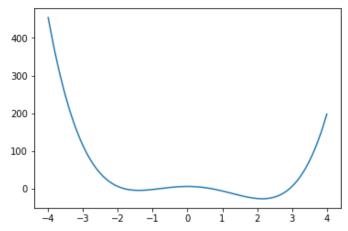
Please refer apt321_ss11381_ML_HW3_Part1_Source_Code.ipynb file for Source Code

Question 1:

Graph function for x in the interval [-4,4]



a.Solution:

Local Minima at x = -1.3971679687499976Global Minima at x = 2.1471808637959735

b.

Solution:

Setting x = -4 and $\eta = 0.001$

Running 6 Iterations:

Before entering the iteration, x is: -4, f(x) is: 454

```
Iteration 1: X = -3.488, f(x) = 240.90741220147203

Iteration 2: X = -3.159231053824, f(x) = 148.52441854620668

Iteration 3: X = -2.9229164225026394, f(x) = 99.4029877988204

Iteration 4: X = -2.742031675863951, f(x) = 70.0712149441725

Iteration 5: X = -2.59779507407776, f(x) = 51.16573699678776

Iteration 6: X = -2.4794003442716166, f(x) = 38.29644231132754
```

The minimum occurs at -2.4794003442716166

Running 1200 Iterations:

Before entering the iteration, x is: -4, f(x) is: 454

```
X converges at Iteration 250  
   Iteration 1195: X = -1.3971808598447308, f(x) = -4.348957724100302  
   Iteration 1196: X = -1.3971808598447308, f(x) = -4.348957724100302  
   Iteration 1197: X = -1.3971808598447308, f(x) = -4.348957724100302  
   Iteration 1198: X = -1.3971808598447308, f(x) = -4.348957724100302  
   Iteration 1199: X = -1.3971808598447308, f(x) = -4.348957724100302  
   Iteration 1200: X = -1.3971808598447308, f(x) = -4.348957724100302
```

The minimum occurs at -1.3971808598447308

The value of x has converged to local minimum.



c.

Solution:

Setting start with x = 4

Running 6 Iterations:

```
Before entering the iteration, x is: 4, f(x) is: 198

Iteration 1: X = 3.68, f(x) = 110.61233152000005

Iteration 2: X = 3.450886144, f(x) = 64.53629857986431

Iteration 3: X = 3.276396901609702, f(x) = 37.31076190742675

Iteration 4: X = 3.138067975365072, f(x) = 19.971643359608052

Iteration 5: X = 3.0252501730040535, f(x) = 8.322601113072949

Iteration 6: X = 2.9312689375235244, f(x) = 0.17557478693807127
```

The minimum occurs at 2.9312689375235244

Running 1200 Iterations:

```
Before entering the iteration, x is: 4, f(x) is: 198

X converges at Iteration 170

Iteration 1195: X = 2.1471808598447315, f(x) = -26.611979775899705

Iteration 1196: X = 2.1471808598447315, f(x) = -26.611979775899705

Iteration 1197: X = 2.1471808598447315, f(x) = -26.611979775899705

Iteration 1198: X = 2.1471808598447315, f(x) = -26.611979775899705

Iteration 1199: X = 2.1471808598447315, f(x) = -26.611979775899705

Iteration 1200: X = 2.1471808598447315, f(x) = -26.611979775899705
```

The minimum occurs at 2.1471808598447315

The value of x has converged to global minimum.

```
d.
```

Solution:

Setting x = -4 and $\eta = 0.01$

Running 1200 Iterations:

```
Before entering the iteration, x is: -4, f(x) is: 454

Iteration 1: X = 1.12, f(x) = -8.71561728

Iteration 2: X = 1.35166976, f(x) = -14.187225687602176

Iteration 3: X = 1.588129914065571, f(x) = -19.554356180837104

Iteration 4: X = 1.8001695002820235, f(x) = -23.55150883046352

Iteration 5: X = 1.9599549783032466, f(x) = -25.64204722189585

Iteration 6: X = 2.0585082124451546, f(x) = -26.383081197323108

X converges at Iteration 18

Iteration 1195: X = 2.147180859844728, f(x) = -26.611979775899698

Iteration 1196: X = 2.147180859844728, f(x) = -26.611979775899698

Iteration 1198: X = 2.147180859844728, f(x) = -26.611979775899698

Iteration 1199: X = 2.147180859844728, f(x) = -26.611979775899698

Iteration 1199: X = 2.147180859844728, f(x) = -26.611979775899698

Iteration 1200: X = 2.147180859844728, f(x) = -26.611979775899698
```

