_Transverse")
18         imshow(data)
19         clim([-1e-8, 1e-8])
```

```

20     draw ()
21     pause (pauseTime)
22
23     data = np.reshape ( self . Simulation . Grid [:, :, 1, 1], ( self .
        ↪ Simulation . ElementSpan [0], self . Simulation . ElementSpan
        ↪ [1]))          #          #
24     figure ("Wave_Movie_Longitudinal")
25     imshow ( data )
26     clim ([-1e-8, 1e-8])
27     draw ()
28     pause (pauseTime)
29
30
31
32     def putSource (self , i , frequency , index , waveType = 0):
33         #Multiply with gaussian to remove edge effects .
34
35         #Adding default Source
36
37         #waveType 0 – Transverse . 1 – Longitudinal
38
39         X_S = round (self . Location [0])
40         Y_S = slice (round (self . Simulation . ElementSpan [0]/2) – round (
        ↪ self . Width [1]/2) , round (self . Simulation . ElementSpan
        ↪ [0]/2) + round (self . Width [1]/2))
41
42         #Raised Cosine Pulse .
43
44         self . Simulation . Grid [Y_S, index , waveType , 2] = (1 – cos (2* pi *
        ↪ frequency * i * self . Simulation . Dt / self . Simulation . Pulses))
        ↪ * cos (2* pi * frequency * i * self . Simulation . Dt) * 1e-8
45
46         #Sine Pulse . Trying to recreate the paper

```

```

47         #self.Simulation.Grid[Y_S, index, waveType, 2] = sin(2*pi*
           ↪ frequency*i*self.Simulation.Dt)*1e-8
48
49         #print self.Simulation.Grid[X_S, round(self.Simulation.
           ↪ ElementSpan[1]/2) - round(self.Width[0]/2) + 1, 0, 2]
50
51         #Line Sources only, currently. Multiple Sources must be
           ↪ accounted for, Must think of a matrix solution. So much
           ↪ fight for something that might not even work. Pain.
52     def setSource(self, Location = None, Width = None, Theta = None)
           ↪ :
53
54         if Location is None:
55             self.Location = [df.LOCATION*self.Simulation.Dimensions
                               ↪ [0]/self.Simulation.Dx]
56         else:
57             self.Location.append(Location*self.Simulation.Dimensions
                                   ↪ [0]/self.Simulation.Dx)
58
59         if Width is None:
60             self.Width = [(df.WIDTH/self.Simulation.Dx)*D for D in
                             ↪ self.Simulation.Dimensions]
61         else:
62             self.Width.append((Width/self.Simulation.Dx)*D for D in
                                ↪ self.Simulation.Dimensions)
63
64         if Theta is None:
65             self.Location = [df.THETA]
66         else:
67             self.Location.append(Theta)
68
69
70

```

```

71     def Solve(self):
72         #First Equation We'll be solving will be the standard wave
73             ↪ equation.
74         self.setSource()
75         #Setting the Source first. Now, let's solve the DE like a
76             ↪ boss
77
78         _X = slice(0,self.Simulation.ElementSpan[0]-2)
79         X = slice(1,self.Simulation.ElementSpan[0]-1)
80         X_ = slice(2,self.Simulation.ElementSpan[0])
81
82         _Y = slice(0,self.Simulation.ElementSpan[1]-2)
83         Y = slice(1,self.Simulation.ElementSpan[1]-1)
84         Y_ = slice(2,self.Simulation.ElementSpan[1])
85
86         #_X indicates previous X coordinate and X_ indicts the one
87             ↪ after
88         r_var = round(self.Simulation.Time/self.Simulation.Dt)
89         #print "Total Iterations are " , r_var
90         c_t2 = pow(self.Simulation.MaterialProperties.WaveVelocityT
91             ↪ ,2)
92         c_l2 = pow(self.Simulation.MaterialProperties.WaveVelocityL
93             ↪ ,2)
94
95         # sdata = sp.zeros((r_var,1))
96         for i in range(1,int(r_var)):
97             dv_y = (self.Simulation.Grid[X,Y_,1,1] - self.Simulation
98                 ↪ .Grid[X,_Y,1,1])/(2*self.Simulation.Dx)
99             d2v_y = (self.Simulation.Grid[X,Y_,1,1] - 2*self.
100                 ↪ Simulation.Grid[X,Y,1,1] + self.Simulation.Grid[X,
101                 ↪ _Y,1,1])/pow(self.Simulation.Dx,2)
102             du_y = (self.Simulation.Grid[X,Y_,0,1] - self.Simulation
103                 ↪ .Grid[X,_Y,0,1])/(2*self.Simulation.Dx)

```

