

Traffic Theory - Questions

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Comment the following statements providing a detailed explanation

- 1 Non irreducible Markov Chains can be ergodic
- 2 In Markov Chains the distribution of $X(n)$, knowing only $X(n-k), X(n-k-1), \dots, X(0)$, only depends on $X(n-k)$
- 3 In renewal arrivals the asymptotic probability of an arrival in t is zero.
- 4 The PASTA property holds for M/M/1 with finite population arrivals.
- 5 The average queuing time in an M/G/1 system can be changed by means of Service Disciplines
- 6 In Jackson's networks we can have queues with LCFS service disciplines
- 7 In Jackson networks we can not have a mix of users that behave as in open networks and closed networks: why?

Outline of the answers

- 1 FALSE. Non irreducible chains can have more asymptotic distributions, depending on initial conditions. Hence are not ergodic, which only have one.
- 2 TRUE. See property 1.53 in class notes
- 3 TRUE. The probability of an arrival in Δt is proportional to Δt , and goes to zero as Δt goes to zero.
- 4 FALSE. In the finite population model arrivals are not Poisson and the PASTA property can not hold. WE have actually evaluated distribution q_i , which is in fact different from distribution p_i
- 5 TRUE, provided that we adopt policies that are not SERVICE INDEPENDENT, such as SJF, or preemptive, such as Processor Sharing...
- 6 TRUE. As long as the occupancy is concerned, the state diagram of a Markovian queueing system, alone or in a network, is not changed by disciplines such as LCFS.