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**Department of Metallurgical Engineering and Materials Science**  
**MM 209: THERMODYNAMICS : 2017-18: FALL**

**Tutorial 3**

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1. Five moles of a monatomic ideal gas are contained adiabatically at 50 atm pressure and 300 K. The pressure is suddenly released to 10 atm, and the gas undergoes an irreversible expansion during which it performs 4000 joules of work. Show that the final temperature of the gas after the irreversible expansion is greater than that which the gas would attain if the expansion from 50 to 10 atm had been conducted reversibly. Calculate the entropy produced as a result of the irreversible expansion.

**Answer**

Given:

State 1:  $P_1 = 50 \text{ atm}$ ,  $T_1 = 300\text{K}$ ,  $n = 5 \text{ moles}$

Lets take reversible process takes the gas from state 1 to state 2 and

Irreversible process takes the gas from state 1 to state 3

State 2:  $n = 5 \text{ moles}$ ,  $P_2 = 10 \text{ atm}$

State 3:  $n = 5 \text{ moles}$ ,  $P_3 = 10 \text{ atm}$

In the initial state 1,  $V_1 = nRT_1/P_1 = (5 \times 0.08206 \times 300)/50 = 2.46 \text{ lit}$

If the adiabatic expansion from 50 to 10 atm is carried out reversibly, then the process path follows  $PV^\gamma = \text{constant}$ , and in the final state 2,

$$V_2 = ((50 \times 2.46^{5/3})/10)^{3/5} = 6.47 \text{ litres}$$

$$T_2 = (10 \times 6.47)/(5 \times 0.08206) = 158\text{K}$$

For the irreversible process, which takes the gas from the state 1 to the state 3, as  $q=0$ ,

$$\Delta U = -W = -4000 = -nC_v(T_3 - T_1)$$

and hence  $T_3 = 236 \text{ K}$ , which is higher than  $T_2$ .

As the irreversible expansion from state 1 to state 3 was conducted adiabatically, no heat entered the system, and hence the difference between the entropy at state 3 and the entropy at state 1 is the entropy created,  $S_{irr}$  as a result of the irreversible process.

As the reversible adiabatic expansion from state 1 to state 2 is isentropic,

$$S_3 - S_1 = S_3 - S_2$$

For the reversible isobaric expansion from state 2 to state 3

$$dS = nC_p dT/T$$

Change in entropy from state 1 to state 3 =

$$= 5 \times 2.5 \times 8.3144 \times \ln(236/158) = 42 \text{ J/K}$$

2. Calculate the adiabatic flame temperature of a gas having 20% CO and 80%  $N_2$  when burnt with 150% excess air. Both the reactants are at 25°C. The adiabatic flame temperature is that temperature reached if all of the heat of the oxidation reaction is used to increase the temperature of the products of the reaction. Air is 21 molar percent  $O_2$  and 79 molar percent  $N_2$ .

Data:

$$\Delta H_f^\circ \text{ of } CO_2 = -94052 \text{ cal/gmol}$$

$$\Delta H_f^\circ \text{ of } CO = -26412 \text{ cal/gmol}$$

Mean heat capacities in cal/gmol.°C are  $CO_2 = 12$ ,  $O_2 = 7.9$ ,  $N_2 = 7.55$

### Answer

1 mole of gas (having 20% CO and 80%  $N_2$ )

Combustion reaction:



Heat of reaction at 25°C for the above reaction is calculated as:

Heat of reaction = heat of formation of products - heat of formation of reactants

$$= -94052 - (-26412) = -94052 + 26412 = -67640 \text{ cal/gmol of CO converted}$$

This represents exothermic heat of reaction.

$$\text{Total heat liberated} = 67640 \times 0.2 = 13528 \text{ cal.}$$

If a base temperature of 25°C is assumed, enthalpy of reactants at 25°C = 0 cal

Total enthalpy of product stream = enthalpy of reactants + heat added by

$$\text{reaction} = 0 + 13528 = 13528 \text{ cal.}$$

This enthalpy rise of product stream with respect to feed is accomplished by a temperature increase, if the reaction is in adiabatic conditions.

