

Tutorial 2

1. ~~Suppose~~ let x_0, x_1, \dots, x_m be not necessarily distinct pts. Let f and g be two polynomials s.t. f and g agree ~~upon~~ on $\underline{x} = x_0, x_1, \dots, x_m$. Also $\deg f \leq m$ and $\deg g \leq m$. Show $f = g$

2. $f(0) = 1$ $f'(0) = 0.5$ $f''(0) = 2$
 $f'''(0) = 3$.

Find a polynomial of degree ≤ 3 which agrees with $f(x)$ at $0, 0, 0, 0$.

3. $f(0.2) = 1.823 \text{ E-1}$
 $f'(0.2) = 8.333 \text{ E-1}$
 $f(0.4) = 3.365 \text{ E-1}$
 $f'(0.4) = 7.143 \text{ E-1}$

- a) Construct the divided difference table
- b) Approximate $f(0.3)$

4. A function $f(x)$ has a double zero at z_1 and a triple zero at z_2 . Determine the form of the polynomial of degree ≤ 5 which interpolates $f(x)$ twice at z_1 , three times at z_2 and once at some other point z_3 (2)

(5) $f(0.2) = 1.987 \text{ E-1}$

$f'(0.2) = 9.801 \text{ E-1}$

$f''(0.2) = -1.987 \text{ E-1}$

$f(0.4) = 3.894 \text{ E-1}$

Construct the divided difference table and approximate $f(0.3)$