

Ensuring (Statistical) Privacy

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@ Harvard SEAS (School of Engineering and Applied Sciences)

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Code for this talk: https://github.com/alabid/pre_college_2019

See full course materials here: <http://people.seas.harvard.edu/~salil/cs208/> [some slides taken from here]

My website: <http://alabidan.me>

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 - Python Code

The Problem

We have a dataset with sensitive information, such as:

1. Health records (e.g. reveals which disease a patient has)
2. Census data (e.g. reveals income range)
3. Social network activity (e.g. which pages you like)

How can we allow:

1. Allow the use of the data?
2. Protect the privacy of the data subjects?
3. Achieve both (1) and (2)?

Some Approaches to Solve the Problem

Encrypt the Data:

Name	Sex	Blood	...	HIV?
James	O	B	...	N
Peter	M	O	...	Y
...
Paul	M	A	...	N
Eve	F	B	...	Y

Some Approaches to Solve the Problem

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Name	Sex	Blood	...	HIV?
10101	01010	01000	...	00001
11010	01101	10111	...	10111
...
10100	10000	11101	...	01111
11000	10001	11110	...	10001

Some Approaches to Solve the Problem

Encrypt the Data: Are we happy with this solution? Why or why not?

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Some Approaches to Solve the Problem

“Anonymize the Data”: Are we happy with this solution? Why or why not?

Name	Sex	Blood	...	HIV?
James	O	B	...	N
Peter	M	O	...	Y
...
Paul	M	A	...	N
Eve	F	B	...	Y



Name	Sex	Blood	...	HIV?
XXXXXX	O	B	...	N
XXXXXX	M	O	...	Y
...
XXXXXX	M	A	...	N
XXXXXX	F	B	...	Y

Some Approaches to Solve the Problem

“Anonymize the Data”: Not sufficient because of linkage attacks!

87% of US population have unique date of birth, gender, and postal code!

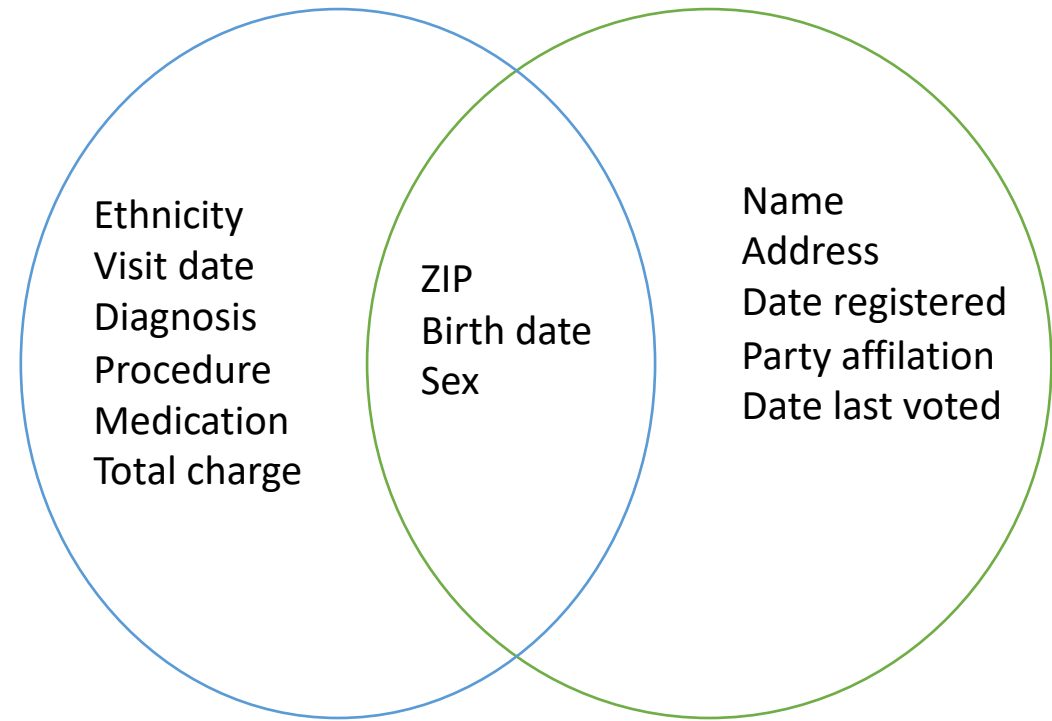
[Golle and Partridge 09]

Some Approaches to Solve the Problem

“Anonymize the Data”: Reidentification via Linkage

Can uniquely identify > 60% of the U.S. population [Sweeny '00, Golle '06, Sweeney '97]

Name	Sex	Blood	...	HIV?
XXXXXX	O	B	...	N
XXXXXX	M	O	...	Y
...
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Medical Data

Voter List

The story so far

- Motivations
 - Reidentification via Linkage Attacks
 - Reconstruction and Inference Attacks

Reconstruction attack: If we have dataset $x \in \{0, 1\}^n$ and person i has sensitive bit x_i and attacker/adversary gets $q_S(x) = \sum_{i \in S} x_i$ for any $S \subseteq [n]$.