```

95         d2u_y = (self.Simulation.Grid[X,Y_,0,1] - 2*self.
           ↪ Simulation.Grid[X,Y,0,1] + self.Simulation.Grid[X,
           ↪ _Y,0,1])/pow(self.Simulation.Dx,2)
96
97         #Solving for Displacements in the X directio
98
99         self.Simulation.Grid[X,Y,0,2] = 2*self.Simulation.Grid[X
           ↪ ,Y,0,1] - self.Simulation.Grid[X,Y,0,0] + pow(self.
           ↪ Simulation.Dt,2)*(c_t2*d2u_y + self.Simulation.
           ↪ MaterialProperties.BetaT*c_t2*(dv_y*d2u_y + du_y*
           ↪ d2v_y))
100        self.Simulation.Grid[X,Y,1,2] = 2*self.Simulation.Grid[X
           ↪ ,Y,1,1] - self.Simulation.Grid[X,Y,1,0] + pow(self.
           ↪ Simulation.Dt,2)*(c_l2*d2v_y + self.Simulation.
           ↪ MaterialProperties.BetaL*c_l2*dv_y*d2v_y + self.
           ↪ Simulation.MaterialProperties.BetaT*c_t2*du_y*d2u_y
           ↪ )
101
102
103
104        self.Simulation.SourceSignal[i,0] = sum(self.Simulation.
           ↪ Grid[:, -2,0,2])/self.Simulation.Grid.shape[1]
105
106
107        self.Simulation.SData[i,0] = sum(self.Simulation.Grid
           ↪[:, 1,1,2])/self.Simulation.Grid.shape[1]
108
109        #self.Simulation.SData[i,0] = sum(self.Simulation.Grid
           ↪[:, 1,0,2])/self.Simulation.Grid.shape[1]
110
111        #print self.Simulation.Grid[15,15,0,2]
112
113        #Boundary COnditions. Making the ends soft reflections.

```



```

114         ↪ Let's see how that works out.
115     '''
116     if self.Simulation.Mixing is not True:
117         self.Simulation.Grid[-1,:,0,2] = self.Simulation.
118             ↪ Grid[-2,:,0,2]
119     else:
120         # self.Simulation.Grid[:,0,1,2] = self.Simulation.
121             ↪ Grid[:,1,1,2]
122         # self.Simulation.Grid[:,0,0,2] = self.Simulation.
123             ↪ Grid[:,1,0,2]
124         self.Simulation.Grid[:, -1,0,2] = self.Simulation.
125             ↪ Grid[:, -2,0,2]
126         # self.Simulation.Grid[:, -2,1,2] = self.Simulation.
127             ↪ Grid[:, -1,1,2]
128
129         #Updates go Here
130     '''
131
132     if (i <= round(self.Simulation.Pulses*(1.0/(self.
133         ↪ Simulation.WaveProperties.Frequency)))/self.
134         ↪ Simulation.Dt)):
135         self.putSource(i, self.Simulation.WaveProperties.
136             ↪ Frequency, 0, TRANSVERSE)
137     else:
138         self.Simulation.Grid[:,1,0,2] = self.Simulation.Grid
139             ↪[:,0,0,2]
140         self.Simulation.Grid[:, -2,0,2] = self.Simulation.
141             ↪ Grid[:, -1,0,2]
142         #self.Simulation.Grid[:,0,1,2] = self.Simulation.
143             ↪ Grid[:,1,1,2]
144
145

```

