

How Boosting is different from Bagging?

- 1. Our base learners will be underfitted in Boosting how can we create underfit base learners?
 - a. Using mean model
 - b. Using a "decision stump"
- 2. Instead of parallelly providing the data to different base learners, we will feed the data sequentially to these learners.

Let's understand this concept with an example.

Let's take 4 students: Prince, Jay, Hardik, Mitanshu

We have a code of 20 lines but it throws errors.

We give this code to Prince. Prince checked & corrected first 5 lines of code then he was busy so he gave this code to Jay.

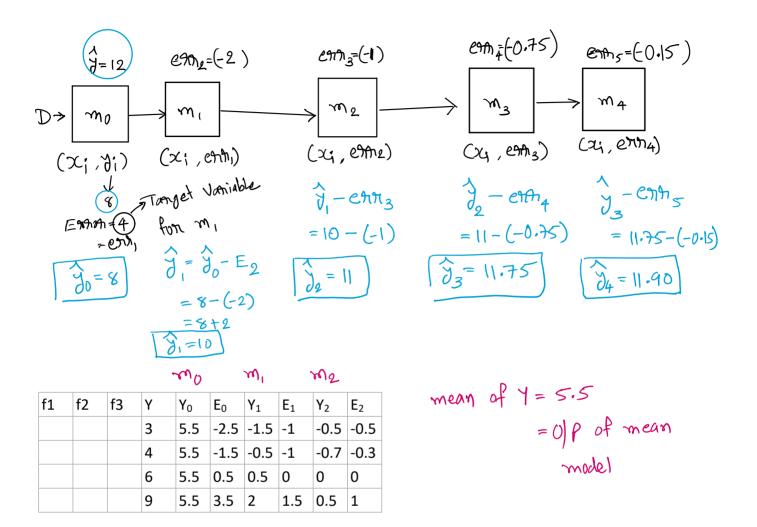
Now what Jay is going to work on? Jay will start working on the code from line 6. Suppose he corrected next 7 line and sent the code to Hardik.

From where Hardik will start? He will start from line 13. Let's say he also improved the next 6 lines and submitted that code to Mitanshu.

Now Mitanshu needs to do? Just the remaining 2 lines.

But how to implement this logically?

- 1. A single datapoint is taken and its label is predicted using "mean model"
- 2. Error in the prediction is calculated



Computation of errors:

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$$e_0 = J - \hat{J}_0$$
; $J = Actual Label & \hat{J}_0 = Predicted label of mean model.$
 $e_1 = J - \hat{J}_0 - \hat{J}_1 \Rightarrow e_1 = J - (\hat{J}_0 + \hat{J}_1)$
 $e_2 = J - \hat{J}_0 - \hat{J}_1 - \hat{J}_2 \Rightarrow e_2 = J - (\hat{J}_0 + \hat{J}_1 + \hat{J}_2)$
 $e_k = J - (\hat{J}_0 + \hat{J}_1 + \hat{J}_2 + \dots + \hat{J}_k)$
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These models m₀, m₁, m₂, ... are predicting errors and we want to minimize these errors. So, let's take the outputs of these models (errors) as a function of X (features) so we can treat that function as our loss function and then we can think of minimizing it.

$$\therefore \hat{J}_0 = h_0(x), \hat{J}_1 = h_1(x), \hat{J}_2 = h_2(x), \dots$$

And let's say our final predictions are represented as $f_i(x)$ then they can be given as:

$$f_{0}(x) = h_{0}(x) + h_{1}(x)$$

.: The step-1 is to cheate & thain out first model m_1 on Cx_1 , e_0) & to get the above output.

Step-2: Cheate & train M2 on (Z;, e,) & to get the following olp:

$$f_{0}(x) = h_{0}(x) + h_{1}(x) + h_{2}(x)$$

But just like we used to compute feature importance, here we want to find "model importance", let's also add weights to the olp of each model. We will call these weights of cgamma)

$$f_1(x) = h_0(x) + \mathcal{F}_1 \cdot h_1(x)$$

$$f_{\epsilon}(x) = h_0(x) + V_1 h_1(x) + V_2 \cdot h_2(x)$$

Continuing till step-k:

$$f_{k}(x) = h_{0}(x) + \gamma_{1} h_{1}(x) + \gamma_{2} h_{2}(x) + \dots + \gamma_{k} h_{k}(x)$$

$$\therefore f_{k}(x) = h_{0}(x) + \sum_{i=1}^{k} \gamma_{i} h_{i}(x)$$

As we can observe, this formula is very similar to Linear Regression:

$$f_n(x) = h_0(x) + Y_1 h_1(x) + Y_2 h_2(x) + \dots + Y_n h_n(x)$$

$$\downarrow G_{n} \text{ adjent Boosting}$$

$$\hat{y} = w_0 + w_1 x_1 + w_2 x_2 + - - - \cdot + w_n x_n$$
Linear Regnession

In L.R., w; can be computed parallely but in G.B. we have to find Y, to calculate) find Y2 so finding weights is a sequential process in Gradient Boosting.

