Analysis of Rolling Sales Data - Bronx (04/01/2020 - 03/31/2021)

Steps

I am going to do the following:

- 1. Import necessary modules
- 2. Load the prepped data per borough
- 3. Analyze the data for trends and seasonality
- 4. Dickey-Fuller Tests and preparing data for ARMA modeling
 - Induce stationarity if needed
- 5. ARMA model of the data
- 6. Error analysis of the ARMA model
 - Try to improve ARMA model
- 7. Comparison with latest data
 - -Test data from 04/01/2021 04/31/2021
- 8. Observations/Conclusions/Recommendations

1. Imports

```
In [1]:
        import pandas as pd
        from pandas.plotting import register_matplotlib_converters
        import matplotlib.pyplot as plt
        import matplotlib as mpl
        from sklearn.metrics import mean_squared_error, r2_score, mean_absolute_error
        import datetime
        from statsmodels.tsa.arima_model import ARMA
        from statsmodels.tsa.stattools import adfuller, acf, pacf
        from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
        import statsmodels.api as sm
        from statsmodels.tsa.seasonal import seasonal_decompose
        import numpy as np
        from matplotlib.pylab import rcParams
        from sklearn.metrics import mean squared error
        from math import sqrt
        import sklearn
        import math
        #Supress default INFO logging
        %matplotlib inline
        import warnings
        warnings.filterwarnings('ignore')
        import logging
        logger = logging.getLogger()
        logger.setLevel(logging.CRITICAL)
        import logging, sys
        warnings.simplefilter(action='ignore', category=FutureWarning)
```

2. Loading the prepared data

Observations:

- Once I loaded the data and sorted it, the SALE DATE values range from 4/1/2020 until 3/31/2021.
- This data was the most recent data when I started working on the project.
- NYC OpenData website updates this data regularly with newer months about every 2-3 months
- The latest data which came out this month gave data up to 4/31/2021, which I can test against the prediction for 30 days

```
In [2]: #Loading prepped data
df = pd.read_csv('datasets/rollingsales_brooklyn.xls_prepped_bare.csv')
df.reset_index(drop=True, inplace=True)
df.sort_values('SALE DATE')
```

Out[2]:		TAX CLASS AT PRESENT	ZIP CODE	SALE PRICE	SALE DATE
	5697	2	11210.0	189000	2020-04-01
	5626	2	11226.0	7185567	2020-04-01
	5627	2	11226.0	7185567	2020-04-01
	5635	2	11226.0	30644330	2020-04-01
	5636	2	11226.0	14582474	2020-04-01
				•••	
	4577	2	11201.0	1717500	2021-03-31

2

2A

4

11624 rows × 4 columns

10456

5706

3039

11296

3. Analyzing the data for trends/seasonality

11232.0

11226.0

11221.0

11249.0

1218500

857000

3755000

75000

2021-03-31

2021-03-31

2021-03-31

2021-03-31

I do the following steps here to help the data work with the modules:

- 1. Convert 'SALE DATE' column to datetime format
- 2. Create new dataframe with 'SALE DATE' as the index and 'SALE PRICE' a s the column $\,$
- 3. Since we have multiple sales per day, I will aggregate the data into daily data by taking the daily average of sales
- 4. Check the data for any nulls/NaNs
 -Decide what to do for Nulls/NaNs
- 5. Use statsmodels to observe the data for trends and seasonality

Observations:

- NaN values came into the data after the data got aggregated.
 - Dropping these rows will result in skewing the data predictions
- I decided to repalce the NaN values with 0 since no sales were don $\ensuremath{\mathrm{e}}$ on that day
 - -This also preserves the 365 day row length

```
In [4]: # 1. Convert 'SALE DATE' column to datetime format

df['SALE DATE'] = pd.to_datetime(df['SALE DATE'])
```

```
[ARMA] Brooklyn - Jupyter Notebook
In [5]: # 2 . Create new dataframe with 'SALE DATE' as the index and 'SALE PRICE' as the
         df price date = pd.DataFrame(df, columns=['SALE DATE', 'SALE PRICE'])
         df_price_date = df_price_date.set_index('SALE DATE')
         df_price_date.head()
Out[5]:
                     SALE PRICE
          SALE DATE
           2020-04-28
                         1300000
           2020-11-30
                           75000
           2020-06-26
                          830000
           2020-07-20
                         1188000
           2021-02-22
                          990000
```

```
In [6]: # 3. Group the sales data by daily average

df_price_date = df_price_date.resample('D').mean()
```

