

# PHYS 305: Computational Physics II

Winter 2018

## Homework #4

(Due: March 5, 2018)

*Each problem is worth 10 points. E-mail your solutions to `steve@physics.drexel.edu` with a subject including PHYS 305 and the Homework number. The e-mail should have as an attachment a zip (or tar) file containing a PDF document containing all discussion, results, and graphs requested, and files containing Python scripts for all programs written.*

1. (a) Incorporate variable time steps, as implemented in the solution to Exercise 6.6, into the  $N$ -body calculation described in Homework 3, problem 3, with the following changes. (i) Each of the two subsystems should have only  $N = 50$  particles (NOTE: each subsystem has mass 1, so the total mass of the full system is 2); (ii) take  $\epsilon = 0.001$  to increase the dynamic range of the calculation; (iii) do not plot the quantity  $R$  defined in Homework 3, but instead plot both the total potential energy  $U$  of the system and the “virial radius”  $R_v$  defined by

$$R_v = -\frac{GM^2}{2U},$$

where  $M$  is the total mass; and (iv) don’t plot snapshots at various times.

Implement variable steps by multiplying the parameter  $\tau$  returned by the integrator by a time step parameter  $\eta$  (set by default and/or on the command line), which can be varied to control the accuracy of the calculation. Print out the time and energy error  $|E - E_0|$  at intervals of 1 time unit, and find a value of  $\eta$  that ensures an energy error of less than  $10^{-4}$  throughout the run. How many total time steps does the calculation take?

(b) Repeat part (a) using the fixed timestep scheme of Homework 3, problem 3. Find a value of  $\delta t$  that ensures an energy error of less than  $10^{-4}$  throughout the run. How many total time steps does the calculation take?

2. (a) Do Exercise 6.7 on the course web page. Specifically, implement a step-doubling scheme for the two-body problem with the given initial conditions, and find the value of the control parameter  $dE_{tol}$  needed to ensure an energy error of less than  $10^{-4}$  throughout the entire run.
3. Repeat problem 1(a) with a step doubling scheme. Find the value of  $dE_{tol}$  needed to ensure an energy error of less than  $10^{-4}$  throughout the entire run, and compare the total number of steps to the values found in parts 1(a) and 1(b).