

	$f_1$	$f_2$	$f_3$	$\dots$	$f_d$	$y$
1						
2						
3						
$\vdots$						
$n = 1000$						

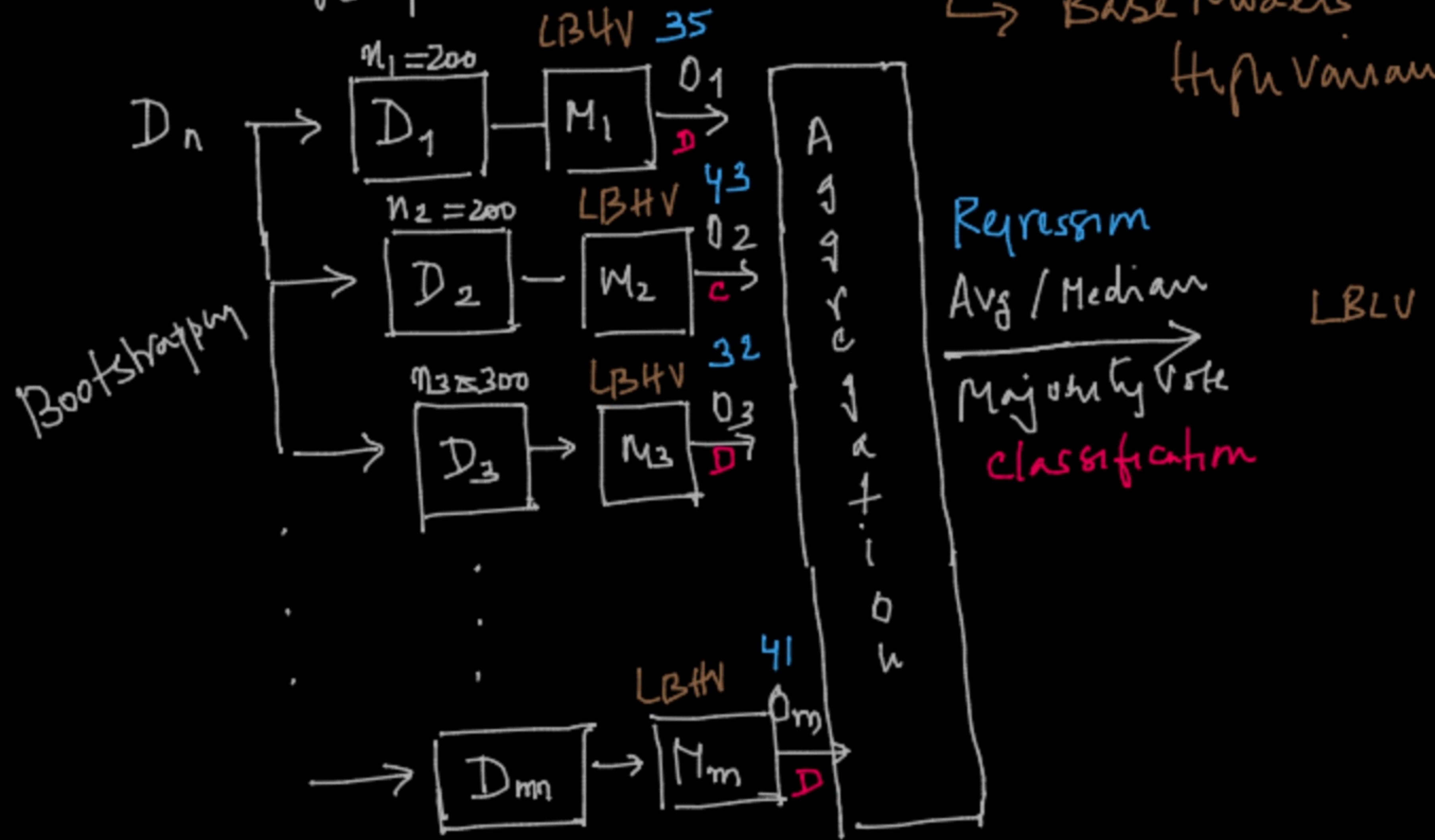
$D_n$

1. Bagging  $\} \rightarrow$  Homogeneous
2. Boosting  $\}$
3. Stacking  $\rightarrow$  Heterogeneous

1. Bagging — Reduces Variance