In [8]: # 4. We see here number of rows went down 293. Why wasn't it 365 rows to represed
df_price_date.info()

```
In [9]: #Here we see that since we resampled by day, there are NaN values for the days the df_price_date['SALE PRICE'].isna().sum()
```

Out[9]: 72

Out[10]: SALE PRICE

```
      SALE DATE

      2020-04-01
      3.977437e+06

      2020-04-02
      8.185471e+05

      2020-04-03
      1.815030e+06

      2020-04-04
      2.333627e+05

      2020-04-05
      0.000000e+00

      ...
      ...

      2021-03-27
      0.000000e+00

      2021-03-28
      0.000000e+00

      2021-03-29
      1.002984e+06

      2021-03-30
      1.058857e+06

      2021-03-31
      1.126519e+06
```

365 rows × 1 columns

```
In [11]: # 5. Checking for trends/seasonality
#Here I check the origional data against its 7-day weekly rolling window to see '

df_price_date['roll_avg'] = df_price_date.rolling(window=7).mean()
    df_price_date
```

Out[11]: **SALE PRICE** roll_avg **SALE DATE** 2020-04-01 3.977437e+06 NaN **2020-04-02** 8.185471e+05 NaN 2020-04-03 1.815030e+06 NaN 2020-04-04 2.333627e+05 NaN 2020-04-05 0.000000e+00 NaN 2021-03-27 0.000000e+00 752500.591285 2021-03-28 0.000000e+00 752500.591285 2021-03-29 1.002984e+06 760118.473764 **2021-03-30** 1.058857e+06 782883.683764

2021-03-31 1.126519e+06 781229.178651

365 rows × 2 columns

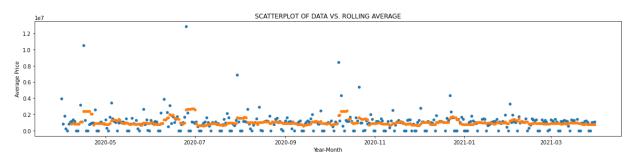
```
In [12]: #Plotting the 7-day rolling average against the origional data

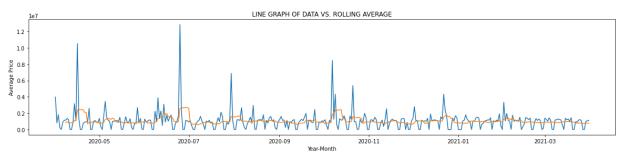
plt.figure(figsize=(20, 4))
plt.title("SCATTERPLOT OF DATA VS. ROLLING AVERAGE")
plt.xlabel("Year-Month")
plt.ylabel("Average Price")

#s=20 to keep dots small in size
plt.scatter(df_price_date.index[:365], df_price_date['SALE PRICE'][:365], s=20)
plt.scatter(df_price_date.index[7:], df_price_date['roll_avg'][7:], s=20);
plt.figure(figsize=(20, 4))

plt.title("LINE GRAPH OF DATA VS. ROLLING AVERAGE")
plt.plot(df_price_date.index[:365], df_price_date['SALE PRICE'][:365])
plt.plot(df_price_date.index[7:], df_price_date['roll_avg'][7:]);
plt.xlabel("Year-Month")
plt.ylabel("Average Price")
```

Out[12]: Text(0, 0.5, 'Average Price')





- The spikes in the data where the price goes to the millions or tens of millions is due to buildings being bought.
- Other than that, the rest are residential properties well under a mill ion in price

