

# Ozyegin University

## CS 321 Programming Languages

### Sample Problems on Interpretation

1. (From PLC, Exercise 1.1) Given the definition of the simple ArithLang below, extend this language with conditional expressions (i.e. “if”) corresponding to Java’s expression  $e_1 ? e_2 : e_3$ , or OCaml’s `if  $e_1$  then  $e_2$  else  $e_3$` . Evaluation of a conditional expression should evaluate  $e_1$  first. If it yields a non-zero value, evaluate  $e_2$ , otherwise evaluate  $e_3$ .

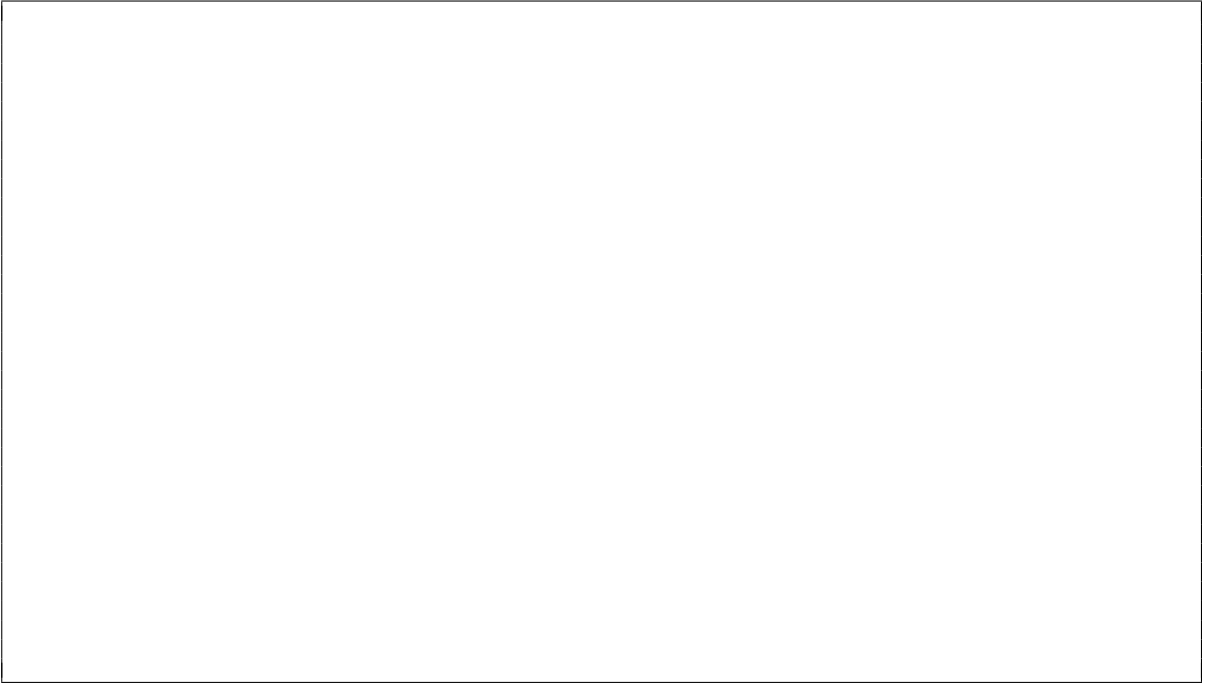
```

type exp = CstI of int
         | Var of string
         | Add of exp * exp
         | Mult of exp * exp
         | Subt of exp * exp
         | Div of exp * exp
         | LetIn of string * exp * exp

(* lookup: string -> (string * int) list -> int *)
let rec lookup x env =
  match env with
  | [] -> failwith ("Unbound name " ^ x)
  | (y,i)::rest -> if x = y then i
                    else lookup x rest

(* eval: exp -> (string * int) list -> int *)
let rec eval e env =
  match e with
  | CstI i -> i
  | Var x -> lookup x env
  | Add(e1, e2) -> eval e1 env + eval e2 env
  | Mult(e1, e2) -> eval e1 env * eval e2 env
  | Subt(e1, e2) -> eval e1 env - eval e2 env
  | Div(e1, e2) -> eval e1 env / eval e2 env
  | LetIn(x, e1, e2) -> let v = eval e1 env
                        in let env' = (x, v)::env
                        in eval e2 env'