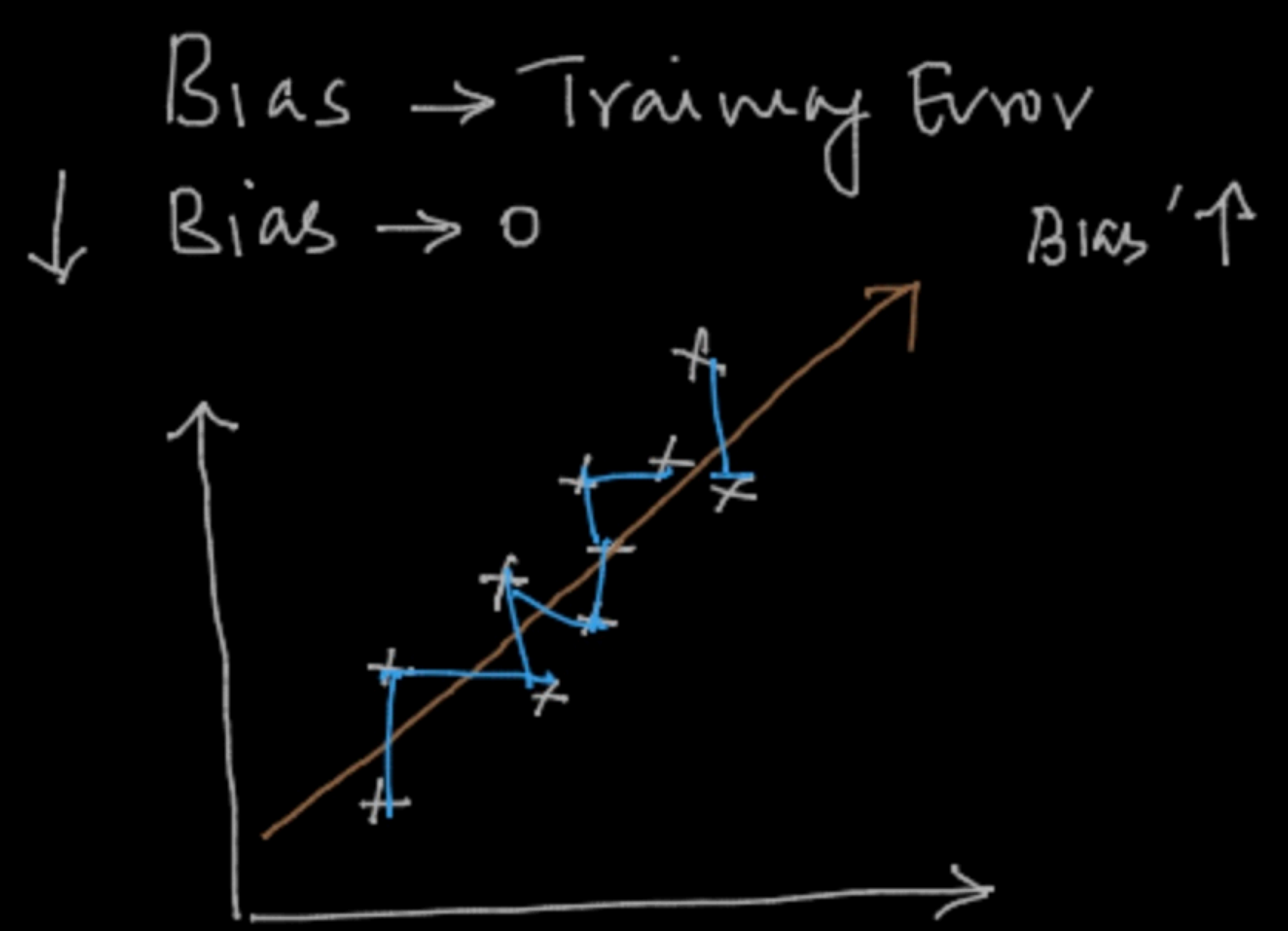
$\hookrightarrow$  Base Models  
 High Variance + Low Bias

Bootstrapping — Sampling with replacement



Bootstrapped Aggregation —  
Bagging  
 Bias & Variance



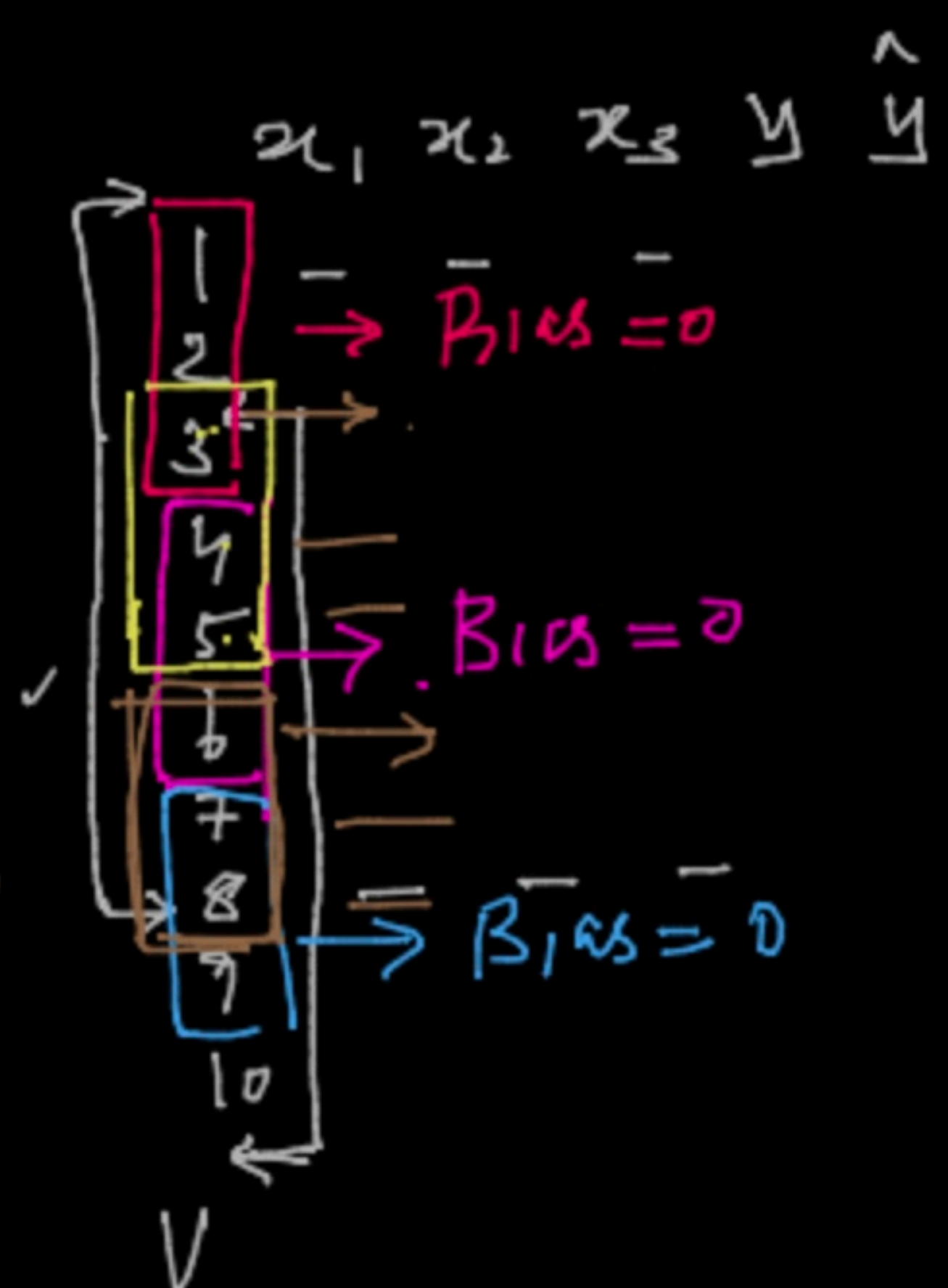


Variance - Testing Error.