The minimum occurs at 2.147180859844728

The value of x has converged to global minimum in early iteration as compared to (c), because the le arning rate is high ($\eta = 0.01$).



e.

Solution:

Setting x = -4 and $\eta = 0.1$

Running 100 Iterations:

```
Before entering the iteration, x is: -4, f(x) is: 454 Iteration 1: X = 47.2, f(x) = 9689505.955200002 Iteration 2: X = -82626.05440000002, f(x) = 9.321875746621314e+19 Iteration 3: X = 451278842347294.06, f(x) = 8.294875771953852e+58 Iteration 4: X = -7.352328532672759e+43, f(x) = 5.8442611657954e+175 Iteration 5: X = -inf, f(x) = nan
```

X value is bouncing all over from positive to negative and never converges on a single point. This is because learning rate is too high ($\eta = 0.1$).

Question 2:

Solution (2)

(a) The pseudocode in fig IIII is performing stochastic gradient descent where the weight Vin for i=2, h=1 is updated once for every training samples analyzed.

These are 500 samples & the algorithm runs on all the 500 samples for every of 100 epochs, so total no. of updates —

500 × 100 = 50000 up dates.

(b) (i)
$$i=2, h=3$$

Enew $(W, v|x) = \frac{1}{2} [3(x_1-y_1)^2 + 7(x_2-y_2)^2]$

$$AV_{ih} = \Delta V_{23} = -\eta \frac{\partial E(V, V|X)}{\partial V_{23}}$$

$$= -\eta \frac{\partial}{\partial V_{23}} \left[\frac{1}{2} \left[3(x_1, y_1)^2 + 7(x_2 - y_2)^2 \right] \right]$$

$$= -\eta \frac{\partial}{\partial V_{23}} \left[\frac{1}{2} \left[7(x_2 - y_2)^2 \right] \right]$$

$$= -7\eta \left(x_2 - y_2 \right) \left[-\frac{\partial}{\partial V_{23}} y_2 \right]$$

$$= -7\eta \left(x_2 - y_2 \right) \left[-\frac{\partial}{\partial V_{23}} y_2 \right]$$

$$AV_{23} = 7\eta \left(x_2 - y_2 \right) \frac{\partial}{\partial V_{23}} \left(v_2^T x \right) = 7\eta \left(x_2 - y_2 \right) \frac{7}{3}$$

$$AV_{23} = 7\eta \left(x_2 - y_2 \right) \frac{\partial}{\partial V_{23}} \left(v_2^T x \right) = 7\eta \left(x_2 - y_2 \right) \frac{7}{3}$$

