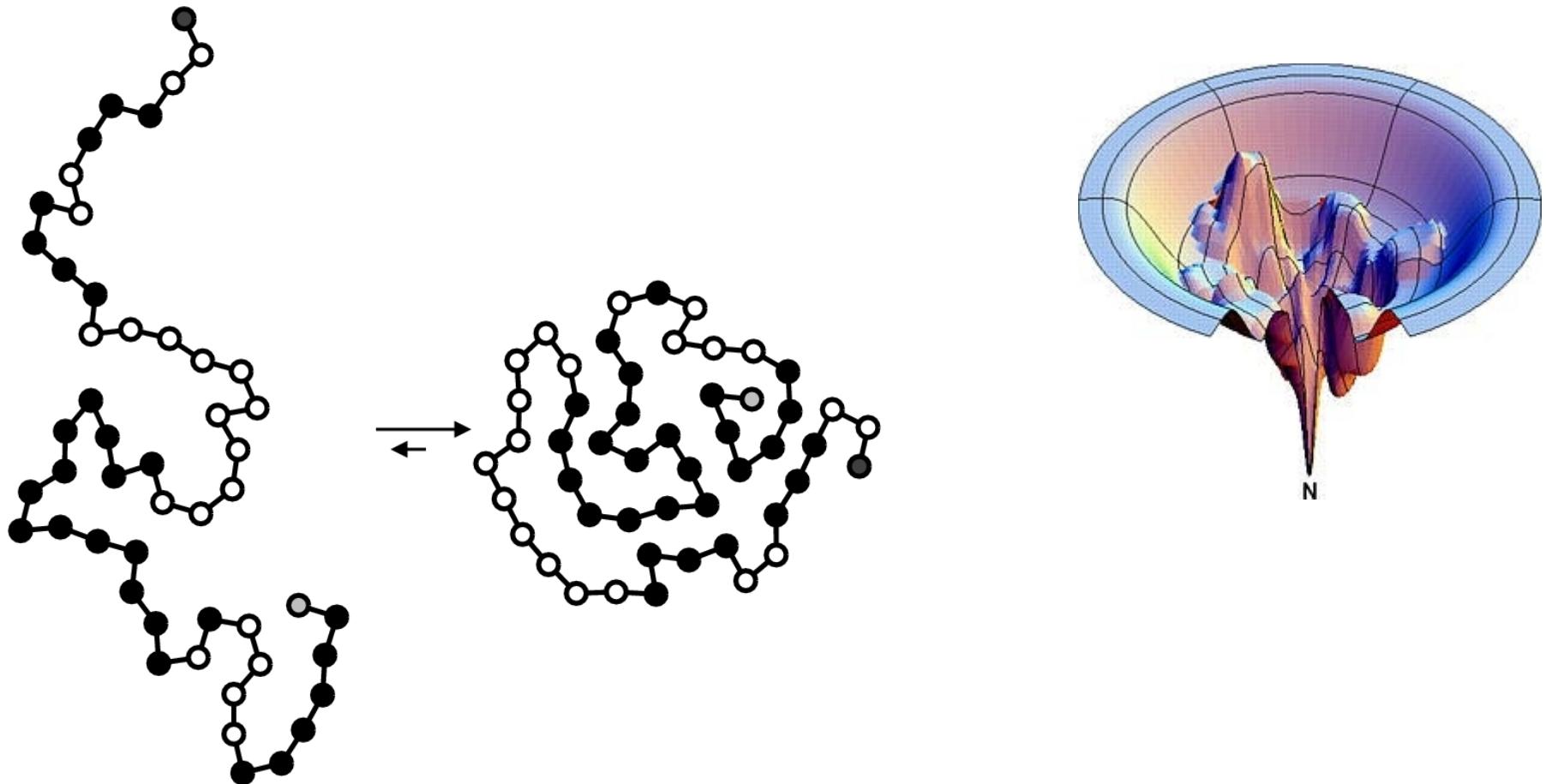


Wintersemester 2016/2017  
Biomolecular Engineering/Nanobiophysics  
Module

# LECTION 4: PROTEIN FOLDING



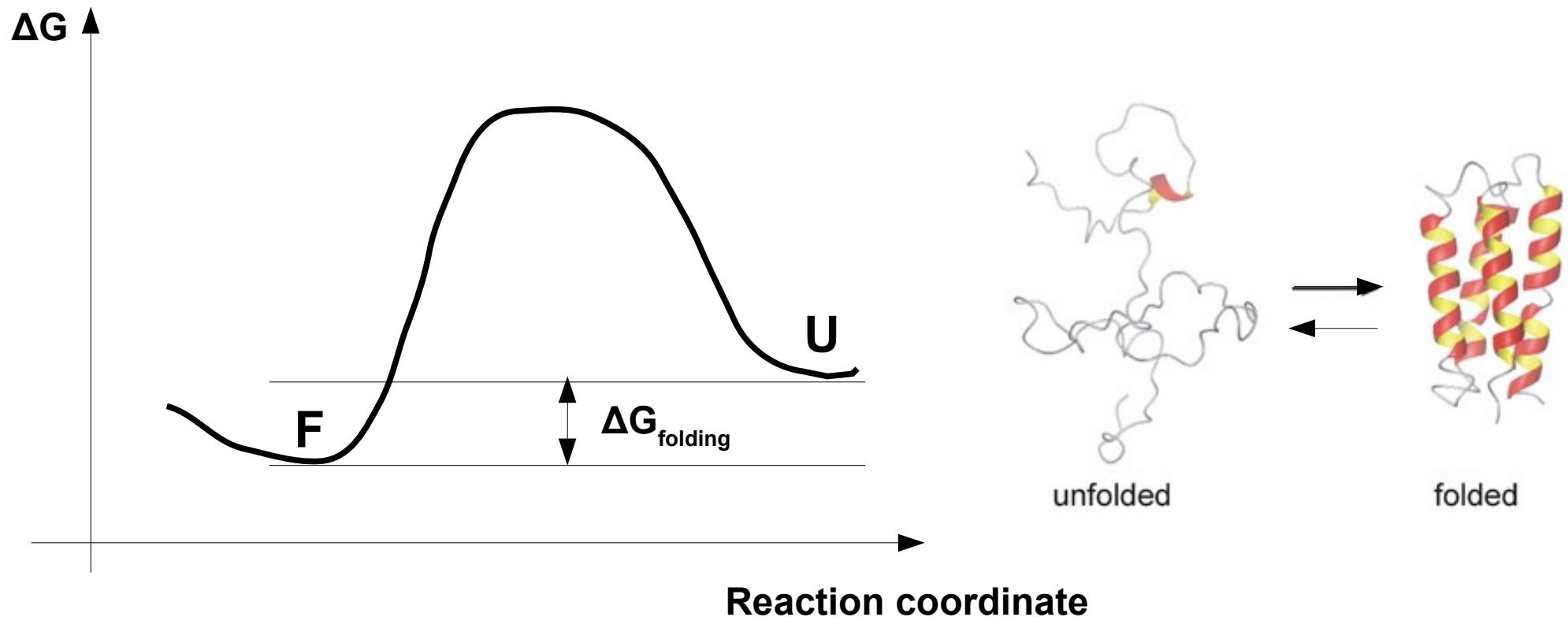
# LECTION 4: PROTEIN FOLDING

- Protein folding and denaturation
- Anfinsen's dogma
- Folding of  $\alpha$ - and  $\beta$ -secondary structures
- Hydrophobic effect
- Levinthal's paradox
- Protein vs other polymers
- Thermodynamics and kinetics of protein folding
- Protein folding in the cell
- Computational approaches to study folding
- CASP
- Case study: folding of an interdomain linker



# FOLDING AND DENATURATION

- Protein folding is the process by which a protein structure assumes its native (functional) conformation.
- Protein denaturation is the process by which a protein loses its native conformation.



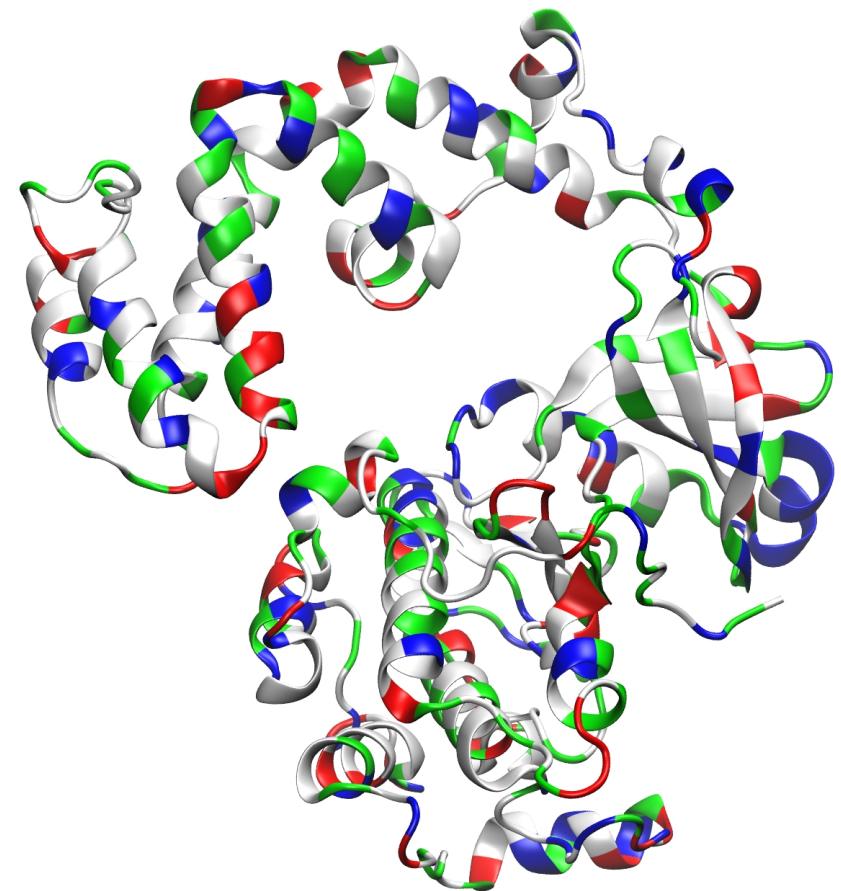
# FOLDING: 1D=>3D

AA sequence

```
>FASTER_FORMAT_SEQUENCE
MDFGSLETVVANSAFIAARGSFDAASSGPASRDRKYLARLKLPPLSKCEALR
ESLDLGFEGLMCLEQPIGKRLFQQFLRTHEQHGPALQLWKDIEDYDTADDAL
RPQKAQALRAAYLEPQAQLFCSFLDAETVARARAGAGDGLFQPLLRAVLAH
LGQAPFQEFLDSLYFLRFLQWKWLEAQPMGEDWFLDFRVLGRGGFGEVFAC
QMKTATGKLYACKKLNKKRLKKRKGYQGAMVEKKILAKVHSRFIVSLAYAFE
TKTDLCLVMTIMNGGDIRYHIYNVDEDNPGFQEPRAIIFYTAQIVSGLEHLH
QRNIYRDLKPENVLLDDDGNNVRISDLGLAVELKAGQTCKGYAGTPGFMA
PELLGEEYDFSVDYFALGVTLYEMIAARGPFRARGEKVENKELKQRVLEQ
AVTYPDKFSPASKDFCEALLQKDPEKRLGFRDGSCDGLRTHPLFRDISWRQ
LEAGMLTPPFVPDSRTVYAKNIQDVGAFTVKGVAFEKADTEFFQEFASGT
CPIPWQEEMIETGVFGDLNVWRPDGHHHHHH
```



Protein structure



- In general — NOW — computationally unfeasible task

# DENATURATION

➤ Caused by:

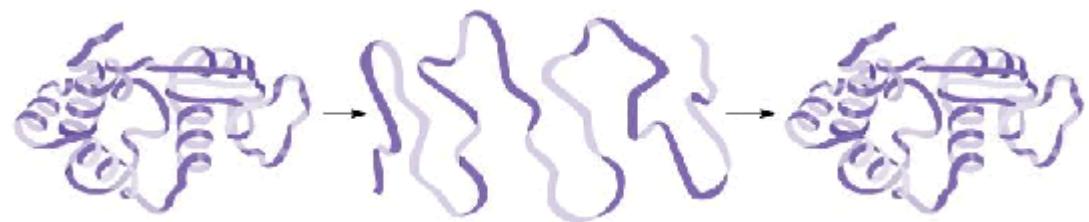
- temperature (high and low)
- pH
- ionic strength
- pressure



$$\Delta G = \Delta H - T\Delta S$$

➤ Reversibility:

- reversible
- irreversible

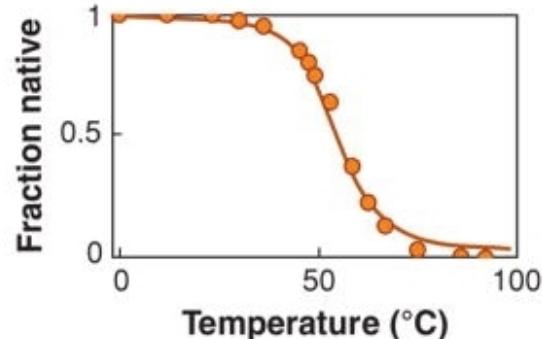
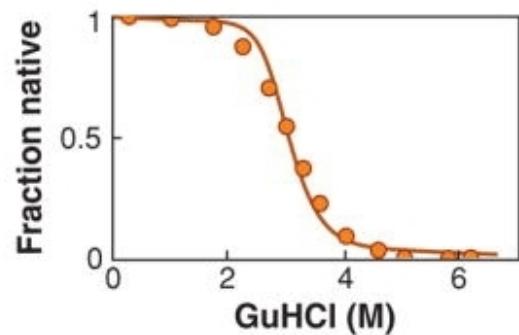


➤ Structural levels affected:

- Tertiary
- Secondary
- \* S-S bridges

➤ Structural levels not affected:

- Covalent bonds
- Primary structure



# PROTEIN STATES

## ➤ Native:

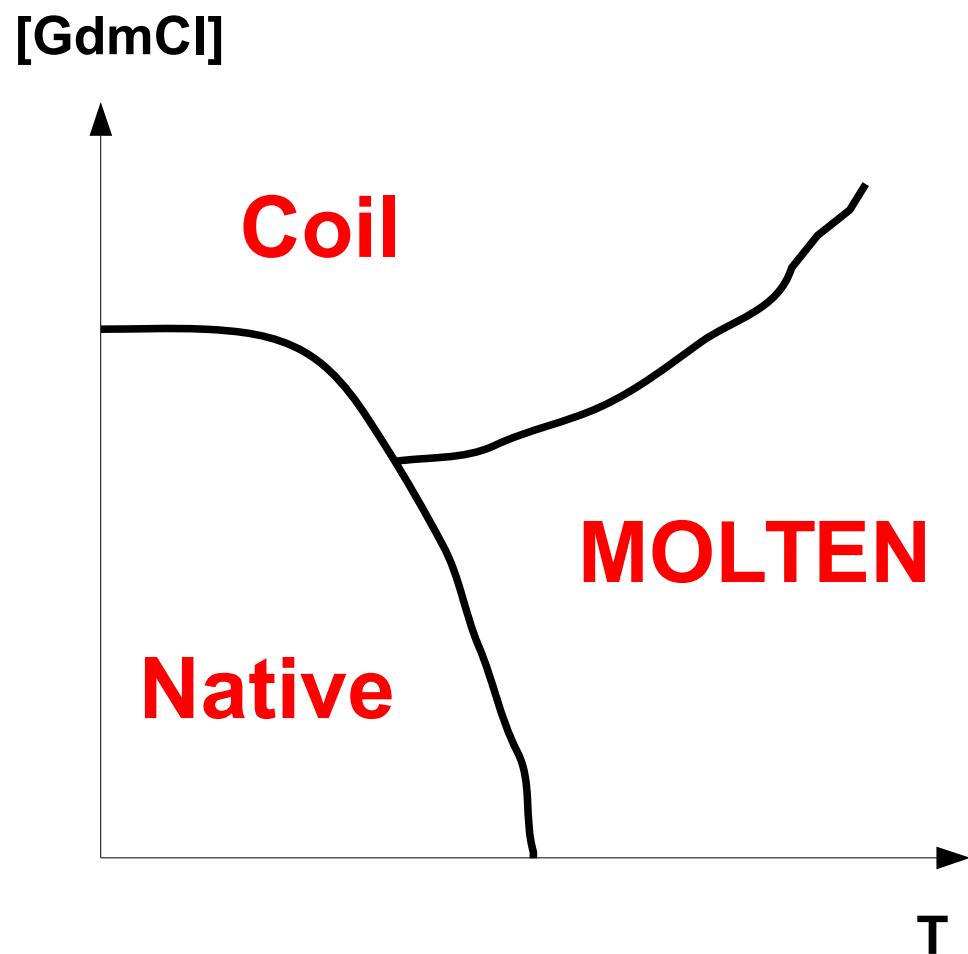
- native function
- accurately defined contacts/residus packing (CD, fluorescence)
- fixed H-exchange rate (NMR)

## ➤ Molten globule:

- still compact but no unique packing
- hydrophobic core fluctuates
- secondary structure, S-S bonds
- increased mobility of side-chains
- partial solvent accessibility of Trp
- absence of some «remote» contacts