$\uparrow$  The model itself changes with small changes in data

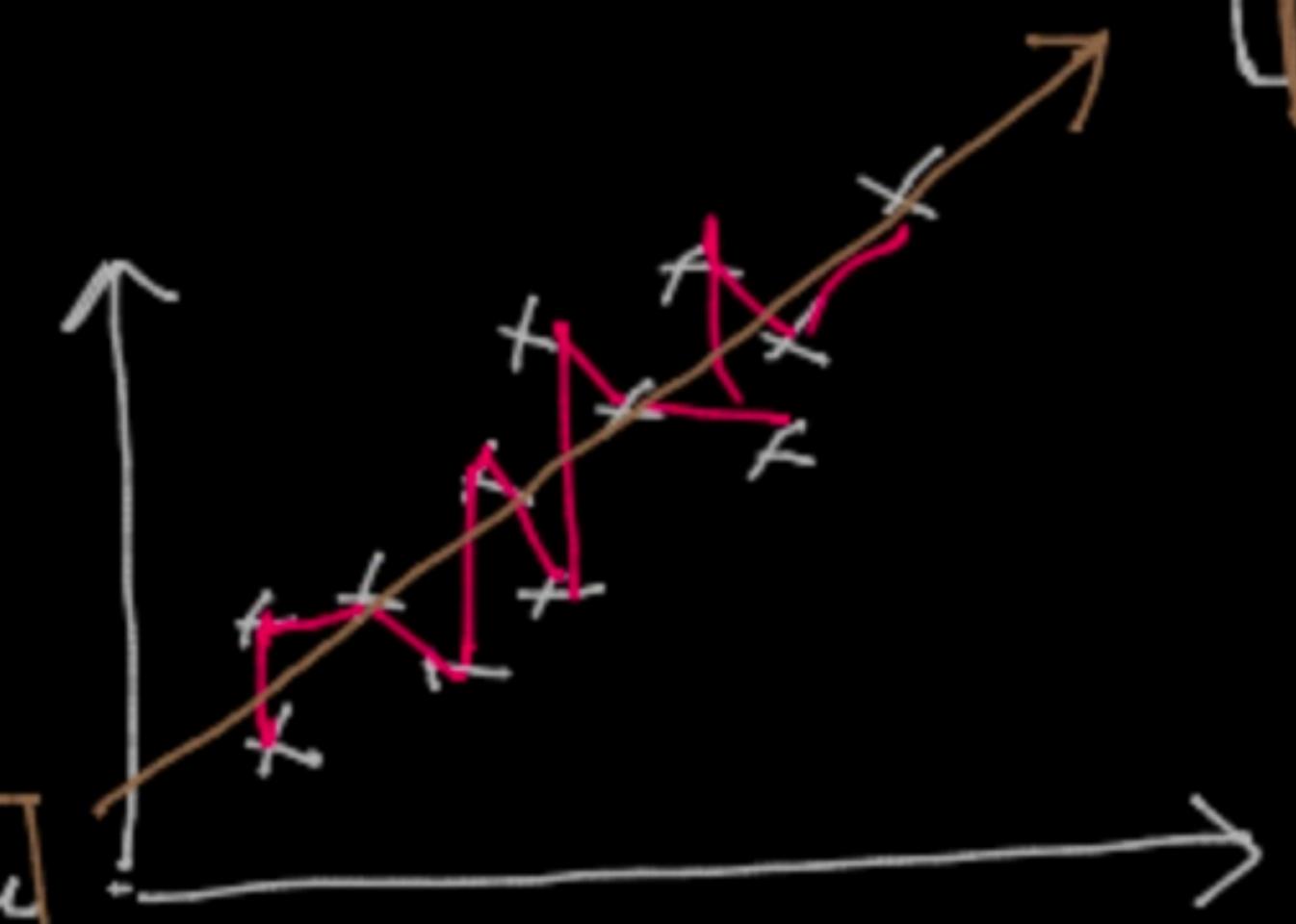
Variance  $\downarrow$

Bias  $\downarrow$ , Low Variance  $\downarrow$



Bagging Reduces Variance  $\rightarrow$  Base Models -

