## Ozyegin University CS 321 Programming Languages Sample Problems on Functional Programming

<ol> <li>Giver</li> </ol>	i the	followi	ng OC	Caml	code.	

```
let x = 3;;
let f y = x * y;;
let x = 5;;
let z = f 2;;
let k = f x;;
x = 10;;
let w = f x;;
let x = "hi";;
```

(b)

(a) What are the values of z, k, and w?

Does the last line cause a type error? If not, what is the final value of $x$ ?	

2. Consider the following OCaml program:

```
let a = 5
in (let b = 3 in a + b) + (let b = 9 in a * b)
```

Assuming we start with the empty environment,

(a) what's the environment in which the expression a + b is evaluated?

(b) what's the environment in which the expression a \* b is evaluated?

(c) what's the environment after the expression is evaluated?

(d) what does the expression evaluate to?

- 1			
- 1			
1			

3. Consider the following OCaml program:

```
(let c = 3 in c + c) + (let c = 9 in c * c)
```

Assuming we start with the empty environment,

(a) what's the environment in which the expression c + c is evaluated?

(b) what's the environment in which the expression c \* c is evaluated?

(c) what's the environment after the expression is evaluated?

(d) what does the expression evaluate to?

4. Consider the following OCaml program:

let x = 7

Assuming we start with the empty environment,

(a) what's the environment in which expression 1 is evaluated?

(b) what's the environment in which expression 2 is evaluated?

(c) what's the environment in which the expression s \* s is evaluated?

(d) what's the environment in which expression 3 is evaluated?

5.	Consider	the	following	OCaml	program:
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```
let x =
  let a = 5
  in let b = 8
      in a + b
in x * 2
```

Assuming we start with the empty environment,

(a) what's the environment in which the expression a + b is evaluated as (a)
--

- 1			
- 1			

(b) what's the environment in which the expression  $\mathbf{x}~*~2$  is evaluated?

(c) what's the environment after the expression is evaluated?

(d) what does the expression evaluate to?

6. Consider the following OCaml program:

```
let x =
  let x = 5
  in let x = 8
      in x + x
in x * 2
```

Assuming we start with the empty environment,

(a) what's the environment in which the expression x + x is evaluated?

(b) what's the environment in which the expression x \* 2 is evaluated?

(c) what's the environment after the expression is evaluated?

I .		
1		
I .		
I .		

(d) what does the expression evaluate to?

7. Write a function stringy: string list -> (string \* int) list that associates each string in its input with the length of the string. You may use String.length to find the length of a string.

```
# stringy ["a"; "bbb"; "cc"; "ddddd"];;
- : (string * int) list = [("a", 1); ("bbb", 3); ("cc", 2); ("ddddd", 5)]
```

8. Write a function positivesOf: int list -> int list that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```

9. Write a function gotcha: ('a -> bool) -> 'a list -> 'a that takes a predicate function p and a list lst, and returns the first element x of lst for which p(x) is true. If there is no such element, the function should fail with the error message "No soup for you!".

```
# gotcha (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int = 8
# gotcha (fun n -> n > 15) [3; 4; 1; 2; 8; 4; 9; -8];;
Exception: Failure "No soup for you!".
```

To make the program fail in the error case, use the (failwith "No soup for you!") expression.

10. Write a function allUntil: ('a -> bool) -> 'a list -> 'a list that takes a predicate function p, a list lst, and returns all the elements of lst up to the first element that does not satisfy p.

```
# allUntil (fun n -> n < 5) [3; 4; 1; 2; 8; 4; 9; -8];;
-: int list = [3; 4; 1; 2]
# allUntil (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
-: int list = []
# allUntil (fun n -> n < 15) [3; 4; 1; 2; 8; 4; 9; -8];;
-: int list = [3; 4; 1; 2; 8; 4; 9; -8]
# allUntil (fun s -> String.length(s) < 4) ["aa"; "bbb"; "c"; "dddd"; "eeeeeeee"; "ffff"];;
-: string list = ["aa"; "bbb"; "c"]</pre>
```

11. Write a function interleave: 'a list -> 'a list \* 'a list that mixes its inputs by interleaving their elements. In this question, you may assume that the inputs will always have the same length; that is, I won't test your function with naughty inputs.

```
# interleave [1;2;3;4;5] [6;7;8;9;10];;
-: int list * int list = ([6; 2; 8; 4; 10], [1; 7; 3; 9; 5])
# interleave [2;3;4;5] [7;8;9;10];;
-: int list * int list = ([7; 3; 9; 5], [2; 8; 4; 10])
```

12. Write a function enumerate: 'a list -> ('a \* int) list that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0. You will want to write a helper function for this problem.