```

135
136     if self.Simulation.Mixing == True:
137
138         if (i <= round(self.Simulation.Pulses*(1.0/(0.997*4*
        ↪ self.Simulation.WaveProperties.Frequency)) / self
        ↪ .Simulation.Dt)):
139             self.putSource(i,0.997*4*self.Simulation.
        ↪ WaveProperties.Frequency,-1,LONGITUDINAL)
140         else:
141             self.Simulation.Grid[:, -1, 1, 2] = self.Simulation
        ↪ .Grid[:, -2, 1, 2]
142             self.Simulation.Grid[:, 0, 1, 2] = self.Simulation.
        ↪ Grid[:, 1, 1, 2]
143             #self.Simulation.Grid[:, -1, 0, 2] = self.
        ↪ Simulation.Grid[:, -2, 0, 2]
144
145     self.Simulation.Grid[:, :, 1, 0] = self.Simulation.Grid
        ↪[:, :, 1, 1]
146     self.Simulation.Grid[:, :, 1, 1] = self.Simulation.Grid
        ↪[:, :, 1, 2]
147
148     self.Simulation.Grid[:, :, 0, 0] = self.Simulation.Grid
        ↪[:, :, 0, 1]
149     self.Simulation.Grid[:, :, 0, 1] = self.Simulation.Grid
        ↪[:, :, 0, 2]
150     #
        print i
151     if i%round(0.05*r_var) == 0:
152         #print i
153         if self.Simulation.ViewMovie == True:
154             self.putMovie(0.01)
155             sys.stdout.write('=='*int(round(i/round(0.1*r_var))))
        ↪ )
156

```

```

157         #p.plot.show()
158         #print self.Simulation.MaterialProperties.BetaL, self.
            ↳ Simulation.MaterialProperties.BetaT, self.Simulation.
            ↳ MaterialProperties.WaveVelocityL, self.Simulation.Dt
159
160     '''
161         figure("Source Signal")
162         plot(self.Simulation.SourceSignal)
163
164         pause(0.01)
165         figure("Non Linear Signal")
166         plot(self.Simulation.SData)
167         show()
168     '''
169
170     #         np.save("TotalSignal",self.Simulation.SourceSignal)
171     #         np.save("LinSignal",sdata)
172     def __init__(self, Simulation = None):
173         if Simulation is None:
174             raise ValueError("Simulation_Cannot_be_None._Please_
            ↳ Initialize_a_New_Simulation_to_proceed")
175         else:
176             self.Simulation = Simulation
177             self.Solve()
178
179     if __name__ == "__main__":
180         raise Exception("Cannot_run_file_as_a_standalone_file._Please_
            ↳ run_through_proper_initialized_channels")

```

3.2 Problem Formulation code Code

```
1 from data import waveProperties , materialProperties
2 import numpy as np
3 import scipy as sp
4 import matplotlib as mp
5 import defaults as df
6 import sys
7 from solver import Solver as sl
8 import scipy.io as sio
9 from matplotlib.pyplot import plot , figure
10
11
12 #
    ↪ #####
    ↪
13 #Rules of code: Class elements always begin with a capital letter.
    ↪ Defaults are always allcaps. Arguments to functions to mimic
    ↪ class members.
14 #
    ↪ #####
    ↪
15
16 class simulation:
17
18     def save(self , filename):
19         sio.savemat(filename , {"SData": self.SData , "SourceSignal":
            ↪ self.SourceSignal })
20
21     def setMixing(self , val):
22         self.Mixing = val
23
24     def setStep(self , Dx):
```

```

25         #Courant Condition check
26         return (Dx/self.MaterialProperties.WaveVelocityL)/2
27
28     def setMesh(self):
29
30         if self.Mesh == 0:
31             return (float)(self.WaveProperties.WaveLength/8.0)
32         elif self.Mesh == 1:
33             return (float)(self.WaveProperties.WaveLength/12.0)
34         elif self.Mesh == 2:
35             return (float)(self.WaveProperties.WaveLength/64.0)
36         elif self.Mesh == 3:
37             return (float)(self.WaveProperties.WaveLength/128.0)
38
39         #Time is of type float; Dimensions is a list of floats.
40
41
42     def setParam(self, paramName, value):
43
44         if paramName == 'l':
45             self.MaterialProperties.l = value
46             #self.MaterialProperties.BetaT = (self.
47                 ↪ MaterialProperties.Lambda + 2*self.
48                 ↪ MaterialProperties.Mu)/self.MaterialProperties.Mu +
49                 ↪ self.MaterialProperties.m/self.MaterialProperties.
50                 ↪ Mu
51
52             self.MaterialProperties.refreshParams()
53         if paramName == 'm':
54             self.MaterialProperties.m = value
55             self.MaterialProperties.refreshParams()
56
57         if paramName == 'BetaT':
58             self.MaterialProperties.BetaT = value

```