Low Bias & High Variance



Homogeneous Ensembles

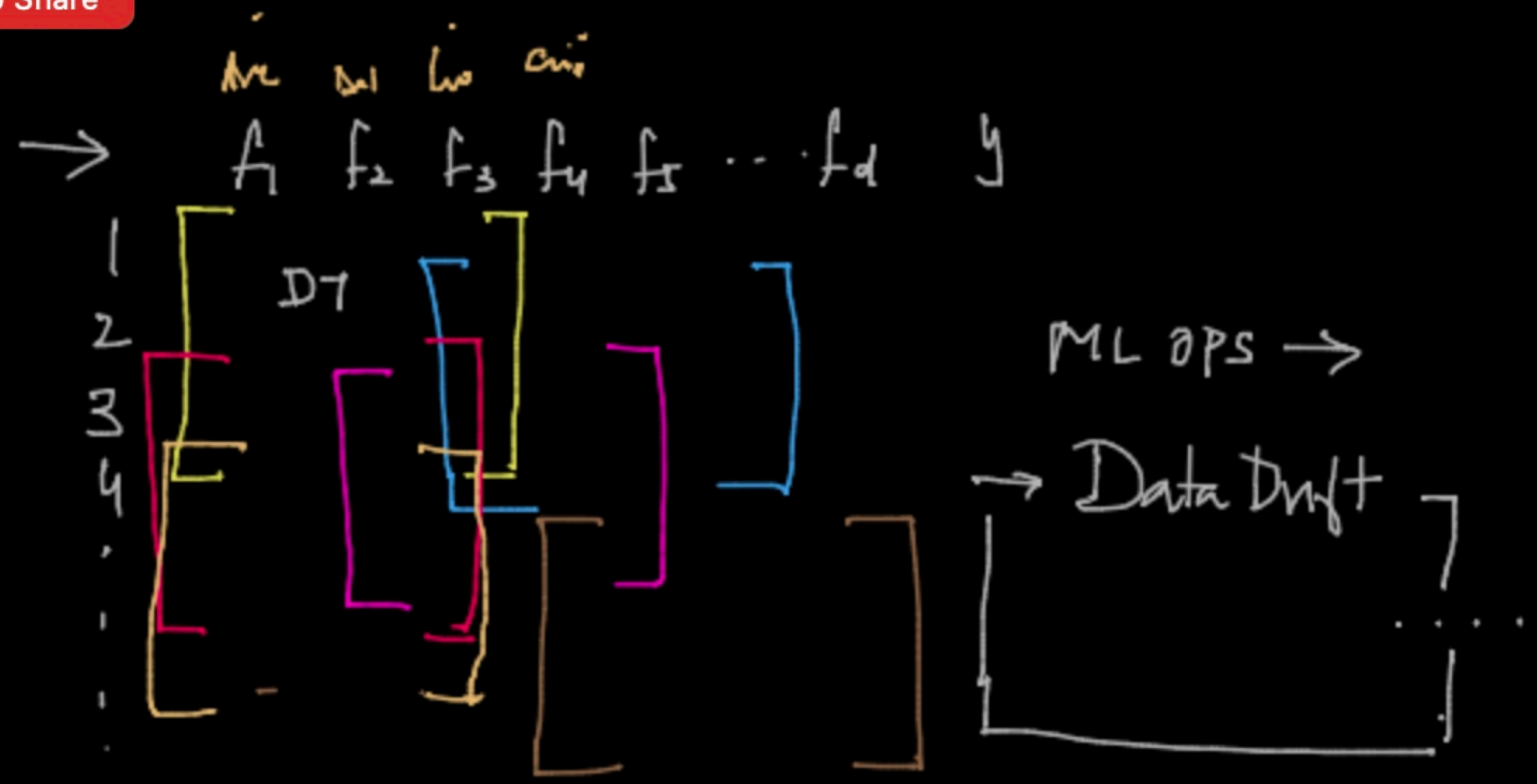
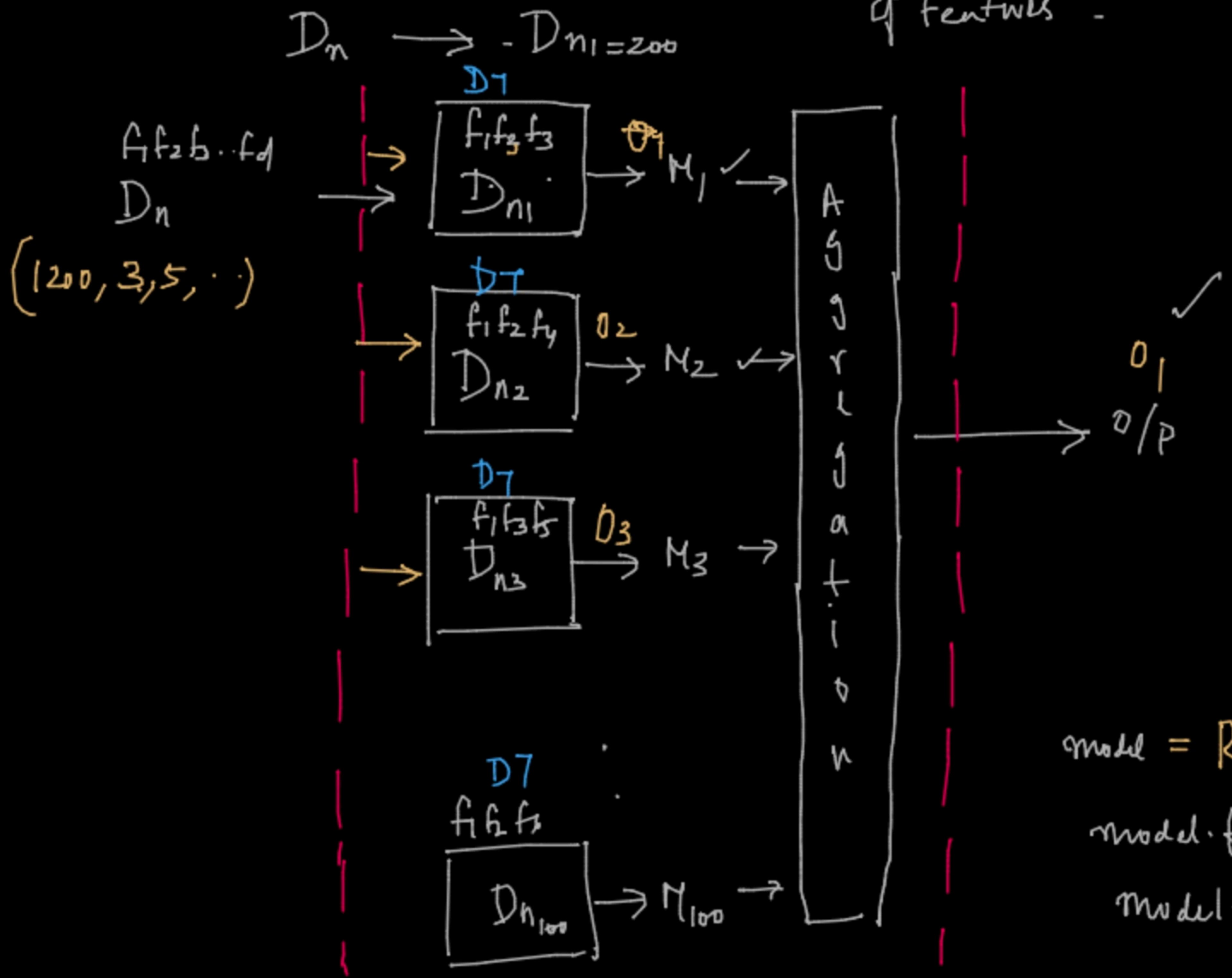
10 ppl  $\rightarrow$  Predicting House price -

