## Ozyegin University CS 321 Programming Languages Sample Problems on Functional Programming

1. Given the following OCaml code.

```
let x = 3;;
let f y = x * y;;
let x = 5;;
let z = f 2;;
let k = f x;;
x = 10;;
let w = f x;;
let x = "hi";;
```

(a) What are the values of z, k, and w?

(b) Does the last line cause a type error? If not, what is the final value of x?

2. Write a function stringy: string list -> (string \* int) list that associates each string in its input with the length of the string. You may use String.length to find the length of a string.

```
# stringy ["a"; "bbb"; "cc"; "ddddd"];;
-: (string * int) list = [("a", 1); ("bbb", 3); ("cc", 2); ("ddddd", 5)]
```

3. Write a function positivesOf: int list -> int list that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```



4. Write a function gotcha: ('a -> bool) -> 'a list -> 'a that takes a predicate function p and a list lst, and returns the first element x of lst for which p(x) is true. If there is no such element, the function should fail with the error message "No soup for you!".

```
# gotcha (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int = 8
# gotcha (fun n -> n > 15) [3; 4; 1; 2; 8; 4; 9; -8];;
Exception: Failure "No soup for you!".
```

To make the program fail in the error case, use the (failwith "No soup for you!") expression.

5. Write a function allUntil: ('a -> bool) -> 'a list -> 'a list that takes a predicate function p, a list lst, and returns all the elements of lst up to the first element that does not satisfy p.

```
# allUntil (fun n -> n < 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = [3; 4; 1; 2]
# allUntil (fun n -> n > 5) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = []
# allUntil (fun n -> n < 15) [3; 4; 1; 2; 8; 4; 9; -8];;
- : int list = [3; 4; 1; 2; 8; 4; 9; -8]
# allUntil (fun s -> String.length(s) < 4) ["aa"; "bbb"; "c"; "dddd"; "eeeeeeee"; "ffff"];;
- : string list = ["aa"; "bbb"; "c"]</pre>
```

6. Write a function interleave: 'a list -> 'a list \* 'a list that mixes its inputs by interleaving their elements. In this question, you may assume that the inputs will always have the same length; that is, I won't test your function with naughty inputs.

```
# interleave [1;2;3;4;5] [6;7;8;9;10];;
- : int list * int list = ([6; 2; 8; 4; 10], [1; 7; 3; 9; 5])
# interleave [2;3;4;5] [7;8;9;10];;
- : int list * int list = ([7; 3; 9; 5], [2; 8; 4; 10])
```

7	Write a formation and the share of the share
	Write a function enumerate: 'a list -> ('a * int) list that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0. You will want to write a helper function for this problem.
	<pre># enumerate ['a';'b';'c';'d';'e'];; - : (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]</pre>
	In all problems below, you must NOT use explicit recursion; use the library functions map, fold_left, and fold_right.
3.	Write a function stringyWithMap that is exactly the same as stringy, but this time use map.
).	Write a function stringyWithFoldRight that is exactly the same as stringy, but this time use fold_righ

10. Write a function stringyWithFoldLeft that is exactly the same as stringy, but this time use fold\_left.

In the problems below, your implementation is required to be tail-recursive.

15. Write a function positivesOf: int list -> int list that returns the positive numbers in its input.

```
# positivesOf [-4; 9; 2; -8; -3; 1; 0];;
- : int list = [9; 2; 1]
```

16. Write a function enumerate: 'a list -> ('a \* int) list that enumerates the elements of its input with their index. The first element in a list is considered to be at index 0.

```
# enumerate ['a';'b';'c';'d';'e'];;
-: (char * int) list = [('a',0);('b',1);('c',2);('d',3);('e',4)]
```

Extra exercise: Solve the same problem when the elements are enumerated from right to left. E.g.

```
# enumerate ['a';'b';'c';'d';'e'];;
-: (char * int) list = [('a',4);('b',3);('c',2);('d',1);('e',0)]
```

17. Write an OCaml function named pick that takes an integer n and a list named lst. The function returns the first n elements of lst. If lst has less than n elements, all the elements are returned.

For this question, you have to use explicit recursion; you may not use any library function including '@'. Points will be deducted if your implementation unnecessarily traverses all the elements of 1st.

```
# pick;;
- : int -> 'a list -> 'a list = <fun>
# pick 5 [8;3;7;1;0;9;2;6];;
- : int list = [8; 3; 7; 1; 0]
# pick 5 [8;3;7];;
- : int list = [8; 3; 7]
```

18. Write an OCaml function named assoc that takes a value a and a list of pairs named 1st. The function returns the **rightmost** value associated with key a in 1st.

That is, assoc a [...; (a,b); ...] = b if (a,b) is the rightmost pair that contains a as its first item. If there is no value associated with a in the list lst, fail with the error message "Not found".

