Ozyegin University
CS 321 Programming Languages
Sample Problems on Functional Programming

1. Write a function `stringy : string list -> (string * int) list` that associates each string in its input with the length of the string. You may use `String.length` to find the length of a string.

```
# stringy ["a"; "bbb"; "cc"; "ddddd"];;
- : (string * int) list = [("a", 1); ("bbb", 3); ("cc", 2); ("ddddd", 5)]
```

2. Write a function `positivesOf : int list -> int list` that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```

3. Write a function `gotcha : ('a -> bool) -> 'a list -> 'a` that takes a predicate function `p` and a list `lst`, and returns the first element `x` of `lst` for which `p(x)` is true. If there is no such element, the function should fail with the error message "No soup for you!".

```
# gotcha (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int = 8
# gotcha (fun n -> n > 15) [3; 4; 1; 2; 8; 4; 9; -8];;
Exception: Failure "No soup for you!".
```

To make the program fail in the error case, use the (`failwith "No soup for you!"`) expression.

4. Write a function `allUntil : ('a -> bool) -> 'a list -> 'a list` that takes a predicate function `p`, a list `lst`, and returns all the elements of `lst` up to the first element that does not satisfy `p`.

```
# allUntil (fun n -> n < 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = [3; 4; 1; 2]
# allUntil (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = []
# allUntil (fun n -> n < 15) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = [3; 4; 1; 2; 8; 4; 9; -8]
# allUntil (fun s -> String.length(s) < 4) ["aa"; "bbb"; "c"; "dddd"; "eeeeeeee"; "fff"];;
- : string list = ["aa"; "bbb"; "c"]
```

5. Write a function `interleave : 'a list -> 'a list -> 'a list * 'a list` that mixes its inputs by interleaving their elements. In this question, you may assume that the inputs will always have the same length; that is, I won't test your function with naughty inputs.

```
# interleave [1;2;3;4;5] [6;7;8;9;10];;
- : int list * int list = ([6; 2; 8; 4; 10], [1; 7; 3; 9; 5])
# interleave [2;3;4;5] [7;8;9;10];;
- : int list * int list = ([7; 3; 9; 5], [2; 8; 4; 10])
```

6. Write a function `enumerate : 'a list -> ('a * int) list` that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0. You will want to write a helper function for this problem.

```
# enumerate ['a';'b';'c';'d';'e'];;
- : (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]
```

In all problems below, you must NOT use explicit recursion; use the library functions `map`, `fold_left`, and `fold_right`.

7. Write a function `stringyWithMap` that is exactly the same as `stringy`, but this time use `map`.

8. Write a function `stringyWithFoldRight` that is exactly the same as `stringy`, but this time use `fold_right`.

9. Write a function `stringyWithFoldLeft` that is exactly the same as `stringy`, but this time use `fold_left`.

10. Write a function `positivesOfWithFoldRight` that is exactly the same as `positivesOf`, but this time use `fold_right`.

11. Write a function `positivesOfWithFoldLeft` that is exactly the same as `positivesOf`, but this time use `fold_left`.

12. Write a function `enumerateWithFoldLeft` that is exactly the same as `enumerate`, but this time use `fold_left`.

In the problems below, you may use explicit recursion or the library functions such as `map`, `fold_left`, and `fold_right`. It is a good idea to try solving the problems using both approaches.

13. Implement the following functions: `rev`, `append`, `flatten`, `map2`, `exists`, `mem`, `partition`, `assoc`, `combine`.

    Their definitions are available in the `List` module:

    `http://caml.inria.fr/pub/docs/manual-ocaml/libref/List.html`

In the problems below, your implementation is required to be tail-recursive.

14. Write a function `positivesOf : int list -> int list` that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```

15. Write a function `enumerate : 'a list -> ('a * int) list` that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0.

```
# enumerate ['a';'b';'c';'d';'e'];;
- : (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]
```

Extra exercise: Solve the same problem when the elements are enumerated from right to left. E.g:

```
# enumerate ['a';'b';'c';'d';'e'];;
- : (char * int) list = [('a',4);('b',3);('c',2);('d',1);('e',0)]
```

16. Define a data type to represent *playing cards*. Each playing card has a *suit*, which is one of ♣, ♠, ♢, ♡. A playing card is either ace, king, queen, jack, or an ordinary card. An ordinary card is associated with a number.

The problems below are based on the following definition of a binary tree:

```
type 'a binTree = BTLeaf of 'a
                | BTNode of 'a * 'a binTree * 'a binTree
```

17. Write a function `areIsomorphic` that takes two binary trees and determines whether the trees are isomorphic. Two trees are said to be isomorphic if their shapes are the same, regardless of the values in the trees.

18. Write a funcion `collect` that takes a binary tree `t` and a predicate function `p`, and returns all the elements of `t` that satisfy `p` in pre-order.

    Extra challenge: Can you solve this problem without using the list append operator (`@`)?

19. Write a funcion `isBST` that takes a binary tree `t` and determines whether `t` is a *binary search tree*. For a tree to be a binary search tree, all the elements to the left of a root must be less and all the elements to the right of a root must be larger than the root. Hint: Flattening the tree first may help you.

20. Write a function `gotcha` that takes a predicate `p` and a binary tree `bt`. The function returns the `Some` of the *first* element that satisfies `p` according to the in-order traversal of `bt`. (Reminder: in-order means left-root-right.) If there is no such element, the function should return `None`. Are you confused by `Some` and `None`? Then you have to read the "Data Types" slides.

The problems below are based on the following definition:

```
type cutelist = Empty
              | Cons of int * cutelist
```

Bart is a funny guy who likes to use his own definitions of data types as much as possible. Instead of the built-in lists, he decides to use a data type named `cutelist` (given above) to represent integer lists. For instance, instead of the list [1;2;3;4], Bart uses

```
Cons(1, Cons(2, Cons(3, Cons(4,Empty))))
```

21. Write an OCaml function `toCList` that takes an `int list` and returns the corresponding `cutelist` representation. **Implement `toCList` using `List.fold_right`. No explicit recursion is allowed!**

```
# toCList [1;2;3;4];;
- : cutelist = Cons (1,Cons (2,Cons (3,Cons (4,Empty))))
# toCList [3;6;8;2;7];;
- : cutelist = Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty)))))
```

22. Write an OCaml function `reverse` that takes a cutelist and returns its reverse. A solution that converts the cutelist to a regular list, then reverses the list, and finally converts the reversed list to a cutelist via `toCList` is NOT acceptable.

```
# reverse (Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty))))));;
- : cutelist = Cons (7,Cons (2,Cons (8,Cons (6,Cons (3,Empty)))))
```