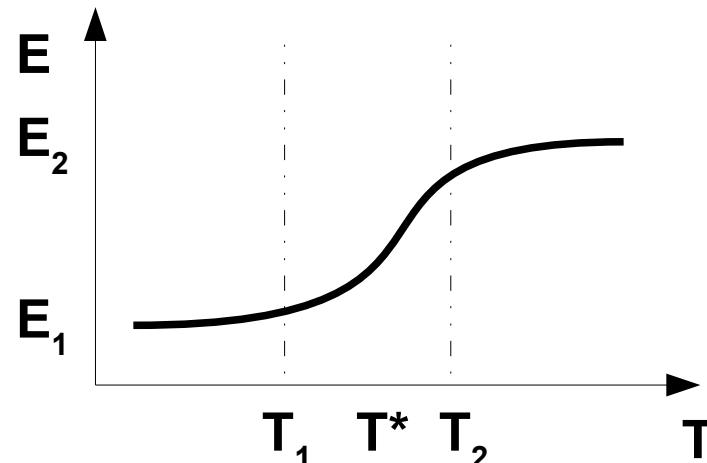
## ➤ Coil:

- function is lost
- most of contacts are lost
- secondary structure partly affected

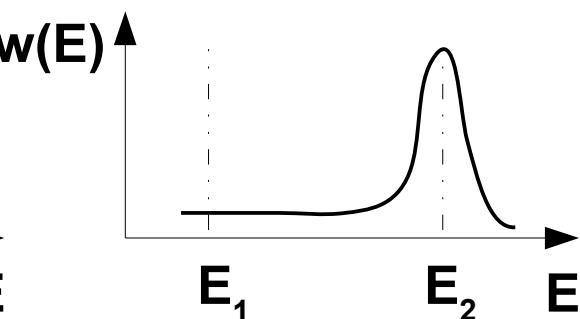
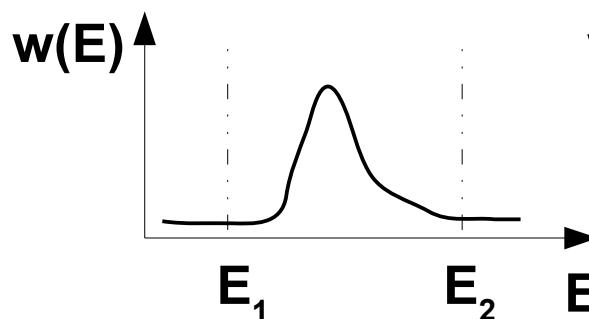
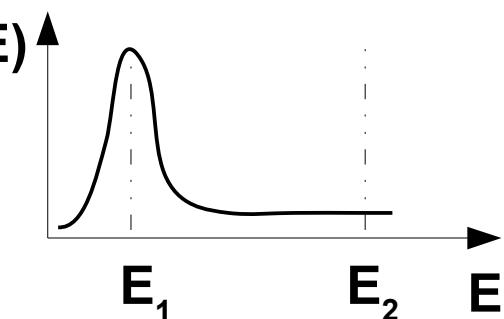


# TRANSITION: «ALL OR NOTHING»

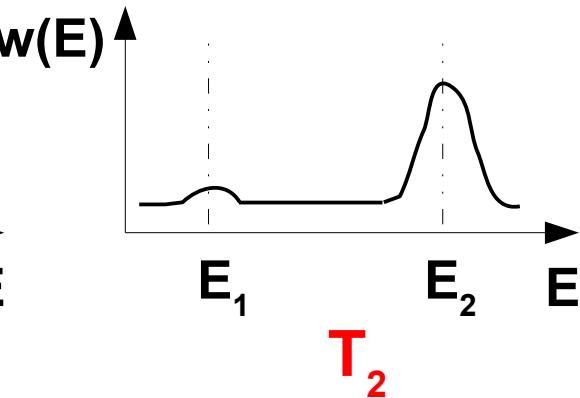
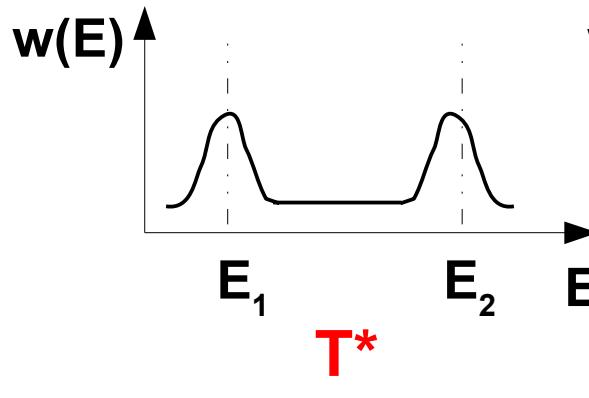
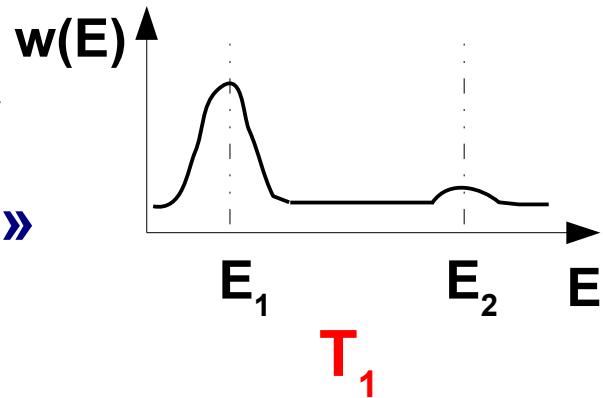
- Protein changes from not native to native state by dramatic change of properties: heat capacity, single molecule energy distribution etc.



**Gradual  
transition**

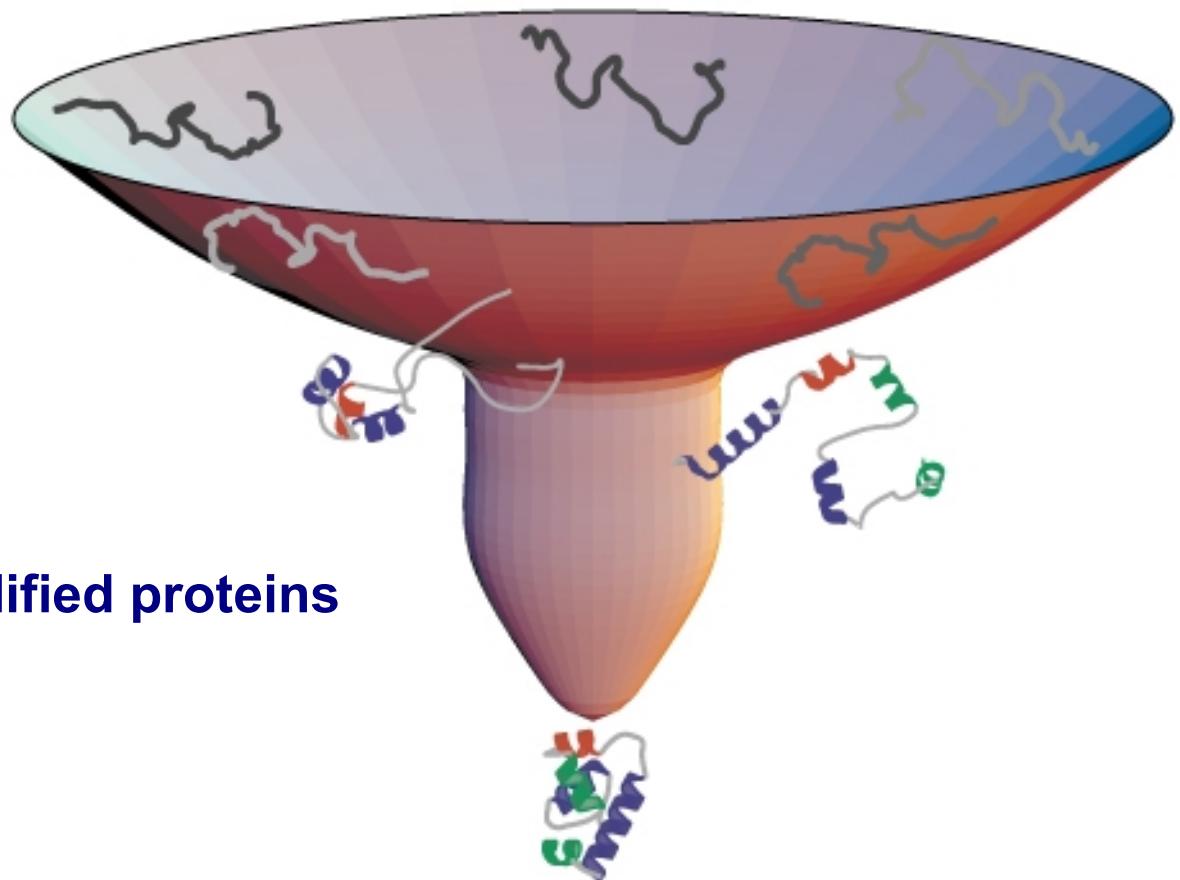


**«All or  
nothing»**



# ANFINSEN'S DOGMA

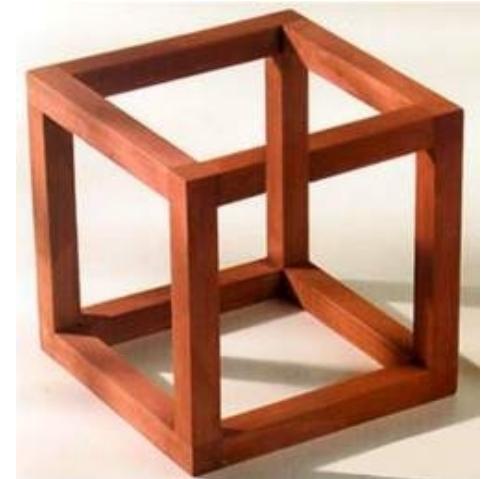
- Protein's native structure is determined by its aa sequence and it is:
  - unique
  - stable
  - kinetically accessible
- Anfinsen's experiment (1957):
  - Bovine ribonuclease A
  - Denaturation
  - Works for not covalently modified proteins
  - $\Delta G_{\text{folding}} \sim 1-10 \text{ kcal/mol}$



# LEVINTHAL'S PARADOX

➤ How much time needs protein to be folded?

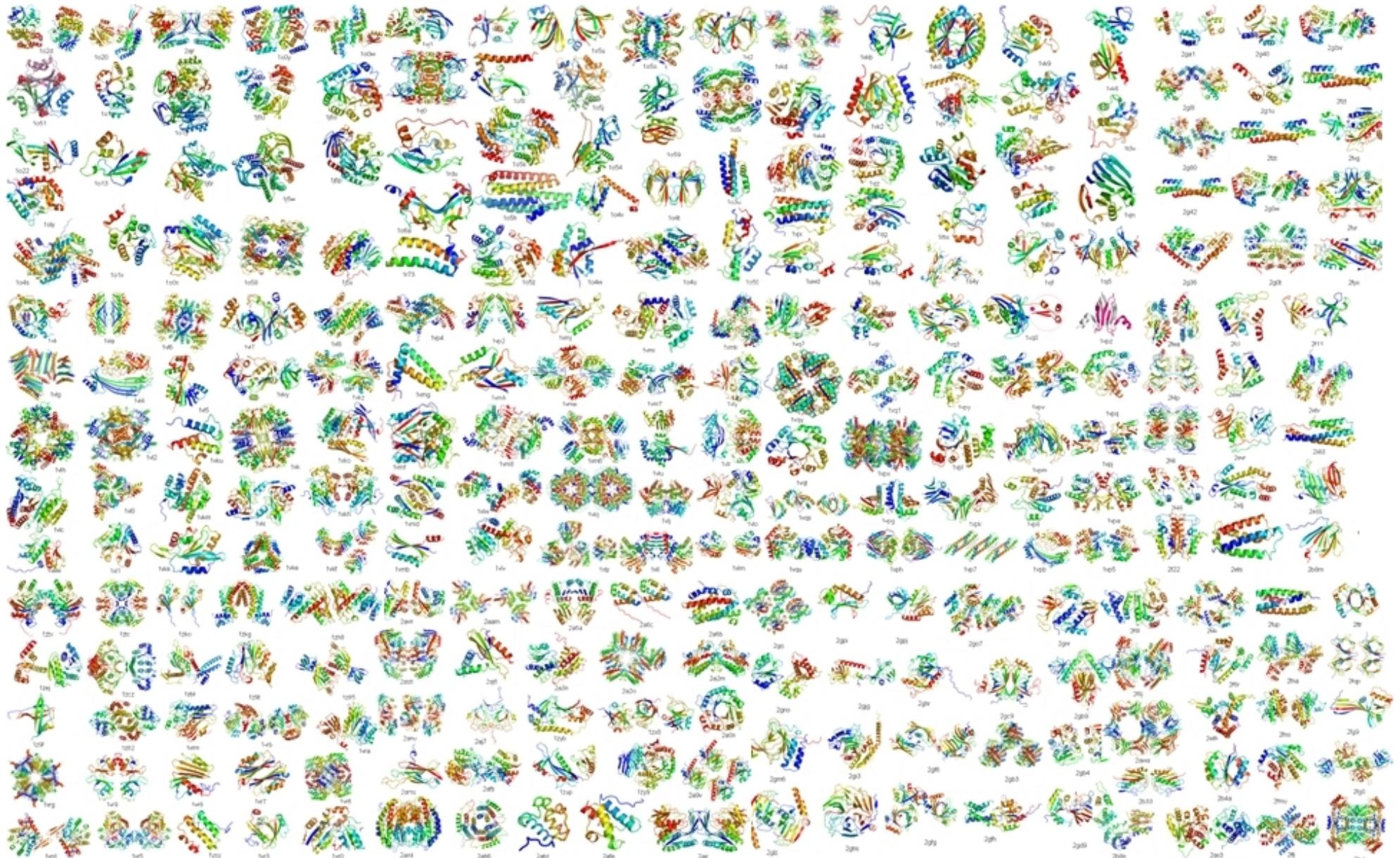
- Every amino acid ~ 10 conformations
- 100-aa polypeptide ~  $10^{100}$  conformations
- Time of 1 conformational change ~  $10^{-13}$  s
- $10^{80}$  years needed, Universe life ~  $10^{10}$
- In reality: folding time ~ minutes-days



➤ Is the native conformation the most stable???

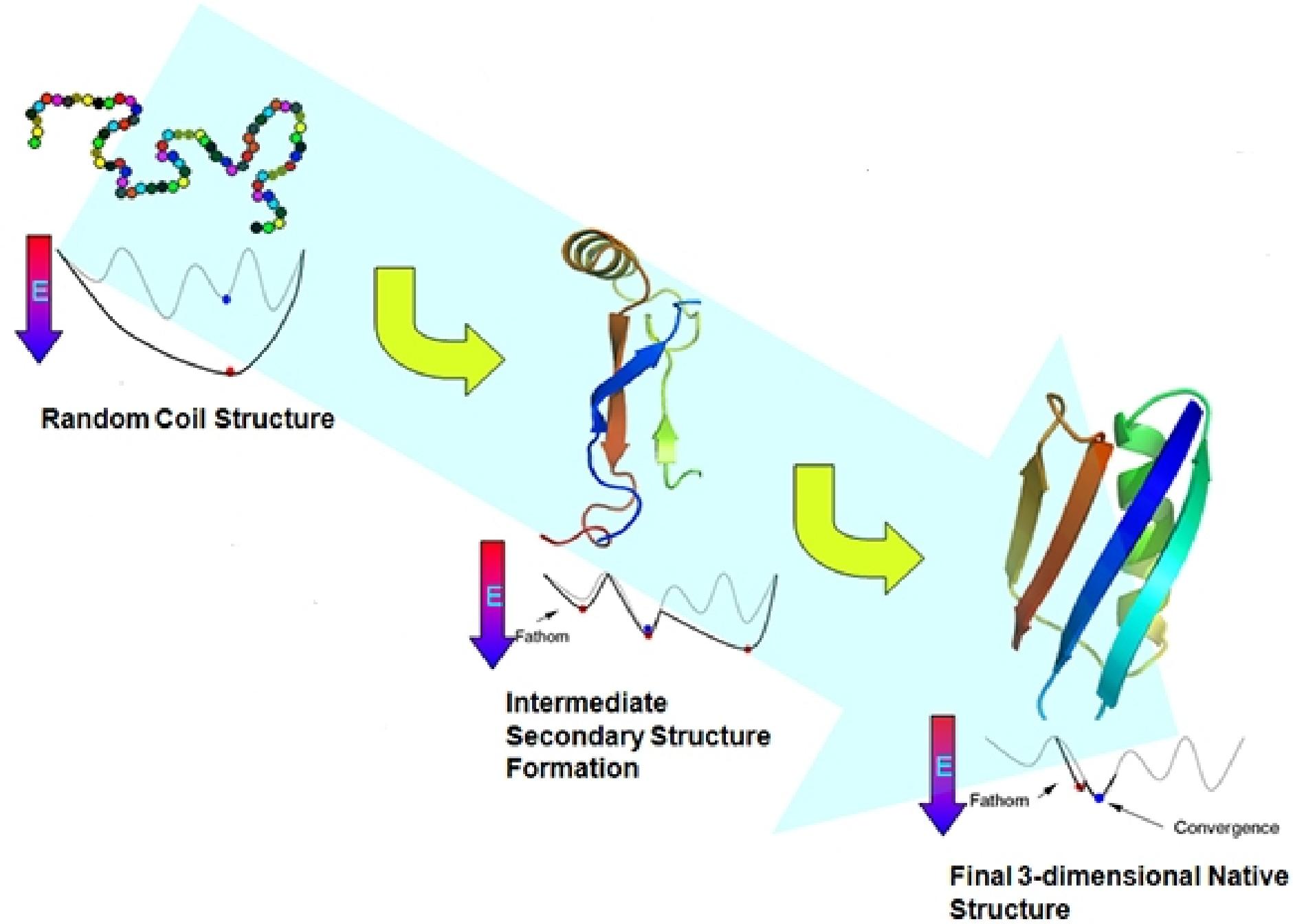
➤ Kinetics or thermodynamics???