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Inference attack: Attacker gets n^2 answers and needs to know if someone is in dataset or not.

The story so far

Message

Releasing too many statistics with too much accuracy can lead to a reconstruction of the entire dataset or inference attacks

Some Approaches to Solve the Problem

So now what?

- Encryption doesn't work
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Possible Responses:

- Privacy is an illusion!
- In the long run, it's better to use data for research! Ignore privacy!
- Never release statistics about any dataset!
- Is there a way to add enough noise to queries and still allow for usefulness?

Main Message of this Talk

Yes, there is a way to add enough noise to queries and still allow for usefulness?

An approach: K-anonymity

[Sweeney '02]: A mechanism satisfies k -anonymity if for every dataset, the output of the mechanism has the property that every distinct row occurs at least k times.

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Intuition: Privacy ensured if I can't isolate you!

An approach: K-anonymity

[Sweeney '02]: A mechanism satisfies k -anonymity if for every dataset, the output of the mechanism has the property that every distinct row occurs at least k times.

3-anonymous dataset:

Zip code	Age	Nationality
021**	< 30	*
021**	< 30	*
021**	< 30	*
021**	> 40	*
021**	> 40	*
021**	> 40	*
021**	3*	*
021**	3*	*
021**	3*	*

An approach: K-anonymity

It's a nice approach but doesn't:

- Compose well (e.g. if you have two k -anonymous datasets)
- Utility not as quantifiable as other approaches

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021**	< 30	*
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Differential Privacy

- Utility
- Privacy
- Definition

Differential Privacy

- Utility: enable “statistical analysis” on datasets
 - Can release (noisy) statistics such as means, sums, medians, etc.
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- Definition: pure and approximate

Differential Privacy

Definition: pure and approximate

[Dwork-McSherry-Nissim-Smith '06]

Other references:

Motivated from and based off of work in

[Dinur-Nissim '03, Dwork-Nissim '04, Blum-Dwork-McSherry-Nissim '05]

Differential Privacy

Definition: pure and approximate

[Dwork-McSherry-Nissim-Smith '06]

Intuition: for a statistic, the effect of each individual (whether in the dataset or not) should be close to nothing.

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Intuition: for a statistic, the effect of each individual (whether in the dataset or not) should be close to nothing.

Worst-case notion: protects against all possible adversaries and any kind of individual.

Differential Privacy

Definition: pure and approximate

[Dwork-McSherry-Nissim-Smith '06]

For any algorithm \mathcal{A} , it satisfies ϵ differential privacy if

For all datasets D, D' differing in exactly one row all queries q

Distribution of $\mathcal{A}(D, q)$ is at most ϵ away from $\mathcal{A}(D', q)$

The smaller ϵ is, the more privacy is ensured!

Differential Privacy

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Distribution of $\mathcal{A}(D, q)$ is at most ϵ away from $\mathcal{A}(D', q)$

For all sets T ,

$$\Pr[\mathcal{A}(D, q) \in T] \leq (1 + \epsilon) \Pr[\mathcal{A}(D', q) \in T]$$

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For all datasets D, D' differing in exactly one row all queries q

Distribution of $\mathcal{A}(D, q)$ is at most ϵ away from $\mathcal{A}(D', q)$

The probability is only over the randomness of the algorithm \mathcal{A}

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Mechanisms for Differential Privacy

Examples:

1. Laplace Mechanism [we'll discuss and implement this one!]
 2. Gaussian Mechanism
 3. Exponential Mechanism
 4. Geometric Mechanism
-

Laplace Mechanism

$\text{Lap}(s)$ is the Laplace Distribution with scale s .

Some properties:

- Has mean 0
- Has standard deviation $\sqrt{2} \cdot s$
- It's a “double-exponential” distribution

Laplace Mechanism for Sum and Average

1. $\mathcal{A}(x) = \sum_{i=1} x_i + \text{Lap}(\frac{1}{\epsilon})$
where $x_i \in [0, 1]$ for all $i \in [n]$.

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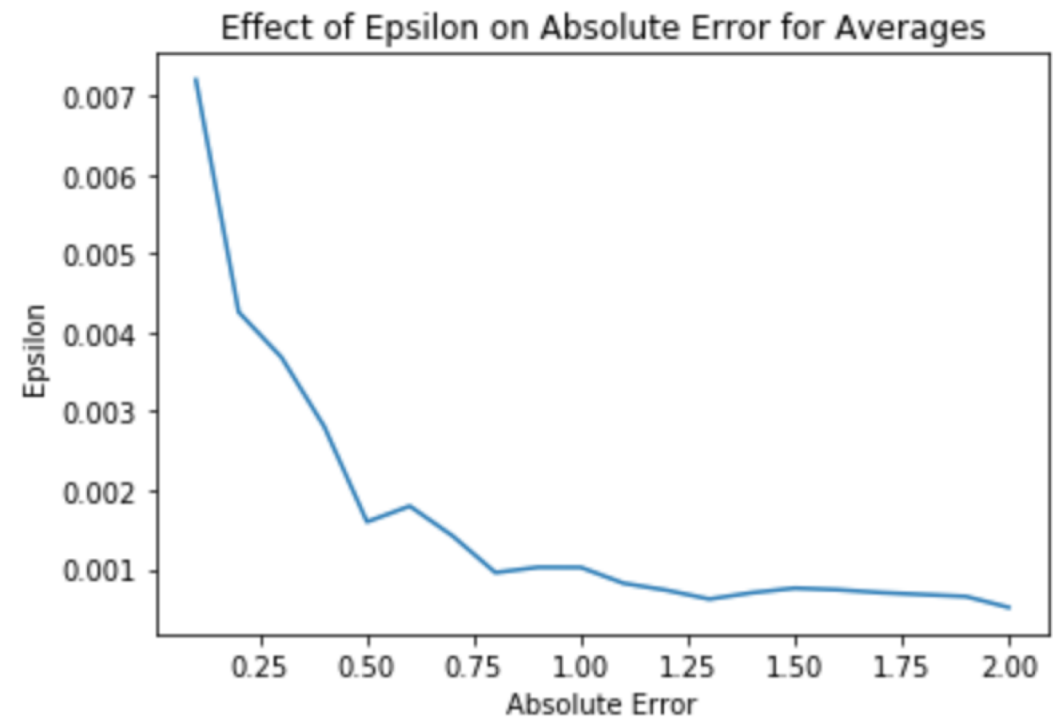
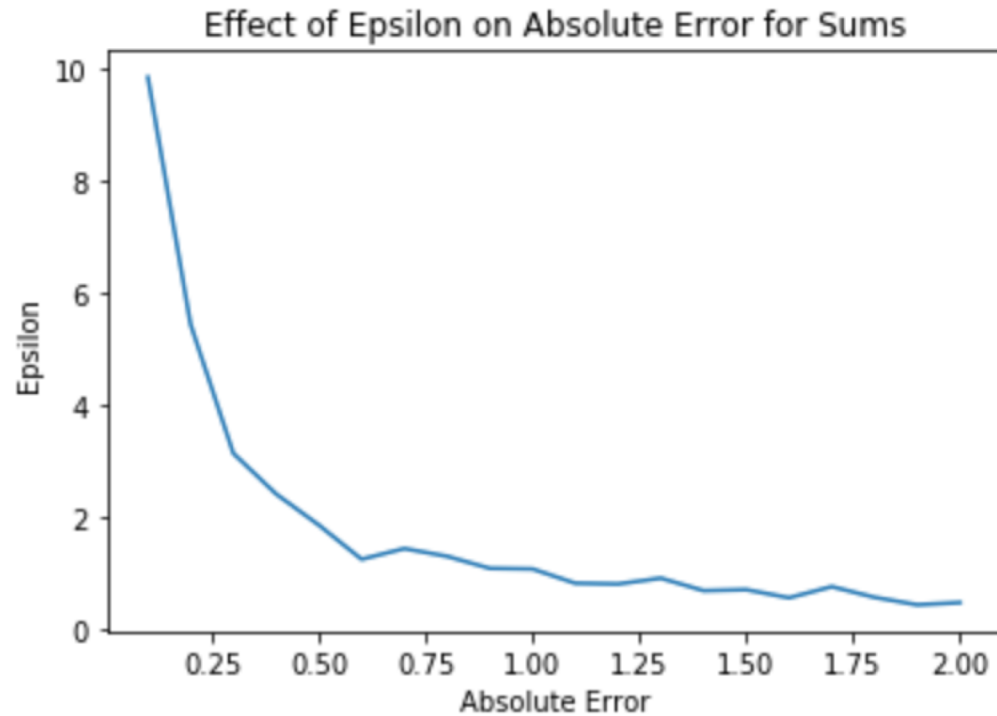
where $x_i \in [0, 1]$ for all $i \in [n]$.

2. $\mathcal{A}(x) = \frac{1}{n} \cdot \sum_{i=1} x_i + \text{Lap}(\frac{1}{n \cdot \epsilon})$

where $x_i \in [0, 1]$ for all $i \in [n]$.

Code Demonstration

- https://github.com/alabid/pre_college_2019



Conclusion

- Differential Privacy is a mathematically rigorous definition of individual data privacy.
- YOU can code it up. See GitHub page – clone it and play with the code there!

https://github.com/alabid/pre_college_2019

- It's being used by the U.S. Census Bureau (for the 2020 Decennial Census), Google, Apple.