

# BnB algorithm for QWSRM problem

**Input:**  $Q_{init}$ ,  $\mathcal{A}$ , and  $\{(c)\}$ .

**Initialize:** Obtain  $c_i$  by solving  $\frac{\delta f(c)}{\delta c_i} = 0$ , for  $i \in \mathcal{N}$ . Set  $k = 1, \mathcal{B} = Q_{init}, u_1 = \gamma_{ub}(Q_{init})$  and  $l_1 = \gamma_{lb}(Q_{init})$ .

Check the feasibility of problem (17) with given

**if feasible then**

$c_0 = \tilde{c}$ ;

**else**

**while**  $u_k - l_k > \epsilon$  **do**

Branching:

- Set  $Q_k = Q$ , where  $Q$  satisfies  $\gamma_{lb}(Q) = l_k$ .
- Split  $Q$  into  $Q_I$  and  $Q_{II}$ , along one of its longest edges.
- Update  $\mathcal{B}_{k+1} = (\mathcal{B}_k \setminus \{Q_k\}) \cup (Q_I, Q_{II})$ .

Bounding:

- Update  $u_{k+1} = \min_{Q \in \mathcal{B}_{k+1}} \{\gamma_{ub}(Q)\}$
- Update  $l_{k+1} = \min_{Q \in \mathcal{B}_{k+1}} \{\gamma_{lb}(Q)\}$

**end while**

Set  $c_0 = c_{min}$ ;

**end if**

**Output:**  $c_0$ .