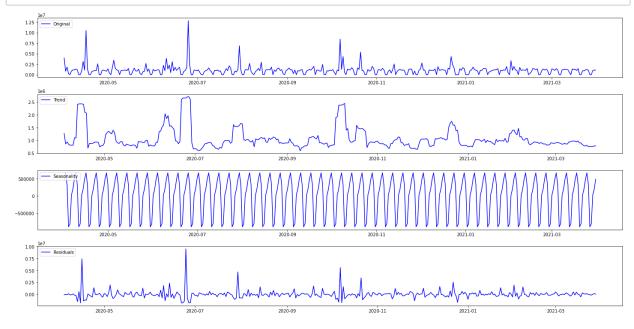
```
In [13]: # Statsmodels decomposition

# Additive model was chosen here. It would not allow multiplicative with "0" value
# Period of 7 for weekly lag

decomposition = seasonal_decompose(df_price_date['SALE PRICE'], model='additive'
observed = decomposition.observed
trend = decomposition.trend
seasonal = decomposition.seasonal
residual = decomposition.resid
```

In [14]: register_matplotlib_converters()

```
In [15]: plt.figure(figsize=(20,10))
   plt.subplot(411)
   plt.plot(observed, label='Original', color="blue")
   plt.legend(loc='upper left')
   plt.subplot(412)
   plt.plot(trend, label='Trend', color="blue")
   plt.legend(loc='upper left')
   plt.subplot(413)
   plt.plot(seasonal,label='Seasonality', color="blue")
   plt.legend(loc='upper left')
   plt.subplot(414)
   plt.plot(residual, label='Residuals', color="blue")
   plt.legend(loc='upper left')
   plt.legend(loc='upper left')
   plt.legend(loc='upper left')
   plt.tight_layout()
```



Observations:

• Looks like there may be some seasonality every month

4. Dickey-Fuller Tests and preparing data for ARMA modeling

- 1. First I will run initial Augmented Dickey Fuller (ADF) test to check if the data is already stationary and does not have a unit root.
- 2. If the data fails the ADF test, I will induce stationarity using the following methods:
 - Differencing
 - Logging the data
 - Rolling mean subtraction

```
In [16]:
         # Initial test
         dftest = adfuller(df_price_date['SALE PRICE'])
         dfoutput = pd.Series(dftest[0:4], index=['Test Statistic','p-value','#Lags Used'
         for key,value in dftest[4].items():
             dfoutput['Critical Value (%s)'%key] = value
         print(dftest)
         print()
         print(dfoutput)
         (-4.665875408357549, 9.749187516484523e-05, 15, 349, {'1%': -3.449226932880019,
          '5%': -2.869857365438656, '10%': -2.571201085130664}, 10619.45547609437)
         Test Statistic
                                          -4.665875
         p-value
                                          0.000097
         #Lags Used
                                         15,000000
         Number of Observations Used 349.000000
         Critical Value (1%)
                                         -3.449227
         Critical Value (5%)
                                         -2.869857
         Critical Value (10%)
                                         -2.571201
```

Augmented Dickey Fuller Test Goals:

Our goal is to induce stationarity and show that the data does not have a unit root.

ADF Test Null Hypothesis: The data has a unit root and is non-stationary.

Requirements for stationarity:

dtype: float64

- 1. If p-value <= 0.05: Reject the null hypothesis (H0), the data does not have a unit root and is stationary.
- If p-value > 0.05: Fail to reject the null hypothesis (H0), the da ta has a unit root and is non-stationary.
- 2. If the Test Statistic is lower than the critical values, then reject the null hypothesis. Data does not have a unity root and is stationary

Results of ADF Test

Test Statistic vs. Critical Values

- Initial test shows Test Statistic of **-4.665875**, this is greater than the critical values for 1% and 5%.
 - We **REJECT** the null hypothesis! The data does not have a unit root and is stationary