# MANY SEQUENCES/FEW FOLDS



SCOP (2008): 1393 folds

# FRAMEWORK MODEL



# $\alpha$ -HELIX ORGANIZATION

$$\delta G_\alpha = G_\alpha - G_{coil} = (n-2) f_{HB} - n T S_\alpha$$

$$g_{init} = -2g_{HB} \quad g_{elong} = g_{HB} - T S_\alpha$$

$$\delta G_\alpha = g_{init} + n g_{elong} \quad \xrightarrow{\hspace{1cm}} \quad n_0$$

$$K = e^{\frac{-\delta G_\alpha}{kT}} = e^{\left(\frac{-g_{init}}{kT}\right)} \left(e^{\left(\frac{-g_{elong}}{kT}\right)}\right)^n = \sigma S^n$$

$$\sigma \ll 1$$

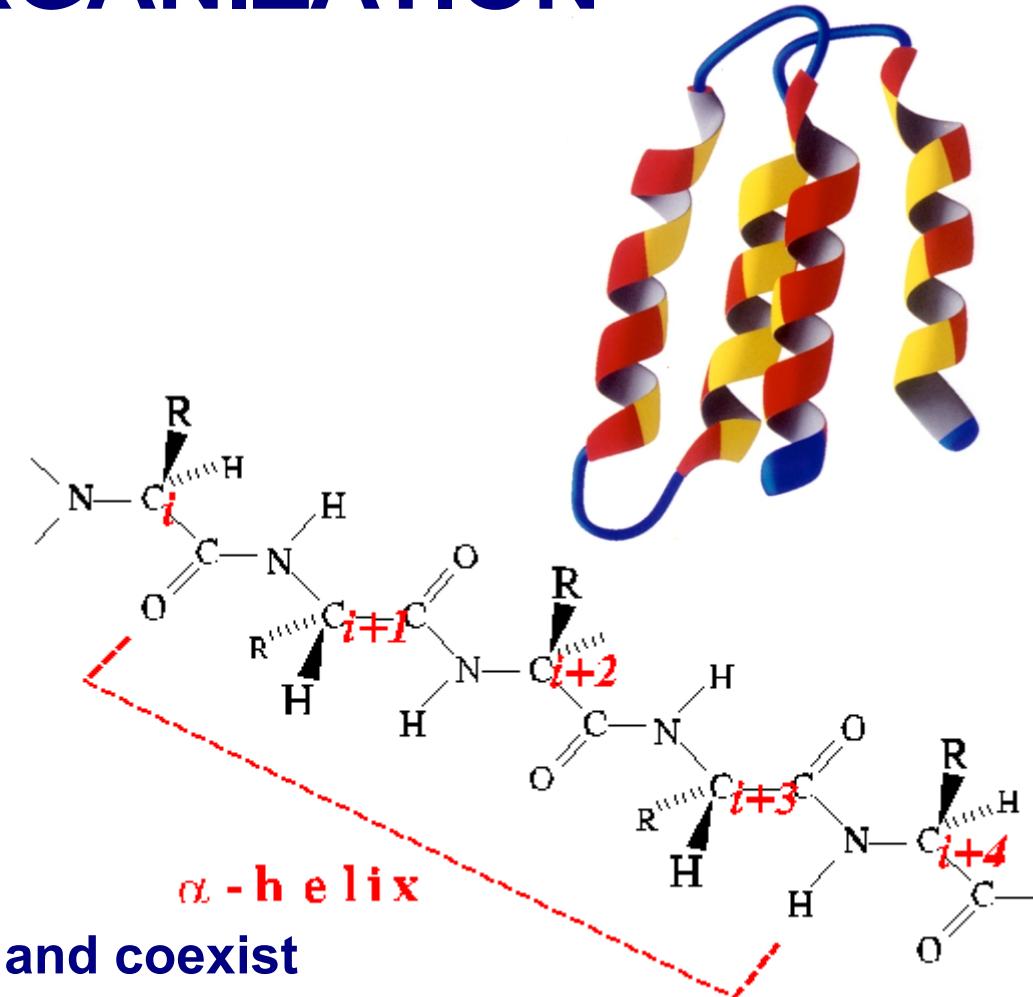
➤ 1D transition, both phases are stable and coexist

➤  $n_0 = f(aa) \approx 30$ ;  $g_{init} \approx 4 \text{ kcal/mol}$ ;  $\sigma \approx 0.001$ ;  $g_{HB} \approx TS_\alpha \approx -2 \text{ kcal/mol}$

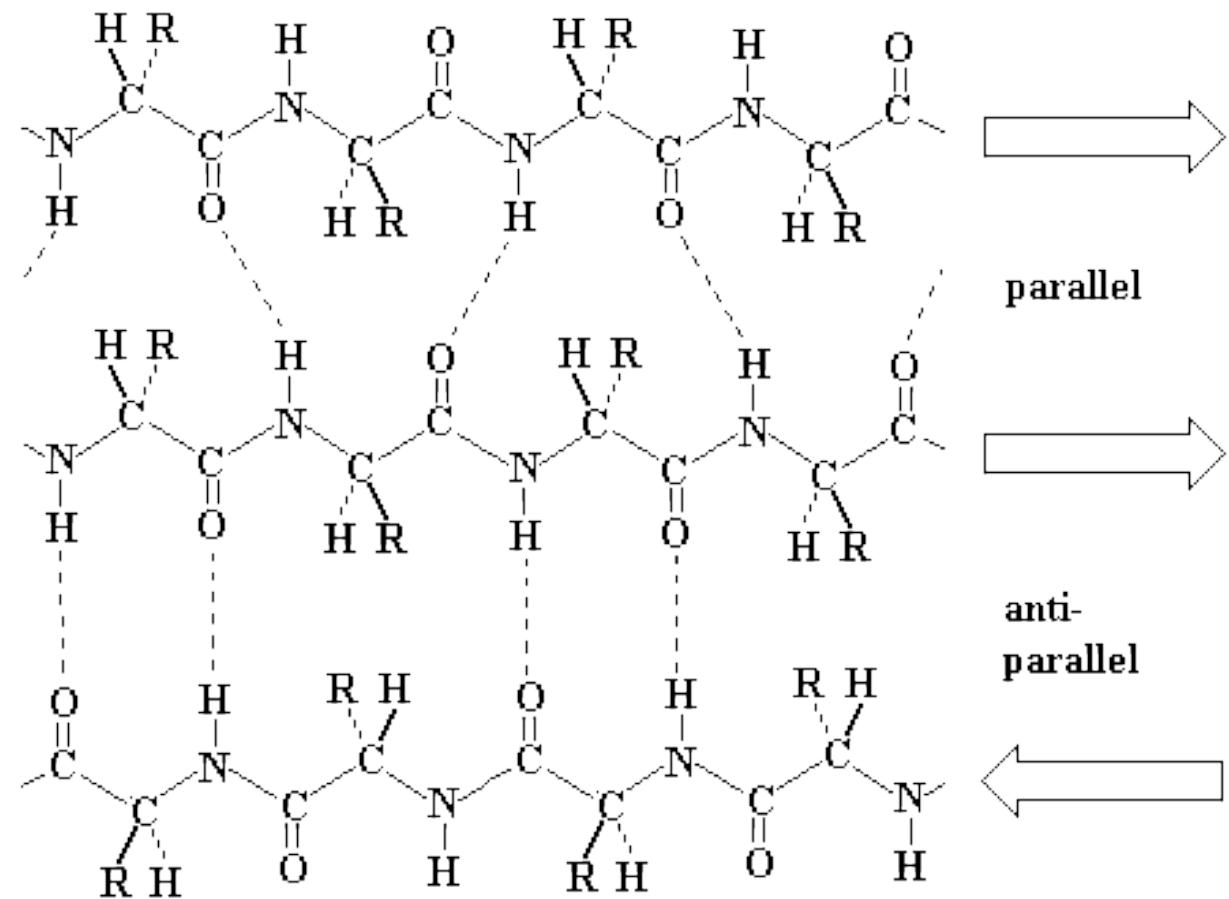
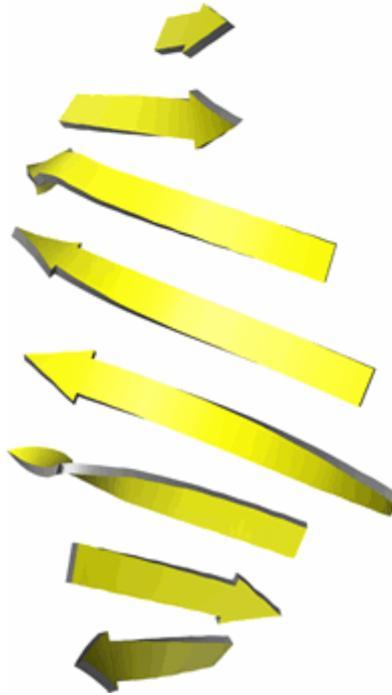
➤  $\uparrow T \Rightarrow \downarrow \text{helix content (helicity)}$

➤ Time<sub>initiation</sub>  $\approx$  Time<sub>full elongation</sub>

➤ Rate  $\approx 1 \text{ aa/ns}$



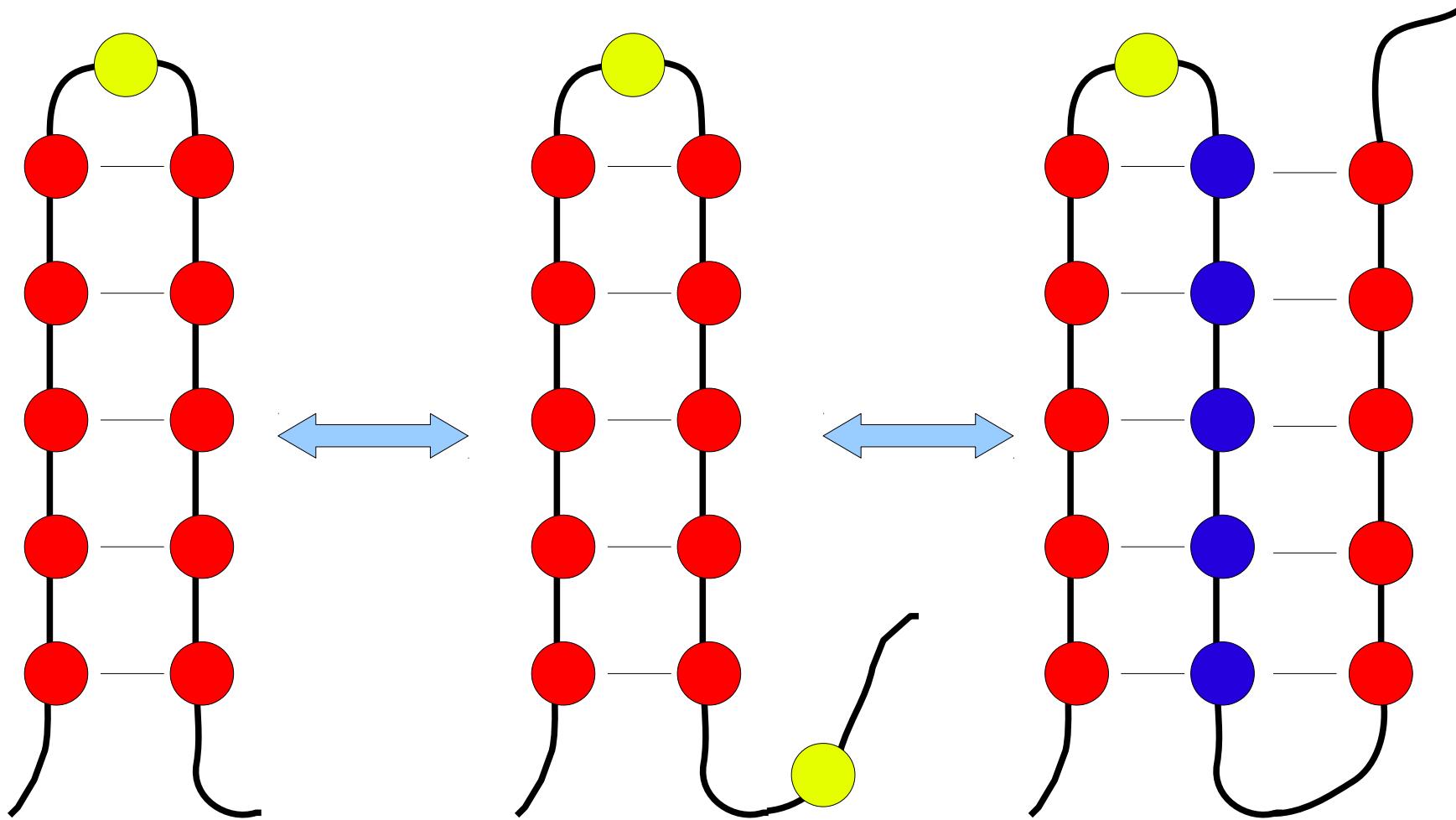
# $\beta$ -SHEET ORGANIZATION



**1D → 2D**

- $\beta$ -sheet assembles much slower than  $\alpha$ -helix (~ms-hours or weeks).

# $\beta$ -SHEET ORGANIZATION



## Unstable

- External  $\beta$ -layers have higher energies than internal.
- II type of transition.
- High energetical barrier.

# $\beta$ -SHEET ORGANIZATION

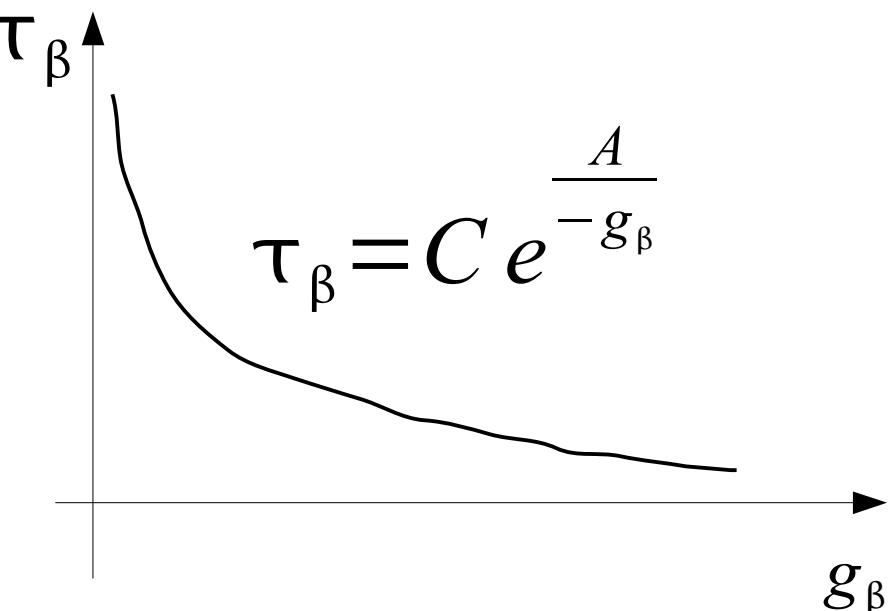
$g_\beta + \delta g_\beta$  – energy of a residue within  $\beta$  – sheet + at the border