```

54
55     def getParam(self , paramName):
56
57         if paramName == 'l':
58             return self.MaterialProperties.l
59         if paramName == 'm':
60             return self.MaterialProperties.m
61         if paramName == 'BetaT':
62             return self.MaterialProperties.BetaT
63
64         return 0
65
66
67     def __init__(self , MaterialProperties = None, WaveProperties =
        ↪ None, Reflections = None, Dimensions = None, WaveGuide =
        ↪ None, Mesh = None, Pulses = None):
68
69         if MaterialProperties is None:
70             self.MaterialProperties = materialProperties()
71         else:
72             self.MaterialProperties = MaterialProperties
73
74         if WaveProperties is None:
75             self.WaveProperties = waveProperties()
76         else:
77             self.WaveProperties = WaveProperties
78
79         if Reflections is None:
80             self.Reflections = df.REFLECTIONS
81         else:
82             self.Reflections = Reflections
83
84         if Dimensions is None:

```

```

85         self.Dimensions = df.DIMENSIONS
86     else:
87         self.Dimensions = Dimensions
88
89     if WaveGuide is None:
90         self.WaveGuide = df.WAVEGUIDE
91     else:
92         self.WaveGuide = WaveGuide
93
94     if Mesh is None:
95         self.Mesh = df.MESH
96     else:
97         self.Mesh = Mesh
98
99     if Pulses is None:
100         self.Pulses = df.PULSES
101     else:
102         self.Pulses = Pulses
103
104     self.Time = 2*self.Reflections*self.Dimensions[1]/self.
        ↳ MaterialProperties.WaveVelocityL
105
106     #1D, 2D or 3D
107     self.DimensionCount = len(self.Dimensions)
108     ##         self.WaveProperties.WaveVelocity = self.MaterialProperties
        ↳ .WaveVelocity
109     self.WaveProperties.WaveLength = (float) (self.
        ↳ MaterialProperties.WaveVelocityL/self.WaveProperties.
        ↳ Frequency)
110     self.Mixing = False
111     self.Dx = self.setMesh()
112     self.Dt = self.setStep(self.Dx)
113

```

```

114         #print self.Dx
115         ##List of elementsb
116         self.ElementSpan = [round(X/self.Dx) for X in self.
            ↪ Dimensions]
117
118         #Append Dimensions
119         self.ElementSpan.append(3)
120         #Append Times
121         self.ElementSpan.append(3)
122
123         self.Grid = sp.zeros(tuple(self.ElementSpan), float)
124         self.NLGrid = sp.zeros(tuple(self.ElementSpan), float)
125         self.SourceSignal = sp.zeros((round(self.Time/self.Dt),1))
126         self.SData = sp.zeros((round(self.Time/self.Dt),1))
127         self.ViewMovie = False
128         self.viewPlot = True
129
130 def __init__():
131     args = sys.argv
132     args = [arg.replace('—',' ') for arg in args]
133     names = []
134     sim = simulation()
135     print sim.Dt
136     if 'mixing' in args:
137         sim.setMixing(True)
138     if 'movie' in args:
139         sim.ViewMovie = True
140     solution = sl(sim)
141
142     if 'noplot' in args:
143         pass
144     else:
145         figure(5)

```



```

146         plot(sim.SData)
147
148     if 'save' in args:
149         try:
150             ind = args.index('savenames')
151             names.append(args[ind+1])
152             names.append(args[ind+2])
153         except:
154             print "Using Default File names to save data"
155             names.append("TotalSignal")
156             names.append("NLinSignal")
157             sio.savemat(names[0],{names[0]:sim.SourceSignal})
158             sio.savemat(names[1],{names[1]:sim.SData})
159
160
161
162 if __name__ == "__main__":
163     __init__()

```