P-Value Analysis

- Our current p-value is **0.000097** which is REALLY close to zero.
 - This means: p-value <= 0.05:
 - We REJECT the null hypothesis! The data does not have a unit root and is stationary

5. ARMA MODELING

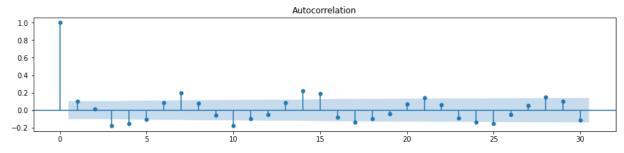
Because ADF test shows data was stationary and does not have a unit root, we can proceed with ARMA model setup.

ACF and PACF will be used to determine the parameters.

```
In [17]: # ACF AND PACF

rcParams['figure.figsize'] = 15, 3
plot_acf(df_price_date['SALE PRICE'], lags=30, alpha=0.05);

rcParams['figure.figsize'] = 15, 3
plot_pacf(df_price_date['SALE PRICE'], lags=30, alpha=0.05);
```



```
Partial Autocorrelation

1.0
0.8
0.6
0.4
0.2
0.0
-0.2
0
5
10
15
20
25
30
```

```
In [19]: # Instantiate & fit model with statsmodels
#p = num lags - ACF
p = 17

# q = lagged forecast errors - PACF
q = 17

#d = number of differences - will compare differenced data RMSE with this model
# d=

# Fitting ARMA model and summary
ar = ARMA(df_price_date['SALE PRICE'],(p,q)).fit()
ar.summary()
```

Out[19]: ARMA Model Results

Dep. Variable: SALE PRICE No. Observations: 365 Model: ARMA(17, 17) Log Likelihood -5588.777 Method: S.D. of innovations css-mle 1047550.052 Sun, 20 Jun 2021 11249.554 Date: **AIC** Time: 15:26:45 BIC 11389.951 Sample: 04-01-2020 **HQIC** 11305.350 - 03-31-2021

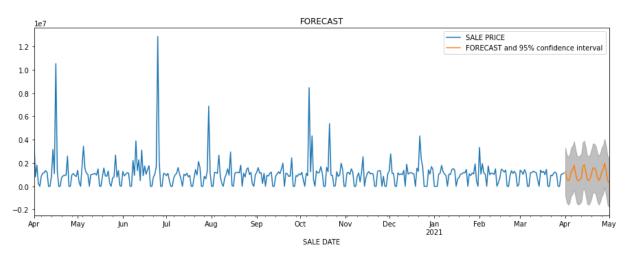
	coef	std err	Z	P> z	[0.025	0.975]
const	1.07e+06	6.32e+04	16.933	0.000	9.46e+05	1.19e+06
ar.L1.SALE PRICE	-0.2998	0.266	-1.125	0.260	-0.822	0.222
ar.L2.SALE PRICE	0.0612	0.132	0.465	0.642	-0.197	0.319

```
In [20]: #plot of ARMA model
plt.figure(figsize=(20,10))
fig, ax = plt.subplots()
# ax = df_price_date['SALE_PRICE_LOGGED'].plot(ax=ax, title='FORECAST')
ax = df_price_date['SALE_PRICE'].plot(ax=ax, title='FORECAST', figsize=(15,5))
fig = ar.plot_predict(365, 395, dynamic=True, ax=ax, plot_insample=True)

handles, labels = ax.get_legend_handles_labels()
labels = ['SALE_PRICE', 'FORECAST and 95% confidence interval']
ax.legend(handles, labels)

plt.show()
```

