

DiffieHellman

November 23, 2022

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[94]: p = 1117  
      g = 6  
      h = 527
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[117]: from math import ceil, sqrt  
  
class DiffieHellmanProtocol:  
    def __init__(self, p, g):  
        self.p=p  
        self.g=g  
  
    def potega_m(self, m):  
        """use python embedded function pow(a,b,n) === a~b (mod n)"""  
        return pow(self.g,m,self.p)  
  
    @staticmethod  
    def generator(g, p):  
        #Z_p* order = phi(p) = p-1  
        group_order = p-1  
        for i in range(1,g-1):  
            if (pow(g,i,p)==1):  
                return False  
        return pow(g,group_order,p)==1  
  
    @staticmethod  
    def gcdExtended(a, p):  
        """  
        Find such numbers x,y that: GCD(a,p) = a*x + b*y  
        where GCD(a,p) - greatest comon divisor of a and b  
        (Extended Euclidean algorithm)  
        """  
        if a == 0 :  
            return p,0,1  
        gcd,x1,y1 = DiffieHellmanProtocol.gcdExtended(p%a, a)  
        x = y1 - (p//a) * x1  
        y = x1  
        return gcd,x,y #x = a~-1
```

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@staticmethod
def euklid(a,p):
    """
    Use Euclidean algorithm for finding  $a^{-1}$ :
     $GCD(a,p) = 1 = a*a^{-1} + p*b \Leftrightarrow$ 
    solve  $a*a^{-1} \equiv 1 \pmod{p}$  where  $a^{-1}$  is a variable in  $Z_p$ 
    """
    return DiffieHellmanProtocol.gcdExtended(a,p)[1]%p

def findPower(self, h):
    """
    Solve the equation  $h = g^x \pmod{p}$  given a prime number  $p$ .

    For more detailed description, of the algorithm, see
    https://en.wikipedia.org/wiki/Baby-step\_giant-step#The\_algorithm
    """
    #  $\phi(p)$  is  $p-1$  if  $p$  is prime
    N = ceil(sqrt(self.p - 1))

    # Baby step:
    # Store hashmap of  $g^{\{1, \dots, m\}} \pmod{p}$ .
    tbl = {pow(self.g, i, self.p): i for i in range(N)}
    c = pow(self.g, N * (self.p - 2), self.p)

    # Giant step:
    # Search for an equivalence in the table.
    for j in range(N):
        y = (h * pow(c, j, self.p)) % self.p
        if y in tbl:
            a = j * N + tbl[y]
            assert pow(self.g, a, self.p) == h
            return a
    return None

if __name__ == "__main__":
    dh = DiffieHellmanProtocol(p,g)
    #  $g^a = h$ 
    a = dh.findPower(h)
    assert pow(g,a,p)==h
    print(a)

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