```

1  import defaults as df
2  from math import sqrt
3
4
5  ## These classes are created to create a default set of elements. I
   ↪ will implement a file reader to get element data later.
   ↪ createing a new object of this type ensures that we get a nice
   ↪ default simulation. Let's hope this works. Solver is yet to be
   ↪ implemented. Sigh
6
7  class waveProperties:
8      def __init__(self, Frequency = None):
9          if Frequency is None:
10             self.Frequency = df.FREQUENCY
11         else:
12             self.Frequency = Frequency
13
14         self.WaveLength = None
15
16
17  class materialProperties:
18      def __init__(self, Mu = None, K = None, Rho = None, A = None, B
   ↪ = None, C = None, l = None, m = None, Lambda = None):
19
20         ##Initialize All defaults if none.
21
22         if Mu is None:
23             self.Mu = df.MU
24         else:
25             self.Mu = Mu
26
27         if K is None:
28             self.K = df.K

```

```

29         else :
30             self.K = K
31
32         if Rho is None:
33             self.Rho = df.RHO
34         else :
35             self.Rho = Rho
36
37         if A is None:
38             self.A = df.A
39         else :
40             self.A = A
41
42         if B is None:
43             self.B = df.B
44         else :
45             self.B = B
46
47         if C is None:
48             self.C = df.C
49         else :
50             self.C = C
51
52         if l is None:
53             self.l = df.l
54         else :
55             self.l = l
56
57         if m is None:
58             self.m = df.m
59         else :
60             self.m = m
61

```

```

62         if Lambda is None:
63             self.Lambda = df.Lambda
64         else:
65             self.Lambda = Lambda
66
67         self.WaveVelocityL = sqrt((self.Lambda + (2*self.Mu))/self.
        ↪ Rho)
68         self.WaveVelocityT = sqrt(self.Mu/self.Rho)
69         self.BetaL = 3 + 2*(self.l + 2*self.m)/(self.Lambda + 2*self
        ↪ .Mu)
70         self.BetaT = (self.Lambda + 2*self.Mu)/self.Mu + self.m/self
        ↪ .Mu
71
72     def refreshParams(self):
73
74
75         self.WaveVelocityL = sqrt((self.Lambda + (2*self.Mu))/self.
        ↪ Rho)
76         self.WaveVelocityT = sqrt(self.Mu/self.Rho)
77         self.BetaL = 3 + 2*(self.l + 2*self.m)/(self.Lambda + 2*self
        ↪ .Mu)
78         self.BetaT = (self.Lambda + 2*self.Mu)/self.Mu + self.m/self
        ↪ .Mu
79
80
81     class waveGuide:
82
83     def __init__(self, Boundary = None):
84         if Boundary is None:
85             self.Boundary = df.BOUNDARY
86         else:
87             self.Boundary = Boundary
88

```

89 *## Boundary Legend*
90 *## 0 – All reflecting*
91 *## 1 – Sides Reflecting Ends PML*
92 *## 2 – Sides PML Ends Reflecting*
93 *## 3 – Everything PML*

1 LONGITUDINAL = 1

2 TRANSVERSE = 0

```

1 from formulation import simulation
2 from solver import Solver as sl
3
4 #Limit of L and M in terms of percentages. How do we combine this?
   ↪ We need to run experiments, check correlations and all. Let's
   ↪ see if it has any effect:w
5
6 __LIMIT = 10
7 __STEP = 1
8 for percent in range(-int(round(__LIMIT)), int(round(__LIMIT))+1,
   ↪ __STEP):
9     sim = simulation()
10    oldl = sim.getParam('BetaT')
11    print percent/100.0
12    newl = oldl*(1 + (percent/100.0))
13    print oldl, newl
14    sim.setParam('BetaT', newl)
15    sim.setMixing(True)
16    sl(sim)
17    sim.save("%d.mat"%percent)
18
19 '''
20 for percent in range(-int(round(__LIMIT)), int(round(__LIMIT))+1,
   ↪ __STEP):
21     sim = simulation()
22     oldl = sim.getParam('m')
23     print percent/100.0
24     newl = oldl*(1 + (percent/100.0))
25     print oldl, newl
26     sim.setParam('m', newl)
27     sim.setMixing(True)
28     sl(sim)
29     sim.save("Simulation_Save_m-%d-percent.mat"%percent)

```