<Figure size 1440x720 with 0 Axes>



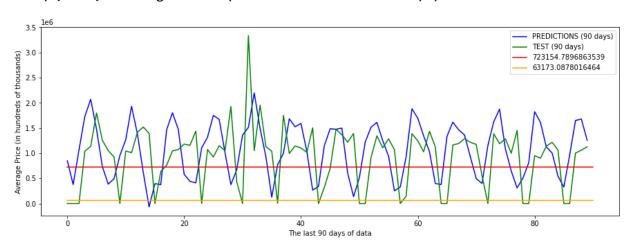
6. Error analysis of ARMA model

```
In [21]: | predictions = list(ar.predict(276, 365))
         test = list(df_price_date['SALE PRICE'][275:365])
         print("\033[1m" + '\033[4m'+ 'Length of Predictions' + "\033[0m", ': ', len(pred)
         print("\033[1m" + '\033[4m'+ 'Length of Test data' + "\033[0m", ': ', len(test))
         #RMSE
         mse = sklearn.metrics.mean_squared_error(test, predictions)
         rmse = math.sqrt(mse)
         print("\033[1m" + '\033[4m'+ 'RMSE' + "\033[0m", ': ', rmse)
         #standard error
         stderr = ar.bse.const
         print("\033[1m" + '\033[4m'+ 'Standard Error' + "\033[0m", ': ', stderr)
         #plot of all
         plt.figure(figsize=(15,5))
         plt.plot(predictions, label='PREDICTIONS (90 days)', color='blue')
         plt.plot(test, label='TEST (90 days)', color='green')
         x=[0,90]
         y=[rmse,rmse]
         plt.plot(x,y, label=rmse, color='red')
         x=[0,90]
         y=[stderr,stderr]
         plt.plot(x,y, label=stderr, color='orange')
         plt.legend(loc='best')
         plt.xlabel("The last 90 days of data")
         plt.ylabel("Average Price (in hundreds of thousands)")
```

Length of Predictions: 90 Length of Test data: 90 RMSE: 723154.7896863539

<u>Standard Error</u>: 63173.0878016464

Out[21]: Text(0, 0.5, 'Average Price (in hundreds of thousands)')



Observation:

RMSE is not too high and not too low compared to the data. Does not indicate a bad fit nor a good fit

- RMSE is 723154.8
- · Standard error is 63173.1

6a. Testing parameters to improve ARMA model

- I will try p of 9 per ACF
- I will try q of 9 per PACF
- I will try d = 7 to difference weekly

```
In [25]: # Instantiate & fit model with statsmodels
         \#p = num \ Lags - ACF
         p = 9
         # q = lagged forecast errors - PACF
         q = 9
         #d = number of differences
         d = 7
         # Fitting ARMA model and summary
         ar1 = ARMA(df_price_date['SALE PRICE'],(p,d,q)).fit()
         ar1.summary()
```

Out[25]: ARMA Model Results

Dep. Variable:	SALE PRICE	No. Observations:	365
Model:	ARMA(9, 7)	Log Likelihood	-5591.866
Method:	css-mle	S.D. of innovations	1071076.702
Date:	Sun, 20 Jun 2021	AIC	11219.731
Time:	15:47:15	BIC	11289.929
Sample:	04-01-2020	HQIC	11247.629
	- 03-31-2021		

	coef	std err	z	P> z	[0.025	0.975]
const	1.07e+06	312.772	3420.002	0.000	1.07e+06	1.07e+06
ar.L1.SALE PRICE	-0.1020	2.44e-05	-4171.827	0.000	-0.102	-0.102
ar.L2.SALE PRICE	0.0734	6.49e-05	1131.002	0.000	0.073	0.074
ar.L3.SALE PRICE	-0.0284	4.52e-05	-628.503	0.000	-0.028	-0.028
ar.L4.SALE PRICE	-0.0871	5.2e-05	-1674.051	0.000	-0.087	-0.087
ar.L5.SALE PRICE	-0.0650	nan	nan	nan	nan	nan
ar.L6.SALE PRICE	-0.0123	4.83e-05	-253.864	0.000	-0.012	-0.012
ar.L7.SALE PRICE	0.9356	nan	nan	nan	nan	nan
ar.L8.SALE PRICE	0.0120	7.6e-05	157.563	0.000	0.012	0.012
ar.L9.SALE PRICE	-0.1141	6.51e-05	-1753.442	0.000	-0.114	-0.114
ma.L1.SALE PRICE	0.0939	0.013	6.994	0.000	0.068	0.120
ma.L2.SALE PRICE	0.0164	0.013	1.222	0.222	-0.010	0.043
ma.L3.SALE PRICE	-0.0069	0.016	-0.445	0.657	-0.037	0.024
ma.L4.SALE PRICE	0.0802	0.015	5.405	0.000	0.051	0.109
ma.L5.SALE PRICE	0.0592	0.013	4.520	0.000	0.034	0.085
ma.L6.SALE PRICE	-0.0196	0.015	-1.345	0.178	-0.048	0.009
ma.L7.SALE PRICE	-0.9639	0.008	-125.340	0.000	-0.979	-0.949