```
# enumerate ['a';'b';'c';'d';'e'];;
-: (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]
```

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	In all problems below, you must NOT use explicit recursion; use the library functions map, fold_left, and fold_right.
13.	Write a function stringyWithMap that is exactly the same as stringy, but this time use map.
14.	Write a function stringyWithFoldRight that is exactly the same as stringy, but this time use fold_r:
15.	Write a function stringyWithFoldLeft that is exactly the same as stringy, but this time use fold_le:
16.	Write a function positivesOfWithFoldRight that is exactly the same as positivesOf, but this times fold_right.

17. Write a function positivesOfWithFoldLeft that is exactly the same as positivesOf, but this time use fold\_left.

8.	Write a function fold_left.	enumerate	VithFoldLeft	that is	exactly	the same	as enu	merate,	but	this	time u

In the problems below, you may use explicit recursion or the library functions such as map, fold\_left, and fold\_right. It is a good idea to try solving the problems using both approaches.

19. Implement the following functions: rev, append, flatten, map2, exists, mem, partition, assoc, combine.

Their definitions are available in the List module:

http://caml.inria.fr/pub/docs/manual-ocaml/libref/List.html

In the problems below, your implementation is required to be tail-recursive.

20. Write a function positivesOf: int list -> int list that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```

21. Write a function enumerate: 'a list -> ('a \* int) list that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0.

```
# enumerate ['a';'b';'c';'d';'e'];;
-: (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]
```

Extra exercise: Solve the same problem when the elements are enumerated from right to left. E.g.:

```
# enumerate ['a';'b';'c';'d';'e'];;
-: (char * int) list = [('a',4);('b',3);('c',2);('d',1);('e',0)]
```

22. Write an OCaml function named pick that takes an integer n and a list named lst. The function returns the first n elements of lst. If lst has less than n elements, all the elements are returned.

For this question, you have to use explicit recursion; you may not use any library function including '@'. Points will be deducted if your implementation unnecessarily traverses all the elements of 1st.

```
# pick;;
- : int -> 'a list -> 'a list = <fun>
# pick 5 [8;3;7;1;0;9;2;6];;
- : int list = [8; 3; 7; 1; 0]
# pick 5 [8;3;7];;
- : int list = [8; 3; 7]
```

23. Write an OCaml function named assoc that takes a value a and a list of pairs named 1st. The function returns the **rightmost** value associated with key a in 1st.

That is, assoc a [...; (a,b); ...] = b if (a,b) is the rightmost pair that contains a as its first item. If there is no value associated with a in the list lst, fail with the error message "Not found".

Implement assoc using explicit recursion. Your solution should do a single pass over the list. In particular, a solution that first reverses the list and then finds the leftmost association is not acceptable. You may want to use a helper function in this problem.

```
# assoc;;
- : 'a -> ('a * 'b) list -> 'b = <fun>
# assoc 5 [(8,'e'); (6,'s'); (5,'f'); (2,'t'); (5,'h'); (5,'p'); (9,'n')];;
- : char = 'p'
# assoc 4 [(8,'e'); (6,'s'); (5,'f'); (2,'t'); (5,'h'); (5,'p'); (9,'n')];;
Exception: Failure "Not found".
```

24. Write an OCaml function named flatten that takes a list of lists, and returns a list where all the elements of the argument are concatenated in the same order.

Implement flatten using fold\_right.

```
# flatten;;
- : 'a list list -> 'a list = <fun>
# flatten [[4;5;8]; [2;1;9;8]; [3]; [8;5;7;6]];;
- : int list = [4; 5; 8; 2; 1; 9; 8; 3; 8; 5; 7; 6]
```

25.	Write an OCaml function named sums that takes a list and produces another where each element is
	the accumulative sum of the elements up to and including the corresponding element in the input list.
	Implement the function using fold_left (and possibly other library functions), but without
	explicit recursion.