```



2. (From PLC, Exercise 1.1) Extend ArithLang to handle three additional operators: “max”, “min”, and “=”. Like the existing binary operators, they take two argument expressions. The equals operator should return 1 when true and 0 when false.

3. Write the representation of the following ArithLang expressions using the `exp` data type.

(a)  $v * 5 - k + 6$

(b)  $x + y + z + p$

(c)  $5 - (y - 3) * (g + 1)$



```
        CstI 7));;  
- : exp = Div(CstI 0, CstI 7)
```


5. Is the grammar shown below ambiguous? If yes, give me an input that at least two different parse trees, and show those trees. If no, prove it.

```
main ::= exp EOF  
exp  ::= INT  
      | NAME  
      | exp PLUS exp  
      | exp STAR exp  
      | LET NAME EQ exp IN exp  
      | IF exp THEN exp ELSE exp
```

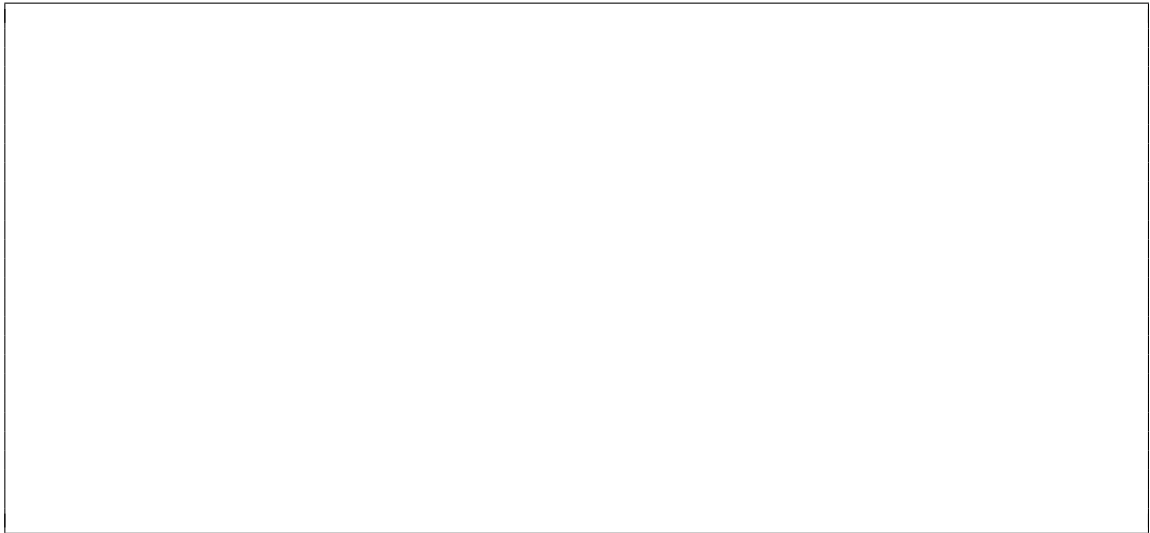
- 6.
- ```
main ::= exp EOF
exp  ::= INT
      | NAME
      | exp SLASH exp
      | exp PLUS exp
      | LET NAME EQ exp IN exp
      | IF exp THEN exp ELSE exp
```

Based on the grammar given above, show two different parse trees for the following inputs. For each, also state whether the ambiguity is related to **precedence** or **associativity**.