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	-0.9023	-0.4356j	1.0020	-0.4284
AR.2	-0.9023	+0.4356j	1.0020	0.4284
AR.3	-0.2404	-0.9746j	1.0039	-0.2885
AR.4	-0.2404	+0.9746j	1.0039	0.2885
AR.5	0.6222	-0.7828j	1.0000	-0.1431
AR.6	0.6222	+0.7828j	1.0000	0.1431
AR.7	1.0659	-0.0000j	1.0659	-0.0000
AR.8	-2.8105	-0.0000j	2.8105	-0.5000

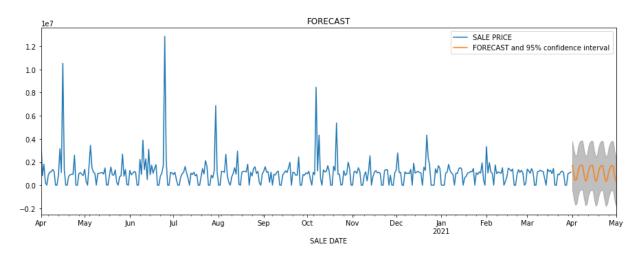
```
-0.0000j
                             2.8907
                                         -0.0000
AR.9
       2.8907
MA.1 -0.9008
                  -0.4342j
                             1.0000
                                         -0.4285
MA.2 -0.9008
                  +0.4342j
                             1.0000
                                          0.4285
MA.3 -0.2506
                  -0.9681j
                             1.0000
                                         -0.2903
      -0.2506
                 +0.9681j
                                          0.2903
MA.4
                             1.0000
                  -0.7826j
                             1.0000
MA.5
       0.6225
                                         -0.1431
MA.6
       0.6225
                  +0.7826j
                             1.0000
                                          0.1431
MA.7
       1.0375
                  -0.0000j
                              1.0375
                                         -0.0000
```

```
In [26]: #plot of ARMA model
   plt.figure(figsize=(20,10))
   fig, ax = plt.subplots()
   ax = df_price_date['SALE PRICE'].plot(ax=ax, title='FORECAST',figsize=(15,5))
   fig = ar1.plot_predict(365, 395, dynamic=True, ax=ax, plot_insample=True)

  handles, labels = ax.get_legend_handles_labels()
  labels = ['SALE PRICE', 'FORECAST and 95% confidence interval']
  ax.legend(handles, labels)

  plt.show()
```