$g_\beta + \delta g_\beta < 0$  –  $\beta$  – hairpin is stable

$g_\beta + \delta g_\beta > 0$  –  $\beta$  – hairpin is unstable

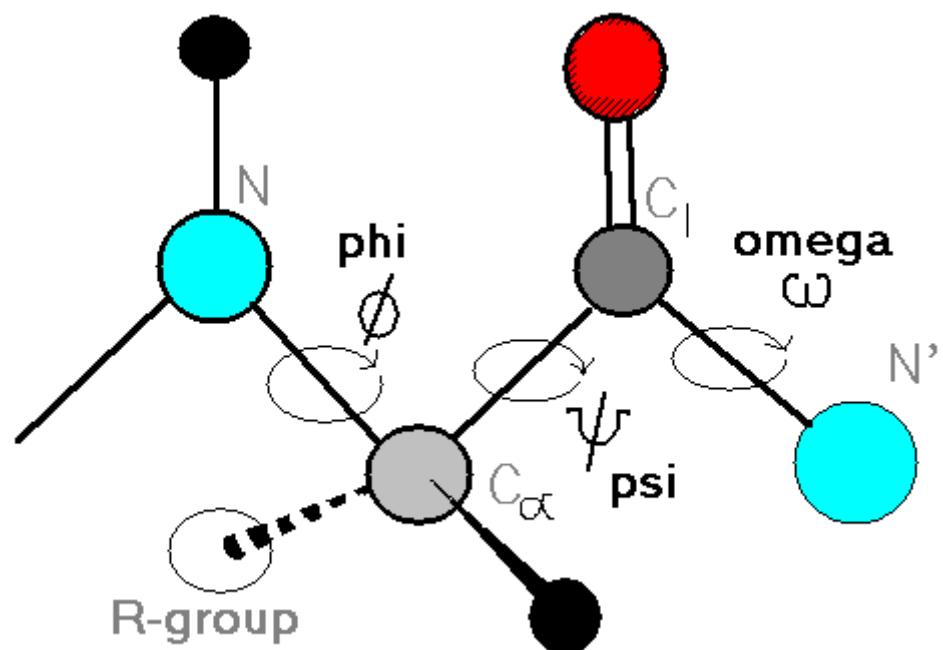
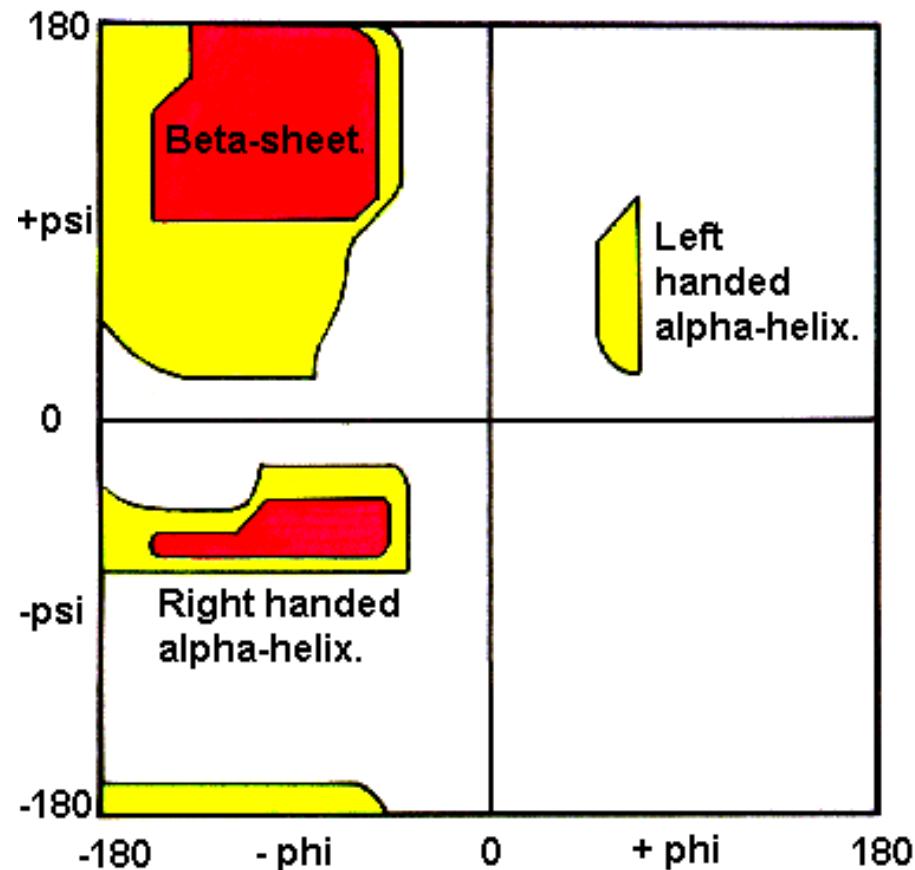
$N_{min} = \frac{g_\beta + \delta g_\beta}{-g_\beta}$  – Minimum number of residues required

- No equilibrium with unfolded structure.
- Initiation is a limiting stage.
- Stable hairpins form as fast as  $\alpha$ -helices.
- $V \sim N^{3/2}$
- $\langle n(\alpha) \rangle = 11$ ;  $\langle n(\beta) \rangle = 6$



# SECONDARY STRUCTURE PROPENSITIES

The Ramachandran Plot.

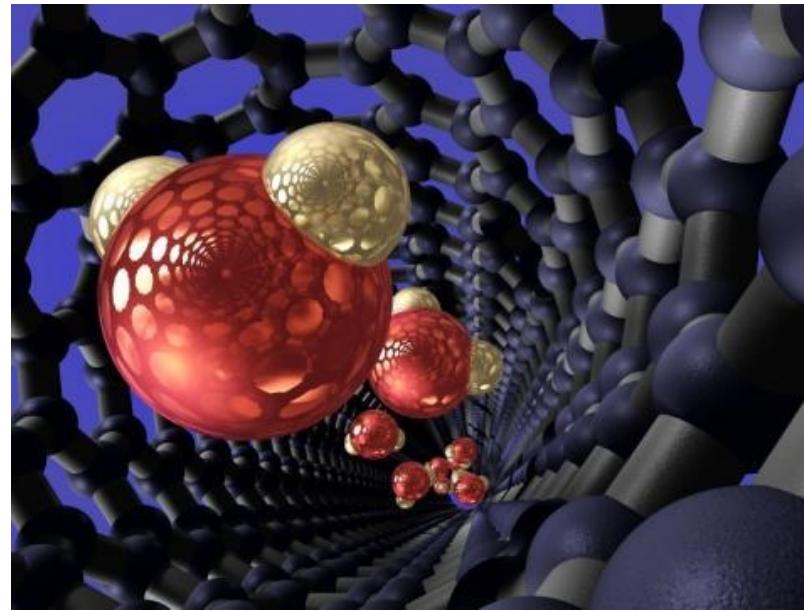


- **$\alpha$ -forming:** Met, Ala, Leu, Glu, Gln, Lys.
- **$\beta$ -forming:** Thr, Ile, Val, Phe, Tyr, Trp.
- **Disorder-supporting:** Gly, Ser, Pro, Asp, Asn.
- **Indifferent to secondary structure:** His, Arg, Cys.

# FOLDING DRIVING FORCES

$$\Delta G = \Delta H - T\Delta S$$

- Enthalpy
- Entropy



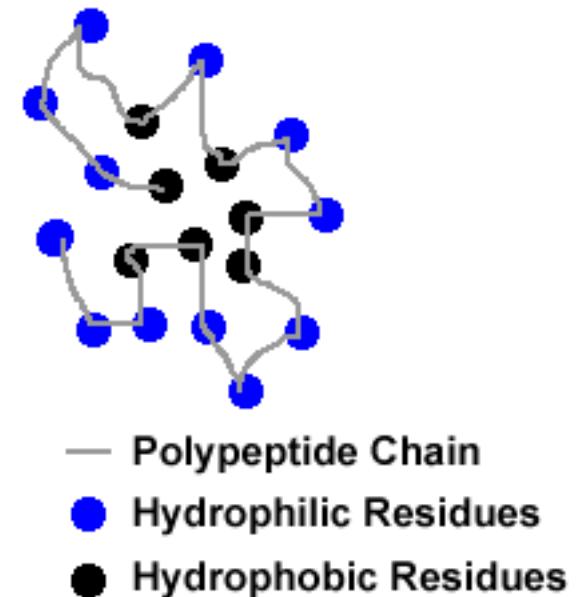
Protein  
+  
Solvent

$$V(\vec{r}) = \sum_{bonds} K_r (r - r_{eq})^2 + \sum_{angles} K_\theta (\theta - \theta_{eq})^2 + \sum_{dihedrals} \frac{V}{2^n} (1 + \cos[n\phi - \gamma]) + \sum_{i < j}^{atoms} \left( \frac{A_{ij}}{R_{ij}^{12}} - \frac{B_{ij}}{R_{ij}^6} \right) + \sum_{i < j}^{atoms} \frac{q_i q_j}{\epsilon R_{ij}}$$

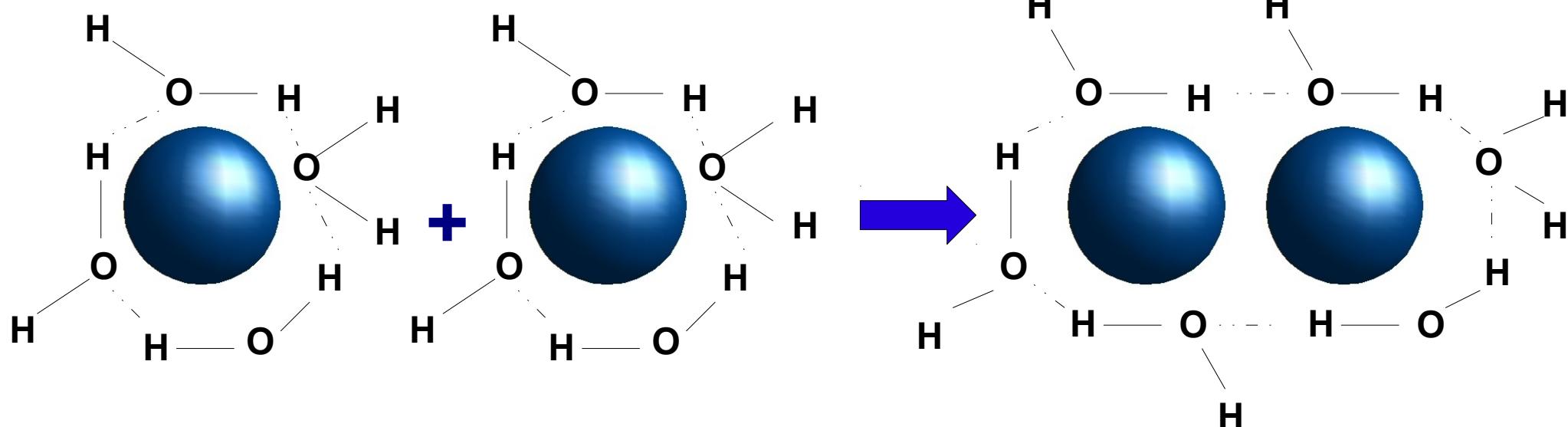
- Electrostatic potential:
  - H-bonds
  - Salt bridges
- Lennard-Jones potential
  - vdW contacts

# HYDROPHOBIC EFFECT

- $[\text{CH}_4]$  above water surface = 10  $[\text{CH}_4]$  in water
- 90% of work spent on protein folding
- Hydrophobic molecules:
  - disturb H-bonds
  - do not create H-bonds themselves

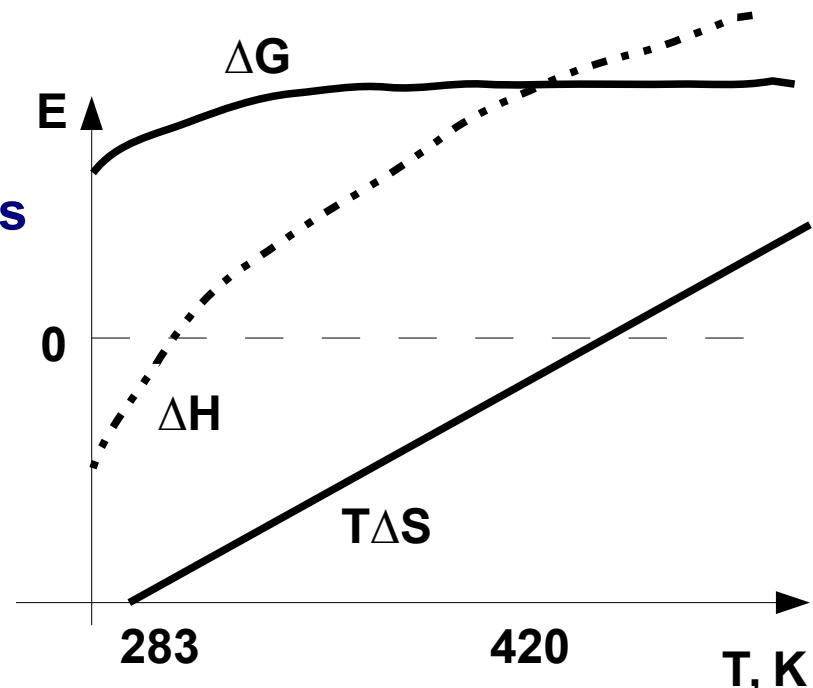


Entropic nature

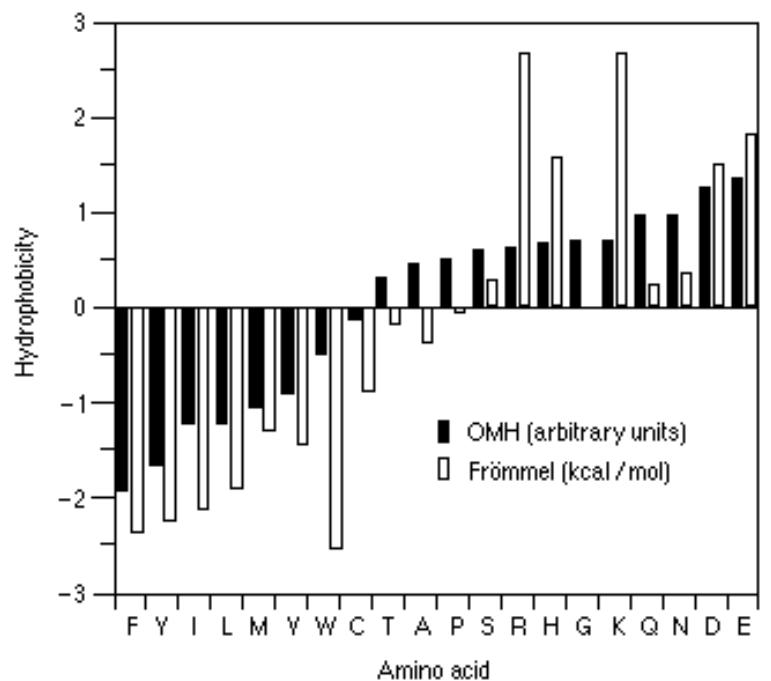


# HYDROPHOBIC EFFECT

- Hydrophobicity = function (T)
  - T↑ up to 420K, HΦ↑, melting surfacial H-bonds
  - T↑ (>420K), HΦ↓
- $\Delta G = k\Delta ASA$ ;  $k \sim 10^{-2}$  kcal/(mol·Å)
- $\Delta G(100 \text{ aa}) \sim \text{kcal/mol}$



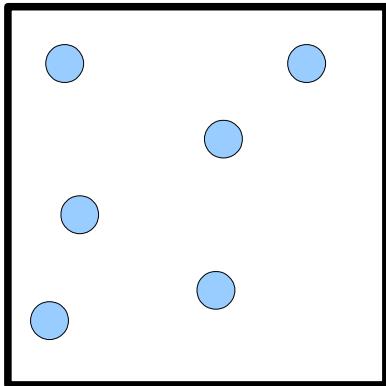
- Index of hydrophobicity for amino acids:  
equilibrium constant between water  
and nonpolar solvent



# POLYMER vs GAS

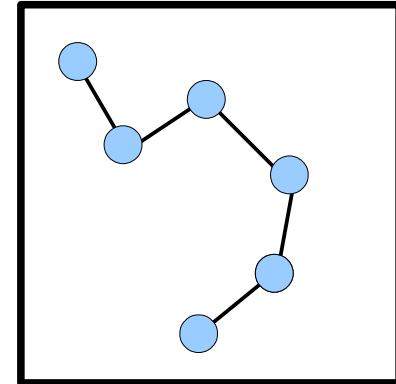
Gas:

V, N, ω



Polymer:

V, N, ω



$$\rho = \frac{N\omega}{V}$$

$$V_{access} = \frac{(V - N\omega)}{N} = \left(\frac{V}{N}\right)(1 - \rho) = \frac{\omega/\rho}{(1 - \rho)}$$

$$\delta S = k \ln(V_{access}) = k \ln((\omega/\rho)(1 - \rho))$$

Could be two  $\Delta G_{min}$  => two phases

$$V_{access} = A(1 - \rho)$$

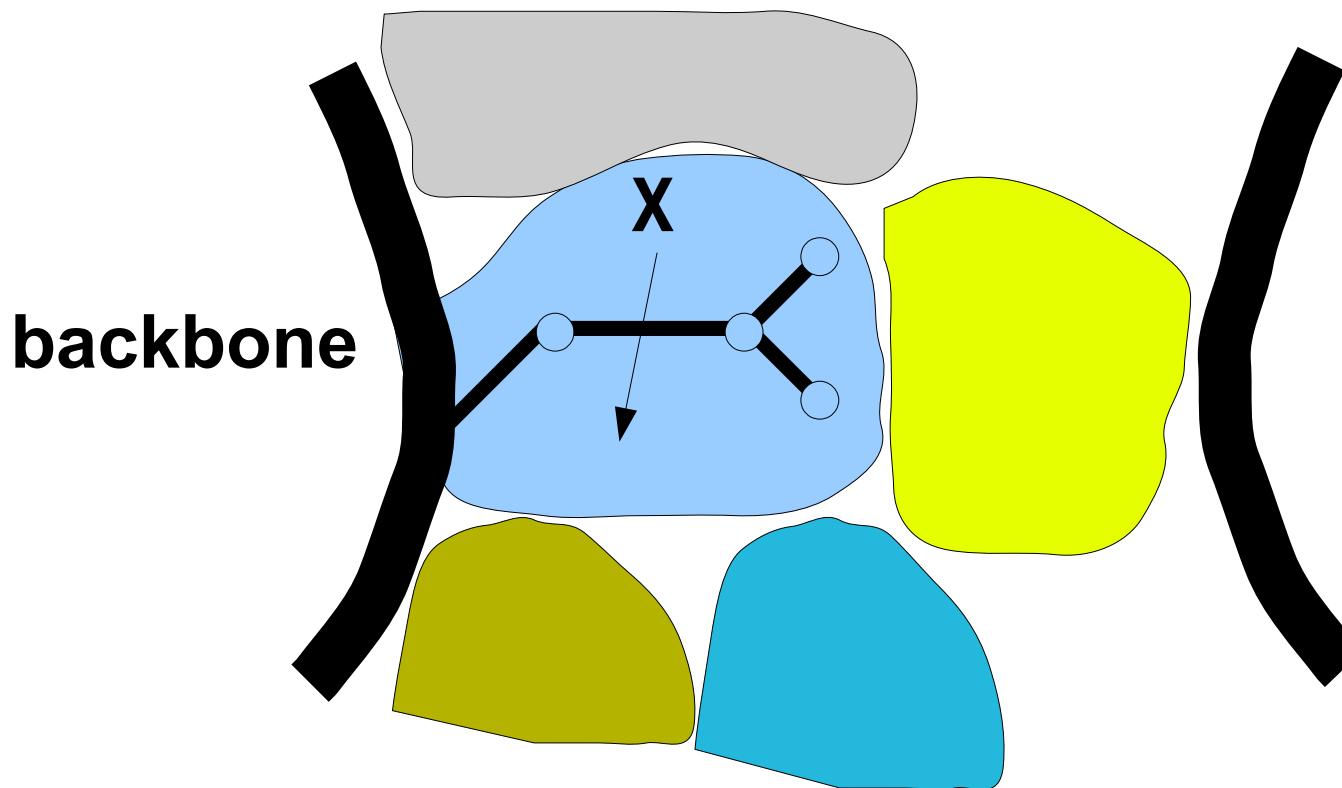
$$\delta S = k \ln(V_{access}) = k \ln(A(1 - \rho))$$

