

Pearson Correlation Coefficient:

This is used for measure the relationship within particular range from $(-1 \text{ to } 1)$.

→ The more towards $+1$ then say more positively correlation.

→ The more towards -1 then say more negatively correlation.

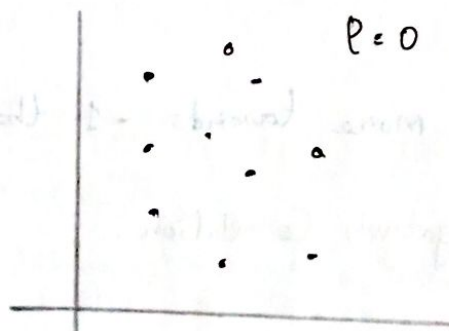
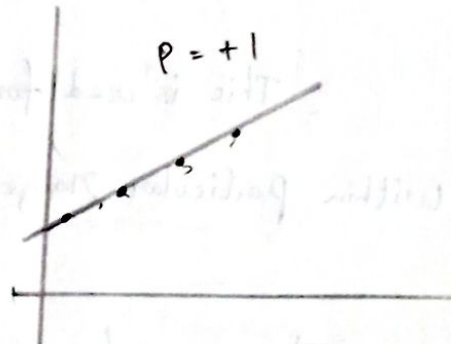
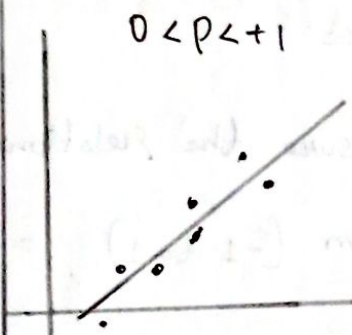
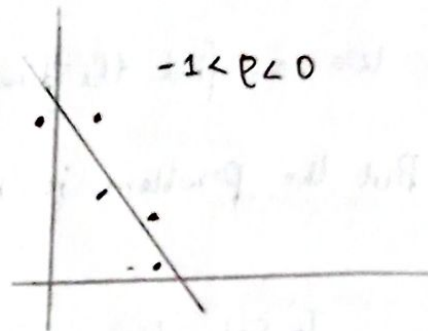
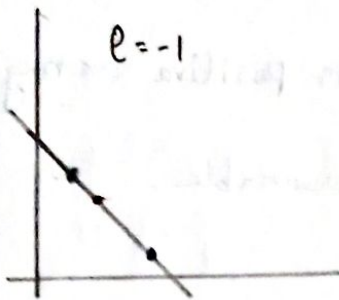
Formula,

$\sigma_x \rightarrow$ sd of feature x

$\sigma_y \rightarrow$ sd of feature y

$$\rho(x, y) = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$$

Value $\in \{-1 \text{ to } 1\}$ (Ans)

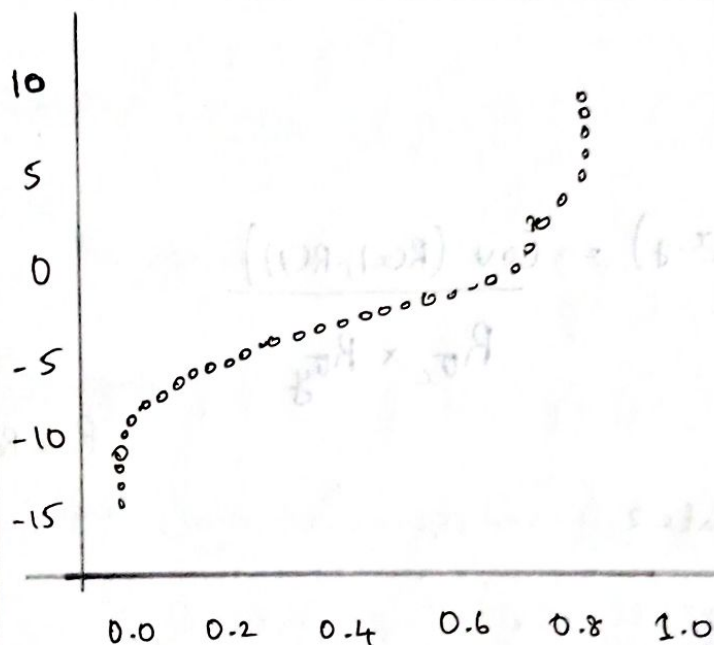


Does not follow straight line we say range from $-1 < \rho < 0$ (or) $0 < \rho < +1$ [Range]

Disadvantage:

→ The Pearson Correlation Coefficient is only works well for Linear properties. Does not fit for non-Linear properties. So, we jump into Spearman rank Correlation.

Spearman's rank Correlation Coefficient:



In this Scenario,

Spearman Correlation = 1

Pearson Correlation = 0.88

Spearman Considered best because, it is non-linear Property. So works well and also show accurate Correlation.

Advantage:

→ It is somewhat similar to Pearson Correlation, The difference is it works well for non-linear Property as well.

→ It also Calculate the relation accurately. (i.e. One point overlap with some distance also Calculate. But, Pearson Cannot).

formula,

$$\text{Spear}(x, y) = \frac{\text{Cov}(R(x), R(y))}{R_{\sigma_x} \times R_{\sigma_y}}$$

R → Rank

How to calculate?

Let Consider,

| x | y | R(x) | R(y) |
|-----|----|------|------|
| 170 | 75 | 2 | 2 |
| 160 | 62 | 3 | 3 |
| 150 | 60 | 4 | 4 |
| 145 | 55 | 5 | 5 |
| 180 | 85 | 1 | 1 |

x → Height

y → weight

Based on the higher value, Rank will be assigned.

The formula only works with $R(x)$, $R(y)$, R_{0x} and R_{0y} . It neglects the original feature x and y while performing.

The main thing of the Spearman Rank Correlation is that it captures non-linear properties as well.