

My research covers two areas of macroeconomic theory. Firstly, my research seeks to develop computational and mathematical foundations for heterogeneous agent macroeconomic models. Secondly, my research seeks to understand the relationship between technological change, income inequality, the environment and growth. I am also interested in applying machine learning techniques to help solve heterogeneous agent models on the computer and understanding the impact of artificial intelligence technologies on growth.

Modelling Heterogeneity in Macroeconomics

It is now widely recognised that traditional representative agent models cannot adequately account for the vast heterogeneity of economic life — heterogeneity in wealth, income, skills and preferences. This criticism, along with the availability of greater computing power, has led to macroeconomists computing models with many heterogeneous agents facing incomplete markets (the seminal papers are Bewley (1977), Aiyagari (1994), Huggett (1993) and Krusell and Smith (1998)).

Macroeconomists now accept that not only are representative agent models unrealistic, but that heterogeneity is important for questions about steady state levels of macroeconomic aggregates such as capital (Aiyagari, 1995), how macroeconomic variables such as consumption and investment respond to monetary policy (Auclert, 2017; Kaplan et al., 2016), to the timing of fiscal policy (Heathcote, 2005) and to aggregate shocks (Krueger et al., 2016).

Heterogeneous agent models are also key to understanding the impact of policy on welfare (Dávila et al., 2012; Park, 2017); for example, policies discouraging saving have a burden on the wealth poor since they depress wage rates, but may in fact benefit the wealthy since they increase the return on capital.

Despite the popularity of heterogeneous agent models, because we no longer have the mathematical simplicity of a representative agent, there remain large gaps in the theoretical and computational foundations of these models. These foundations can help us understand how heterogeneity affects aggregate macroeconomic relationships (for example, point 2 below), allow us to model more realistic forms of aggregate uncertainty and individual diversity and help create more efficient and faster algorithms to perform policy analysis. My research agenda focuses on helping develop this foundation. In particular, the following questions form the core of my immediate research agenda:

1. When do recursive rational expectations equilibria in heterogeneous agent models exist? When does a computational algorithm converge to the equilibrium (see Cao (2016) for a technical summary of the issues)?
2. Under what circumstances can we represent people's decision rules and aggregate relationships as functions of simple statistics, such as the mean, of aggregate distributions? When do we require each person's decision rule to depend on the entire high dimensional distribution of all other people (see discussion by Heathcote et al. (2009), p32 and appendix of Krueger et al. (2016))?
3. How can we accurately and efficiently represent high dimensional distributions on the computer? What are the best ways to overcome the curse of dimensionality in computer simulations of heterogeneous agent models? How can we apply techniques emerging from the machine learning literature, such as reinforcement learning, to compute equilibrium models?

To date, my PhD thesis has focused on foundations of optimal policy in heterogeneous agent models. I have proven an existence theorem for social planner problems in a standard heterogeneous agent model with production (Shanker, 2017). The proof overcomes the mathematical challenges brought on by the infinite dimensional structure of the policy problem by developing a new maximum theorem for non-compact topological spaces.

The existence proof implied optimal policies have a recursive structure, which allowed me to develop an algorithm guaranteed to converge to the true optima, based on infinite dimensional value function iteration (paper in progress). To speed up the computational procedure, I use a novel application of adaptive sparse grids with reinforcement learning (Pfluger, 2010; Brumm and Scheidegger, 2017; Garcke and Klompmaker, 2014). The procedure reduces grid points for the high dimensional state-space and avoids having to perform infinite dimensional optimisation at each iteration. To the best of my knowledge this is the first time value function iteration and reinforcement has been used in a model where the state is infinite dimensional.

Growth and Technological Change

Alongside the rational expectations revolution in macroeconomics, growth theory also sought to explain long-run growth using micro-founded, profit driven

entrepreneur behaviour — endogenous growth theory due to Romer (1990) and Aghion and Howitt (1992). Initially endogenous growth theory featured symmetric technologies, again allowing us to represent the aggregate macro-economy using simple, deterministic balanced growth relationships using a half dozen or fewer equations.

It was not till the work of Acemoglu (2002) that the focus of growth theory shifted to understanding the direction of technical change, how technical change augments different factors of production. Directed technical change theory has been used to explain rising wage inequality (Acemoglu, 2002), the stylized fact of a constant capital-output ratio (Acemoglu, 2003) and how policy can lead to an environmentally sustainable growth path (Acemoglu et al., 2012), among other questions.

My immediate research in this area seeks to understand how new forms of technologies that can substitute for labour, namely artificial intelligence (AI), affect income inequality. Acemoglu and Restrepo (2017) show how AI can exasperate the income gap between high and low skilled workers. My immediate agenda is to extend this framework¹ to understand how AI affects the *shape* of the distribution — for example, is it that the top of the wealth distribution gets further and further away from the middle? Or is it that the middle and top half of the distribution get richer leaving behind a bottom?

To this point in my PhD thesis, I have used the theory of directed technical change to understand the relationship between energy and growth (Shanker and Stern, 2017). For most of the twentieth and twenty first centuries, the energy intensity of Gross Domestic Product (GDP) across the world has declined, while energy prices have stayed stationary. Much of the energy and climate policy modelling literature treated this decline as an exogenous autonomous trend (the AEEI). In (Shanker and Stern, 2017), we show how energy intensity can decline as a result of profit driven energy augmenting technical change, which firms undertake even if prices do not rise. However, whether or not this decline in energy intensity continues depends on how much current research increases the productivity of future research. The autonomous decline in energy intensity may in fact stop if current research has a high impact on the productivity of future research, implying the assumption of a continued AEEI made by climate policy models may be overly optimistic.

¹Building on ideas in such as Acemoglu and Cao (2015) and Jones and Kim (2017), where the growth process is linked to Pareto distributions in wealth.

I conclude with two longer term areas of research, both which sparked my initial interest to study macroeconomic theory. First, in the spirit of Schumpeter (1942), who envisioned growth through entrepreneurial creative destruction as being inherently unstable, how can we link the key themes raised in this research statement — growth, technical change and business cycles in a general equilibrium heterogeneous agent framework?² In particular, as AI dominates technical change, should we expect economies to be more or less volatile?

Secondly, is sustained growth possible within environmental limits? Is some sort of automatic decoupling inevitable? Can a sustainable development path be cost-less or even improve welfare (the Porter-Hypothesis)? Both Acemoglu et al. (2012) and Shanker and Stern (2017) seem to suggest that without government intervention, growth eventually leads to environmental disaster.³ How do our answers change with broader assumptions on technical change, such as in the presence of rapid AI driven technical change?

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²Some progress in this regard has been made by the agent-based modelling literature, see for example, Dosi et al. (2010).

³See also Hassler et al. (2016) who show a slow down in growth from resource scarcity

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