```

1  import numpy as np
2  import scipy.io as sp
3  from matplotlib import pyplot as plt
4  import os
5
6  __DIR = "../data/sensitivity/tentoten"
7  __TOTALLENGTH = 2048
8  __STARTINDEX = 4900
9  __ENDINDEX = 5600
10 __PADDING = __TOTALLENGTH - (__ENDINDEX - __STARTINDEX)
11 __FILE = "amplitude_BetaT1010.txt"
12 files = [os.path.join(__DIR, f) for f in os.listdir(__DIR)]
13
14 fi = open(__FILE, 'w+')
15
16
17 def fft(signal):
18     fftsignal = np.zeros(__TOTALLENGTH)
19     #fftsignal[0:(__TOTALLENGTH - __PADDING)] = signal[__STARTINDEX:
20         ↪ __ENDINDEX]
21     fftsignal_2 = signal[__STARTINDEX:__ENDINDEX]
22     ftp = abs(np.fft.fft(fftsignal_2))
23     plot = plt.plot(ftp)
24     return plot
25
26 def ampcalc(data):
27     return abs(min(data) - max(data))
28
29 for f in files:
30     print f.split('/')
31     datafile = sp.loadmat(f)
32     fftplot = fft(datafile['SourceSignal'])
33     amplitude = ampcalc(datafile['SourceSignal'])

```

```
33     plt.savefig("%s.png"%f.split('/')[4])
34     plt.close()
35     fi.write('%s_%.25f\n'%(f.split('/')[4], amplitude))
```

```

1 from sklearn.gaussian_process import GaussianProcess as GMM
2 #from sklearn.svm import SVR as GMM
3 import numpy as np
4 import matplotlib.pyplot as plt
5 FILE = 'data/sheet.csv'
6 dataset = np.vstack((set(map(tuple,np.genfromtxt(FILE, delimiter=',')
    ↪ ))))
7
8 def addNoise(snr):
9     signal = dataset[:, -1]
10    print signal
11    signalstd = np.std(signal)
12    noisestd = signalstd/np.sqrt(snr)
13    noise = np.random.normal(0, noisestd, len(signal))
14    datasetnoisy = dataset
15    datasetnoisy[:, -1] = datasetnoisy[:, -1] + noise
16    return datasetnoisy
17
18 def ensemble(value, noise):
19
20    #mixture = GMM(C = 100, epsilon = 1e-20)
21    mixture = GMM()
22    newdataset = addNoise(noise)
23    for ensemble in range(0, value):
24        np.random.shuffle(newdataset)
25        mixture.fit(newdataset[0:-10, 0:-2], newdataset[0:-10, -1])
26        preds = mixture.predict(newdataset[-10:-1, 0:-2])
27        errorabs = abs(dataset[-10:-1, -1] - preds)
28        meanerrorabs = np.mean(errorabs)
29        stderrorabs = np.std(errorabs)
30        print meanerrorabs, stderrorabs
31        #plt.plot(abs(dataset[-10:-1, -1] - preds))
32        #plt.ylim(-5e-12, 5e-12)

```

```
33         #plt.scatter(dataset[-10:-1,0],dataset[-10:-1,-1])
34         #plt.plot(preds)
35         #plt.show()
36 ensemble(5, 10)
```

```

1 FREQUENCY = 2.5e6
2 A = -3.1*(10^11)
3 B = 0
4 C = 0
5 BOUNDARY = 0 #Purely Reflecting
6 DIMENSIONS = [.010 , 0.030] #metres
7 MESH = 2 #0, 1, 2, 3 Coarse, Medium, fine and extrafine mesh 1/8, 1
    ↪ 1/12, 1/64, 1/128
8 MU = 2.68e10
9 Lambda = 5.43e10
10 K = 76e9
11 RHO = 2719
12 TIME = 1.5 #seconds
13 WAVEGUIDE = 1
14 LOCATION = 0.5
15 THETA = 0
16 WIDTH = 0.25
17 PULSES = 10
18 REFLECTIONS = 2
19 l = -38.75e10
20 m = -35.8e10

```

REFERENCES