Only one  $\Delta G_{min}$  => gradual transition

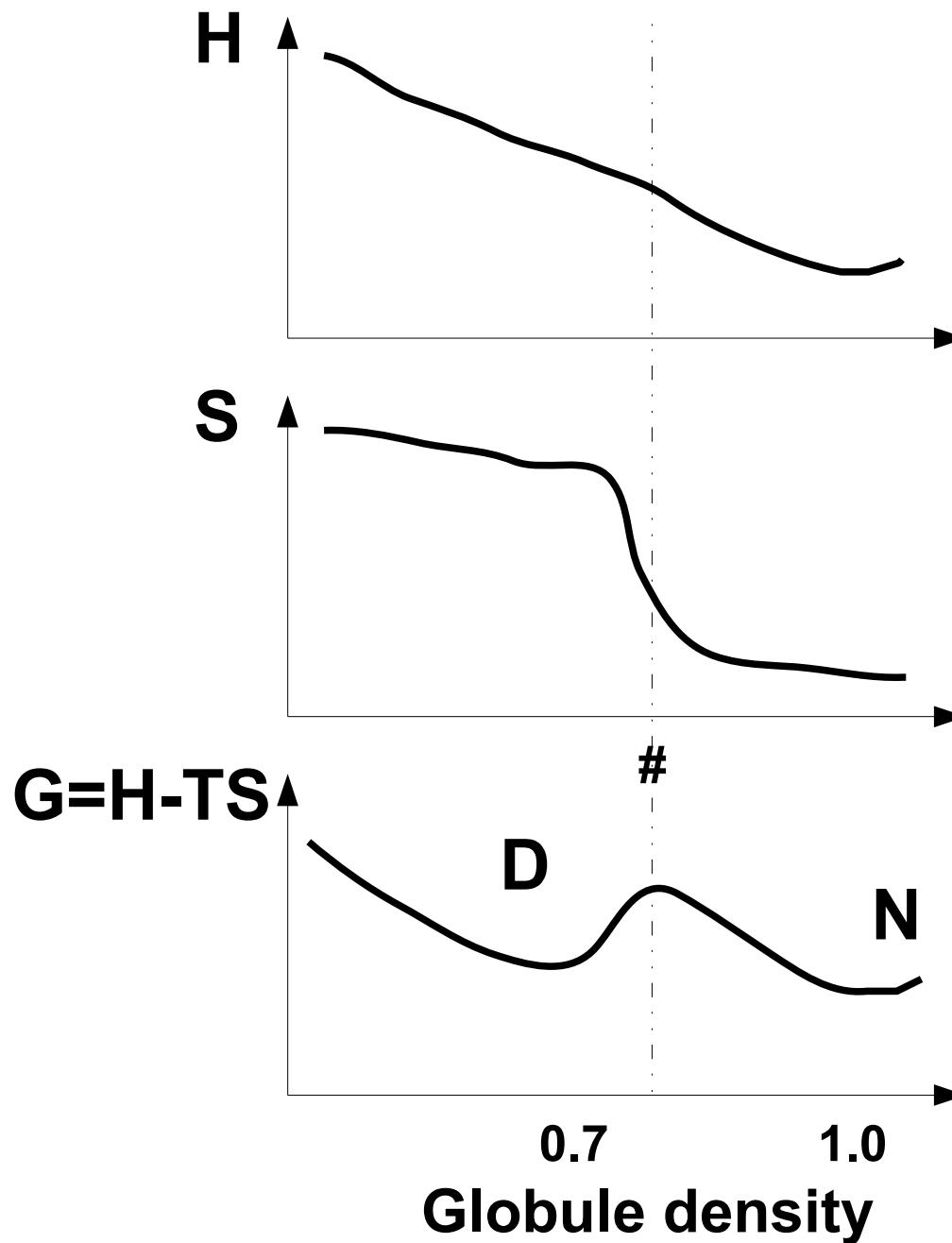
- Why protein does not fold like a normal polymer?

# PHYSICS OF «ALL OR NOTHING»

- Protein is not a standard polymer: high heterogeneity.
- Rigid backbone and more flexible side-chains.
- $V_{vdW}$  occupy 70-80% of  $V_{protein}$ . Roughly equal distribution of free  $V$ .
- Rotamers associated entropy jump occurs in unfolding + action of solvent (minimal frustration concept).
- Density remains high.



# THERMODYNAMICS



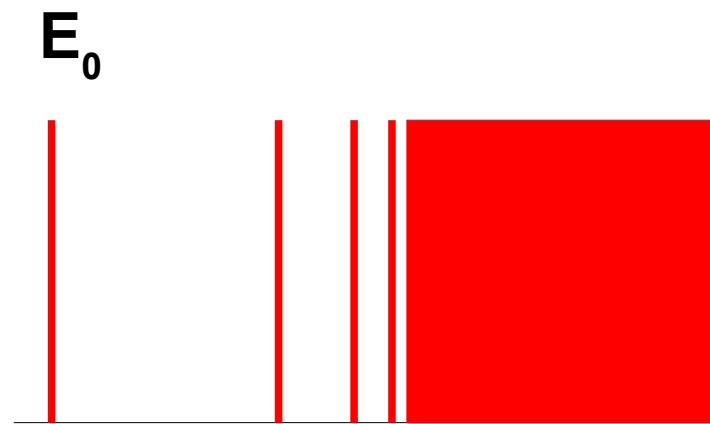
# POLYMER vs PROTEIN: SPECTRUM

Regular homopolymer



$$\Delta E < kT$$

Protein

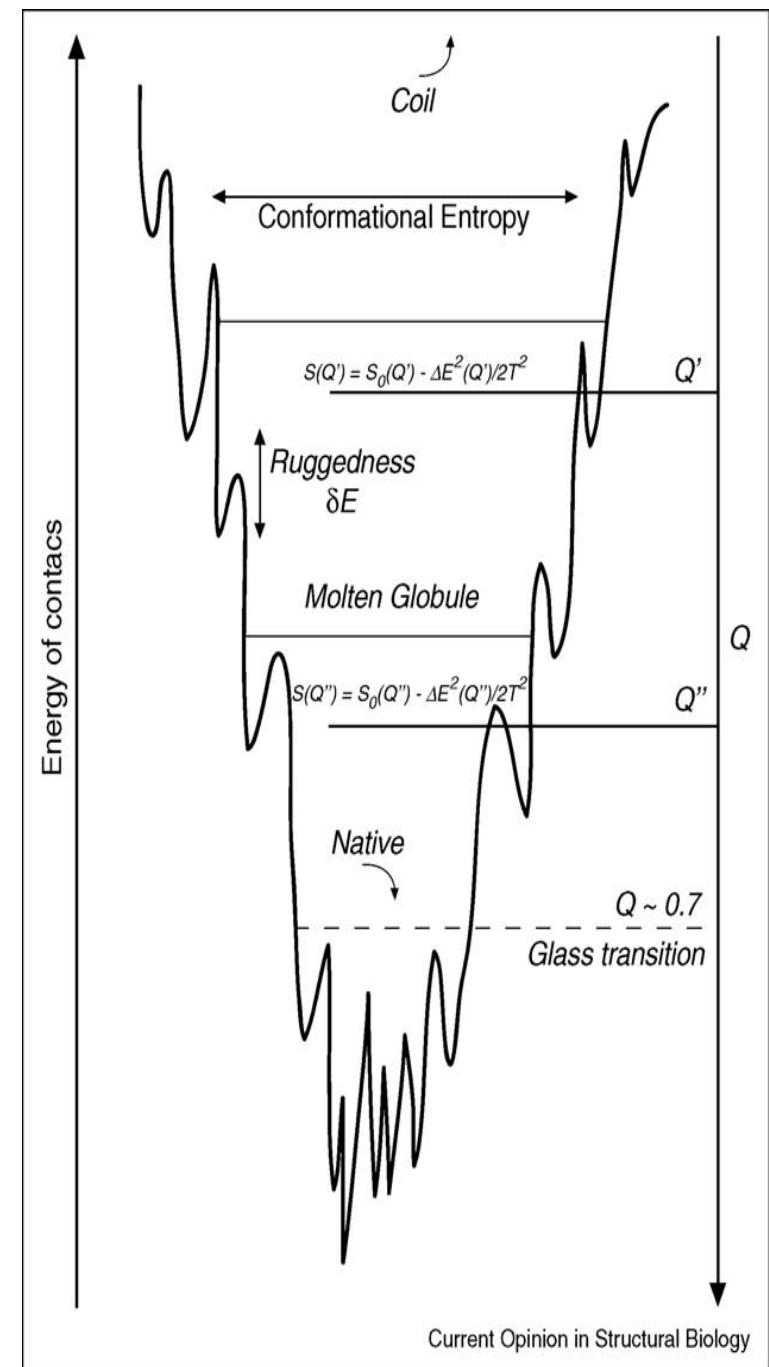
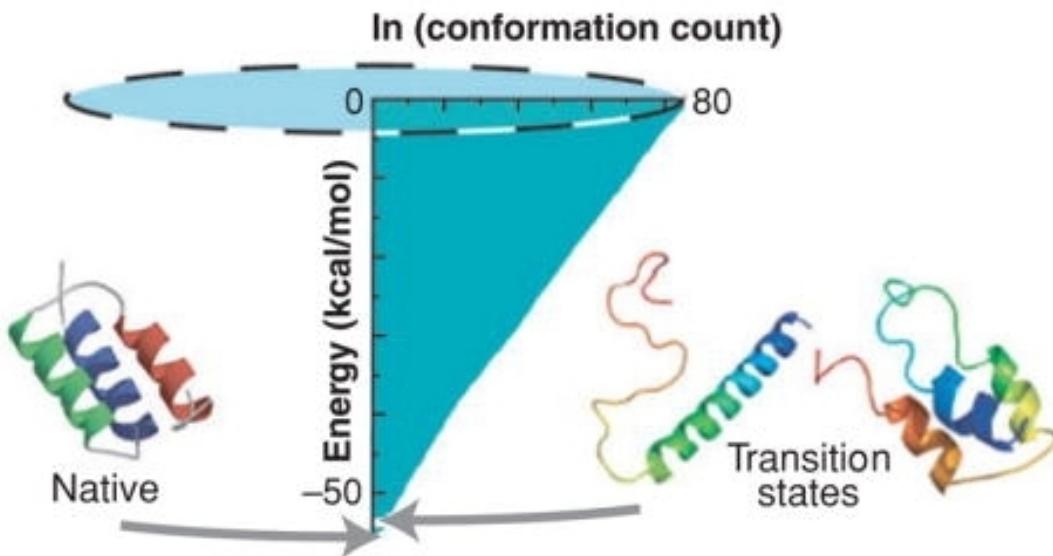


$$\Delta E \gg kT$$

- Protein has anomalous stable energetic state (native).
- $\Delta E \sim 10 \text{ kcal/mol} \Rightarrow p = \exp(-\Delta E/kT) \sim 10^{-8}$
- If there are  $> 1$  stable structure  $p = \exp(-2\Delta E/kT) \sim 10^{-16}$ 
  - polyLys, prions,  $\beta$ -amyloids, serpins

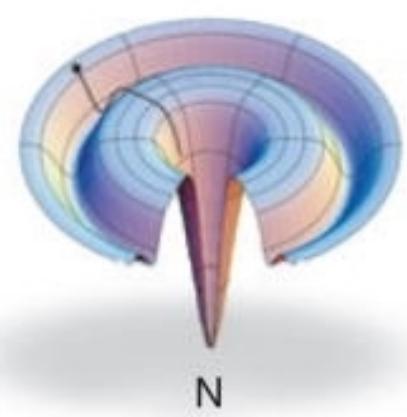
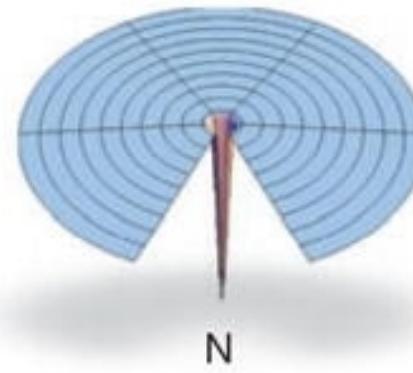
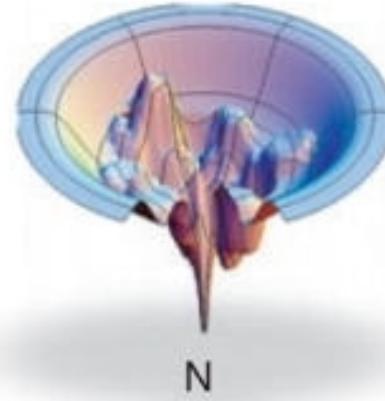
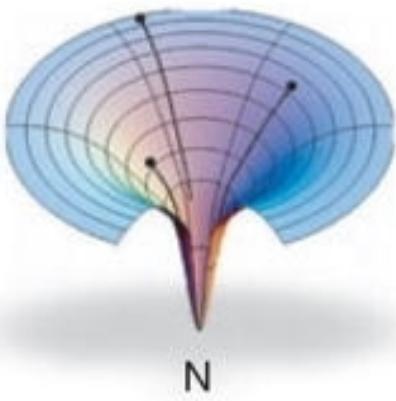
# THERMODYNAMICS vs KINETICS

- Protein folding is not only determined by a native state thermodynamical properties but also by a kinetic path:
  - fast
  - selected during evolution
  - leads to native state
- Energy landscapes have hierarchical organization



# FUNNELS

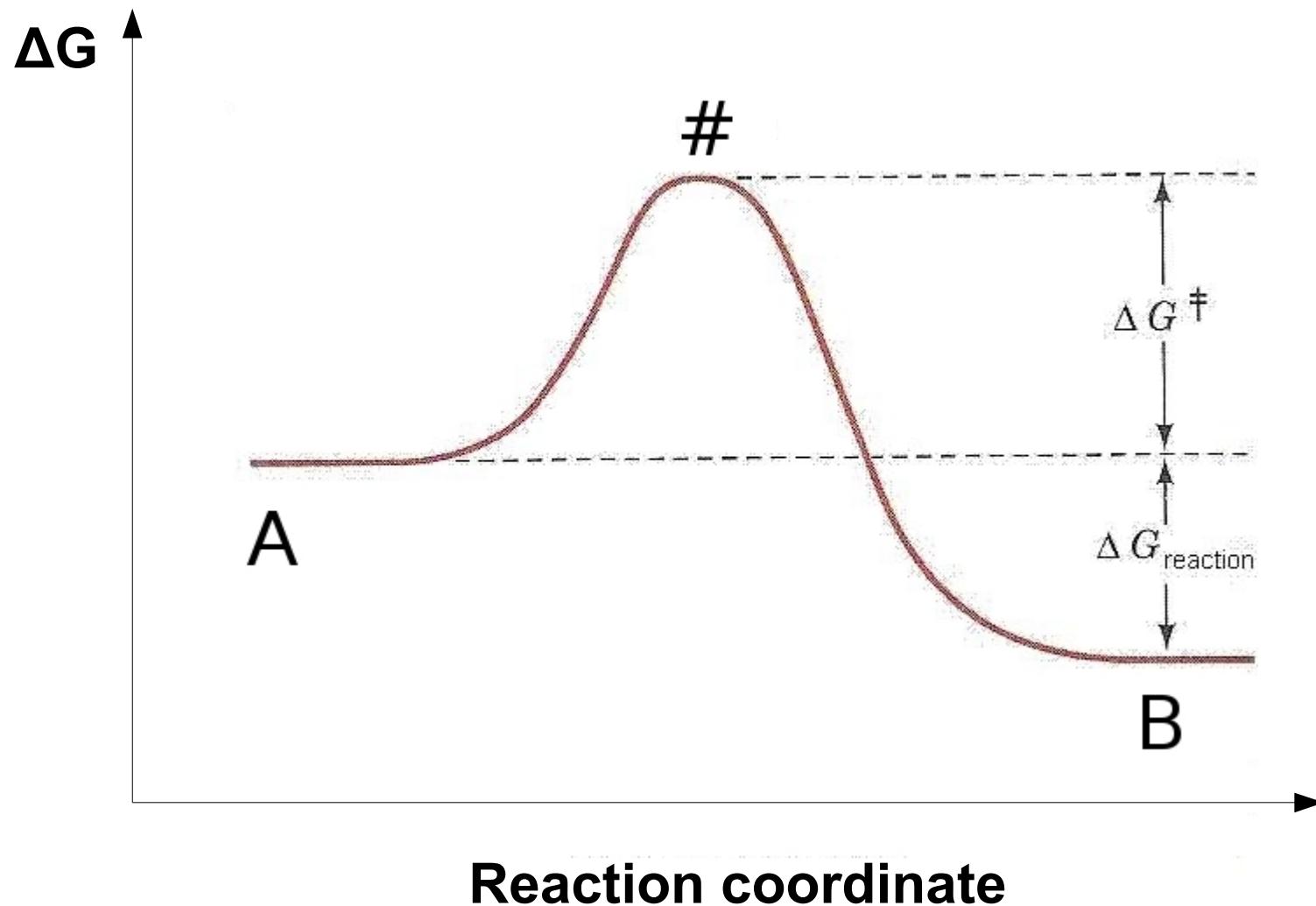
- The folding funnel hypothesis is a the energy landscape theory of protein folding assuming that a protein's native state corresponds to its free energy minimum.



