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In[5]:= GeneralLinearAnizatrophy[α0_, U0_, χ0_, θ0_, β0_, P0_] :=
Module[
{α = α0, U = U0, χ = χ0, θ = θ0, β = β0, P = P0},

(*α - dissipation, α=v/ω, ω→ω(1+iα)*)
(*U - anizatrophy: p^2=4πε^2*n/m, b=eB/(mc), v=p^2/ω^2,
u=b^2/ω^2, and with dissipation: v→v(1-iα), u→U(1-iα)*)
(*χ - dimensionless wave vector magnitude; χ=k0L, and L=1*)
(*θ - ngl between wave vector and XOZ*)
(*β - angle between wave vector and magnetic field direction*)
(*P - wave polarisation; 2d-vector*)

(*=====
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(*Plasma configuration*)
X = 3; (*plasma boundary*)
Δ = 0.05; (*smoothing width, in parts of plasma whight*)

n = 1 / Δ; smoothingFunc = Function[x, (1 - (x/X)^2n)^-1];

v = Function[x, (x^2 - 1) * smoothingFunc[x] * (1 - i * α)]; u = U (1 - i * α);

Eps = 
$$\begin{pmatrix} 1 - \frac{v[x]}{1-u} & i \frac{\sqrt{u}}{1-u} v[x] & 0 \\ -i \frac{\sqrt{u}}{1-u} v[x] & 1 - \frac{v[x]}{1-u} & 0 \\ 0 & 0 & 1 - v[x] \end{pmatrix};$$


(*Plot[{Re[Eps[[3,3]]],Im[Eps[[3,3]]]},{x,-2X,2X}]*)

(*=====
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(*Wave configuration*)
A = 1; (*wave magnitude*)
k = χ 
$$\begin{pmatrix} \cos[\theta] \sin[\beta] \\ \sin[\theta] \\ \cos[\theta] \cos[\beta] \end{pmatrix}^T[[1]]; (*wave vector*)$$


E = 
$$\frac{A}{\text{Norm}[P]} \begin{pmatrix} \cos[\beta] & -\sin[\theta] \sin[\beta] \\ 0 & \cos[\theta] \\ -\sin[\beta] & -\sin[\theta] \cos[\beta] \end{pmatrix} \cdot P;$$


(*Electric field (!!!ESCAPE_SEQUENCE!!!)*)
B = 
$$\frac{\mathbf{k} \times \mathbf{E}}{\chi}; (*Magnetic field (!!!ESCAPE_SEQUENCE!!!)*)$$


(*=====
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(*Maxwell equations*)
GeneralSystem = {
(*Ex[x]*Eps[x][[1,1]]+Ey[x]*Eps[x][[1,2]]==kz*By[x]-ky*Bz[x],
Bx[x]==ky*Ez[x]-kz*Ey[x],*)
Ey'[x] == i * χ * 
$$\left( ky * \frac{(kz * By[x] - ky * Bz[x] - Ey[x] * Eps[[1, 2]])}{Eps[[1, 1]]} + Bz[x] \right),$$

(*Ey'[x]==i*χ*(ky*Ex[x]+Bz[x])*)

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Ez'[x] == i * chi * (kz * (kz * By[x] - ky * Bz[x] - Ey[x] * Eps[[1, 2]]) / Eps[[1, 1]] - By[x]),
(*Ez'[x] == i * chi * (kz * Ex[x] - By[x]) *)
By'[x] == i * chi * (ky * (ky * Ez[x] - kz * Ey[x]) - Eps[[3, 3]] * Ez[x]),
(*By'[x] == i * chi * (ky * Bx[x] - Eps[x][[3, 3]] * Ez[x]) *)
Bz'[x] == i * chi * (kz * (ky * Ez[x] - kz * Ey[x]) + Eps[[2, 1]] *
(kz * By[x] - ky * Bz[x] - Ey[x] * Eps[[1, 2]]) / Eps[[1, 1]] + Eps[[2, 2]] * Ey[x])
(*Bz'[x] == i * chi * (kz * Bx[x] + Eps[x][[2, 1]] * Ex[x] + Eps[x][[2, 2]] * Ey[x]) *)
} /. {kx -> k[[1]] / chi, ky -> k[[2]] / chi, kz -> k[[3]] / chi};

GeneralInitials =
{Ey[2 X] == E[[2]], Ez[2 X] == E[[3]], By[2 X] == B[[2]], Bz[2 X] == B[[3]]};
Sol = NDSolveValue[{GeneralSystem, GeneralInitials},
{Ey, Ez, By, Bz}, {x, -2 X, 2 X}];

(*=====*)

(*Polarisation rotations*)
Transmitted =

If[P[[1]] == 0, Conjugate[P[[2]]] / Abs[P[[2]]], Conjugate[P[[1]]] / Abs[P[[1]]]] (P[[1]] / Norm[P])^T[[1]];

(*Transmitted wave*)
IW =
( (Cos[beta] 0 -Sin[beta]
-Sin[beta] Sin[theta] Cos[theta] -Cos[beta] Sin[theta]) . ( (kz*By[x]-ky*Bz[x]-Ey[x]*Eps[[1,2]]) / Eps[[1,1]]
Ey[x]
Ez[x] ) )^T[[1]] /. {kx -> k[[1]] / chi, ky -> k[[2]] / chi, kz -> k[[3]] / chi, Ey[x] -> Sol[[1]][x],
Ez[x] -> Sol[[2]][x], By[x] -> Sol[[3]][x], Bz[x] -> Sol[[4]][x]};
IP =
(a /. NSolve[{a * Exp[i * k[[1]] (-2 X)] + b * Exp[-i * k[[1]] (-2 X)] == IW[[1]] /. x ->
(a /. NSolve[{a * Exp[i * k[[1]] (-2 X)] + b * Exp[-i * k[[1]] (-2 X)] == IW[[2]] /. x ->
})^T[[1]];
Initial =

If[IP[[1]] == 0, Conjugate[IP[[2]]] / Abs[IP[[2]]], Conjugate[IP[[1]]] / Abs[IP[[1]]]] (IP[[1]] / Norm[IP])^T[[1]];

(*Initial wave*)
RW = ( (Cos[pi - beta] 0 -Sin[pi - beta]
-Sin[pi - beta] Sin[-theta] Cos[-theta] -Cos[pi - beta] Sin[-theta]) . ( (kz*By[x]-ky*Bz[x]-Ey[x]*Eps[[1,2]]) / Eps[[1,1]]
Ey[x]
Ez[x] ) )^T[[1]] /.
{kx -> k[[1]] / chi, ky -> k[[2]] / chi, kz -> k[[3]] / chi, Ey[x] -> Sol[[1]][x],
Ez[x] -> Sol[[2]][x], By[x] -> Sol[[3]][x], Bz[x] -> Sol[[4]][x]};

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RP =
  ( b /. NSolve[{a * Exp[i * k[[1]] (-2 X)] + b * Exp[-i * k[[1]] (-2 X)] == RW[[1]] /. x ->
    b /. NSolve[{a * Exp[i * k[[1]] (-2 X)] + b * Exp[-i * k[[1]] (-2 X)] == RW[[2]] /. x ->
      })^T[[1]];
Reflected =
  If[RP[[1]] == 0,  $\frac{\text{Conjugate}[RP[[2]]]}{\text{Abs}[RP[[2]]]}$ ,  $\frac{\text{Conjugate}[RP[[1]]]}{\text{Abs}[RP[[1]]]}$  ]  $\left( \begin{array}{c} \frac{RP[[1]]}{\text{Norm}[RP]} \\ \frac{RP[[2]]}{\text{Norm}[RP]} \end{array} \right)^T[[1]]$ ;

(*Reflected wave*)
(*Dissipation*)
Dissipation = 1 -  $\frac{\text{Norm}[RP]}{\text{Norm}[IP]}$ ;

(*=====
=====*)

{Eps, k, Sol, Initial, Reflected, Transmitted, Dissipation}

]

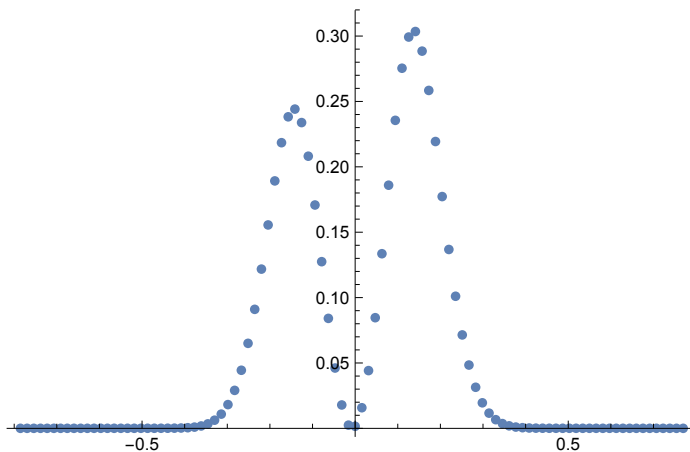
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In[102]:= DissipationFromΘ = {};
beginning = -π / 4; end = π / 4; nstep = 100;
ProgressIndicator[Dynamic[(Θ - beginning) / (end - beginning)]]
For[Θ = beginning, Θ < end, Θ += (end - beginning) / nstep,
  DissipationFromΘ = Append[DissipationFromΘ,
    {Θ, GeneralLinearAnizatrophy[0.000001, 0.000001, 30, Θ,  $\frac{\pi}{2}$ , {0, 1}][[7]]}];
];
ListPlot[DissipationFromΘ, PlotRange -> Full]

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Out[104]=



Out[106]=