- (a)  $9 + 5 + 2$



(b)  $9 + 5 / 2$



7. The following is an ambiguous grammar. Non-terminals in the notation are written using lowercase letters; terminals are all in capital letters. Give a term that has at least two different parse trees in this grammar. Show those two trees.

```
expr ::= expr PLUS atom
      | IF expr THEN expr ELSE expr
      | BOOL
```

```
atom ::= NAME
```

8. Write a lexer that recognizes all character sequences consisting of *a* and *b* where two *a*'s are always separated by at least one *b*. For instance, these four strings are legal: *b*, *a*, *ba*, *ababbbaba*; but these two strings are illegal: *aa*, *babaa*. Your lexer should take a list of chars, and return true if the input is legal, otherwise return false.

9. Extend the Deve language interpreter to handle parenthesized expressions such as  $(3 + 4) * 5$ .
10. Instead of having a separate AST constructor for each binary operator (e.g. **Add**, **Subt**, etc.), use a single constructor named **Binary** to handle any binary operator. For this, change the definition of the **exp** data type. In a **Binary**, in addition to the left and the right operands, keep the operator as a string.  
E.g. **Add**(*e*<sub>1</sub>, *e*<sub>2</sub>) becomes **Binary**("+", *e*<sub>1</sub>, *e*<sub>2</sub>);  
**Mult**(*e*<sub>1</sub>, *e*<sub>2</sub>) becomes **Binary**("\*", *e*<sub>1</sub>, *e*<sub>2</sub>);  
**Subt**(*e*<sub>1</sub>, *e*<sub>2</sub>) becomes **Binary**("-", *e*<sub>1</sub>, *e*<sub>2</sub>).
11. Extend the Deve interpreter (i.e. lexer, parser, and the eval function) to handle two relational operators: less-than (<) and less-than-or-equals (<=).
12. Change the definition of the interpreter so that boolean values are not handled as 0 and 1, but handled separately as **true** and **false**. You will need to define a new data type named, say, **value**, for this. The **eval** function should now return a **value**, instead of an **int**.
13. Extend the language with pairs: (*e*<sub>1</sub>, *e*<sub>2</sub>) and the **fst**, **snd** functions: **fst**(*e*), **snd**(*e*)  
E.g: **let** *p* = (6+8, 9-5) **in** **fst**(*p*) + **snd**(*p*) should evaluate to **Int** 18.



You will need to extend the definition of `value` for this.

E.g: `let p = (6+8, 9-5) in (snd(p), fst(p))` should evaluate to `Pair(Int 4, Int 14)`.

Another example: `let p = (6+8, 9-5) in (snd(p), (fst(p) < 10, 5))` evaluates to `Pair(Int 4, Pair(Bool false, Int 5))`

You can treat `fst` and `snd` as unary operators (i.e. operators that take a single argument).

14. Extend the language to handle a simple match expression for pairs in the following form:

`match e1 with (x,y) -> e2`

Here,  $e_1$  and  $e_2$  are arbitrary expressions,  $x$  and  $y$  are arbitrary names.  $e_1$  is expected to evaluate to a pair.  $x$  and  $y$  may be used inside  $e_2$ ; so the match expression should bind  $x$  and  $y$  to the first and second item, respectively, of the pair that we obtain from evaluating  $e_1$ .

E.g. `match (5+6, 2*3) with (f,s) -> f + s` evaluates to `Int 17`.

15. Extend the language with the boolean negation (i.e. logical-not) operator: `not(e)`. For simplicity of parsing, we require parentheses here. So, there are no ambiguity risks.
16. Extend the language with the greater-than-or-equal-to operator:  $e_1 \geq e_2$ .  
Do NOT change the definition of the `eval` function for this. Instead, simply parse a `>=` as a logical-NOT of a `<`. E.g.  $e_1 \geq e_2$  should be parsed as if it were `not(e1 < e2)`. Note that our language already handles `<` and `not`.
17. Extend the language with two more binary operators, `min` and `max`, with the following syntax: `min(e1, e2)` and `max(e1, e2)`. You can still use the `Binary` constructor for `min` and `max` although they are not infix operators.