- One path or several:
  - thermodynamic view
  - statistical physics view

# TRANSITIONAL STATE

- For small proteins (one-domain proteins) folding process includes only one energetical barrier.



$$k_{A \rightarrow B} = k_0 e^{\frac{-(G^\ddagger - G_A)}{RT}}$$

$$k_{B \rightarrow A} = k_0 e^{\frac{-(G^\ddagger - G_B)}{RT}}$$

$$t_{A \rightarrow B} = \frac{1}{k_{A \rightarrow B}} \sim e^{G^\ddagger}$$

# ESTIMATION OF G<sup>#</sup> BARRIER

➤ During folding:

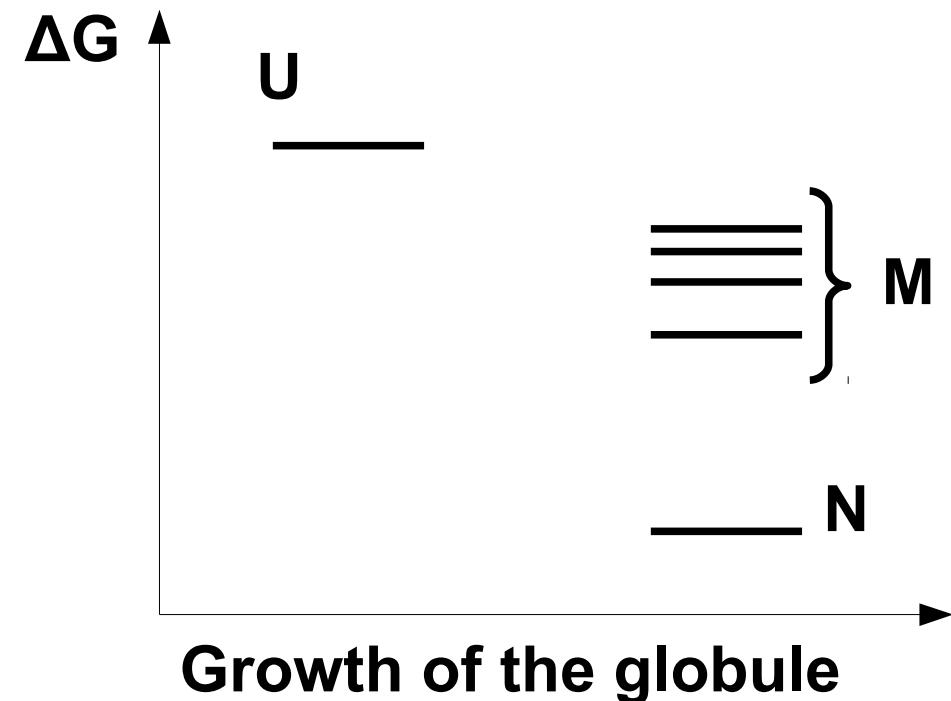
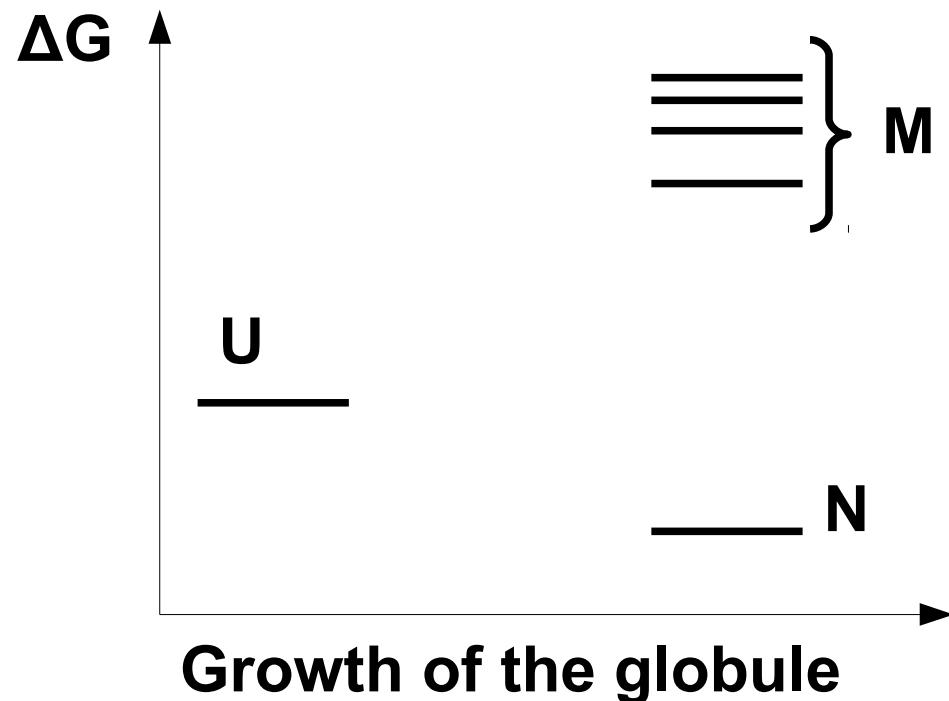
- $\Delta H = An + Bn^{2/3}$ , decreases

- $\Delta S = Cn + Dn^{2/3}$ , decreases

- $\Delta G = \Delta H - T\Delta S \Rightarrow$  equilibrium  $F \leftrightarrow U$  if there were no surfacial effects!

➤  $G^{\#} \sim n^{2/3}$

➤ Folding time  $\sim \exp [(1 \pm 0.5)N^{2/3}]$  10ns, defined by amount of native contacts.



# CHEVRON FIGURES

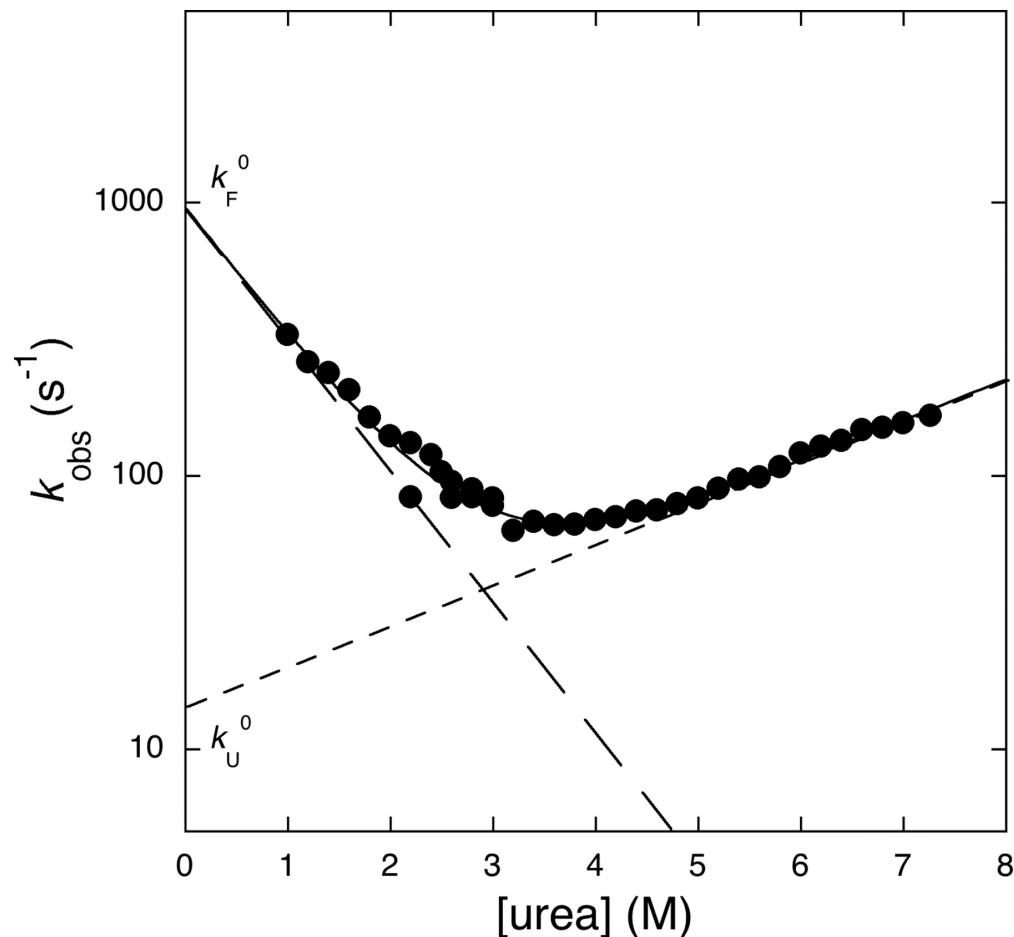
$$K_{B:A} = \frac{n_B^\infty}{n_A^\infty} = \frac{k_{A \rightarrow B}}{k_{B \rightarrow A}}$$

$$\frac{dn_A}{dt} = -k_{A \rightarrow B} n_A + k_{B \rightarrow A} n_B$$

$$n_A + n_B = n_0$$

$$n_A(t) = (n_A(0) - n_A^\infty) e^{-(k_{A \rightarrow B} + k_{B \rightarrow A}) t} + n_A^\infty$$

$$k_{obs} = k_{A \rightarrow B} + k_{B \rightarrow A}$$



# MUTAGENESIS IN FOLDING STUDIES

➤ Mutation affects:

- folding rate
- stability of the native state

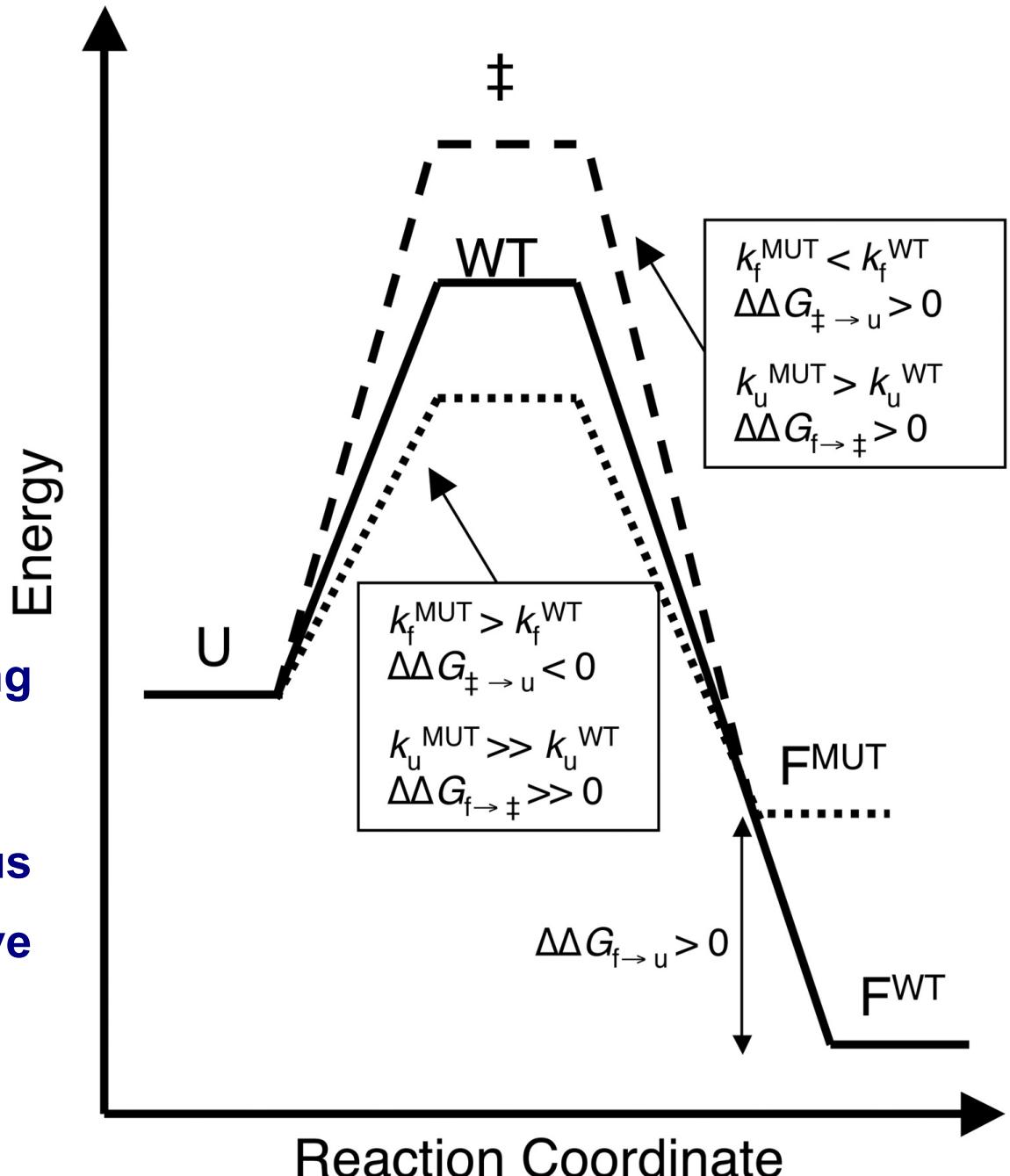
➤ Nucleation mechanism

$$\varphi_f = \frac{\delta(G^\ddagger - G_U)}{\delta(G_F - G_U)}$$

➤  $\Phi_f \approx 1$ , residue is in folding

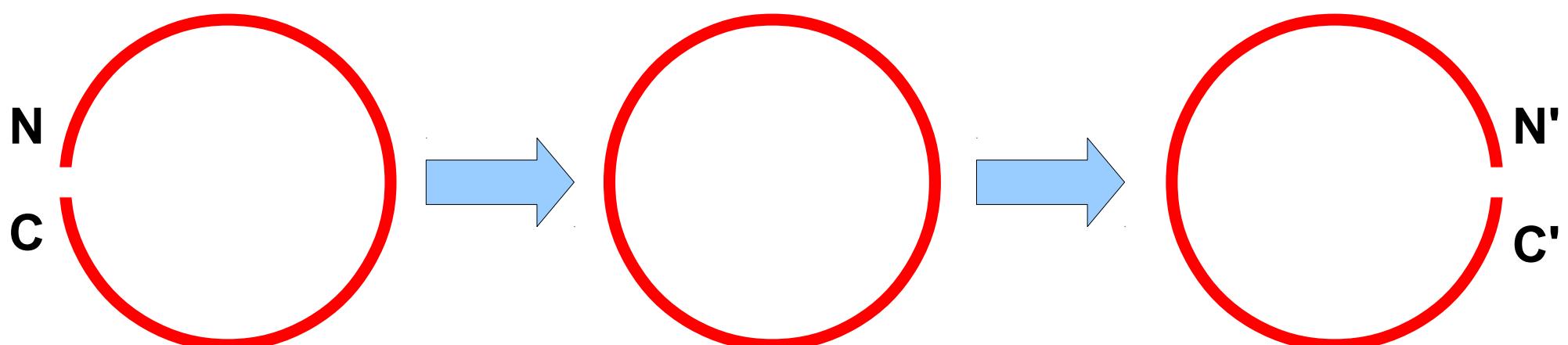
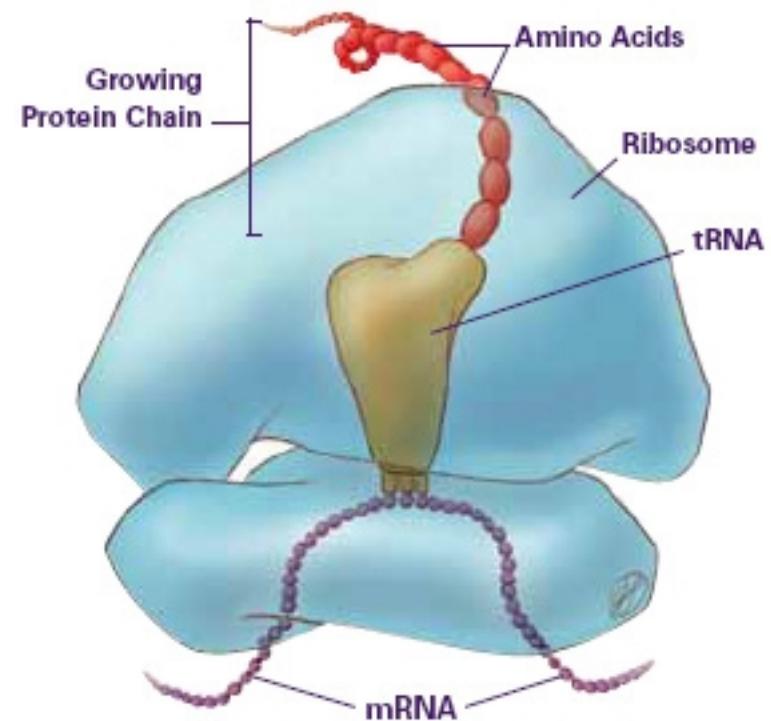
nucleus;  $\Phi_f \approx 0$ , not.