Constituents of product stream are estimated as follows:

$$\text{CO}_2 \text{ in the product stream} = 0.2 \text{ gmol}$$

$$\text{O}_2 \text{ theoretically needed} = 0.2 \times 0.5 = 0.1 \text{ gmol.}$$

$$\text{O}_2 \text{ actually entering (150\% excess)} = 0.1 \times 2.5 = 0.25 \text{ gmol}$$

$$\text{N}_2 \text{ entering along with O}_2 \text{ in the air} = 0.25 \times 79/21 = 0.9405 \text{ gmol}$$

$$\text{O}_2 \text{ in the leaving gases (assuming complete combustion of CO to CO}_2\text{)} = 0.25 - 0.1 = 0.15 \text{ gmol}$$

$$\text{N}_2 \text{ in the leaving gases} = 0.9405 + 0.8 = 1.7405 \text{ gmol.}$$

Adiabatic temperature (T) is calculated as follows:

$$13528 = 0.2 \times 12 \times (T - 25) + 0.15 \times 7.9 \times (T - 25) + 1.7405 \times 7.55 \times (T - 25)$$

$$\text{i.e., } 13528 = 16.726 (T - 25)$$

$$808.8 = T - 25$$

$$T = 808.8 + 25 = 833.8^\circ\text{C}$$

$$\text{Adiabatic flame temperature} = 833.8^\circ\text{C}$$

3. The analysis of 15000 litre of gas mixture at standard conditions is as follows:

$$\text{CO}_2 = 9.5\% ; \text{SO}_2 = 0.5\% ; \text{O}_2 = 12.0\% ; \text{N}_2 = 78.0\%.$$

How much heat must be added to this gas to change its temperature from  $25^\circ\text{C}$  to  $700^\circ\text{C}$ ?

Data: Specific heat values in  $\text{kcal}/(\text{kmol} \cdot ^\circ\text{K})$

Gas	CO <sub>2</sub>	SO <sub>2</sub>	O <sub>2</sub>	N <sub>2</sub>
C <sub>p</sub> at $25^\circ\text{C}$	8.884	9.54	7.017	6.961
C <sub>p</sub> at $700^\circ\text{C}$	11.303	11.66	7.706	7.298

### Answer

15000 litre of gas

22.4 litre is occupied by 1 gmol of gas at  $0^\circ\text{C}$ .

therefore, number of gmol of gas in the volume of 15000 litre at  $25^\circ\text{C}$ , is estimated as:

$$PV = nRT \text{ (Ideal gas equation)}$$

From the above equation,

$$n_2 P_1 V_1 / T_1 = n_1 P_2 V_2 / T_2$$

here  $P_1$  and  $P_2$  are the same.

Therefore,

$$n_2 \times 22.4 / 273 = 1 \times 15000 / (273 + 25)$$

$$n_2 = 613.5 \text{ gmol} = 0.6135 \text{ kmol}$$

Component	Mole fraction	No of moles, kmol
CO <sub>2</sub>	0.095	$0.6135 \times 0.095 = 0.0583$
SO <sub>2</sub>	0.005	$0.6135 \times 0.005 = 0.0031$

O <sub>2</sub>	0.12	0.6135 x 0.12 = 0.0736
N <sub>2</sub>	0.78	0.6135 x 0.78 = 0.4785

Heat required (H) to raise the temperature from 25°C to 700°C is given by,  
 $H = n_i C_{Pmi} (T_2 - T_1) = n_i C_{Pmi} (700 - 25)$

Where  $n_i$  is the moles of component 'i', and  $C_{Pmi}$  is the mean molal specific heat of component 'i'.

The calculations are shown in the following table.

Co m po ne nt	kmol	C <sub>p</sub> at 25°C kcal/(kmol.°K)	C <sub>p</sub> at 700°C kcal/(kmol.°K)	C <sub>Pm</sub> kcal/(kmol.°K)	Heat to be added, kcal
CO <sub>2</sub>	0.058 3	8.884	11.303	$(8.884 + 11.303)/2 = 10.0935$	$0.0583 \times 10.0935 \times (700 - 25) = 397.2$
SO <sub>2</sub>	0.003 1	9.54	11.66	10.6	22.18
O <sub>2</sub>	0.073 6	7.017	7.706	7.3615	365.72
N <sub>2</sub>	0.478 5	6.961	7.298	7.1295	2302.74
Total heat to be added					<b>3087.84 kcal</b>