- 90%  $\rightarrow$
- 1  $\rightarrow$  BTM
  - 2  $\rightarrow$  Indramay
  - 3  $\rightarrow$  HSR
  - 4  $\rightarrow$  BTM
  - 5  $\rightarrow$  Indramay
  - ...
- 100  
100  
70  
80  
+
- 90%



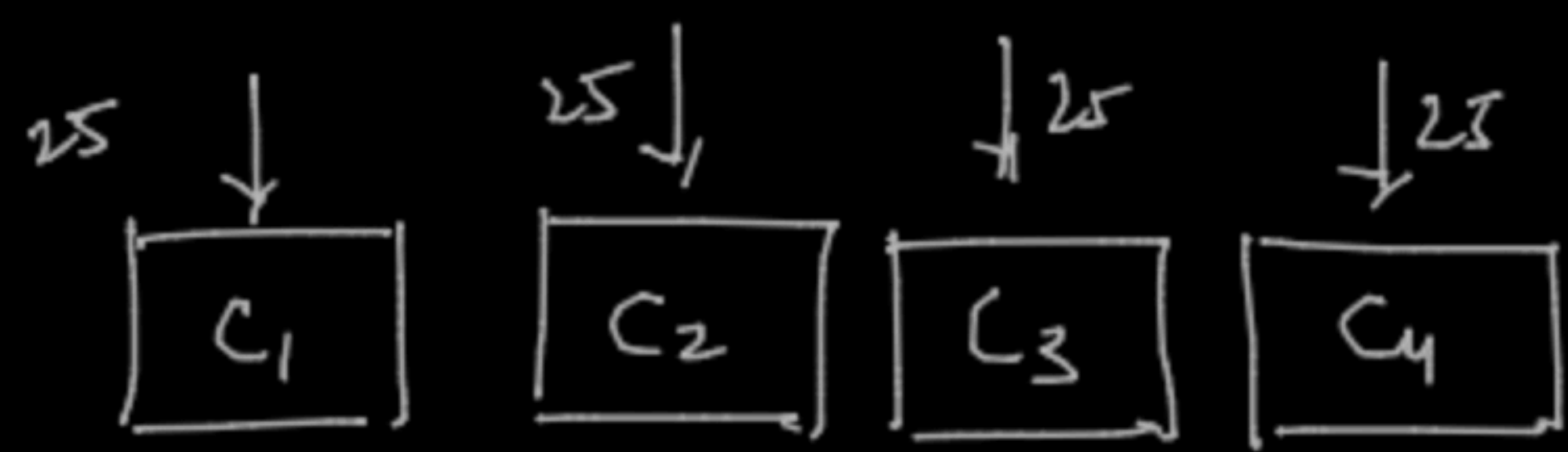
# Random Forest → Bagging Technique

- 1. All Base models are Decision Trees ✓
- 2. Row sampling + Feature Sampling  
↳ only a subset of Features



$n = 80\%$

Parallelize the model.  
→ Quad Core 25%



`model = RandomForest(n_estimators=100)`

`model.fit(X_train)`

`model.predict(X_test)`





\* Only the first model predicts 'y'  
 All subsequent models predict the errors from the previous

# Boosting

- Reduces Bias ✓
- Sequential Model -
- Additive Model

	$f_1$	$f_2$	$f_3$	$y$	$\hat{y}$	$\epsilon_0$
$x_1$	$\leftarrow x_1 \rightarrow$			$y_1$		
$x_2$	$\leftarrow x_2 \rightarrow$			$y_2$		
$x_3$						
$\vdots$						
$x_n$	$\leftarrow x_n \rightarrow$			$y_n$		

Stage '0':

$M_0$

$$D_n \Rightarrow \{x_i, y_i\}_{i=1}^n$$

$$\hat{y} = f_0(x)$$

$$\epsilon_0 = y - \hat{y} = y - f_0(x)$$

Base Models

High Bias & Low Variance

LBLV.

Stage 1:

$M_1$

$$\{x_i, \epsilon_{0i}\}_{i=1}^n$$

$$\hat{\epsilon}_0 = f_1(x)$$

$$\epsilon_1 = \epsilon_0 - \hat{\epsilon}_0 = y - f_0(x) - f_1(x)$$

Stage 2

$M_2$

$$\{x_i, \epsilon_{1i}\}_{i=1}^n$$

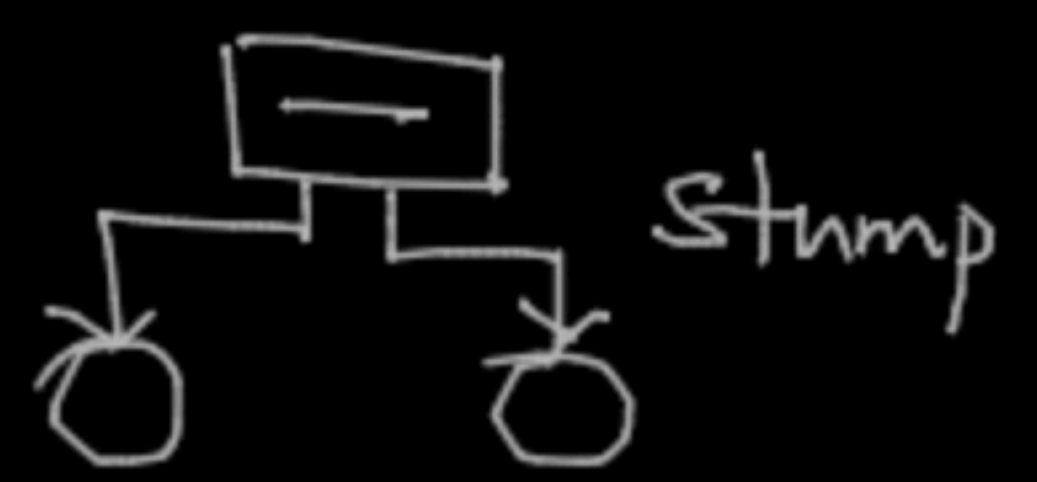
$$\hat{\epsilon}_1 = f_2(x)$$

$$\epsilon_2 = \epsilon_1 - \hat{\epsilon}_1 = y - f_0(x) - f_1(x) - f_2(x)$$

$$y = f_0(x) + f_1(x) + f_2(x) \rightarrow \text{Additive}$$