➤ Most of mutations in nucleus affect stability of the native structure.

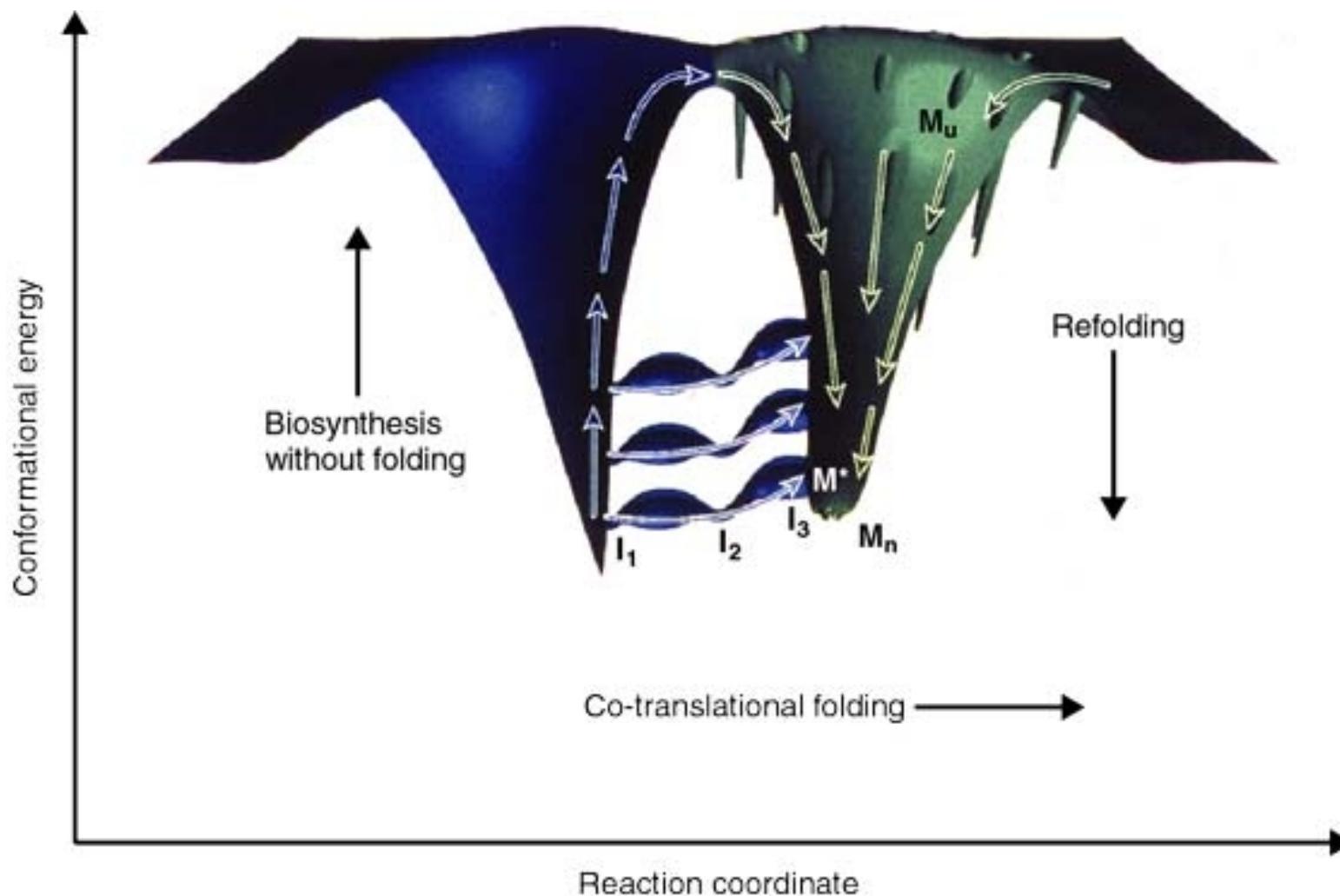


# FOLDING IN THE CELL

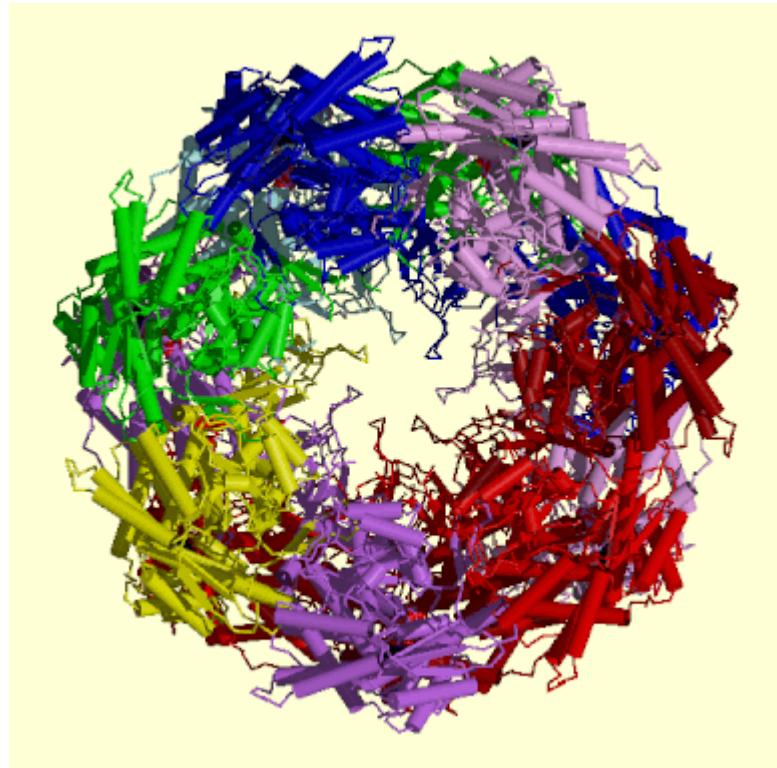
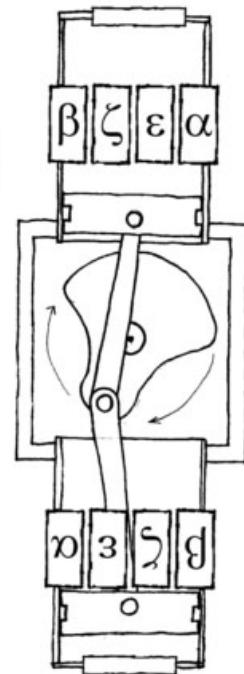
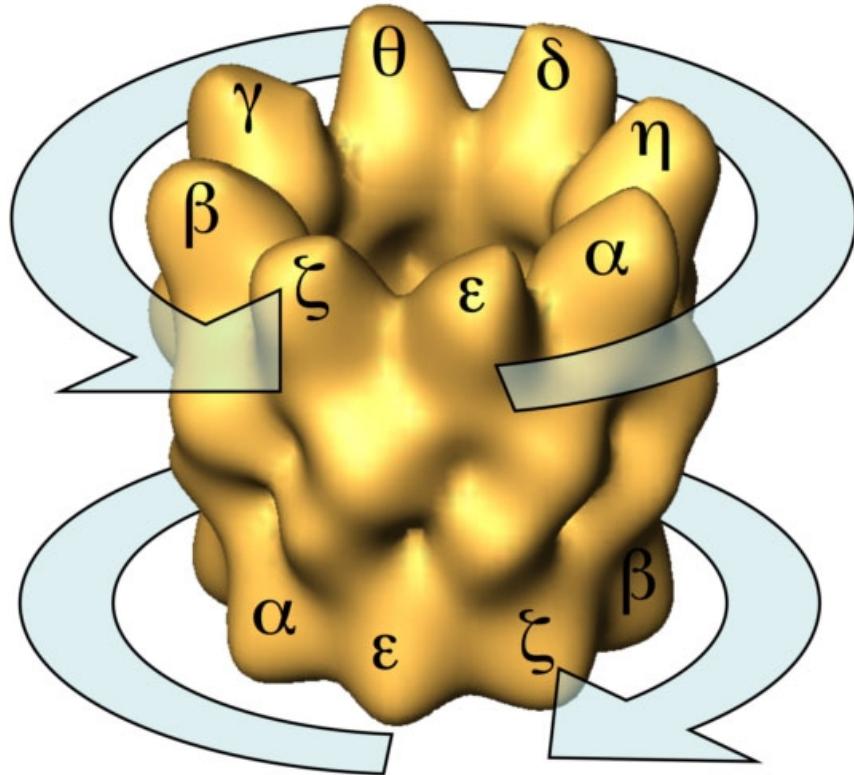
- Ribosome synthesis ~ 1 minute.
- Synthesis speed is not constant.
- For multidomain proteins N-terminal domains are folded before the synthesis is completed.
- Domain is a unit of folding (*in vitro*; globin).
- Cotranslational folding (luciferase).
- Self-organization experiments: chemical synthesis and cyclic proteins.



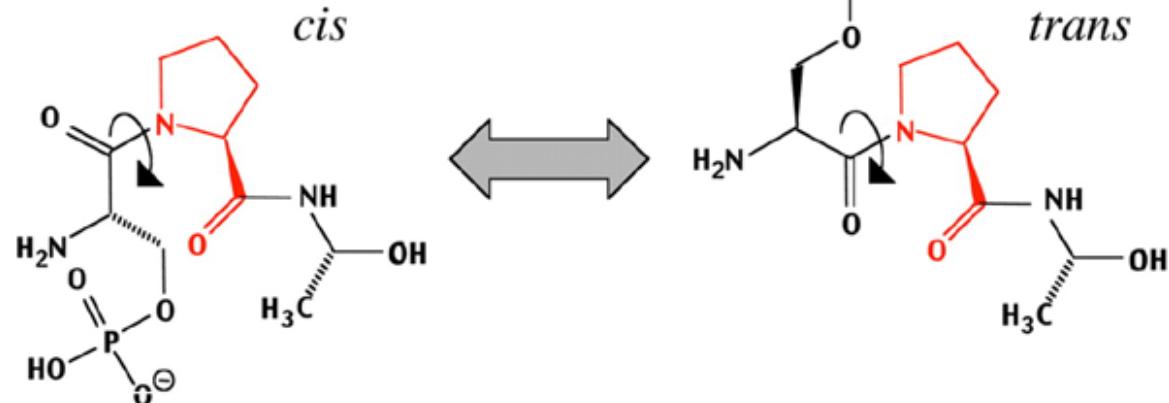
# ENERGETICS OF COTRANSLATIONAL FOLDING



# CHAPERONS



- Hsp(Heat Shock Proteins): Hsp60, Hsp70, Hsp100 etc. Regulated by T, pH etc.
- Use ATP hydrolysis
- Decrease the hydrophobic  $\Delta\text{ASA}$
- Ribosomes selves
- Prolyl- and disulfide-isomerase



# COMPUTATIONAL APPROACHES

- MD
  - replica exchange
  - Principal Component Analysis (PCA)
  - Clustering by contacts/RMSD/radius of gyration/H-bonds
- Monte Carlo
- «Zip and assemble» approach
- Up to 100 aa proteins could be tractable:
  - 36-residue villin, RMSD = 4.5 Å (Duan, Kollman, 1998)
  - 20-residue Trp-cage peptide, RMSD = 1 Å (Simmerling, 2002)
  - 47-residue albumin-binding domain, RMSD = 2 Å (Lei, 2007)
  - $\beta$ -hairpins up to 20-residues

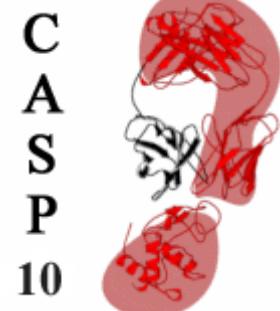


# CASP COMPETITION

- Critical Assessment of Techniques for Protein Structure Prediction
- [predictioncenter.com](#)
- Goal: to obtain an in-depth and objective assessment of current abilities in the area of protein structure prediction
- Prediction of 'soon known structures', no postpredictions
- CASP questions:
  - Models similarity to the corresponding experimental structures
  - Mapping of the target sequence onto the proposed structure
  - Model usefulness for similar structures
  - Model accuracy vs best template use
  - Has there been progress from the earlier CASPs?
  - What methods are most effective?
  - Where can future effort be most productively focused?

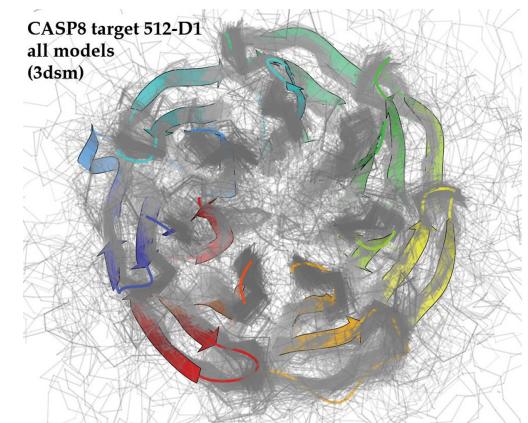
## ▼ [CASP Experiments](#)

- [CASP ROLL](#)
- [CASP10 \(2012\)](#)
- [CASP9 \(2010\)](#)
- [CASP8 \(2008\)](#)
- [CASP7 \(2006\)](#)
- [CASP6 \(2004\)](#)
- [CASP5 \(2002\)](#)
- [CASP4 \(2000\)](#)
- [CASP3 \(1998\)](#)
- [CASP2 \(1996\)](#)
- [CASP1 \(1994\)](#)

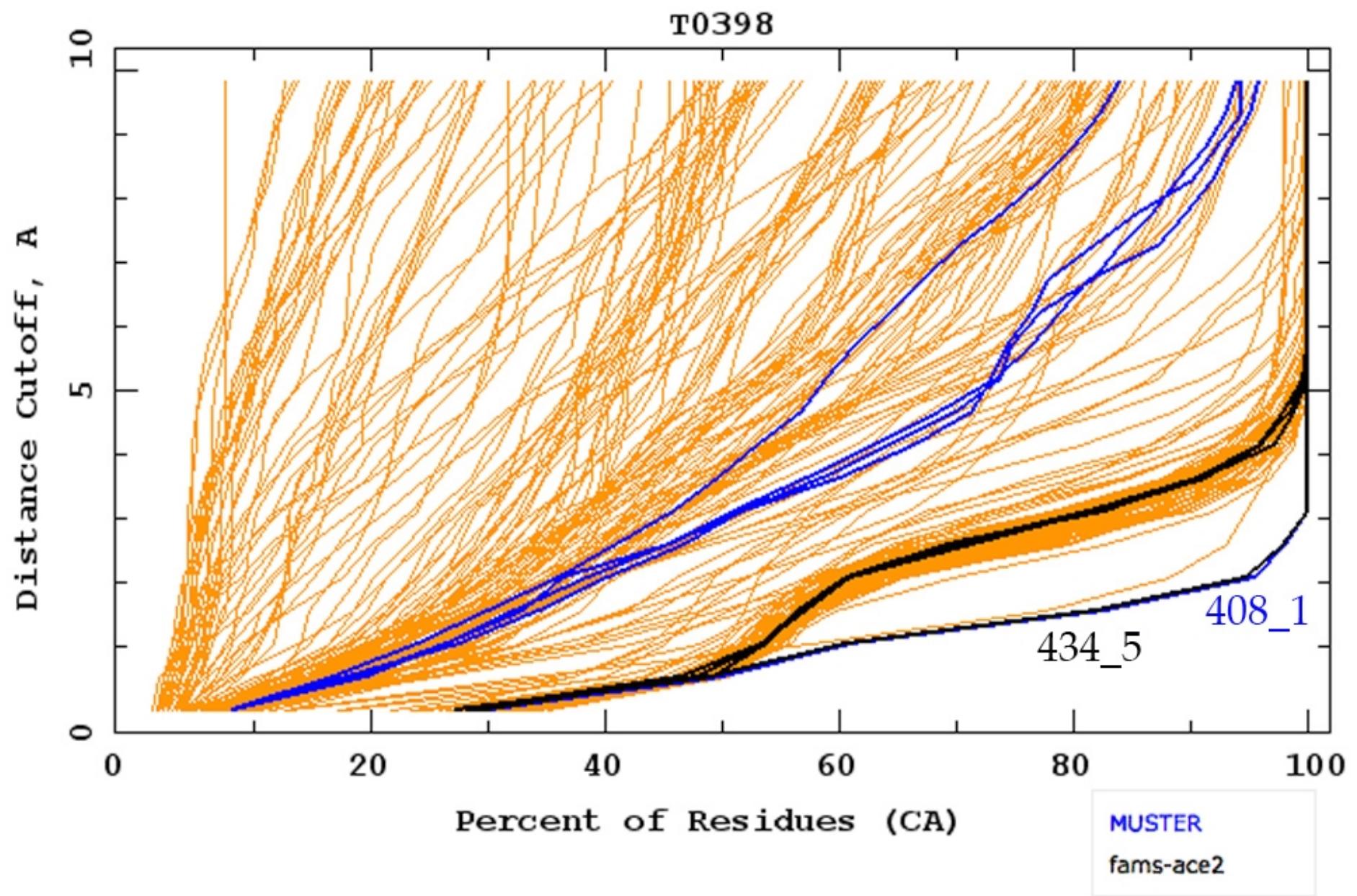


# SCOPE OF CASP

- **Tertiary structure prediction:**
  - The 'Template based modelling'
  - The 'Template free modelling'
  - Detailed analysis of the side chains, loops, and active sites for those structure models where the backbone is sufficiently accurate.
    - Success in refining models beyond the quality obtained by simply copying from a single template will be analyzed.
- **Other prediction categories:**
  - Detecting residue-residue contacts in proteins.
  - Identifying disordered regions in target proteins.
  - Function prediction (prediction of binding sites).
  - Quality assessment of models in general and the reliability of predicting certain residues in particular.