<Figure size 1440x720 with 0 Axes>



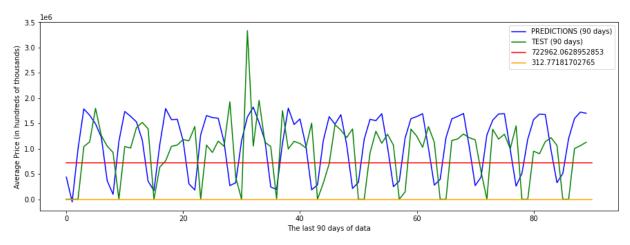
6a - Error Analysis of new model

```
In [27]: predictions = list(ar1.predict(276, 365))
          test = list(df_price_date['SALE PRICE'][275:365])
          print("\033[1m" + '\033[4m'+ 'Length of Predictions' + "\033[0m", ': ', len(pred)
          print("\033[1m" + '\033[4m'+ 'Length of Test data' + "\033[0m", ': ', len(test))
          #RMSE
          mse = sklearn.metrics.mean squared error(test, predictions)
          rmse = math.sqrt(mse)
          print("\033[1m" + '\033[4m'+ 'RMSE' + "\033[0m", ': ', rmse)
          #standard error
          stderr = ar1.bse.const
          print("\033[1m" + '\033[4m'+ 'Standard Error' + "\033[0m", ': ', stderr)
          #plot of all
          plt.figure(figsize=(15,5))
          plt.plot(predictions, label='PREDICTIONS (90 days)', color='blue')
plt.plot(test, label='TEST (90 days)', color='green')
          x=[0,90]
          y=[rmse,rmse]
          plt.plot(x,y, label=rmse, color='red')
          x=[0,90]
          y=[stderr,stderr]
          plt.plot(x,y, label=stderr, color='orange')
          plt.legend(loc='best')
          plt.xlabel("The last 90 days of data")
          plt.ylabel("Average Price (in hundreds of thousands)")
```

<u>Length of Predictions</u>: 90 <u>Length of Test data</u>: 90 <u>RMSE</u>: 722962.0628952853

Standard Error: 312.77181702765

Out[27]: Text(0, 0.5, 'Average Price (in hundreds of thousands)')



Observation:

• Here RMSE is lower than original model. We will stick with new model.

7. Comparing predictions with fresh data from June 2021 dataset (4/1/2021 - 4/31/2021)

Here I do the following:

- 1. Load data with only specific columns to borough
 - Sale price
 - · Sale data
 - Borough
- 2. Clean the data to get rid of issues when plotting/calculating errors

- This dataset was in .csv format, different from the origional rolling dataset
- · I had to filter the data and change columns from strings to int
- · Change 'SALE DATE' to datetime
- · Resample the data to match origional rolling data
 - aggregate by day
- 3. Plot the new data versus the predicted data and calculate RMSE

```
In [28]: #Loading the data and reset the index
         excel_df = pd.read_csv('NYC_Citywide_Rolling_Calendar_Sales.csv', usecols=['BOROL
         excel_df = excel_df[excel_df['BOROUGH']=='BROOKLYN']
         excel_df.reset_index(drop=True, inplace=True)
In [29]: #Fixes to the data
         excel_df['SALE PRICE'] = excel_df['SALE PRICE'].str.replace(',','')
         excel_df['SALE PRICE'] = excel_df['SALE PRICE'].astype(int)
         excel_df['SALE DATE'] = pd.to_datetime(excel_df['SALE DATE'])
In [30]: #Create new dataframe and aggregate to days like I did with origional rolling da
          excel_price_date = pd.DataFrame(excel_df, columns=['SALE DATE', 'SALE PRICE'])
          excel_price_date = excel_price_date.set_index('SALE DATE')
         #aggregate by day
         excel_price_date = excel_price_date.resample('D').mean()
In [31]: # Again, if I drop NaN here, it will change the dates which will affect the plot
         # I decide to fillna(0) similar to origional rolling data
         excel_price_date = excel_price_date.fillna(0)
In [32]: excel_price_date.head()
Out[32]:
                      SALE PRICE
          SALE DATE
           2020-05-01 9.110564e+05
           2020-05-02 1.650000e+05
           2020-05-03 0.000000e+00
           2020-05-04 6.289992e+05
           2020-05-05 1.752086e+06
```

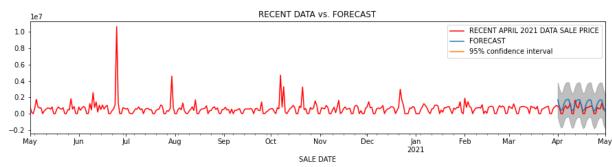
```
In [35]: # Plotting the data versus the ar.plot_predict values

fig, ax = plt.subplots()

ax = excel_price_date['SALE PRICE'].plot(title='RECENT DATA vs. FORECAST', colorating = ar1.plot_predict(365, 395, dynamic=True, ax = ax, plot_insample=True)

handles, labels = ax.get_legend_handles_labels()
labels = ['RECENT APRIL 2021 DATA SALE PRICE', 'FORECAST','95% confidence interval ax.legend(handles, labels)

plt.show()
```