ADABOOST ✓  
 XGBOOST ✓  
 { M-estimators = ?  
 Each Tree →

Decision stump





Stage 0

Area	y	$\hat{y}$	$\epsilon_0$
1200	35	22	13
2300	53	34	19
1700	47	38	9
3000	96	81	15
3500	94	82	12

Stage 1

Area	$\epsilon_0$	$\epsilon_1$	$\epsilon_2$
1200	13	8	5
2300	19	10	9
1700	9	2	7
3000	15	6	9
3500	12	5	7

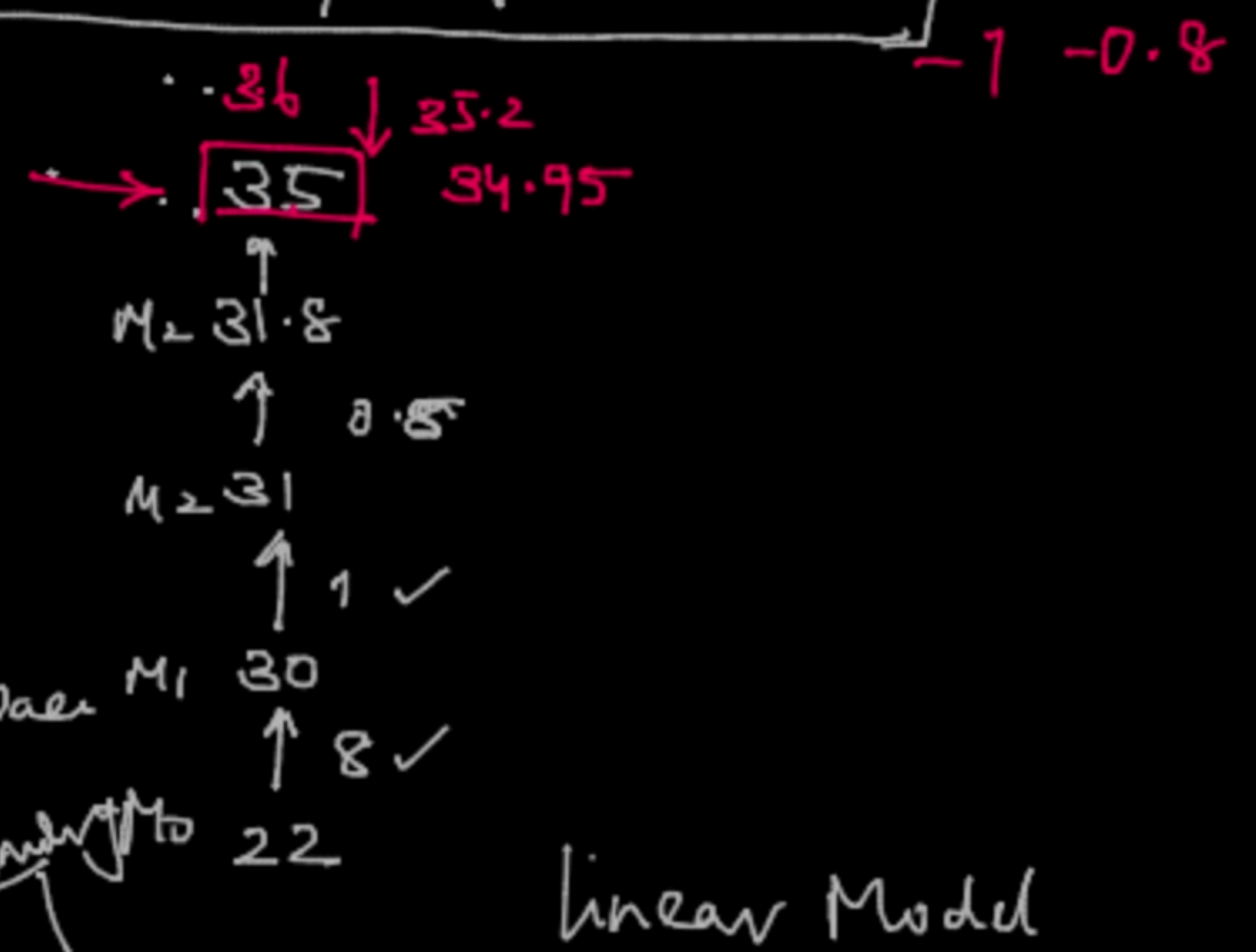
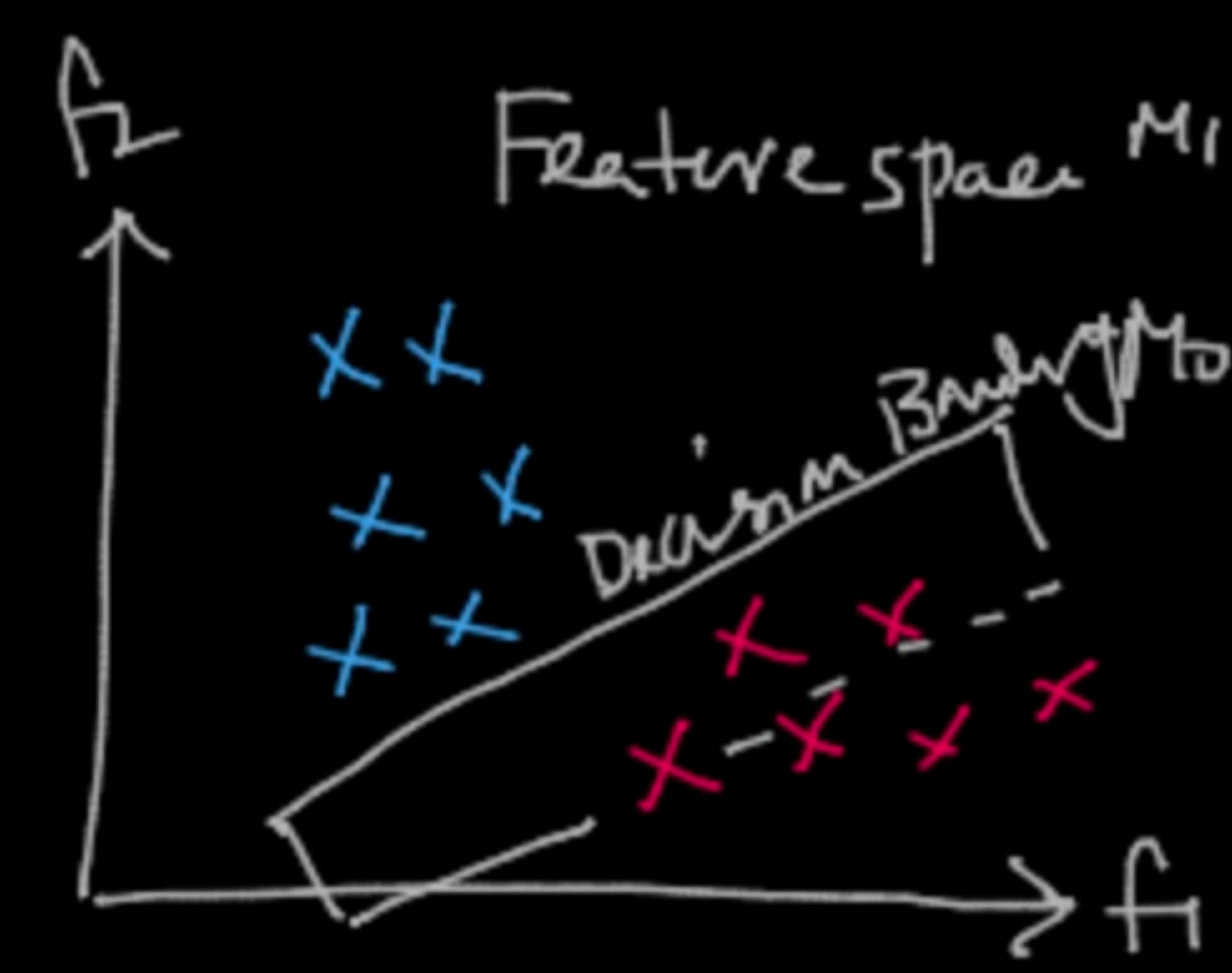
Stage 2