```
# sums;;
- : int list -> int list = <fun>
# sums [6;3;9;1;7;2];;
- : int list = [6; 9; 18; 19; 26; 28]
```

26. Run-length encoding (RLE) is a data compression technique in which maximal (non-empty) consecutive occurrences of a value are replaced by a pair consisting of the value and a counter showing how many times the value was repeated in that consecutive sequence. For example, RLE would encode the list [1;1;1;2;2;2;2;3;1;1;1;1] as [(1,3);(2,4);(3,1);(1;5)].

Write a function rle that takes a list and encodes it using the RLE technique. You may not use any library functions.

27. Define a data type to represent *playing cards*. Each playing card has a *suit*, which is one of  $\clubsuit$ ,  $\spadesuit$ ,  $\diamondsuit$ ,  $\heartsuit$ . A playing card is either ace, king, queen, jack, or an ordinary card. An ordinary card is associated with a number.

- 28. Define an OCaml data type to represent numbers. There are three kinds of numbers:
  - a *Real number*, which is defined by three integer values as its *significand*, *base*, and the *exponent*. E.g.:

$$12.3456 = \underbrace{123456}_{\text{significand}} \times \underbrace{10}_{\text{base}} \overset{\text{exponen}}{-4}$$

- a Rational number, which is defined as a quotient of two integers (i.e. the numerator and the denominator). E.g.  $\frac{42}{79}$
- a Complex number, which is defined by a real part and an imaginary part, both of which are floating point numbers. E.g.:

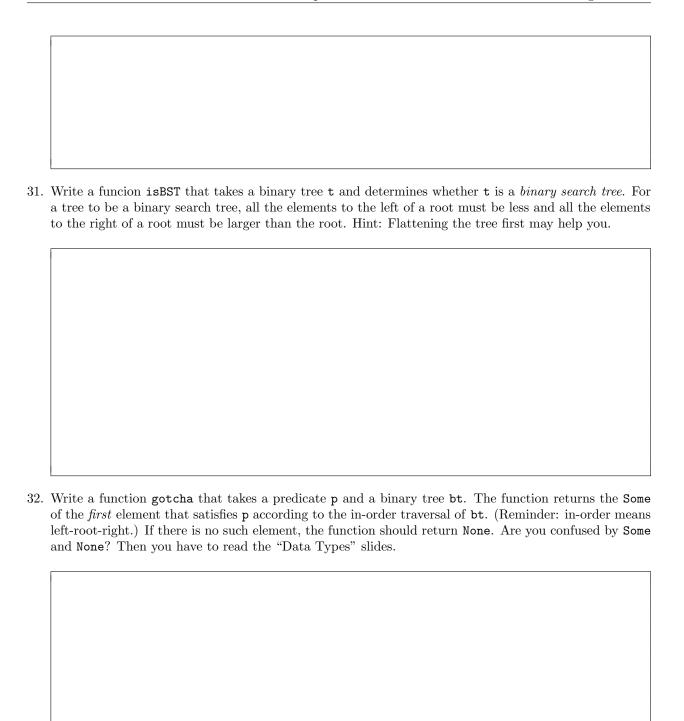
$$\underbrace{3.14}_{\text{real}} + \underbrace{67.891}_{\text{imaginary}} i$$

The problems below are based on the following definition of a binary tree:

29. Write a function are Isomorphic that takes two binary trees and determines whether the trees are isomorphic. Two trees are said to be isomorphic if their shapes are the same, regardless of the values in the trees.

30. Write a funcion collect that takes a binary tree t and a predicate function p, and returns all the elements of t that satisfy p in pre-order.

Extra challenge: Can you solve this problem without using the list append operator (0)?



The problems below are based on the following definition:

Bart is a funny guy who likes to use his own definitions of data types as much as possible. Instead of

the built-in lists, he decides to use a data type named cutelist (given above) to represent integer lists. For instance, instead of the list [1;2;3;4], Bart uses

```
Cons(1, Cons(2, Cons(3, Cons(4, Empty))))
```

33. Write an OCaml function to CList that takes an int list and returns the corresponding cutelist representation. Implement to CList using List.fold\_right. No explicit recursion is allowed!

```
# toCList [1;2;3;4];;
- : cutelist = Cons (1,Cons (2,Cons (3,Cons (4,Empty))))
# toCList [3;6;8;2;7];;
- : cutelist = Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty)))))
```

34. Write an OCaml function reverse that takes a cutelist and returns its reverse. A solution that converts the cutelist to a regular list, then reverses the list, and finally converts the reversed list to a cutelist via toCList is NOT acceptable.

```
# reverse (Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty))))));;
- : cutelist = Cons (7,Cons (2,Cons (8,Cons (6,Cons (3,Empty)))))
```

35. Write a function named append that takes two cutelists and returns their concatenation. Do NOT consider converting the cutelist values to built-in lists to solve this problem.

```
# append (Cons(3, Cons(4, Cons(5, Empty)))) (Cons(9, Cons(8, Empty)));;
- : int cutelist = Cons(3,Cons(4,Cons(5,Cons(9,Cons(8,Empty)))))
```