Implement assoc using explicit recursion. Your solution should do a single pass over the list. In particular, a solution that first reverses the list and then finds the leftmost association is not acceptable. You may want to use a helper function in this problem.

```
# assoc;;
- : 'a -> ('a * 'b) list -> 'b = <fun>
# assoc 5 [(8,'e'); (6,'s'); (5,'f'); (2,'t'); (5,'h'); (5,'p'); (9,'n')];;
- : char = 'p'
# assoc 4 [(8,'e'); (6,'s'); (5,'f'); (2,'t'); (5,'h'); (5,'p'); (9,'n')];;
Exception: Failure "Not found".
```

19. Write an OCaml function named flatten that takes a list of lists, and returns a list where all the elements of the argument are concatenated in the same order.

Implement flatten using fold\_right.

```
# flatten;;
- : 'a list list -> 'a list = <fun>
# flatten [[4;5;8]; [2;1;9;8]; [3]; [8;5;7;6]];;
- : int list = [4; 5; 8; 2; 1; 9; 8; 3; 8; 5; 7; 6]
```

20. Write an OCaml function named sums that takes a list and produces another where each element is the accumulative sum of the elements up to and including the corresponding element in the input list. Implement the function using fold\_left (and possibly other library functions), but without explicit recursion.

```
# sums;;
- : int list -> int list = <fun>
# sums [6;3;9;1;7;2];;
- : int list = [6; 9; 18; 19; 26; 28]
```

21. Define a data type to represent *playing cards*. Each playing card has a *suit*, which is one of  $\clubsuit$ ,  $\spadesuit$ ,  $\diamondsuit$ ,  $\heartsuit$ . A playing card is either ace, king, queen, jack, or an ordinary card. An ordinary card is associated with a number.

- 22. Define an OCaml data type to represent numbers. There are three kinds of numbers:
  - a *Real number*, which is defined by three integer values as its *significand*, *base*, and the *exponent*. E.g.:

$$12.3456 = \underbrace{123456}_{\text{significand}} \times \underbrace{10}_{\text{base}}^{\text{exponent}}$$

- a Rational number, which is defined as a quotient of two integers (i.e. the numerator and the denominator). E.g.  $\frac{42}{79}$
- a Complex number, which is defined by a real part and an imaginary part, both of which are floating point numbers. E.g.:

$$\underbrace{3.14}_{\text{real}} + \underbrace{67.891}_{\text{imaginary}} i$$

	The problems below are based on the following definition of a binary tree:
	type 'a binTree = BTLeaf of 'a
	BTNode of 'a * 'a binTree * 'a binTree
20	
23.	Write a function are Isomorphic that takes two binary trees and determines whether the trees are isomorphic. Two trees are said to be isomorphic if their shapes are the same, regardless of the values in the trees.
24.	Write a funcion collect that takes a binary tree t and a predicate function p, and returns all the elements of t that satisfy p in pre-order.
	Extra challenge: Can you solve this problem without using the list append operator (@)?

25. Write a funcion is BST that takes a binary tree t and determines whether t is a binary search tree. For a tree to be a binary search tree, all the elements to the left of a root must be less and all the elements to the right of a root must be larger than the root. Hint: Flattening the tree first may help you.



26. Write a function gotcha that takes a predicate p and a binary tree bt. The function returns the Some of the *first* element that satisfies p according to the in-order traversal of bt. (Reminder: in-order means left-root-right.) If there is no such element, the function should return None. Are you confused by Some and None? Then you have to read the "Data Types" slides.

The problems below are based on the following definition:

Bart is a funny guy who likes to use his own definitions of data types as much as possible. Instead of the built-in lists, he decides to use a data type named cutelist (given above) to represent integer lists. For instance, instead of the list [1;2;3;4], Bart uses

```
Cons(1, Cons(2, Cons(3, Cons(4, Empty))))
```

27. Write an OCaml function to CList that takes an int list and returns the corresponding cutelist representation. Implement to CList using List.fold\_right. No explicit recursion is allowed!

```
# toCList [1;2;3;4];;
- : cutelist = Cons (1,Cons (2,Cons (3,Cons (4,Empty))))
# toCList [3;6;8;2;7];;
- : cutelist = Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty)))))
```

28.	Write an OCaml function reverse that takes a cutelist and returns its reverse. A solution that converts the cutelist to a regular list, then reverses the list, and finally converts the reversed list to a cutelist via toCList is NOT acceptable.
	<pre># reverse (Cons (3,Cons (6,Cons (8,Cons (2,Cons (7,Empty))))));; - : cutelist = Cons (7,Cons (2,Cons (8,Cons (6,Cons (3,Empty)))))</pre>