Area	$\epsilon_1$	$\epsilon_2$	$\epsilon_3$
1200	5	1	4
2300	9	3	6
1700	7	2	5
3000	9	3	6
3500	7	4	3

$$\begin{aligned}
 y &= f_0(x) + f_1(x) + f_2(x) + \dots \\
 &= 22 + 8 + 1 + -0.5 \\
 &= 31
 \end{aligned}$$

Classification

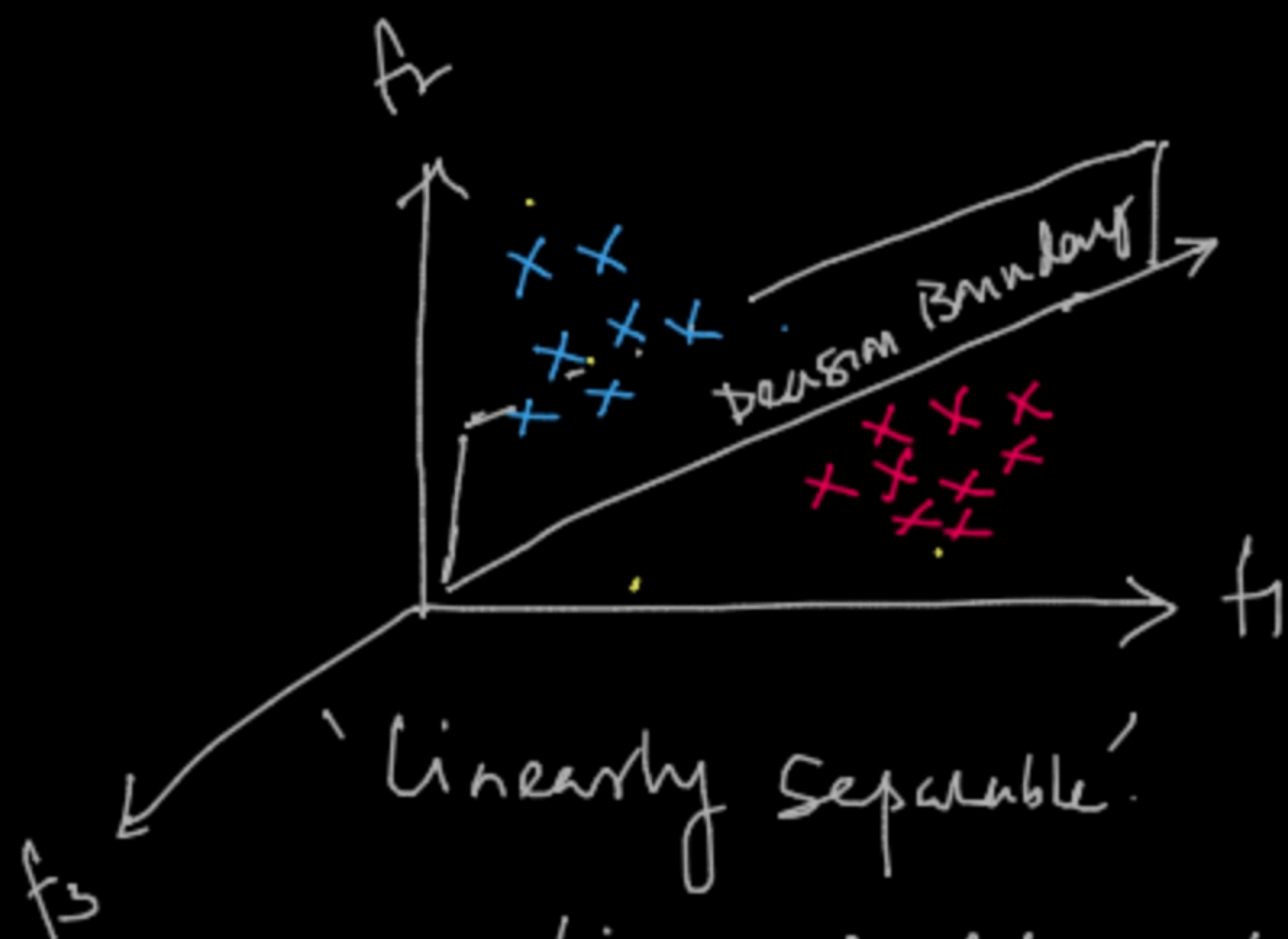
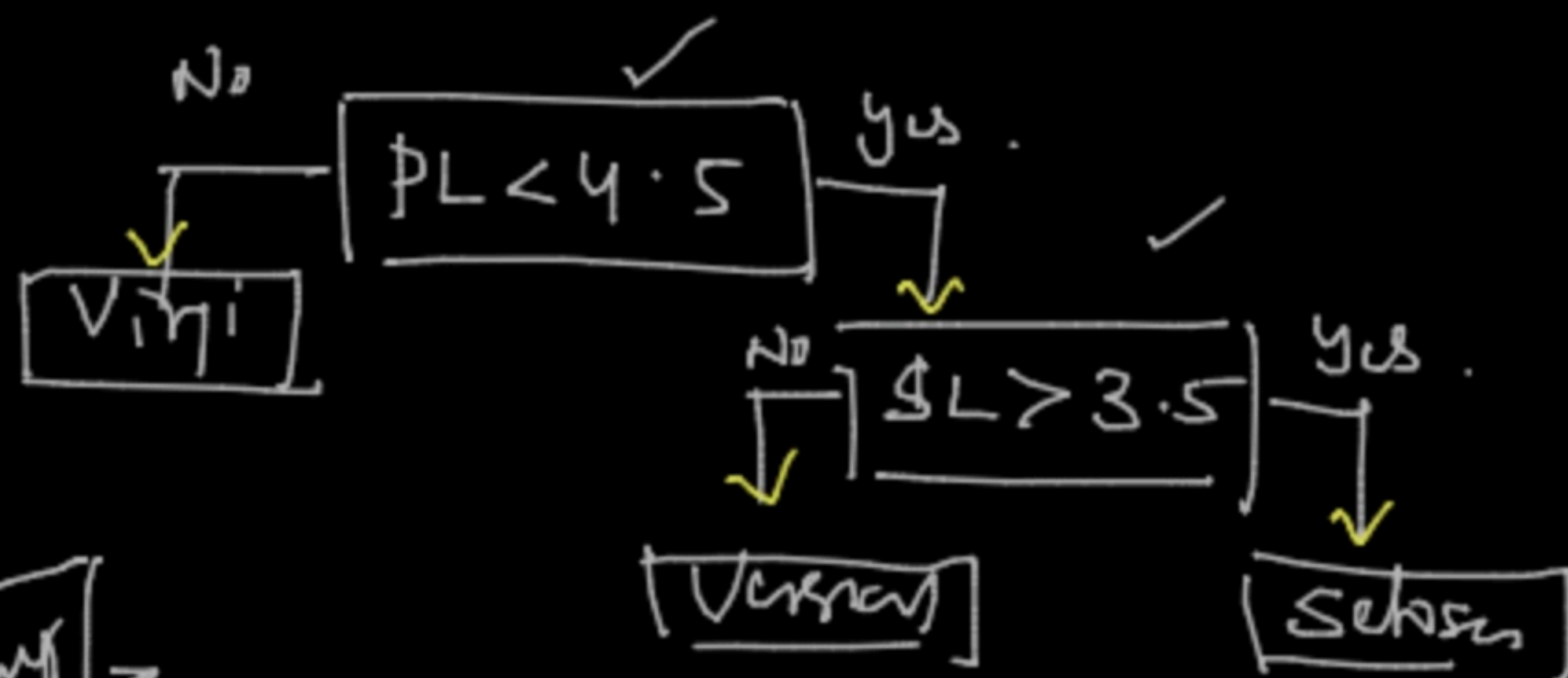
"Partition the feature space into pure regions belonging to each class"



'Linearly Separable' - linear surface



✓ PL ✓ SL species



Linear Models → Logistic Regression