(i)
$$\Delta V_{nj} = -N \frac{\partial E}{\partial v_{nj}}$$

$$= -N \frac{\partial E}{\partial y^{(t)}} \cdot \frac{\partial y^{(t)}}{\partial y^{(t)}} \cdot \frac{\partial z_{n}^{(t)}}{\partial w_{nj}} \cdot \frac{\partial z_{n}^{(t)}}{\partial w_{nj}} \cdot \frac{\partial z_{n}^{(t)}}{\partial w_{nj}} \cdot \frac{\partial z_{n}^{(t)}}{\partial y^{(t)}} = -N \frac{\partial E}{\partial y^{(t)}} \cdot \frac{\partial E}{\partial y^{(t)}} \cdot \frac{\partial z_{n}^{(t)}}{\partial y^{(t)}} = -3 \left(s^{(t)} - y^{(t)} \right) \cdot \frac{\partial E^{(2)}}{\partial y^{(2)}} = -7 \left(s^{(2)} - y^{(2)} \right) \cdot \nabla_{n} z_{n}^{(t)} \cdot \left(1 - z_{n}^{(t)} \right) \cdot x_{j}^{(t)} + \left[-7 \left(s^{(2)} - y^{(2)} \right) \cdot \nabla_{n} z_{n}^{(t)} \cdot \left(1 - z_{n}^{(t)} \right) \cdot x_{j}^{(t)} + \left[-7 \left(s^{(2)} - y^{(2)} \right) \cdot \nabla_{n} z_{n}^{(t)} \cdot \left(1 - z_{n}^{(t)} \right) \cdot x_{j}^{(t)} + \left[-7 \left(s^{(2)} - y^{(2)} \right) \cdot \nabla_{n} z_{n}^{(t)} \cdot \left(1 - z_{n}^{(t)} \right) \cdot x_{j}^{(t)} + \left[-7 \left(s^{(2)} - y^{(2)} \right) \cdot \nabla_{n} z_{n}^{(t)} \cdot \left(1 - z_{n}^{(t)} \right) \cdot x_{j}^{(t)} \right] \right]$$

Question 3:

a.

Solution:

As NeuralNetRK uses a linear function, it can output values that are negative numbers. NeuralNetCB, NeuralNetCK and NeuralNetRZeroOne cannot produce negative output.

b.

Solution:

Here, only NeuralNetCK ensures that the sum of the outputs y_1, \ldots, y_k will be 1.

c.

Solution:

Here, K=3 (p_1 , p_2 and p_3 -> Probabilities of class face, cat and tree).

Therefore, it would be appropriate to use NeuralNetCK, since K > 2 classes and the sum of the outputs p_1 , p_2 , p_3 is 1.

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d.

Solution:

NeuralNetCK is the appropriate option as:

- 1. It is a classification problem and there are two values 0/1 which sum to 1.
- 2. NeuralNetCB cannot applied as it is a single output solution.
- 3. Problem expects probabilities for politics and style. Eg. if politics: $x_1=1$, else 0, if formal_style: $x_2=1$, else 0

Question 4:

a.

Solution:

Neural Net Algorithm learns from weight which is not appropriate in this case.

Example consider - almond = 1, anise = 2, creosote = 3, and fishy = 4:

Here, neural net algorithm will consider the 'fishy' value as weighted value(Prediction = weight * odor) 4 (double of anise), which is not true.

Whereas in case of Random Forest, it will support rules such as:

```
if odor = 1:
    //encoding of almond
    process algo...
else if odor = 2:
    //encoding of anise
    Process algo...
```

Therefore, if an algorithm is learning by weight, we should not use label encoding and hence, in our case, it would be fine to do this if we were using a random forest, rather than a neural net. An alternative solution would be to use one-hot encoding.

b.

i. Solution:

For transforming attribute 'stalk shape', we can add one-hot encoding in our existing transformed dataset: if $stalk_shape=taperin: z_5=1$, else 0.

Transformed Dataset:

	z_1	Z 2	Z 3	Z 4	Z 5	label
X ₁	0	0	0	1	1	0
X 2	0	0	1	0	0	0

ii. Solution:

If we use one-hot encoding, there is a problem of losing the hierarchy (high > medium > low) and hence, it is better to use label encoding which retains the order.

iii. Solution:

Here, it is appropriate to use (0,1) instead of one-hot encoding as it will generate the same dataset.

Example: Dataset for Coin Tosses.

Attributes	Outcome
X ₁	Heads
X 2	Tails
X 3	Heads

Use (0,1) encoding -> if heads: x=1, if tails: x=0

Attributes	Outcome	
X 1	1	
X ₂	0	
X 3	1	

Using one-hot encoding will give

Attributes	z ₁ =Heads	z ₂ =Tails
X ₁	1	0
X ₂	0	1
X 3	1	0

Here, z_2 is redundant and can be eliminated as z_1 can alone represented the whole dataset.

In case of three attributes, the value of attribute can be either of 3 outcomes and hence, it is appropriate to use one-hot encoding to represent the data.