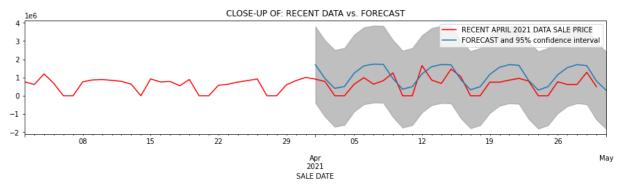
```
In [36]: # Plotting the data versus the ar.plot_predict values
#Here I do a close up

fig, ax = plt.subplots()

ax = excel_price_date['SALE PRICE'][305:365].plot(title='CLOSE-UP OF: RECENT DAT/
fig = ar1.plot_predict(365, 395, dynamic=True, ax = ax, plot_insample=True)

handles, labels = ax.get_legend_handles_labels()
labels = ['RECENT APRIL 2021 DATA SALE PRICE', 'FORECAST and 95% confidence intel
ax.legend(handles, labels)

plt.show()
```



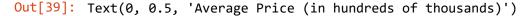
Observation

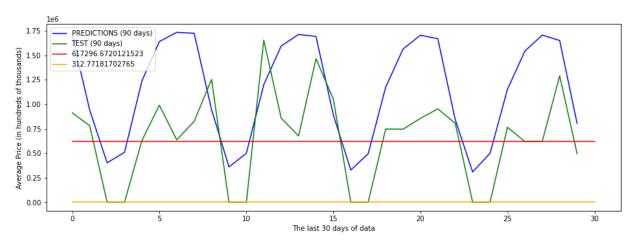
• We see that the model looks like it fits well versus the test data of 4/1/2021 until 4/31/2021

```
In [39]: | #RMSE, Standard error
          # Last 30 days of data
          predictions = list(ar1.predict(365, 394))
          test = list(excel_price_date['SALE PRICE'][335:365])
          print("\033[1m" + '\033[4m'+ 'Length of Predictions' + "\033[0m", ': ', len(pred: print("\033[1m" + '\033[4m'+ 'Length of Test data' + "\033[0m", ': ', len(test))
          #RMSE
          mse = sklearn.metrics.mean_squared_error(test, predictions)
          rmse = math.sqrt(mse)
          print("\033[1m" + '\033[4m'+ 'RMSE' + "\033[0m", ': ', rmse)
          #standard error
          stderr = ar1.bse.const
          print("\033[1m" + '\033[4m'+ 'Standard Error' + "\033[0m", ': ', stderr)
          #plot of all
          plt.figure(figsize=(15,5))
          plt.plot(predictions, label='PREDICTIONS (90 days)', color='blue')
          plt.plot(test, label='TEST (90 days)', color='green')
          x=[0,30]
          y=[rmse,rmse]
          plt.plot(x,y, label=rmse, color='red')
          x=[0,30]
          y=[stderr,stderr]
          plt.plot(x,y, label=stderr, color='orange')
          plt.legend(loc='best')
          plt.xlabel("The last 30 days of data")
          plt.ylabel("Average Price (in hundreds of thousands)")
```

Length of Predictions : 30
Length of Test data : 30
RMSE : 617296.6720121523

Standard Error: 312.77181702765





Observation

1. RMSE is lower here when comparing the new month data with predicted values

8. Observations/Conclusions/Recommendations

- 1. The point of this analysis was to see if the borough was good to invest in $\ensuremath{\mathsf{S}}$
- 2. Based on the model:
 - We can enter to buy or exit to sell based on when the market will do well
- 3. The borough sales look predictable
 - There is predicable fluctuation in Brooklyn
- 4. We can look at the top 10 building permit heavy locations further