One another difference is that we can increase on decrease number of models from gradient boosting but we can not remove ladd features in Linear Reg.

hence no. of Yi can change but not no. of Wi

Errors (Residuals) at kth stage:

If we take "squared loss" (taking squares of the errors) as our loss function:

$$L(y, f_k(x)) = (y - f_k(x))^2$$

$$L(\lambda^{1}, f_{k}(x)) = (\lambda - f_{k}(x))^{2}$$

Let's take
$$f_k(x)$$
 as $Z_i = f_k(x)$

$$\frac{\partial L}{\partial z_{i}} = \frac{\partial}{\partial z_{i}} (y - z_{i})^{2}$$

$$= 2(y_{i} - z_{i}) \cdot \frac{\partial}{\partial z_{i}} (-z_{i})$$

$$\frac{\partial L}{\partial z_i} = -2\left(y_i - z_i\right)$$

$$\frac{-\partial L}{\partial z_i} = 2 (y_i - z_i)$$
 -> Negative of Ghadient

$$\frac{\partial L}{\partial z_i} \sim (J_i - z_i)$$
sendo entrogis

OR

$$\frac{-\partial L}{\partial f_k(x)} = \partial_i - f_k(x_i)$$

Input: training set $\{(x_i,y_i)\}_{i=1}^n$, a differentiable loss function L(y,F(x)), number of iterations M.

Algorithm:

1. Initialize model with a constant value P(y,F(x)) = P(y) = P(

Hyper-parameter tuning:

Hyper parameter - 1: Number of base learners (models) Let's call it m'.

What will happen if *m* is too large?

Error values will be minimized (tend to 0)

Final Model Overfits

What will happen if *m* is too small?

Output will be close to mean value

Final Model Underfits

Hyper parameter - 2: Depth of each base learner. Let's call it 'd'.

What will happen if d is too large?

Each base learner will overfit

What will happen if d is too small?

Each base learner will underfit - preferred in Boosting

Regularizer/Regularization:

$$f_{m}(x) = h_{0}(x) + y \neq f_{i} h_{i}(x)$$

$$T_{i=1}$$

$$\text{Regularized Regularization}$$

$$\text{constant } [0 < y < \omega]$$

$$T_{i} = y = 0 \Rightarrow f_{m}(x) = h_{0}(x)$$

If
$$y=0$$
 \Rightarrow $f_{m}(x) = h_{0}(x)$
 $\Rightarrow olp of mean model$
 $\Rightarrow Underfit$

as $y \Rightarrow \omega \Rightarrow f_{m}(x) = h_{0}(x) + \sum_{i=1}^{m} Y_{i} h_{i}(x)$
 $\Rightarrow regligible dominant$

Problems with GBDT (Gradient Boosted Decision Tree): GBDT = pseudo residuals + Additive Combining

- Slow
- Sequential
- It starts overfitting very quickly

Impact of Outliers:

Then how can we improve our GBDT?

Ans:

- 1. XGBOOST
- 2. Light GBM

We will also learn other Ensemble Techniques:

- 1. Bagging
- 2. Boosting
 - a. GBDT
 - b. XGBoost

- c. LightGBM
- 3. Stacking
- 4. Cascading

XGBOOST:

Why?

Because GBDT is slow in training & very slow if we do hyperparameter tuning Motivation:

Reduce the training time

How?

Optimizing training process

How a typical GBDT works:

No (x) = mean model

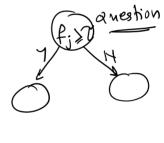
h,(x): Decision Thee with very small depth.

Thow will we cheate this 9.

(P. 7)

Ans- We calculate IG of every feature of the feature

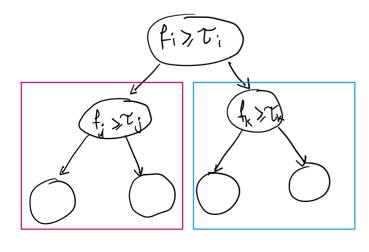
with max. I.G.



Hence, rather than considering all features let's randomly choose a few of them only and train our model on those features. This is one way (column sampling/feature selection)

Moreover, we can also do the feature selection parallelly in order to calculate IG.

2nd Idea: Parallelization in building subtrees



Although the 0/p of h2(x) can't be computed patrallely with 0/p of h.(x), we can parallely cheate the sub-trees of h.(x) of that of h2(x).

3rd Idea: Creating optimal bins on the numerical features to reduce number of thresholds for numerical columns

bin
1 - 10
1 - 10
11 - 20
11 - 20
1 - 10
11 - 20

2. Light GBM

Uses GOSS - Gradient-based One Sided Sampling

Cascading

We use cascading when the margin of error is extremely low or in other words, we cannot afford mistakes.

e.g.,

Medical field: classifying a malignant tumors and benign tumors

Finance sector: fraudulent vs. genuine transactions

Suppose we have the data of several transactions as below:

1000 transactions 990 genuine 1000 fraudulent

Clearly the data is extremely imbalanced. What can we do to it?

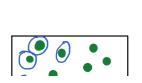
Options: SMOTE?

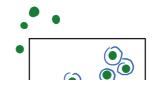
What do we do in SMOTE?

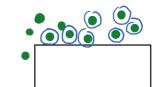
SMOTE will create 980 "artificial/generated" transactions which will be labelled as "fraudulent" (by SMOTE) to balance the data. So at the end we will have 1980 data points in which 980 (nearly half of them) are synthetic! Can we expect a model that is train on this data not to get wrong?

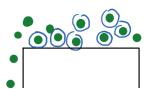
Then how can we solve this problem?

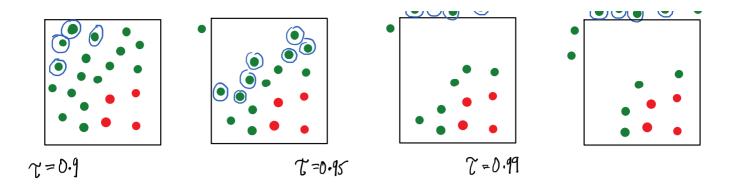
Solution: Visualize the bucket of data as shown in the figure. If we create a model that can predict probability of a particular transaction of being in majority class (being genuine), it will predict different probabilities for different transaction. Now let's decide a threshold (usually very high) e.g., 90%











In terms of ML language: