

# Convex Hull

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11:11 PM

## 1. Code

```
using System;
using System.Collections.Generic;
using System.Text;
using System.Drawing;
using System.Linq;
using _1_convex_hull;

namespace _2_convex_hull
{
    class ConvexHullSolver
    {
        System.Drawing.Graphics g;
        System.Windows.Forms.PictureBox pictureBoxView;

        public ConvexHullSolver(System.Drawing.Graphics g, System.Windows.Forms.PictureBox pictureBoxView)
        {
            this.g = g;
            this.pictureBoxView = pictureBoxView;
        }

        public void Refresh()
        {
            // Use this especially for debugging and whenever you want to see what you have drawn so far
            pictureBoxView.Refresh();
        }

        public void Pause(int milliseconds)
        {
            // Use this especially for debugging and to animate your algorithm slowly
            pictureBoxView.Refresh();
            System.Threading.Thread.Sleep(milliseconds);
        }

        public void Solve(List<System.Drawing.PointF> pointList)
        {
            List<System.Drawing.PointF> sortedPoints = pointList.OrderBy(o => o.X).ToList();
            ConvexHull hull = DivideAndConquer(sortedPoints);
            Draw(hull);
        }

        private ConvexHull DivideAndConquer(List<System.Drawing.PointF> p_pointList)
        {
            {
                if (p_pointList.Count == 2)
                {
                    MakeClockwise(p_pointList);
                    return new ConvexHull(p_pointList);
                }
                else if (p_pointList.Count == 3)
                {
                    MakeClockwise(p_pointList);
                    return new ConvexHull(p_pointList);
                }
                else
                {
                    int midpoint;
                    ConvexHull leftHull;
                    ConvexHull rightHull;

                    if (p_pointList.Count % 2 == 1)
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    {
        midpoint = (p_pointList.Count / 2) + 1;
        leftHull = DivideAndConquer(p_pointList.GetRange(0, midpoint));
        rightHull = DivideAndConquer(p_pointList.GetRange(midpoint, midpoint-1));
    }
    else
    {
        midpoint = p_pointList.Count / 2;
        leftHull = DivideAndConquer(p_pointList.GetRange(0, midpoint));
        rightHull = DivideAndConquer(p_pointList.GetRange(midpoint, midpoint));
    }

    return Merge(leftHull, rightHull);
}
}

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private ConvexHull Merge(ConvexHull p_left, ConvexHull p_right)
{
    FindUpperTangent(p_left, p_right);
    FindLowerTangent(p_left, p_right);
    List<PointF> newHullPoints = new List<PointF>();

    List<PointF> leftList = p_left.Points;
    int leftStartIndex = leftList.IndexOf(p_left.UpperTangentPoint);
    int leftIndex = leftStartIndex;
    int leftEndIndex = leftList.IndexOf(p_left.LowerTangentPoint);

    if (leftList.Count < 4)
    {
        while (leftIndex != leftEndIndex)
        {
            newHullPoints.Add(leftList[leftIndex]);
            leftIndex--;
            if (leftIndex < 0)
            {
                leftIndex = leftList.Count - 1;
            }
        }
        newHullPoints.Add(leftList[leftEndIndex]);
    }
    else
    {
        for (int i = 0; i <= leftEndIndex; i++)
        {
            newHullPoints.Add(leftList[i]);
        }
        for (int i = leftStartIndex; i < leftList.Count; i++)
        {
            //newHullPoints.Add(leftList[leftIndex]);
        }
    }

    List<PointF> rightList = p_right.Points;
    int rightStartIndex = rightList.IndexOf(p_right.LowerTangentPoint);
    int rightIndex = rightStartIndex;
    int rightEndIndex = rightList.IndexOf(p_right.UpperTangentPoint);

    if (rightList.Count < 4)
    {
        while (rightIndex != rightEndIndex)
        {
            newHullPoints.Add(rightList[rightIndex]);
            rightIndex--;
            if (rightIndex < 0)
            {

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        rightIndex = rightList.Count - 1;
    }
}
newHullPoints.Add(rightList[rightEndIndex]);
}

return new ConvexHull(newHullPoints);
}

private void FindUpperTangent(ConvexHull p_left, ConvexHull p_right)
{
    Boolean leftPointChange = true;
    Boolean rightPointChange = true;
    List<PointF> leftList = p_left.Points;
    List<PointF> rightList = p_right.Points;
    PointF leftPoint = p_left.Rightmost;
    PointF rightPoint = p_right.Leftmost;

    Boolean tangentChanged = true;
    while (tangentChanged) {
        float slope = CalculateSlope(leftPoint, rightPoint);
        float checkSlope = slope;
        int leftIndex = leftList.IndexOf(leftPoint) == 0 ? leftList.Count-1 : leftList.IndexOf(leftPoint) - 1;
        do {
            float currSlope = CalculateSlope(leftList[leftIndex], rightPoint);
            if (currSlope < checkSlope) {
                checkSlope = currSlope;
                leftPoint = leftList[leftIndex];
                leftPointChange = true;
                if (leftIndex == 0) {
                    leftIndex = leftList.Count;
                }
                leftIndex--;
            }
            else {
                leftPointChange = false;
            }
        } while (leftPointChange);

        int rightIndex = rightList.IndexOf(rightPoint) == rightList.Count - 1 ? 0 : rightList.IndexOf(rightPoint) + 1;
        do {
            float currSlope = CalculateSlope(leftPoint, rightList[rightIndex]);
            if (currSlope > checkSlope) {
                checkSlope = currSlope;
                rightPoint = rightList[rightIndex];
                rightPointChange = true;
                if (rightIndex == rightList.Count - 1) {
                    rightIndex = -1;
                }
                rightIndex++;
            }
            else {
                rightPointChange = false;
            }
        } while (rightPointChange);
        if (checkSlope != slope) {
            tangentChanged = true;
        }
        else {
            tangentChanged = false;
        }
    }
    p_left.UpperTangentPoint = leftPoint;
    p_right.UpperTangentPoint = rightPoint;
}

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}

private void FindLowerTangent(ConvexHull p_left, ConvexHull p_right)
{
    Boolean leftPointChange = false;
    Boolean rightPointChange = false;
    List<PointF> leftList = p_left.Points;
    List<PointF> rightList = p_right.Points;
    PointF leftPoint = p_left.Rightmost;
    PointF rightPoint = p_right.Leftmost;

    Boolean tangentChanged = true;
    while (tangentChanged)
    {
        float slope = CalculateSlope(leftPoint, rightPoint);
        int leftIndex = leftList.IndexOf(leftPoint) == leftList.Count - 1 ? 0 : leftList.IndexOf(leftPoint) + 1;
        float checkSlope = slope;
        do {
            float currSlope = CalculateSlope(leftList[leftIndex], rightPoint);
            if (currSlope > checkSlope) {
                checkSlope = currSlope;
                leftPoint = leftList[leftIndex];
                leftPointChange = true;
                if (leftIndex == leftList.Count - 1) {
                    leftIndex = -1;
                }
                leftIndex++;
            }
            else {
                leftPointChange = false;
            }
        } while (leftPointChange);

        int rightIndex = rightList.IndexOf(rightPoint) == 0 ? rightList.Count - 1 : rightList.IndexOf(rightPoint) - 1;
        do {
            float currSlope = CalculateSlope(leftPoint, rightList[rightIndex]);
            if (currSlope < checkSlope) {
                checkSlope = currSlope;
                rightPoint = rightList[rightIndex];
                rightPointChange = true;
                if (rightIndex == 0)
                {
                    rightIndex = rightList.Count;
                }
                rightIndex--;
            }
            else
            {
                rightPointChange = false;
            }
        } while (rightPointChange);

        if (checkSlope != slope)
        {
            tangentChanged = true;
        }
        else
        {
            tangentChanged = false;
        }
    }
    p_left.LowerTangentPoint = leftPoint;
    p_right.LowerTangentPoint = rightPoint;
}

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private float CalculateSlope(PointF leftPoint, PointF rightPoint)
{
    return ((leftPoint.Y - rightPoint.Y)/(rightPoint.X - leftPoint.X));
}

private void MakeClockwise(List<PointF> p_list)
{
    if (p_list.Count == 2)
    {
        float slope = CalculateSlope(p_list[0], p_list[1]);
        if (slope > 0)
        {
            PointF temp = p_list[0];
            //p_list[0] = p_list[1];
            //p_list[1] = temp;
        }
    }
    else
    {
        float slopeOne = CalculateSlope(p_list[0], p_list[1]);
        float slopeTwo = CalculateSlope(p_list[0], p_list[2]);
        if (slopeOne < slopeTwo)
        {
            PointF temp = p_list[1];
            p_list[1] = p_list[2];
            p_list[2] = temp;
        }
    }
}

public void Draw(ConvexHull p_hull)
{
    List<PointF> points = p_hull.Points;
    for (int i = 0; i < points.Count; i++)
    {
        PointF currPoint = points[i];
        PointF nextPoint;
        if (i == points.Count-1)
        {
            nextPoint = points[0];
        }
        else
        {
            nextPoint = points[i + 1];
        }
        g.DrawLine(Pens.Black, currPoint, nextPoint);
    }
}

class ConvexHull
{
    List<PointF> m_Points;
    PointF m_leftmost;
    PointF m_rightmost;
    PointF m_upperTangentPoint;
    PointF m_lowerTangentPoint;

    public ConvexHull() { }

    public ConvexHull(List<PointF> _list)
    {

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        m_Points = _list;
        m_leftmost = findLeftMost();
        m_rightmost = findRightMost();
        if (_list.Count == 3)
        {
            MakeClockwise();
        }
    }

private void MakeClockwise()
{
    if (m_Points.Count == 2)
    {
        float slope = CalculateSlope(m_Points[0], m_Points[1]);
        if (slope > 0)
        {
            PointF temp = m_Points[0];
            //m_Points[0] = m_Points[1];
            //m_Points[1] = temp;
        }
    }
    else
    {
        float slopeOne = CalculateSlope(m_Points[0], m_Points[1]);
        float slopeTwo = CalculateSlope(m_Points[0], m_Points[2]);
        if (slopeOne < slopeTwo)
        {
            PointF temp = m_Points[1];
            m_Points[1] = m_Points[2];
            m_Points[2] = temp;
        }
    }
}

public List<PointF> Points { get => m_Points; set => m_Points = value; }
public PointF Leftmost { get => m_leftmost; set => m_leftmost = value; }
public PointF Rightmost { get => m_rightmost; set => m_rightmost = value; }
public PointF UpperTangentPoint { get => m_upperTangentPoint; set => m_upperTangentPoint = value; }
public PointF LowerTangentPoint { get => m_lowerTangentPoint; set => m_lowerTangentPoint = value; }

private PointF findLeftMost()
{
    PointF leftMost = m_Points[0];
    for (int i = 0; i < m_Points.Count; i++)
    {
        if (m_Points[i].X < leftMost.X)
        {
            leftMost = m_Points[i];
        }
    }
    return leftMost;
}

private PointF findRightMost()
{
    PointF rightMost = m_Points[m_Points.Count-1];
    for (int i = 0; i < m_Points.Count; i++)
    {
        if (m_Points[i].X > rightMost.X)
        {
            rightMost = m_Points[i];
        }
    }
    return rightMost;
}

```

	<pre> private float CalculateSlope(PointF leftPoint, PointF rightPoint) {     return ((leftPoint.Y - rightPoint.Y) / (rightPoint.X - leftPoint.X)); } } </pre>
2. Time and Space Complexity	<p>DivideAndConquer: Space was <math>O(\log n)</math>. Time was <math>O(n \log n)</math></p> <p>Merge: ,</p> <p>FindUpperTangent: Worst case <math>O(n)</math> if each side moved on each iteration of the loop. But very unlikely. Probably closer to <math>O(\log n)</math> with large input size</p> <p>FindLowerTangent: Worst case <math>O(n)</math>, for same reasoning as finding the upper tangent. Average case <math>O(\log n)</math> for large input size.</p> <p>Draw:</p>
3. Raw and mean experimental outcomes, plot, and discussion	
4. Observations	
5. Screenshot	