

Homework Set 4, CPSC 8420, Fall 2023

Last Name, First Name

Due 12/10/2023, Sunday, 11:59PM EST

Problem 2

Please use spectral clustering to segment the image ‘clemson.jpeg’ in the file.

Problem 3

Frequently, the affinity matrix is constructed as:

$$A_{ij} = e^{-d(x_i, x_j)^2 / \sigma} \quad (1)$$

where σ is some user-specified parameter. The best that we can hope for in practice is a near block-diagonal affinity matrix. It can be shown in this case, that after projecting to the space spanned by the top k eigenvectors, points which belong to the same block are close to each other in a euclidean sense. The steps are as follows:

- Construct an affinity matrix A using the above equation.
 - Symmetrically ‘normalize’ the rows and columns of A to get a matrix N such that $N(i, j) = \frac{A(i, j)}{\sqrt{d(i)d(j)}}$, where $d(i) = \sum_k A(i, k)$.
 - Construct a matrix Y whose columns are the first k eigenvectors of N .
 - Normalize each row of Y such that it is of unit length.
 - Cluster the dataset by running k -means on the set of embedded points, where each row of Y is a data-point.
1. Run k -means on the datasets provided in the .zip file. For text.mat, take $k = 6$. For all others use $k = 2$.
 2. Implement the above spectral clustering algorithm and run it on the four provided datasets using the same k . Plot your clustering results using $\sigma = .025, .05, .2, .5$. Hints: You may find the MATLAB functions `pdist` and `eig` to be helpful. A function `plotClusters.m` has been provided to help visualize clustering results.
 3. Plot the first 10 eigenvalues for the rectangles.mat and text.mat datasets when $\sigma = .05$. What do you notice?
 4. How do k -means and spectral clustering compare?