# CASP EXAMPLE

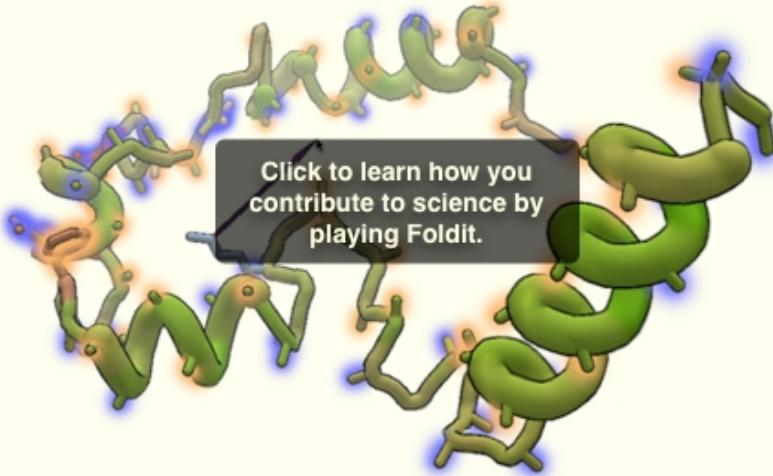


# FOLDIT

 **foldit**<sub>BETA</sub>  
Solve Puzzles  
for Science

13:34:46 GMT

PUZZLES  CATEGORIES GROUPS PLAYERS RECIPES CONTESTS  
BLOG  FEEDBACK FORUM WIKI FAQ ABOUT CREDITS



Click to learn how you contribute to science by playing Foldit.

**NANOCRAFTER** Try our new scientific discovery game!  
Be creative and build extraordinary tiny machines!

**What's New** 

**New Release!**

Hey everyone,

We're releasing a small update to the main game in preparation for some upcoming drug design puzzles. You shouldn't notice any impact on gameplay.

Thanks!

(Thu, 10/29/2015 - 20:04 | **0 comments**)

**GET STARTED: DOWNLOAD**

Windows (XP/Vista/7/8)    OSX (10.7 or later)    Linux (64-bit)

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# FOLDING@HOME

WHAT  
IF...



you  
could help ?  
find a cure?

↑ PLAY VIDEO

Help Stanford University scientists studying Alzheimer's, Huntington's, Parkinson's, and many cancers by simply running a piece of software on your computer.

The problems we are trying to solve require so many calculations, we ask people to donate their unused computer power to crunch some of the numbers.

# FOLDING@HOME

In just 5 minutes ...

Add your computer to over **163,000** others around the world outputting **38,000** teraflops of computing power to form the world's largest distributed supercomputer.

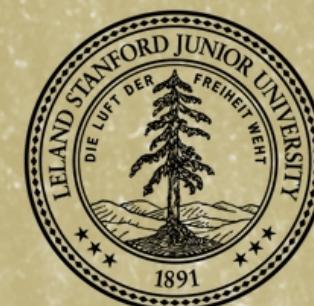
**Step 1.** Download protein folding simulation software called Folding@home.

**Step 2.** Run the installation. The software will automatically start up and open a web browser with your control panel.

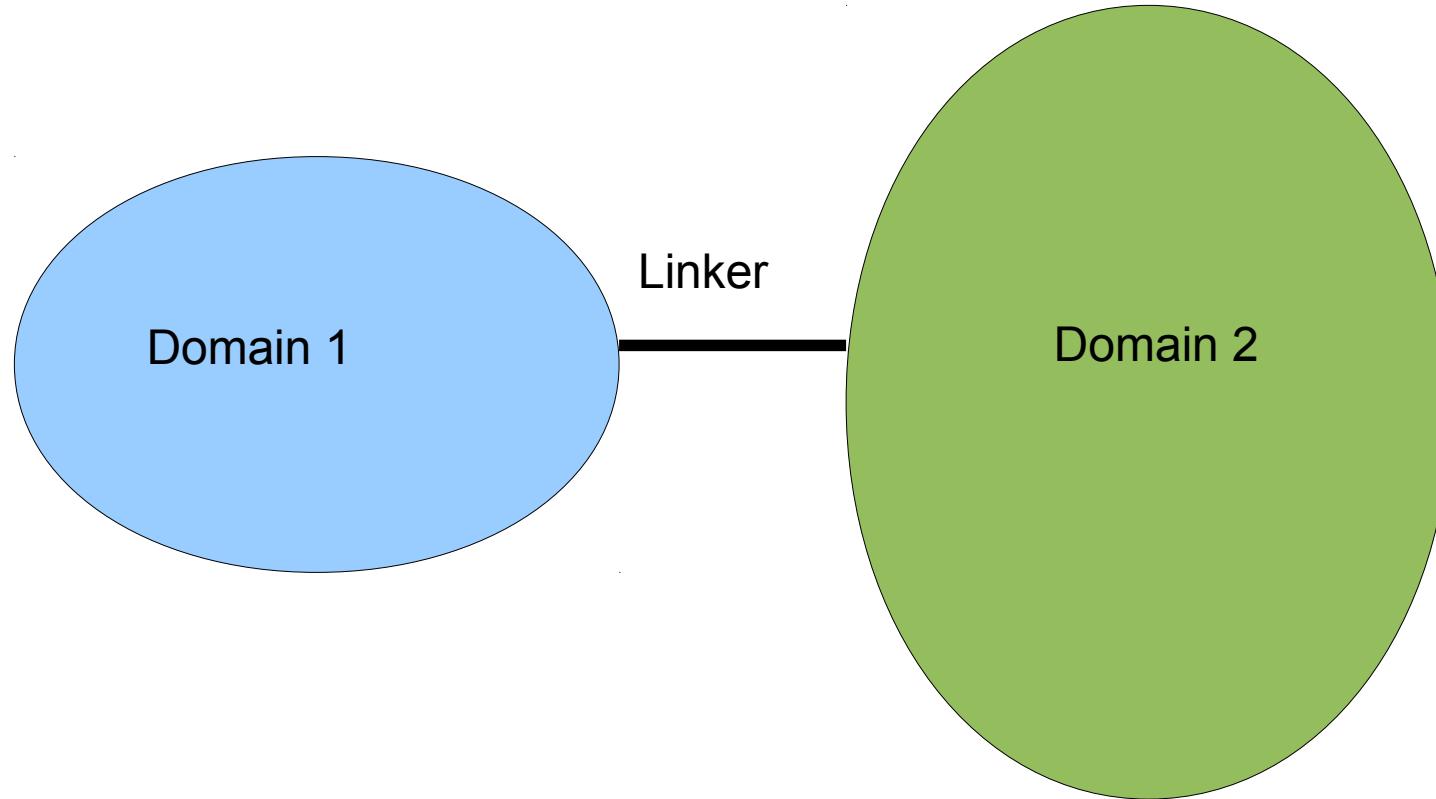
**Step 3.** Follow the instructions to Start Folding.

Stanford University will send your computer a folding problem to solve. When your first job is completed, your computer will swap the results for a new job.

 **START FOLDING**



# CASE STUDY: FOLDING AN INTERDOMAIN LINKER



➤ No structure of KDR motif in the linker is available

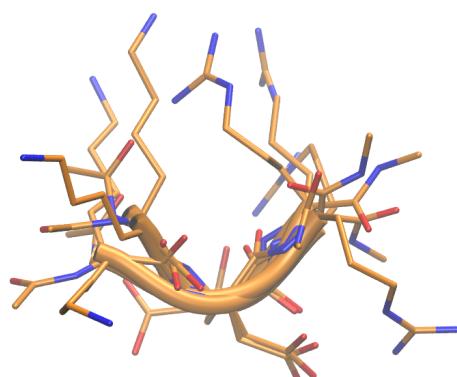
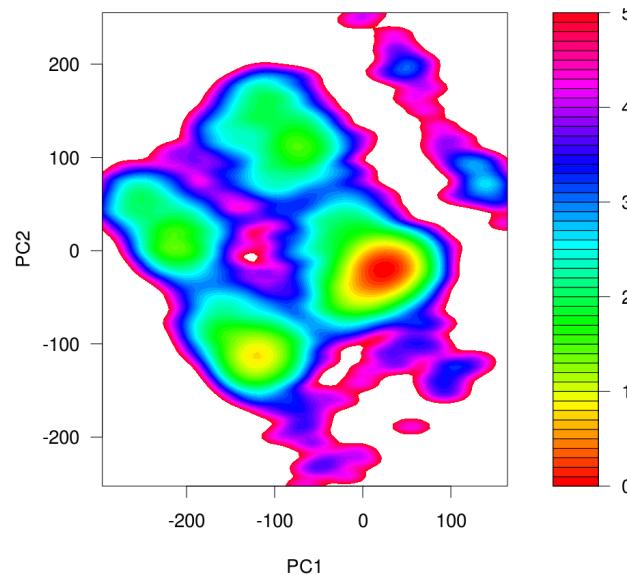
Aim: to calculate the conformation of the linker

# CASE STUDY: FOLDING AN INTERDOMAIN LINKER

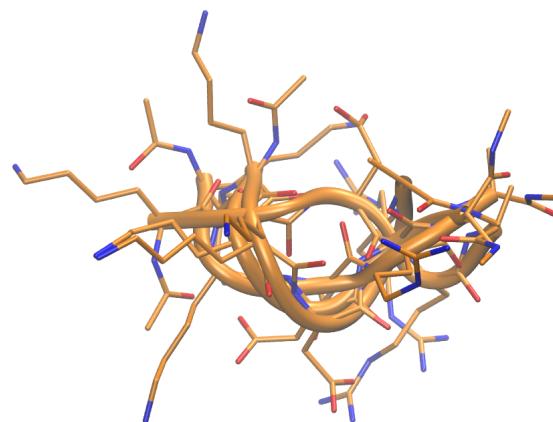
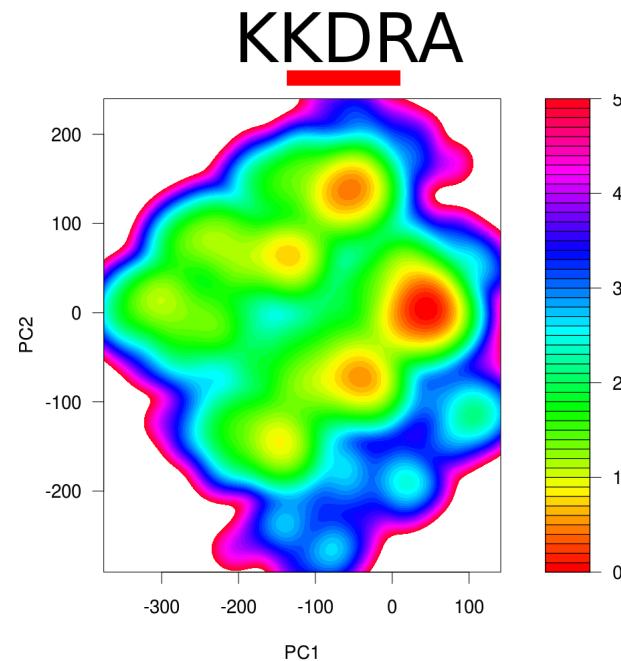
- Methodology: REMD
- Peptides: KDR, KKDRA, PKKDRAR, RPKKDRARQ

# CASE STUDY: FOLDING INTERDOMAIN LINKER

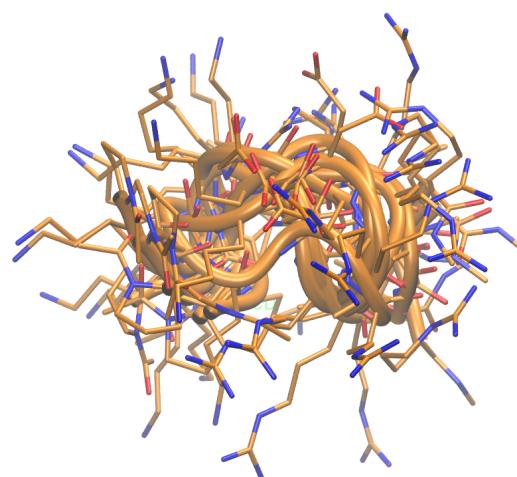
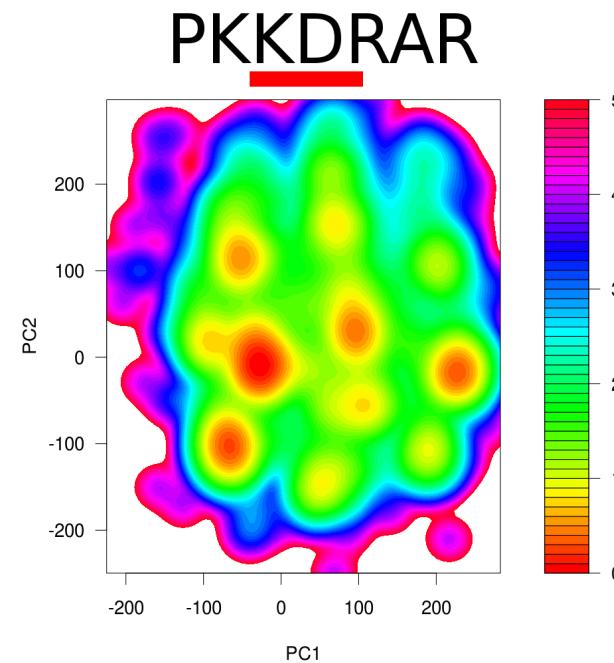
KDR



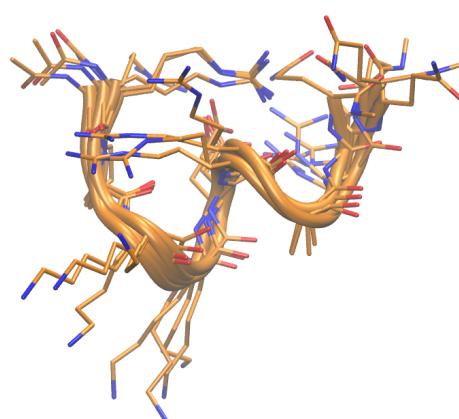
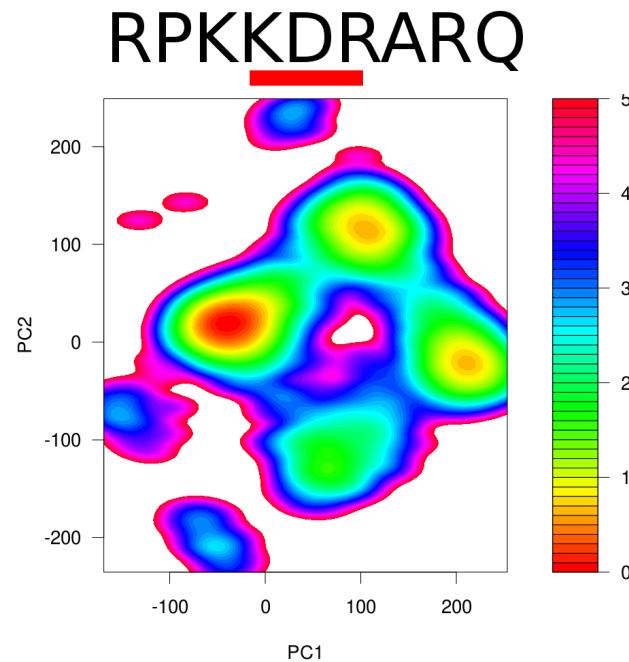
# CASE STUDY: FOLDING AN INTERDOMAIN LINKER



# CASE STUDY: FOLDING AN INTERDOMAIN LINKER



# CASE STUDY: FOLDING AN INTERDOMAIN LINKER



# CASE STUDY: FOLDING AN INTERDOMAIN LINKER

The studied interdomain linker folds into  $\alpha$ -helix

# LECTION 4: PROTEIN FOLDING

- Protein folding and denaturation: «all or nothing»
- Anfinsen's dogma
- Folding of  $\alpha$ - and  $\beta$ -secondary structures
- Hydrophobic effect
- Levinthal's paradox
- Protein vs other polymers
- Thermodynamics and kinetics of protein folding
- Protein folding in the cell
- Computational approaches to study folding
- CASP
- Case study: folding of an interdomain linker

